Causality, 2

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Returning to Pager's experiment

The causal effect

For observation *i* is equal to callback_crimTRUE_i - callback_crimFALSE_i

The fundamental problem of causal inference is that we only observe one of these outcomes

The counterfactual and potential outcomes

	callback	crimrec	${\tt callback_crimT}$	${\tt callback_crimF}$
1	1	1	1	NA
2	Θ	Θ	NA	0
3	1	Θ	NA	1
4	1	Θ	NA	1
5	0	1	Θ	NA
6	Θ	1	0	NA
	2 3 4 5	1 1 2 0 3 1 4 1 5 0	1 1 1 2 0 0 0 3 1 0 4 1 0 5 0 1	2 0 0 NA NA 1 0 NA 4 1 0 NA 5 0 1 0

Randomized experiments (or RCTs)

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- By randomizing assignment to treatment, we can treat units as equivalent
- If units are equivalent, we can estimate the average treatment effect as a difference in means on the outcome between the treatment and control group
- If we don't randomize, we have no assurance that the treated and control groups are equivalent, meaning we don't have a strong case that we've observed the counterfactual

Obtaining a sample average treatment effect

The sample average treatment effect is defined as:

SATE =
$$\frac{1}{n} \sum_{i=1}^{n} Y_i(1) - Y_i(0)$$

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$$\frac{1}{n} \sum_{i=1}^{n} Y_i(1) - Y_i(0)$$

In practice, since we only observe $Y_i(1)$ OR $Y_i(0)$, we instead estimate a difference-in-means of the outcome between the treatment and control: mean(Y(1)) - mean(Y(0)). If assignment has been randomized, these values are identical.

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Why we randomize

An experiment on voting and a social pressure

Civic duty: The whole point of democracy is that citizens are active participants in government; that we have a voice in government. Your voice starts with your vote. On August 8, remember your rights and responsibilities as a citizen. Remember to vote. DO YOUR CIVIC DUTY – VOTE

An experiment on voting and a social pressure

Civic duty: The whole point of democracy is that citizens are active participants in government; that we have a voice in government. Your voice starts with your vote. On August 8, remember your rights and responsibilities as a citizen. Remember to vote. DO YOUR CIVIC DUTY – VOTE

Hawthorne effect (surveillance): This year, we're trying to figure out why people do or do not vote. We'll be studying voter turnout in the August 8 primary election. Our analysis will be based on public records, so you will not be contacted again or disturbed in any way. Anything we learn about your voting or not voting will remain confidential and will not be disclosed to anyone else. DO YOUR CIVIC DUTY – VOTE

An experiment on voting and a social pressure

 $social <- \ read_csv("https://raw.githubusercontent.com/kosukeimai/qss/master/CAUSALITY/social.csv") \\ head(social)$

```
## # A tibble: 6 x 6
           yearofbirth primary2004 messages primary2006 hhsize
##
    sex
    <chr>
                 <fdb>
                             <dbl> <chr>
                                                    <fdh> <fdh>>
##
## 1 male
                  1941
                                 0 Civic Duty
## 2 female
                 1947
                                 0 Civic Duty
## 3 male
                 1951
                                 0 Hawthorne
                                                               3
## 4 female
                                 0 Hawthorne
                 1950
                                                               3
## 5 female
                 1982
                                 0 Hawthorne
                                                               3
## 6 male
                  1981
                                 0 Control
                                                               3
```

Obtaining mean voting by treatment/control

0.338

1

```
control <- social %>%
 filter(messages == "Control") %>%
 summarise(primary2006 = mean(primary2006))
treatment <- social %>%
 filter(messages != "Control") %>%
 summarise(primary2006 = mean(primary2006))
control
## # A tibble: 1 x 1
    primary2006
##
          < fdh>>
##
          0.297
## 1
treatment
## # A tibble: 1 x 1
    primary2006
##
          <dbl>
##
```

The difference in means (causal effect)

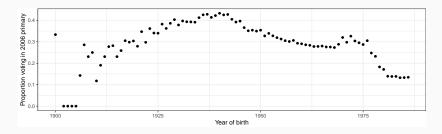
1 0.04164458

```
effect <- treatment - control
effect
## primary2006</pre>
```

Why randomization matters

```
prop_vot<-social %>%
  group_by(yearofbirth) %>%
  summarise(voting_prop = sum(primary2006)/n())

ggplot(prop_vot,
    aes(x = yearofbirth, y = voting_prop)) +
  geom_point() +
  ylab("Proportion voting in 2006 primary") +
  xlab("Year of birth")
```



Why randomization matters (continued)

```
sex_hh<-social %>%
  group_by(sex, hhsize) %>%
  summarise(voting prop = sum(primary2006)/n())
ggplot(sex_hh,
        aes(x = hhsize, y = voting prop, color = sex)) +
  geom_point() +
  xlab("Household size") +
  ylab("Proportion voting in 2006 primary")
Proportion voting in 2006 primary
                                                                                                             sex
                                                                                                                 female
                                                                                                                 male
                                                 Household size
```

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- We note these differences between observed variables and our outcome: primary2006
- We didn't measure very much here. They could also differ across unobserved or unobservable variables!
- Randomization (given a large enough n) ensures that treatment and control groups are identical across all observed and unobserved/unobservable differences prior to treatment
- This condition statistically identical treatment and control groups

 is a necessary condition for causal inference. Randomization is the
 most straightforward way to achieve this condition.

Causal inference in observational data

Estimating the impact of a minimum wage increase

In 1992, New Jersey raised it's minimum wage from \$4.25 to \$5.05. Pennsylvania did not.

 $\label{limiting} $$\min $$ < - \ read_csv("https://raw.githubusercontent.com/kosukeimai/qss/master/CAUSALITY/minwage.csv")$$ head(minwage)$$

##	#	# A tibble: 6 x 8									
##		chain	location	wageBefore	wageAfter	${\tt fullBefore}$	${\tt fullAfter}$	partBefore	partAfter		
##		<chr></chr>	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>		
##	1	wendys	PA	5	5.25	20	0	20	36		
##	2	wendys	PA	5.5	4.75	6	28	26	3		
##	3	burgerking	PA	5	4.75	50	15	35	18		
##	4	burgerking	PA	5	5	10	26	17	9		
##	5	kfc	PA	5.25	5	2	3	8	12		
##	6	kfc	PA	5	5	2	2	10	9		

Describing the data, categoricals

```
table(minwage$chain)
##
## burgerking
                   kfc
                          roys
                                     wendys
##
         149
                   75
                               88
                                         46
table(minwage$location)
##
## centralNJ
            northNJ
                               shoreNJ
                                          southNJ
##
         45
                 146
                            67
                                     33
                                               67
```

Did NJ minimum wage increase the wages paid to employees?

```
minwage %>%
 group_by(location) %>%
 summarise(wageBefore_mn = mean(wageBefore),
           wageAfter_mn = mean(wageAfter))
## # A tibble: 5 x 3
    location wageBefore_mn wageAfter_mn
    <chr>
                     <fdb1>
                                  <fdh>>
##
## 1 centralNJ
                     4.63
                                  5.09
## 2 northNJ
                     4.63
                                  5.09
                     4.65
                                   4.61
## 3 PA
## 4 shoreNJ
                   4.64
                                   5.07
## 5 southNJ
                     4.54
                                   5.06
```

Another way to look at change in wages

```
minwage %>%
  group_by(location) %>%
  summarise(prop below before = mean(wageBefore>=5.05),
            prop below after = mean(wageAfter>=5.05))
## # A tibble: 5 x 3
##
    location prop below before prop below after
   <chr>
##
                           <dbl>
                                             <dbl>
## 1 centralNJ
                          0.133
                                            0.978
## 2 northNJ
                          0.0753
## 3 PA
                          0.0597
                                            0.0448
## 4 shoreNJ
                          0.121
## 5 southNJ
                          0.0746
                                            1
```

```
###Compute proportion full time before
###And after
minwage<- minwage %>%
 mutate(prop_ft_pre =
           fullBefore /
           (fullBefore + partBefore))
minwage <- minwage %>%
 mutate(prop_ft_post =
           fullAfter /
           (fullAfter + partAfter))
```

Look at our outcome variable

```
minwage %>%
 group_by(location) %>%
 summarise(prop_ft_pre = mean(prop_ft_pre),
           prop_ft_post = mean(prop_ft_post))
## # A tibble: 5 x 3
   location prop_ft_pre prop_ft_post
   <chr>
                   <dbl>
                                 <fdb>>
##
## 1 centralNJ
                 0.311
                                 0.251
## 2 northNJ
                    0.321
                                 0.375
## 3 PA
                    0.310
                                 0.272
## 4 shoreNJ
                    0.286
                                 0.345
## 5 southNJ
                    0.239
                                 0.236
```

Assumption: PA is a no-treatment counterfactual

Estimate the causal effect

```
control <- minwage %>%
  filter(location == "PA") %>%
  summarise(prop_ft_post = mean(prop_ft_post))

treatment <- minwage %>%
  filter(location != "PA") %>%
  summarise(prop_ft_post = mean(prop_ft_post))

treatment - control
```

```
## prop_ft_post
## 1 0.04811886
```

Is this a valid estimate of the causal effect?

Confounding jeopardizes causal inference

 Confounding bias: a third variable is associated with both the treatment and the outcome

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Correlation != Causation

Dealing with confounding

· Randomize treatment!

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- · When we can't...

Dealing with confounding

- · Randomize treatment!
- · When we can't...
- Statistical control: within-subgroup analysis based on confounder values

Are NJ and PA the same (at least when it comes to fast food jobs?)?

```
## # A tibble: 5 x 5
##
    location prop_wendys prop_bk prop_kfc prop_roys
##
    <chr>
                  <fd>< fdb>
                         <fdb1>
                                  <fdb>
                                           <fdb>>
## 1 centralNJ
                 0.0889
                         0.378 0.244
                                           0.289
## 2 northNJ
                 0.130
                         0.459 0.158
                                           0.253
## 3 PA
                 0.164
                         0.463
                                 0.149
                                           0.224
## 4 shoreNJ
                 0.152
                         0.364
                                 0.303
                                           0.182
                         0.328
## 5 southNJ
                 0.104
                                  0.313
                                           0.254
```

Maybe restaurant chain matters? Let's control for it!

```
control<-minwage %>%
  filter(location=="PA") %>%
  group_by(chain) %>%
  summarise(prop_ft_post = mean(prop_ft_post))
```

Maybe restaurant chain matters? Let's control for it!

```
treatment<-minwage %>%
  filter(location!="PA") %>%
  group_by(chain) %>%
  summarise(prop_ft_post = mean(prop_ft_post))
```

Maybe restaurant chain matters? Let's control for it!

```
treatment$effect<-treatment$prop_ft_post -
  control$prop_ft_post
treatment</pre>
```

Maybe region matters: central and south vs north and shore

```
control<-minwage %>%
  filter(location=="PA") %>%
  summarise(prop_ft_post = mean(prop_ft_post))
treatment<-minwage %>%
  filter(location!="PA") %>%
  group by(location) %>%
  summarise(prop ft post = mean(prop ft post))
control
## # A tibble: 1 x 1
     prop_ft_post
##
            <fdb>>
##
## 1
           0.272
treatment
## # A tibble: 4 x 2
    location prop ft post
##
    <chr>
                      <fdh>>
## 1 centralNl
                     0.251
## 2 northNJ
                     0.375
## 3 shoreNJ
                     0.345
## 4 southNJ
                      0.236
```

Maybe region matters?

```
treatment$effect<-treatment$prop_ft_post -
  control$prop_ft_post
treatment</pre>
```

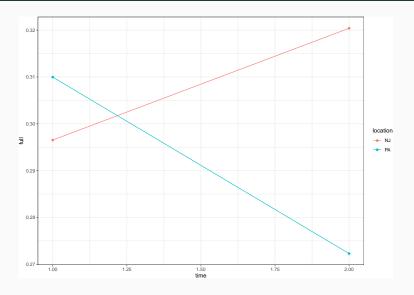
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- Longitudinal data: repeated measurements of the same unit on the same variables over time
- · Cross-sectional data: one measurement of many units
- Panel data (or time series cross-sectional data): repeated measurements of many units on the same variables over time
- Key advantages to panel data: variables may differ across units and within-units over time (trends).

Before and after design (longitudinal)



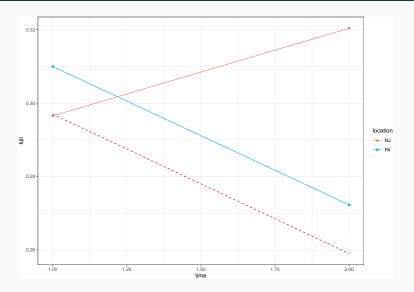
Difference in Differences

 What if we treated PA as the counterfactual, and used information about it's trend in employment to estimate the effect of NJ's minimum wage increase?

Difference in Differences

- What if we treated PA as the counterfactual, and used information about it's trend in employment to estimate the effect of NJ's minimum wage increase?
- Assumption: The trend in the outcome over time would have been identical across all units if the treatment had never been imposed (parallel trends)

Difference in Differences (visual)



Estimating the causal effect: Differenc in Differences

Where y_{ij} is the outcome for treatment group i=1 and post-treatment time j=1

$$DiD = (\bar{y}_{1,1} - \bar{y}_{1,0}) - (\bar{y}_{2,1} - \bar{y}_{2,0})$$

Assuming that the counterfactual outcome for the treatment group has a parallel time trend to that observed for the control group.

Compute the DiD estimator

Compute the DiD estimator

```
## # A tibble: 2 x 3
## location prop_ft_pre prop_ft_post
## <chr> <dbl> <dbl> <dbl>
## 1 NJ 0.297 0.332
## 2 PA 0.310 0.272
```

$$\mathrm{DiD} = (\bar{y}_{1,1} - \bar{y}_{1,0}) - (\bar{y}_{2,1} - \bar{y}_{2,0})$$

Compute the DiD estimator

$$DiD = (\bar{y}_{1,1} - \bar{y}_{1,0}) - (\bar{y}_{2,1} - \bar{y}_{2,0})$$

```
### the DiD Estimator
(0.320 - 0.297) - (0.272 - 0.310)
```

```
## [1] 0.061
```

Descriptive Statistics

Summarizing a variable

Reduce a vector to a single or smaller set of values that tell us something useful

Examples we've already used: - minimum: min() - maximum: max() - median: median() - mean: mean()

Quantiles

- The median is the 0.5 quantile (50th percentile)
- Quantiles are less sensitive to outliers than are other measures (like the mean)
- Quantiles tell you the proportion of a data that falls below some cutpoint

Quantiles: example

```
quantile(minwage$wageBefore, 0.25)
```

```
## 25%
## 4.25
```

Quantiles: example

```
quantile(minwage$wageBefore, 0.75)
```

```
## 75%
## 4.9875
```

Quantiles: example

```
quantile(minwage$wageBefore, c(0.05, 0.25, 0.5, .75, 0.95))
## 5% 25% 50% 75% 95%
## 4.2500 4.2500 4.5000 4.9875 5.2500
```

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- It provides a measure of how much each observation of a variable differs from the mean of the variable

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$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

- The standard deviation (SD, σ) is a measure of the spread of a variable
- It provides a measure of how much each observation of a variable differs from the mean of the variable
- You can use the sd() function in R
- The variance (var() function) is the square of the standard deviation

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

variance =
$$\sigma^2$$

Compute an SD for these variables

Standard deviations and meaningful differences

How meaningful is a ten point difference on a test?

```
### draw 50 random scores from a test with a minimum of zero and maximum of 100
testA<-runif(50, 0, 100)
### draw 50 random scores from a test with a minimum of zero and maximum of 1000
testB<-runif(50, 0, 1000)</pre>
```

Visualizing the distributions

The mean

A 10 point jump from the mean

A 1 SD jump from the mean

Homework

- HW4 posted to Slack
- make sure to use na.rm = TRUE for mean(), quantile() and other functions
- \cdot $group_by(\)$ and $summarize(\)$ are very helpful on this one