

# Stats camp day 1

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Welcome to Graduate statistics  
training!

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# Stats camp goals

1. Get your software set up
2. Remind you what these things mean:

$$\log(x)$$

$$y = 2 + 3x$$

$$\frac{d}{dx}x^3 = 3x^2$$

$$\sum_{x=1}^{10} x$$

# Today: Let's install software

## Step 1

Install R. <https://cran.r-project.org/>

## Step 2

Install RStudio. <https://www.rstudio.com/>

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- Does anyone have problems with regular access to a computer that can run R?

# Problems?

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- The script and the console

- The script and the console
- Make it pretty! (You will be spending lots of time here...)
  - Themes
  - Pane layouts



- Install packages

```
install.packages("tidyverse")
```

## Getting started in RStudio: packages

- Load packages

```
library(tidyverse)
```

```
## -- Attaching packages -----
```

```
## v ggplot2 3.3.2      v purrr    0.3.4
```

```
## v tibble  3.0.3      v dplyr    1.0.1
```

```
## v tidyr   1.1.1      v stringr  1.4.0
```

```
## v readr   1.3.1      v forcats  0.5.0
```

```
## -- Conflicts -----
```

```
## x dplyr::filter() masks stats::filter()
```

```
## x dplyr::lag()    masks stats::lag()
```

Problems?

---

## Using R as a (very fancy) calculator

```
2 + 2
```

## Using R as a (very fancy) calculator

```
2 * 2
```

## Using R as a (very fancy) calculator

2 / 2

## Using R as a (very fancy) calculator

```
2 ^ 3
```

## Using R as a (very fancy) calculator

```
sqrt(4)
```



## Using R as a (very fancy) calculator

```
# I am a comment! I help you read code!  
# the <- operator makes assignments  
# Make a new variable called 'x', set it equal to 2  
x <- 2  
x^2
```

## Using R as a (very fancy) calculator

Compute the following in R (with  $x = 2$ )

$$\cdot x^3$$

## Using R as a (very fancy) calculator

Compute the following in R (with  $x = 2$ )

- $x^3$
- $2x$

## Using R as a (very fancy) calculator

Compute the following in R (with  $x = 2$ )

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- $2x$

- $\frac{x}{2}$

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- Are you running RStudio?

## Before we proceed

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- Have you installed tidyverse?



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Exciting! You are programming in R!

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# Break



Welcome back: math time!

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# Agenda today

1. Math notation and key concepts
2. Exponents, logarithms
3. Lines and graphs

## Real numbers (doubles)

- Any continuous number
- E.g. 4, 4.189,  $2/3$ ,  $\pi$

## Integers

- Any whole number
- 10, -10, 24, 87

- May take on any value
- Represented by letters, such as  $x$ ,  $y$ ,  $z$
- Can be used in any mathematical operation



- Maps each element of set  $x$  to an element of set  $y$
- Often denoted by  $f, g, h$
- $f(x) = 2x + 3$

- Variable that represent a feature of a population
- Represented by Greek letters, such as  $\mu, \sigma, \varepsilon$

Represented as  $\sum$ , with integer begin and end points

$$\sum_{x=1}^3 x$$

# Summation

Represented as  $\sum$ , with integer begin and end points

$$\sum_{x=1}^3 x$$

$$\sum_{x=1}^3 x = 1 + 2 + 3 = 6$$

In R, we can calculate a sum using the `sum()` function

```
# make an integer vector from 1 to 3
```

```
x<-1:3
```

```
# x<-c(1,2,3) is equivalent
```

```
sum(x)
```

```
## [1] 6
```

Compute the following by hand, and then in R

$$\sum_{x=3}^8 (x + 1)$$

$$\sum_{x=1}^4 2x$$

Compute the following in R

$$\sum_{x=3}^8 (x + 1)$$

$$\sum_{x=1}^4 2^x$$

## Exercises (solutions)

Compute the following in R

$$\sum_{x=3}^8 (x + 1)$$

```
x<-3:8 # or c(3, 4, 5, 6, 7, 8)
sum(x+1)
```

$$\sum_{x=1}^4 2x$$

```
x<-c(1, 2, 3, 4) # or 1:4
sum(2*x)
```



# Products

Represented as  $\prod$ , with integer begin and end points

$$\prod_{x=1}^4 x$$

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$$\prod_{x=1}^4 x$$

$$\prod_{x=1}^4 x = 1 \times 2 \times 3 \times 4$$

In R:

```
x<-1:4  
prod(x)
```

```
## [1] 24
```

## Exponents and logarithms

---

# Exponents

$a^n$  Is equal to a multiplied by itself n times

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$$\cdot 2^3 = 2 \times 2 \times 2 = 8$$

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$a^n$  Is equal to  $a$  multiplied by itself  $n$  times

$$\cdot 2^3 = 2 \times 2 \times 2 = 8$$

$$\cdot 5^4 = 5 \times 5 \times 5 \times 5 = 625$$

In R, we can calculate exponents using the `^`

```
2^3
```

```
## [1] 8
```

```
5^4
```

```
## [1] 625
```

## Some rules of exponents

$$x^1 = x$$



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## Exponents in R

```
x<-4
```

```
x^3
```

```
## [1] 64
```

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```
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```
x^3
```

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## [1] 64
```

```
x^(2+3)
```

```
## [1] 1024
```

## Exponents in R

```
x<-4
```

```
x^3
```

```
## [1] 64
```

```
x^(2+3)
```

```
## [1] 1024
```

```
## for base e, use exp()
```

```
exp(4)
```

```
## [1] 54.59815
```

A logarithm is the power  $x$  required to raise a base  $c$  to a given number  $a$ .

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$$\log_c(a) = x$$

$$c^x = a$$

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$$3^2 = 9$$



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$$\log_c(a) = x$$

$$c^x = a$$

$$3^2 = 9$$

$$\log_3(9) = 2$$

- The most common log bases are 2, 10, and  $e = 2.718$
- Log with base  $e$  is called a natural log,  $\ln$
- The R function `log()` has a default base  $e$
- We use log base  $e$  to model many exponential growth processes

## Logarithms are the inverse of exponents

$$10^2 = 100$$

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$$\log_{10}(100) = 2$$

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$$e^2 = 7.389056$$

$$\log_e(7.389056) = 2$$

$$\log(x \cdot y) = \log(x) + \log(y)$$

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$$\log(x^n) = n \log(x)$$



$$\log(x \cdot y) = \log(x) + \log(y)$$

$$\log(x^n) = n \log(x)$$

$$\log\left(\frac{x}{y}\right) = \log(x) - \log(y)$$

For statistics, it is safe to assume that *log* means *ln*. In R, this is the default

```
log(10)
```

```
## [1] 2.302585
```

```
log(10, base = 10)
```

```
## [1] 1
```

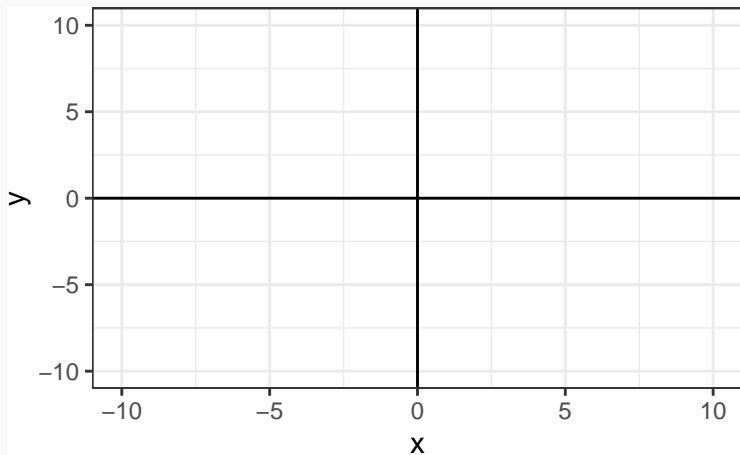
Compute the following in R. Assume  $x = 6$

1.  $x^4$
2.  $2x^{5+x}$
3.  $e^x$
4.  $\log(x)$
5.  $\log(2x + 3)$
6.  $\log(\frac{1}{2x})$

## Coordinates and lines

---

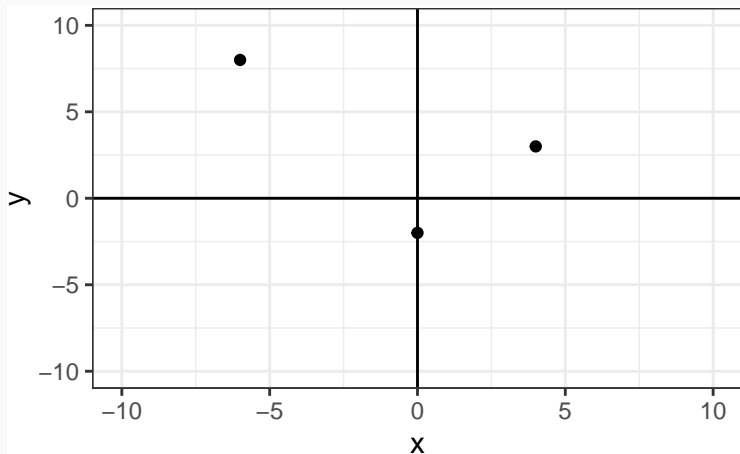
# The coordinate plane



## Plotting points

For coordinate pairs  $(x_1, y_1)$ ,  $(x_2, y_2)$ ,  $(x_3, y_3)$ , we can plot each point along an x and y axis.

**Example:**  $(0, -2)$ ,  $(4, 3)$ ,  $(-6, 8)$



The typical equation for a line is  $y = mx + b$  where  $m$  is the slope and  $b$  is the y-intercept.

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You will often see a line expressed as a regression equation:

$$y = \beta_0 + \beta_1 x$$

where  $\beta_0$  is the y-intercept and  $\beta_1$  is the slope.



## The slope

Slope measures the steepness of a line. A line with a positive slope has increasing values of  $y$  as  $x$  increases. A line with a negative slope has decreasing values of  $y$  for increasing values of  $x$ .

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We can calculate the slope with two coordinates on the line

$$(x_1, y_1), (x_2, y_2)$$

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We can calculate the slope with two coordinates on the line  
 $(x_1, y_1), (x_2, y_2)$

The slope is the ratio of the difference in  $y$  values to the difference in  $x$  values.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

## The y-intercept

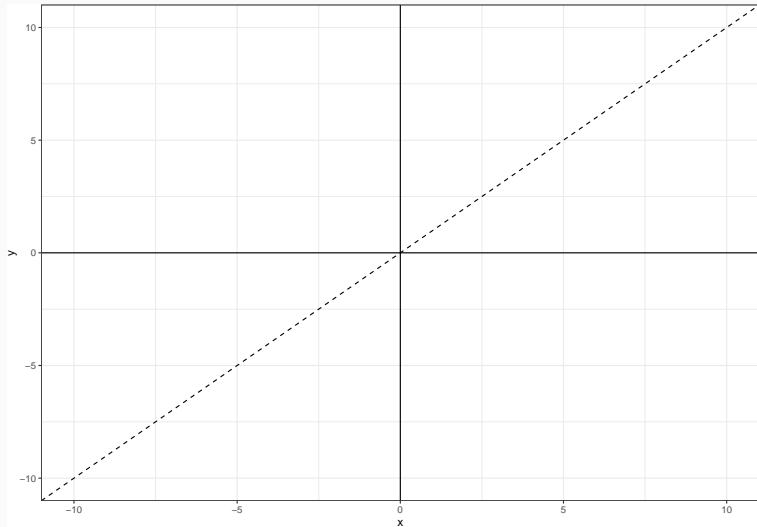
The y-intercept is the value of  $y$  when  $x = 0$ . If we have the value of one point on the line, and the slope, we can obtain the y-intercept

## The y-intercept

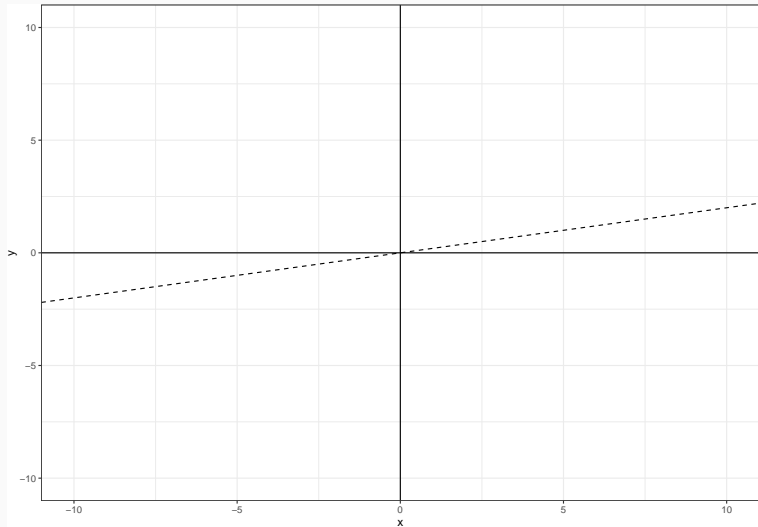
The y-intercept is the value of  $y$  when  $x = 0$ . If we have the value of one point on the line, and the slope, we can obtain the y-intercept

$$b = y_1 - m \cdot x_1$$

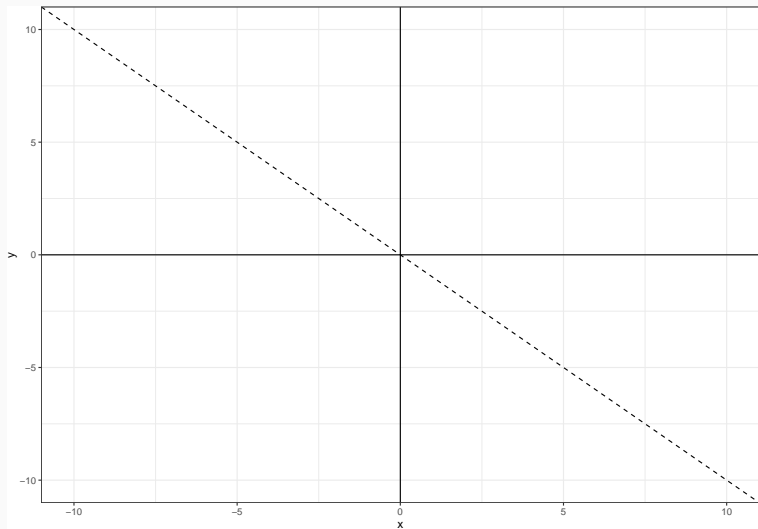
Example: intercept = 0, slope = 1



Example: intercept = 0, slope = 0.2

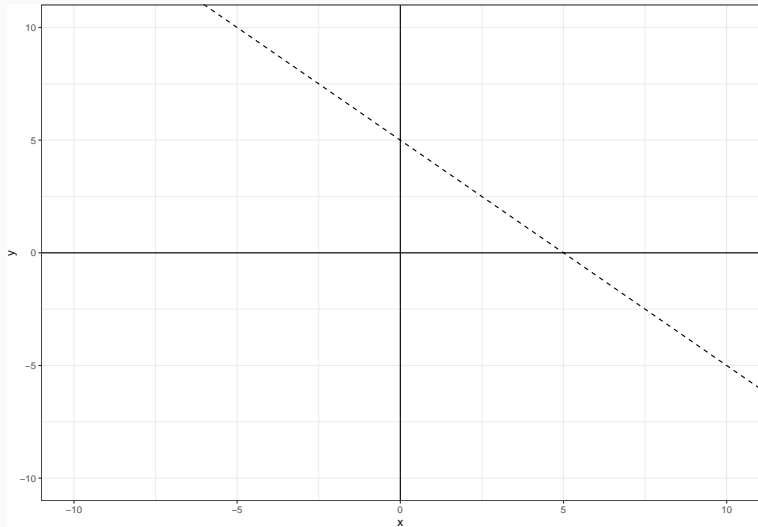


Example: intercept = 0, slope = -1

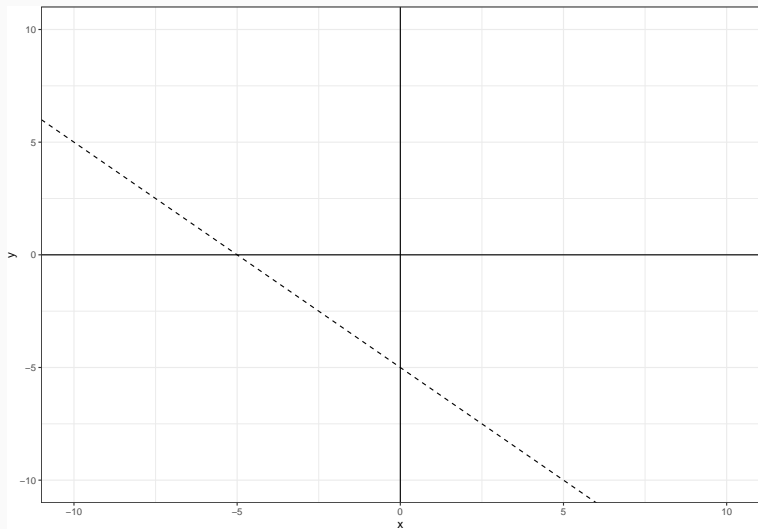




Example: intercept = 5, slope = -1

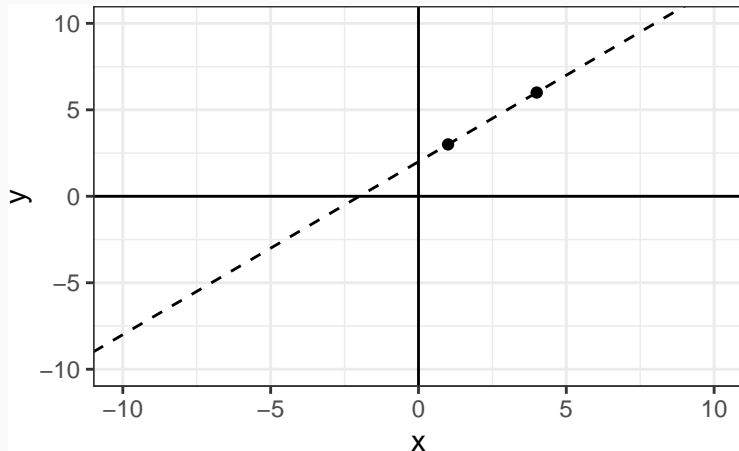


Example: intercept = -5, slope = -1



## Example

Given the points  $(1, 3)$  and  $(4, 6)$ , the slope is  $m = \frac{6-3}{4-1} = 1$  and the y-intercept is  $b = 3 - 1 \cdot 1 = 2$ . The equation of the line is  $y = 1x + 5$



# Functions

---

A function maps each element in a set  $X$  to an element in set  $Y$

- Linear function:  $f(x) = x + 5$

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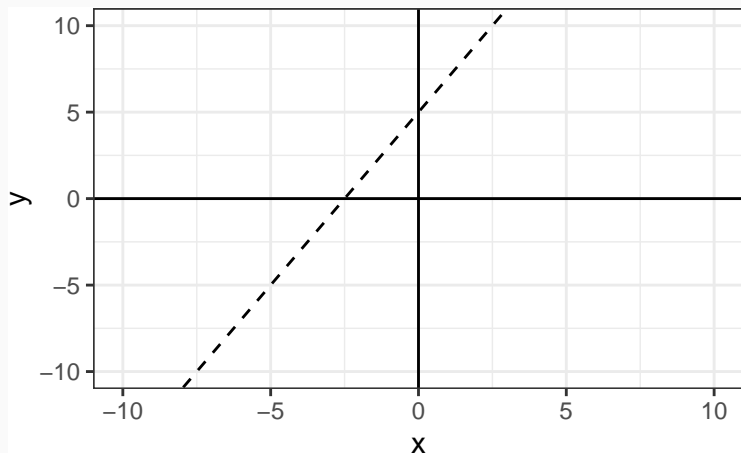
- Linear function:  $f(x) = x + 5$
- Quadratic function:  $f(x) = x^2 + 2x + 3$

A function maps each element in a set  $X$  to an element in set  $Y$

- Linear function:  $f(x) = x + 5$
- Quadratic function:  $f(x) = x^2 + 2x + 3$
- Exponential function:  $f(x) = e^{2x} + 6$

## Graphical forms of functions: linear

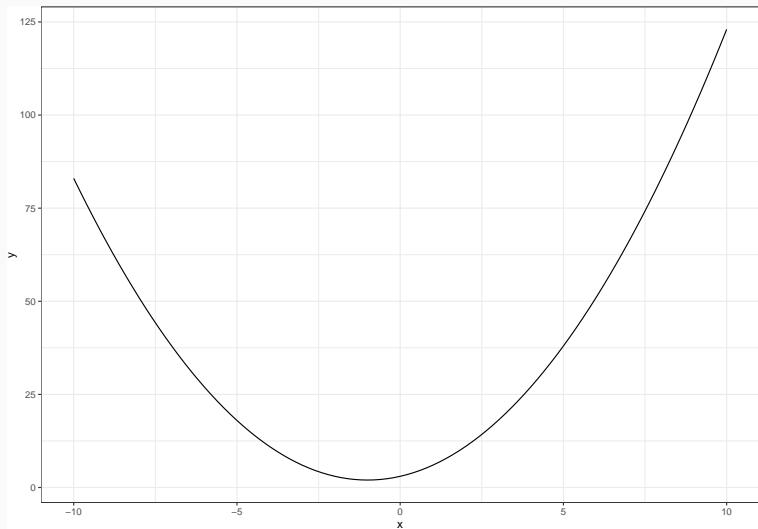
$$f(x) = 2x + 5$$





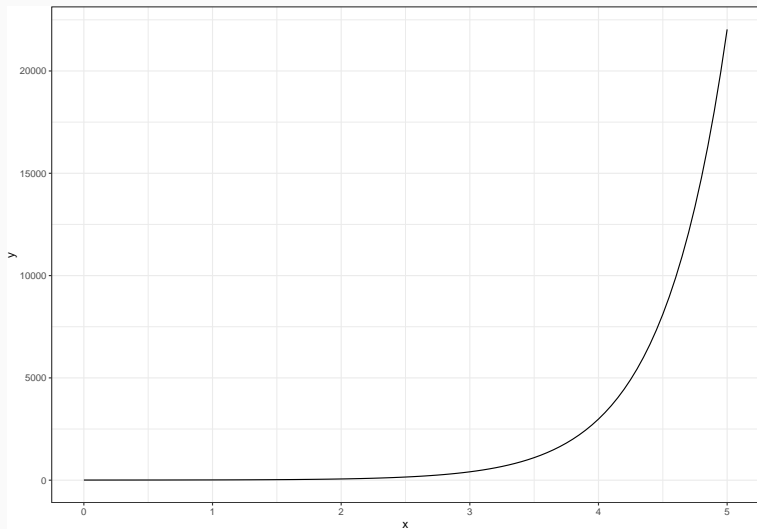
## Graphical forms of functions: quadratic

$$f(x) = x^2 + 2x + 3$$



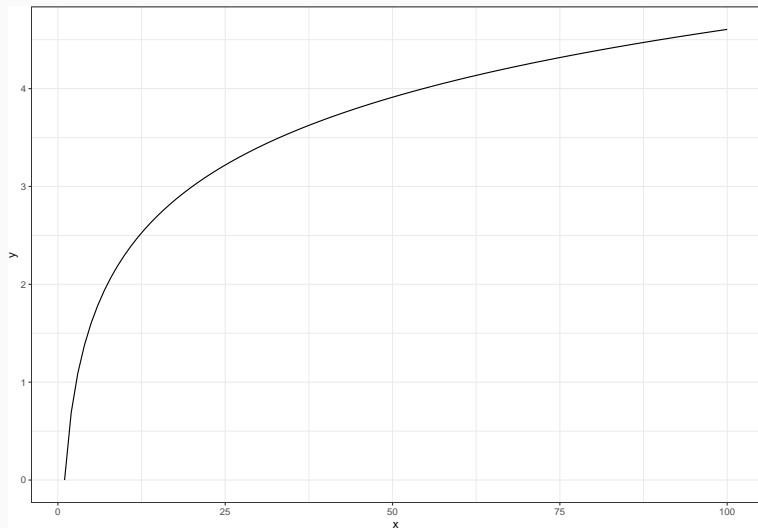
## Graphical forms of functions: exponential

$$f(x) = e^{2x} + 6$$



# Graphical forms of functions: logarithmic

$$f(x) = \log(x)$$



# Functions in R

We can easily define functions in R.

$$f(x) = 2(x + 3)^3$$

```
f_x<-function(x){2 * (x + 3)^2}  
f_x(3)
```

```
## [1] 72
```

# Functions in R

We can easily define functions in R.

$$f(x) = 2(x + 3)^3$$

```
f_x<-function(x){2 * (x + 3)^2}  
f_x(3)
```

```
## [1] 72
```

$$g(x) = \frac{x - 1}{5}$$

```
g_x<-function(x){(x-1)/5}  
g_x(4)
```

```
## [1] 0.6
```

Define and evaluate the following functions in R. Assume  $x = 2$

1.  $f(x) = 2x$

2.  $f(x) = \frac{x}{2}$

3.  $f(x) = 2(x + 1)^3$