

ARJUN BHATTI – Assignment 1 – 100915440 – ELEC 4700

Part 1: Electron Modelling

```
clc
clear all
%% constants

m0 = 9.10938356e-31;
m = 0.26*m0;
T = 300;
k = 1.38064852e-23;
VTH = sqrt(2*k*T/m)*.0010 % formula
disp("187 km/hr");
MFP = VTH*0.2;
disp(MFP); %% nm
```

1. What is the thermal velocity v_{th} ? Assume $T = 300K$. $VTH = 187.0191$ km/hr
2. If the mean time between collisions is $\tau_{mn} = 0.2ps$ what is the mean free path? $MFP=37.4038$ nm

Variables used :

```
H = 100e-9; %Height
L = 200e-9; %length
population_size = 3000;
Population_toPlot = 20; % values from pdf
time = H/VTH/100;
iterations = 1000; % from pdf
Movie_ONOFF = 0; % movie =1 or 0 for no movie

% generating matrix with zeroes.includes velocity and position
Matrix1 = zeros(population_size, 4);
Zeroes = zeros(iterations, Population_toPlot*2);
Zeroes1 = zeros(iterations,1); %Zeroes1
```

Q3 • Assign each particle a random location in the $x - y$ plane within the region defined by the extent of the Silicon. For simplicity you may use a small number of particles (1000-10000 works well) but you can start much smaller initially if you like.

- Assign each particle with the fixed velocity given by v_{th} but give each one a random direction.
 - At a fixed time interval of $4t$, update the particle location using Newton's laws of motion. You will need to pick a time step size that takes into account the velocity of your particles and the size of the region. Typically the spacial step should be smaller than $1/100$ of the region size. Simulate for nominally 1000 timesteps. This should allow each particle to bounce around quite a bit inside the region.
 - For a few of the particles trace out their trajectories using the 'plot' command in Matlab. To plot the trajectories you should keep the previous x and y positions.
- use the 'pause' command in Matlab to have the plot update in a loop.
- Show a 2-D plot of all (or a subset) of the particles that updates with each time step. Hint: use the 'pause' command in Matlab to have the plot update in a loop.

- For the y direction use a boundary condition where the particle reflects at the same angle (specular) and retains its velocity.
- For the x direction use a periodic boundary condition where the particle jumps to the opposite edge. i.e. if it reaches the right side it appears at the left with the same velocity.
- Calculate and display the semiconductor temperature on the plot at a fixed time interval and verify that it stays constant.
- Your program should plot trace trajectories producing something like Figure

```
% initial population - for figure 1

for i = 1:population_size
    angle = 2*pi*rand;
    Matrix1(i,:) = [L*rand H*rand VTH*cos(angle) VTH*sin(angle)];
end

%iteration over time - changes matrix1
for i = 1:iterations
    Matrix1(:,1:2) = Matrix1(:,1:2) + time.*Matrix1(:,3:4);

    j = Matrix1(:,1) > L;
    %greter than length
    Matrix1(j,1) = Matrix1(j,1) - L;

    j = Matrix1(:,1) < 0;
    Matrix1(j,1) = Matrix1(j,1) + L;

    j = Matrix1(:,2) > H; %greater than height
    Matrix1(j,2) = 2*H - Matrix1(j,2);
    Matrix1(j,4) = -Matrix1(j,4);

    j = Matrix1(:,2) < 0;
    Matrix1(j,2) = -Matrix1(j,2);
    Matrix1(j,4) = -Matrix1(j,4);

    Zeroes1(i) = (sum(Matrix1(:,3).^2) +
    sum(Matrix1(:,4).^2))*m/k/2/population_size;
```

```

% Record the Zeroes
for j=1:Population_toPlot
    Zeroes(i, (2*j):(2*j+1)) = Matrix1(j, 1:2);
end

% create movie every 5 changes

if Movie_ONOFF && mod(i,5) == 0
    figure(1);
    subplot(2,1,1);
    hold off;
    plot(Matrix1(1:Population_toPlot,1)./1e-9,
Matrix1(1:Population_toPlot,2)./1e-9, 'O');
    axis([0 L/1e-9 0 H/1e-9]);
    title(sprintf('Zeroes for %d of %d Electrons with Fixed
Velocity (Part 1)',...
Population_toPlot, population_size));
    xlabel(' x - (nm) ');
    ylabel(' y - (nm) ');

if i > 1
    subplot(2,1,2);
    hold off;
    plot(time *(0:i-1), Zeroes1(1:i));
    axis([0 time *iterations min(Zeroes1)*0.98
max(Zeroes1)*1.02]);
    title('Semiconductor');
    xlabel('Time (s) ');
    ylabel('Temp (K) ');
end
    pause(0.02);
end
end

% Figure 1 shows movement of electrons with constant
velocity, along with Time vs temperature graph.
figure(1);
subplot(2,1,1);
title(sprintf('Electron Zeroes for %d of %d Electrons with Fixed
Velocity (Part 1)',...
Population_toPlot, population_size));
xlabel('x (nm) ');
ylabel('y (nm) ');
axis([0 L/1e-9 0 H/1e-9]);
hold on;

```

```

for i=1:Population_toPlot
    plot(Zeroes(:,i*2)./1e-9, Zeroes(:,i*2+1)./1e-9, '.');
end

if(~Movie_ONOFF)
    subplot(2,1,2);
    hold off;
    plot(time *(0:iterations-1), Zeroes1);
    axis([0 time *iterations min(Zeroes1)*0.98 max(Zeroes1)*1.02]);
    title(' N-type Si semiconductor crystal@ 300K');
    xlabel('Time (s)');
    ylabel(' (K) ');
end

```

```

%% Part 2: Collisions with Mean Free Path
% Maxwell-Boltzmann distribution

```

```

p_scatt = 1 - exp(-time /0.2e-12)

```

p_scatt =

0.0264

avg_v =

1.8699e+05

Histogram :

```

% Show histogram of speeds

```

```

subplot(3,1,3);

```

```

b = sqrt(Matrix1(:,3).^2 + Matrix1(:,4).^2);

```

```

title('Histogram of Electron Speeds');

```

```

histogram(b);

```

```

xlabel('Speed (m/s)');

```

```

ylabel('Number of particles');

```

```
pause(0.05);
```

Part 3: **Enhancements**

```
% create box as obstacles.
```

```
% create simulation for boxes.
```

```
% each box values
```

```
boxes = 1e-9.*[80 120 0 40; 80 120 60 100];
```

```
boxes_specular = [0 1];
```

```
for i = 1:iterations
```

```
Matrix1(:,1:2) = Matrix1(:,1:2) + time .*Matrix1(:,3:4);
```

```
j = Matrix1(:,1) > L;
```

```
Matrix1(j,1) = Matrix1(j,1) - L;
```

```
j = Matrix1(:,1) < 0;
```

```
Matrix1(j,1) = Matrix1(j,1) + L;
```

```
j = Matrix1(:,2) > H;
```

```
top_Value =0;
```

```
bottom_val =0;
```

```
if(top_Value)
```

```
Matrix1(j,2) = 2*H - Matrix1(j,2);
```

```
Matrix1(j,4) = -Matrix1(j,4);
```

```
else % Diffusive
```

```
% The electron bounces off at a random angle
```

```
Matrix1(j,2) = H;
```

```
b = sqrt(Matrix1(j,3).^2 + Matrix1(j,4).^2);
```

```
angle = rand([sum(j),1])*2*pi;
```

```
Matrix1(j,3) = b.*cos(angle);
```

```
Matrix1(j,4) = -abs(b.*sin(angle));
```

```
End
```

```
% Scatter particles
```

```
j = rand(population_size, 1) < p_scatter;
```

```
Matrix1(j,3:4) = random(v_pdf, [sum(j),2]);
```

```
Zeroes1(i) = (sum(Matrix1(:,3).^2 +  
sum(Matrix1(:,4).^2))*m/k/2/population_size;
```

```
-----  
subplot(3,1,3);
```

```
b = sqrt(Matrix1(:,3).^2 + Matrix1(:,4).^2);
```

```
title('Histogram of Electron Speeds');
```

```
histogram(b);
```

```
xlabel('Speed (m/s)');
```

```
ylabel('# of particles');
```

```
pause(0.03);
```

References

<https://github.com/villetiukuvaara/elec-4700-assignment-1>. (n.d.). Retrieved from github.com.