

公式(7)和(8)的推导，推导过程中请注意 a_k 与 b_k 在窗口 w_k 中是恒定的：

$$\begin{aligned}
 0 &= \frac{\partial E}{\partial b_k} = \sum_{i \in w_k} 2(a_k I_i + b_k - p_i) \\
 b_k &= \sum_{i \in w_k} (p_i - a_k I_i) \\
 &= \sum_{i \in w_k} p_i - a_k \sum_{i \in w_k} I_i \\
 &= \bar{p}_k - a_k \mu_k
 \end{aligned} \tag{1-1}$$

$$\begin{aligned}
 0 &= \frac{\partial E}{\partial a_k} = \sum_{i \in w_k} (2(a_k I_i + b_k - p_i)I_i + 2\varepsilon a_k) \\
 &= \sum_{i \in w_k} ((a_k I_i + b_k - p_i)I_i + \varepsilon a_k) \\
 &= \sum_{i \in w_k} ((a_k I_i + \bar{p}_k - a_k \mu_k - p_i)I_i + \varepsilon a_k) \\
 &= \sum_{i \in w_k} ((a_k I_i^2 + \varepsilon a_k - a_k \mu_k I_i) + (\bar{p}_k - p_i)I_i) \\
 a_k &= \frac{\sum_{i \in w_k} (p_i - \bar{p}_k)I_i}{\sum_{i \in w_k} (I_i^2 + \varepsilon - \mu_k I_i)} \\
 &= \frac{\sum_{i \in w_k} p_i I_i - \bar{p}_k \sum_{i \in w_k} I_i}{\sum_{i \in w_k} (I_i^2 + \varepsilon - \mu_k I_i)} \\
 &= \frac{\frac{1}{|w|} \sum_{i \in w_k} p_i I_i - \frac{1}{|w|} \bar{p}_k \sum_{i \in w_k} I_i}{\frac{1}{|w|} \sum_{i \in w_k} (I_i^2 + \varepsilon - \mu_k I_i)} \\
 &= \frac{\frac{1}{|w|} \sum_{i \in w_k} p_i I_i - \bar{p}_k \mu_k}{\frac{1}{|w|} \sum_{i \in w_k} (I_i^2 - \mu_k I_i) - \varepsilon} \\
 &= \frac{\frac{1}{|w|} \sum_{i \in w_k} p_i I_i - \bar{p}_k \mu_k}{\frac{1}{|w|} \sum_{i \in w_k} I_i^2 - \frac{1}{|w|} \mu_k \sum_{i \in w_k} I_i - \varepsilon} \\
 &= \frac{\frac{1}{|w|} \sum_{i \in w_k} p_i I_i - \bar{p}_k \mu_k}{\frac{1}{|w|} \sum_{i \in w_k} I_i^2 - \mu_k^2 - \varepsilon} \\
 &= \frac{\frac{1}{|w|} \sum_{i \in w_k} p_i I_i - \bar{p}_k \mu_k}{\delta_k^2 - \varepsilon}
 \end{aligned} \tag{1-2}$$