

Fig. 1 Moon Phase Angle

x''y''-axes = fixed frame of Sun

 ψ = moon phase angle = $\pi/2 + (\phi - \theta)$