

$$e = \lim_{n \rightarrow \infty} \left( 1 + \frac{1}{n} \right)^{1 \cdot n}$$

The base for continuous growth is  
the unit quantity earning unit interest for unit time,  
compounded as fast as possible