

# Learning For Search Result Diversification

Paper Presentation

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Why use search result diversification ?

To tackle the ambiguous or multi-faceted information  
needs of different users

## Existing methods:

- heuristic predefined ranking function; implicit and explicit methods.
- Usually are “based on greedy approximation, which sequentially select a ‘local-best’ document from the remanent candidate set”

## Proposed Solution:

- Relational Learning To Rank framework
- New definitions for ranking function and loss function based on the foundation of sequential selection process for diverse ranking.

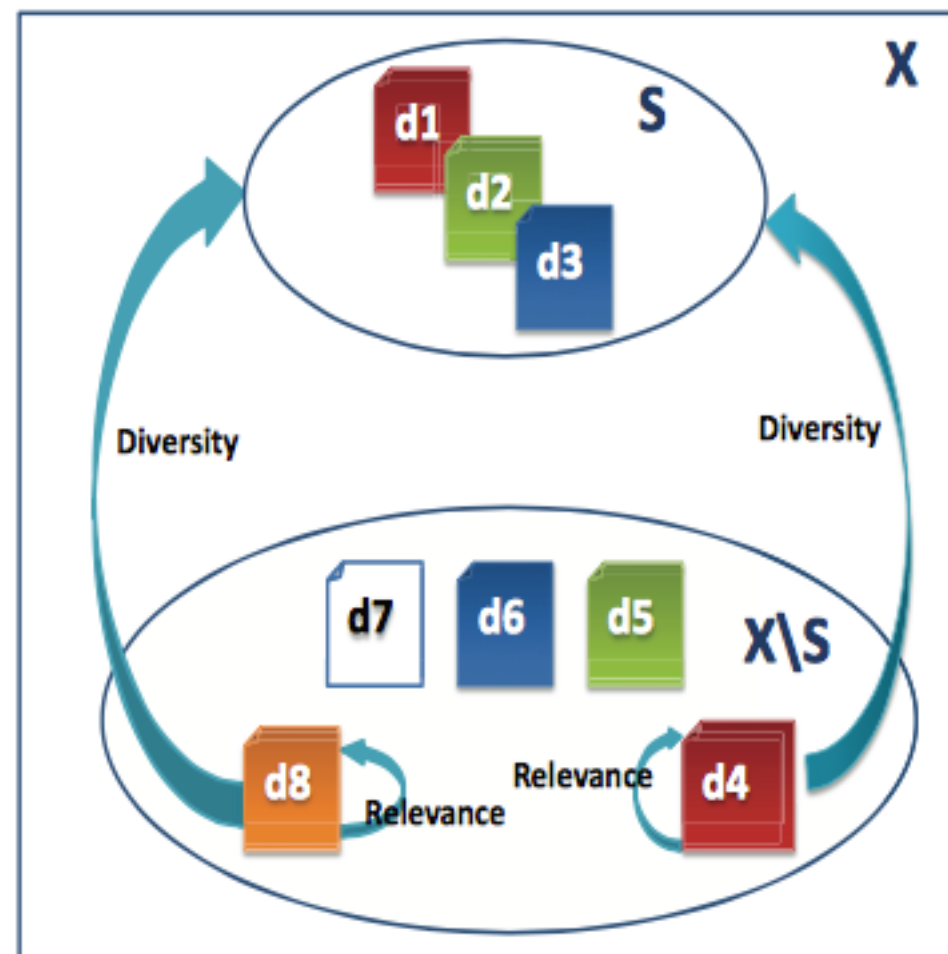
## Definitions:

- Ranking Function: “the combination of relevance score and diversity score”
- loss function: “the likelihood loss of the generation probability”

# R-LTR

- Documents ranking is obtained by looking to the document's relevance AND the relations between documents

# Adding a new document to the ranking list in a sequential order



# R-LTR: Ranking Function

$$f_S(x_i, R_i) = \omega_r^T \mathbf{x}_i + \omega_d^T h_S(R_i), \forall x_i \in X \setminus S, \quad (2)$$

where :

$x_i$  : the relevance feature vector of the candidate document  $x_i$

$R_i$  : the matrix of relationships between document  $x_i$  and other selected documents

$h_S(R_i)$  : the relational function on  $R_i$

$\omega_r^T$  &  $\omega_d^T$  : the corresponding relevance and diversity weight vector



# R-LTR: Ranking Function

$h_S(R_i)$ : represents the diversity relationship between the current document  $x_i$  and the previously selected documents in  $S$ .

In the paper,  $h_S(R_i)$  is presented as the distance of  $x_i$  to the set  $S$ , thus  $h_S(R_i)$  can be represented by three ways:

- **Minimal Distance:** the distance between a document  $x$  and a set  $S$  is defined as the minimal distance of all the document pairs  $(x, x_i), x_i \in S$ .
- **Average Distance:** The distance between a document  $x$  and a set  $S$  is defined as the average distance of all the document pairs  $(x, x_i), x_i \in S$ .
- **Maximal Distance:** The distance between a document  $x$  and a set  $S$  is defined as the maximal distance of all the document pairs  $(x, x_i), x_i \in S$ .

# How to capture Diversity

- **Semantic Diversity:**
  - Subtopic Diversity
  - Text Diversity
  - title diversity
  - anchor text diversity
  - ODP-based diversity; using existing ODP taxonomy, “the distance between documents on similar topics in the taxonomy is likely to be small”
- **Structural Diversity:**
  - linked-based diversity, and URL-based diversity

# Constructing Training Data

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**Algorithm 1 Construction of Approximate Ideal Ranking List**

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**Input:**

$$(q_i, X^{(i)}, \mathbf{T}_i, P(x_j^{(i)}|t)), t \in \mathbf{T}_i, x_j^{(i)} \in X^{(i)}$$

**Output:**  $\mathbf{y}^{(i)}$

1: Initialize  $S_0 \leftarrow \emptyset, \mathbf{y}^{(i)} = (1, \dots, n_i)$

2: **for**  $k = 1, \dots, n_i$  **do**

3:   bestDoc  $\leftarrow \operatorname{argmax}_{x \in X^{(i)} \setminus S_{k-1}} ODM(S_{k-1} \cup x)$

4:    $S_k \leftarrow S_{k-1} \cup \text{bestDoc}$

5:    $y^{(i)}(k) = \text{the index of bestDoc}$

6: **end for**

7: **return**  $\mathbf{y}^{(i)} = (y^{(i)}(1), \dots, y^{(i)}(n_i)).$

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# Optimization Process

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**Algorithm 2 Optimization Algorithm**

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**Input:** training data  $\{(X^{(i)}, R^{(i)}, \mathbf{y}^{(i)})\}_{i=1}^N$ ,  
parameter: learning rate  $\eta$ , tolerance rate  $\epsilon$

**Output:** model vector:  $\omega_r, \omega_d$

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1: Initialize parameter value  $\omega_r, \omega_d$ 
2: repeat
3:   Shuffle the training data
4:   for  $i = 1, \dots, N$  do
5:     Compute gradient  $\Delta\omega_r^{(i)}$  and  $\Delta\omega_d^{(i)}$ 
6:     Update model:  $\omega_r = \omega_r - \eta \times \Delta\omega_r^{(i)}$ ,  
                    $\omega_d = \omega_d - \eta \times \Delta\omega_d^{(i)}$ 
7:   end for
8:   Calculate likelihood loss on the training set
9: until the change of likelihood loss is below  $\epsilon$ 
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# Ranking Prediction

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**Algorithm 3 Ranking Prediction via Sequential Selection**

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**Input:**  $X^{(t)}, R^{(t)}, \omega_r, \omega_d$

**Output:**  $\mathbf{y}^{(t)}$

- 1: Initialize  $S_0 \leftarrow \emptyset, \mathbf{y}^{(t)} = (1, \dots, n_t)$
  - 2: **for**  $k = 1, \dots, n_t$  **do**
  - 3:   bestDoc  $\leftarrow \operatorname{argmax}_{x \in X_t} f_{S_{k-1}}(x, R)$
  - 4:    $S_k \leftarrow S_{k-1} \cup \text{bestDoc}$
  - 5:    $y^{(t)}(k) \leftarrow$  the *index* of bestDoc
  - 6: **end for**
  - 7: **return**  $\mathbf{y}^{(t)} = (y^{(t)}(1), \dots, y^{(t)}(n_t))$
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# Feature Importance Analysis

**Table 6: Order list of diversity features with corresponding weight value.**

feature	weight
$R_{ij1}(\text{topic})$	3.71635
$R_{ij3}(\text{title})$	1.53026
$R_{ij4}(\text{anchor})$	1.34293
$R_{ij2}(\text{text})$	0.98912
$R_{ij5}(\text{ODP})$	0.52627
$R_{ij6}(\text{Link})$	0.04683
$R_{ij7}(\text{URL})$	0.01514

## Evaluation:

- TREC dataset.
- Intent-aware measures: Precision-IA & Subtopic recall
- Performance comparison with state-of-art approaches

# Experiment Setup

## Implementation:

- Retrieval platform: Indri toolkit
- Data processing: porter stemmer and stopwords removing for both indexing and query processing.



# Evaluation Results

**Table 2: Performance comparison of all methods in official TREC diversity measures for WT2009.**

Method	ERR-IA	$\alpha$ -NDCG	NRBP
QL	0.1637	0.2691	0.1382
ListMLE	0.1913 (+16.86%)	0.3074 (+14.23%)	0.1681 (+21.64%)
MMR <sub>list</sub>	0.2022 (+23.52%)	0.3083 (+14.57%)	0.1715 (+24.09%)
xQuAD <sub>list</sub>	0.2316 (+41.48%)	0.3437 (+27.72%)	0.1956 (+41.53%)
PM-2 <sub>list</sub>	0.2294 (+40.13%)	0.3369 (+25.20%)	0.1788 (+29.38%)
SVMDIV	0.2408 (+47.10%)	0.3526 (+31.03%)	0.2073 (+50.00%)
R-LTR <sub>min</sub>	<b>0.2714</b> (+65.79%)	0.3915 (+45.48%)	<b>0.2339</b> (+69.25%)
R-LTR <sub>avg</sub>	0.2671 (+63.16%)	<b>0.3964</b> (+47.31%)	0.2268 (+64.11%)
R-LTR <sub>max</sub>	0.2683 (+63.90%)	0.3933 (+46.15%)	0.2281 (+65.05%)
TREC-Best	0.1922	0.3081	0.1617

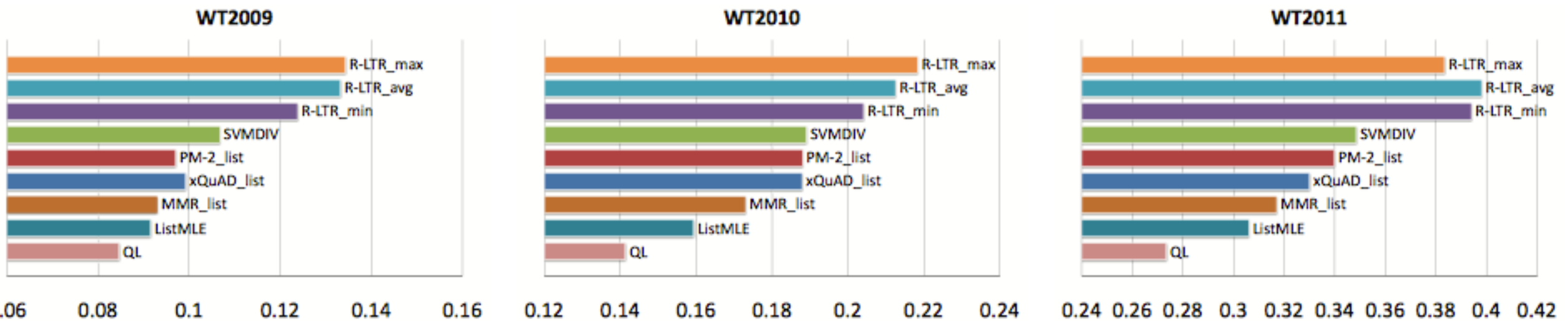
**Table 3: Performance comparison of all methods in official TREC diversity measures for WT2010.**

Method	ERR-IA	$\alpha$ -NDCG	NRBP
QL	0.1980	0.3024	0.1549
ListMLE	0.2436 (+23.03%)	0.3755 (+24.17%)	0.1949 (+25.82%)
MMR <sub>list</sub>	0.2735 (+38.13%)	0.4036 (+33.47%)	0.2252 (+45.38%)
xQuAD <sub>list</sub>	0.3278 (+65.56%)	0.4445 (+46.99%)	0.2872 (+85.41%)
PM-2 <sub>list</sub>	0.3296 (+66.46%)	0.4478 (+48.08%)	0.2901 (+87.28%)
SVMDIV	0.3331 (+68.23%)	0.4593 (+51.88%)	0.2934 (+89.41%)
R-LTR <sub>min</sub>	<b>0.3647</b> (+84.19%)	<b>0.4924</b> (+62.83%)	<b>0.3293</b> (+112.59%)
R-LTR <sub>avg</sub>	0.3587 (+81.16%)	0.4781 (+58.10%)	0.3125 (+101.74%)
R-LTR <sub>max</sub>	0.3639 (+83.79%)	0.4836 (+59.92%)	0.3218 (+107.74%)
TREC-Best	0.2981	0.4178	0.2616

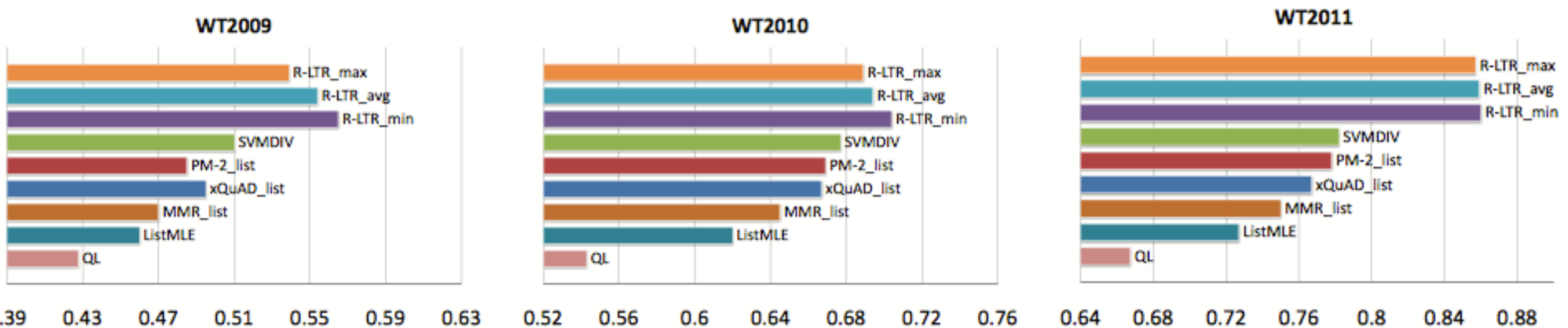
# Some Highlights of the Comparison

- explicit methods(xQuAD & PM-2) outperformed implicit methods (MMR) in the test
- “SVMDIV simply uses weighted word coverage as a proxy for explicitly covering subtopics, while our R-LTR approach directly models the generation probability of the diverse ranking based on the sequential ranking formulation.”
- R-LTR outperformance is significantly different (p-value  $<0.01$ )

# Evaluation on Traditional Diversity Metrics



**Figure 2: Performance comparison of all methods in Precision-IA for WT2009, WT2010, WT2011.**



**Figure 3: Performance comparison of all methods in Subtopic Recall for WT2009, WT2010, WT2011.**

# Robustness Analysis

**Table 5: The robustness of the performance of all diversity methods in Win/Loss ratio**

	WT2009	WT2010	WT2011	<i>Total</i>
ListMLE	20/18	27/16	26/11	73/45
MMR <sub>list</sub>	22/15	29/13	29/10	80/38
xQuAD <sub>list</sub>	28/11	31/12	31/12	90/35
PM-2 <sub>list</sub>	26/15	32/12	32/11	90/38
SVMDIV	30/12	32/11	32/11	94/34
R-LTR <sub>min</sub>	<b>34/9</b>	<b>35/10</b>	<b>35/9</b>	<b>104/28</b>
R-LTR <sub>avg</sub>	33/9	34/11	34/10	101/30
R-LTR <sub>max</sub>	33/10	35/10	34/10	102/30

# Future improvements

- Algorithms running time :  $O(n * K)$
- Average training time:

ListMLE ( $\sim 1.5h$ ) < SVMDIV ( $\sim 2h$ ) < R-LTR ( $\sim 3h$ )

# Discussion

- where would this approach be most useful?
- what features that you think should be considered in this approach ?
- what parts of the paper needs more clarification ?

# Source Paper

Learning for Search Result Diversification

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