Note: time unit conversions

- 1ns = 1e-6 ms = 0.000001 millisecond
- 1 millisecond (ms) = 0.001 seconds
- 1 microsecond = 0.001 millseconds
- alternatively
  - 10e-9 = nanosecond (ns)
  - 10e-6 = microsecond (mu s)
  - 10e-3 = millisecond (ms)

# Computing $\pi$

We now start with the first paralellization tasks. We will

- see how a python application can be parallelized
- discuss data parallelism and task parallelism

We use the example of computing  $\pi$  because it is a simple example that still takes some time to compute, so perfect for our instructional purposes.

The way this works is with Monte-Carlo methods--this means approximating exact results with random numbers and simulation.

### The geometry behind

#### add figure from online material

- · link to online material
- · assume a unit radius
- then the surface of the square is 4r^2
- the surface of the circle is pi r^2
- if we can compute the surfaces, we can call them M for the circle and N for the square
- then we have  $M / N = pi r^2 / 4 r^2$
- solving for pi we get pi = 4 M / N

How do we get M and N?

### Exercise: implement the algorithm (time?)

• using only standard python and the random.uniform function

537 ms  $\pm$  1.77 ms per loop (mean  $\pm$  std. dev. of 7 runs, 1 loop each)

```
In [2]: time_forloop = %timeit -o calc_pi(10**6)
```

Before starting to parallelize, we should make the inner function (the for loop) as efficient as possible. We discuss two options

- 1. vectorization with numpy
- 2. native code generation with numba

Vectorization works by applying the computation over an array of numbers, instead of each number individually.

What does numba do?

- when we execute python code, the line is *interpreted* and directly performed. the speed of this depends on how the programming language is designed (*interpretation*)
- an alternative is *compiled* code, where we write in some language and the translate the code to machine code. Only after this we execute the program. (ahead-of-time compilation)

- numba sits in between the two and performs *just-in-time compilation*. It generates optimized machine code---that is faster than python code---, at runtime. This means that our code is compiled to machine code as we define the function.
  - this is faster than python code but has additional overhead from compiling

#### Numpy

```
In [3]: # can use this to show how to get to the function below
        import numpy as np
        np.random.uniform(-1, 1, (1, 1))
        points = np.random.uniform(-1, 1, (2, 100))
        (points**2).sum(axis=0)
        (points**2).sum(axis=0) < 1
        np.count_nonzero((points**2).sum(axis=0) < 1)</pre>
        M = np.count_nonzero((points**2).sum(axis=0) < 1)</pre>
        4 * M / 100
Out[3]: 3.36
In [4]: def calc_pi_numpy(N):
             "Compute pi using N samples with numpy"
            points = np.random.uniform(-1, 1, (2, N))
            \# M = np.count_nonzero((points**2).sum(axis=0) < 1)
            M = np.count_nonzero((points**2).sum(axis=0) < 1)</pre>
            return 4 * M / N
In [5]: calc pi numpy(10**6)
Out[5]: 3.140208
In [6]: time_numpy = %timeit -o calc_pi_numpy(10**6)
       15.8 ms \pm 103 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
In [7]: speedup = time_forloop.average / time_numpy.average
        print(f"Using numpy is {speedup:.2f} times faster than using the for loop")
       Using numpy is 34.01 times faster than using the for loop
```

This is a *vectorized* version of the algorithm: It demonstrates **data parallelism** where a single operation is applied over a collection of data

This contrasts to **task parallelism** where different independent procedures are applied in parallel. Example: cutting vegetables while simmering the split peas.

#### Discussion: Is this all better?

What are the downside of the vectorized implementation, and of data parallelism in general?

- it uses more memory
- it is perhaps less intuitive
- it is more monolithic and it cannot easily be broken up into parts -- in contrast to the example below.

#### **Challenge: Daskify**

In [10]: calc pi dask(10\*\*6)

Write calc\_pi\_dask to make the numpy version parallel. Compare speed and memory performance with the numpy version. Remember that dask.array mimics the numpy API.

```
In [8]: #can use this to illustrate how get to to the function below
    import dask.array as da
    points = da.random.uniform(-1, 1, (2, 100))
        (points**2).sum(axis=0).compute() < 1
        work = da.count_nonzero((points**2).sum(axis=0) < 1)
        work.compute()

Out[8]: 83

In [9]: def calc_pi_dask(N):
        "Compute pi using N samples with dask"
        points = da.random.uniform(-1, 1, (2, N))
        work = da.count_nonzero((points**2).sum(axis=0) < 1)

        # using the physical number of cores, as we found out in previous episode
        M = work.compute(num_workers=4)
        return 4 * M / N</pre>
```

```
In [11]: time_dask = %timeit -o calc_pi_dask(10**6)
        22.2 ms \pm 89.7 \mus per loop (mean \pm std. dev. of 7 runs, 10 loops each)
In [12]: speedup = time_forloop.average / time_dask.average
         print(f"Using dask is {speedup:.2f} times faster than using the for loop")
        Using dask is 24.20 times faster than using the for loop
         Compare memory and performance
In [13]: from memory profiler import memory usage
         import matplotlib.pyplot as plt
In [14]: # Little wrappers to make life easy
         N = 10**8
         def pi_with_numpy():
              return calc pi numpy(N)
         def pi with dask():
              return calc_pi_dask(N)
In [15]: memory_numpy = memory_usage(pi_with_numpy, interval=0.01)
         time_numpy = %timeit -o pi_with_numpy()
        2.52 \text{ s} \pm 47.8 \text{ ms} per loop (mean \pm \text{ std}. dev. of 7 runs, 1 loop each)
In [16]: memory_dask = memory_usage(pi_with_dask, interval=0.01)
         time dask = %timeit -o pi with dask()
        686 ms \pm 4.41 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
In [17]: speedup = time_numpy.average / time_dask.average
         print(f"Using dask is {speedup:.2f} times faster than using numpy")
        Using dask is 3.68 times faster than using numpy
In [18]: plt.plot(memory_numpy, label="numpy")
         plt.plot(memory dask, label="dask")
         plt.xlabel("Time step")
         plt.ylabel("Memory in MB")
         plt.legend()
         plt.show()
           4000
                        numpy
                        dask
           3500
           3000
        Memory in MB
           2500
           2000
           1500
           1000
            500
               0
                                      100
                    0
                             50
                                               150
                                                        200
                                                                  250
                                                                            300
                                              Time step
```

## Using numba to accelerate python code

Out[10]: 3.143152

numba makes it easy for us to build accelerated functions. We can call the decorator numba.jit. What does it do? -- It sends the function, to which we apply the decorator, to machine code when we execute the cell

```
In [19]: import numba
@numba.jit
def sum_range_numba(a):
    "Compute the sum of the numbers in the range [0, a)"
```

```
x = 0
for i in range(a):
   x += 1
return x
```

```
Let's time three different versions of this.
In [20]: ## Naive python iterators
          time naive = %timeit -o sum(range(10**7))
        122 ms \pm 5.32 ms per loop (mean \pm std. dev. of 7 runs, 10 loops each)
In [21]: # numpy
          time_numpy = %timeit -o np.arange(10**7).sum()
        13.5 ms \pm 11.6 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
In [22]: # numba
          time numba = %timeit -o sum range numba(10**7)
          # sometimes a warning appears "[could be that ..] intermediate result is being cached".
         # re-running usually helps
        132 ns \pm 2.38 ns per loop (mean \pm std. dev. of 7 runs, 10,000,000 loops each)
In [23]: speedup = time numpy.average / time numba.average
          print(f"Using numba is {speedup:.2f} times faster than using numpy")
        Using numba is 102703.03 times faster than using numpy
          So, numba is 100k times faster (?)
          (14.7.5 * 10e-3) / (128 * 10e-9) = (17.5 * 10e-3) / (12.8 * 10e-8) = 10e-5
          numba JIT does not work on every python or numpy feature, but a function is a good candidate if written with a python for-loop over a
          large range of values, as with sum range numba().
          Note on just-in-time compilation
```

- there may be little or no speed-up when function is called the first time
- similarly, when using timeit you may get the following message
  - The slowest run took 14.83 times longer than the fastest. This could mean that an intermediate result is being cached.
- reason: on the first call, the JIT compiler needs to compile the function. on subsequent runs, the function is reused
- . the same function can only be reused if it is called with the same argument types (int, float, etc)

```
In [24]: %time sum range numba(10**7)
        CPU times: user 2 μs, sys: 1 μs, total: 3 μs
        Wall time: 5.01 \mu s
Out[24]: 10000000
In [25]: %time sum range numba(10.**7)
        CPU times: user 32.4 ms, sys: 136 \mus, total: 32.5 ms
        Wall time: 39 ms
Out[25]: 1000000
In [26]: %time sum range numba(10.**7)
        CPU times: user 3 \mus, sys: 1 \mus, total: 4 \mus
        Wall time: 5.72 µs
Out[26]: 10000000
         Challenge: numbify calc pi
         Create a numba version of calc pi. Time it.
In [27]: # note we're moving back to a function that looks similar to the original function
         @numba.jit
```

```
def calc pi numba(N):
    "Compute pi using N samples with numba"
    M = 0
    for i in range(N):
       # Simulate random coordinates
        x = random.uniform(-1, 1)
        y = random.uniform(-1, 1)
        if x^{**2} + y^{**2} < 1.0: # don't need sqrt b/c 1^{**2} = 1
            M += 1
    return 4*M/N
```

also: random number generator changes

Using numba is 103.68 times faster than using dask

## Conclusion

- measuring knowing: always profile your code to see which parallelization method works best
- numba often outperforms other methods, but it is not always possible to rewrite code so that one can use numba with it

Processing math: 100%