$$e = \lim_{n \to \infty} \left(1 + \frac{1}{n}\right)^{1 \cdot n}$$

The base for continuous growth is
the unit quantity earning unit interest for unit time,
compounded as fast as possible