Status Oct3 2021.

CALPERE function (additional comments to the TXT file):

it calculates the perimeter of an ellipse by the given halfparameter a and b.

HowTo (can be done manually; take only b>a):

- a) solve **t** which will verify ((pi/4)*t**AE) ((1/2) (SQRT(2)/pi))*sin(pi*t) = (pi/2) atan (b/a)
- b) with the **t** from above, calculate $\frac{(SQRT(a^{**}2+b^{**}2))}{(1-((1/2)-(SQRT(2)/pi)^*(cos(pi^*t)-1))}$
- c).. the result of it is your perimeter

AE = 1000*ae (ae=1.15965218091; see page 3 of https://www.physik.uzh.ch/dam/jcr:3efb63a6-21c8-4481-bbb0-c0e2a4aa4d8d/kt19 protonff.pdf or page 56 of https://arxiv.org/pdf/1909.12245.pdf which is called the electron magnetic moment anomaly, ae, is: ae $\approx 1.15965218091 \times 10^{-3}$ see page 351 of ISBN 978-3-030-36418-2).

Why this "ae" factor (from quantum mechanic) appear here is not explained for now.

Maximum deviation of the CALPERE calculus: 0.025% on the HP41 with the current SOLVING and serial calculation setups. See results below of CMPPERE for 100 steps of an isoperimeter of 4.

CALPERE cannot be considered for now as an approximation function:

- a) identification of used curve of type "cycloid" and a point of it must be found (numerically)
- b) constant ae from quantum mechanic is used

ELLIPSE CALC ISOPERIME OF 4.000000000 *** IN 100.0000000 *** STEPS

X & Y

0.636619771 *** 0.636619774 ***

CALPERE

4.000000000 ***

in % vs PERIM: 0.000000000 *** **RADIUS & ANGLE** 0.900316316 *** 0.785398162 *** -----X & Y 0.630253573 *** 0.642954297 *** **CALPERE** 4.000003944 *** in % vs PERIM: 0.000098600 *** **RADIUS & ANGLE** 0.900338711 *** 0.775423121 *** -----X & Y 0.623887376 *** 0.649226087 *** **CALPERE** 4.000015216 *** in % vs PERIM: 0.000380400 *** **RADIUS & ANGLE** 0.900405447 *** 0.765497843 *** -----X & Y 0.617521178 *** 0.655436030 *** **CALPERE** 4.000033028 *** in % vs PERIM:

0.000825700 ***
RADIUS & ANGLE
0.900515849 ***
0.755622107 ***

X & Y

0.611154980 ***

0.661584965 ***

CALPERE

4.000056620 ***

in % vs PERIM:

0.001415500 ***

RADIUS & ANGLE

0.900669238 ***

0.745795715 ***

X & Y

0.604788783 ***

0.667673702 ***

CALPERE

4.000085280 ***

in % vs PERIM:

0.002132000 ***

RADIUS & ANGLE

0.900864942 ***

0.736018477 ***

X & Y

0.598422585 ***

0.673703000 ***

CALPERE

4.000118324 ***

in % vs PERIM:

0.002958100 ***

RADIUS & ANGLE 0.901102282 *** 0.726290222 *** X & Y 0.592056387 *** 0.679673589 *** **CALPERE** 4.000155124 *** in % vs PERIM: 0.003878100 *** **RADIUS & ANGLE** 0.901380582 *** 0.716610789 *** -----X & Y 0.585690189 *** 0.685586159 *** **CALPERE** 4.000195048 *** in % vs PERIM: 0.004876200 *** **RADIUS & ANGLE** 0.901699162 *** 0.706980030 *** -----X & Y 0.579323992 *** 0.691441368 *** **CALPERE** 4.000237536 ***

in % vs PERIM: 0.005938400 *** RADIUS & ANGLE

CALPERE

4.000282048 ***

in % vs PERIM:

0.007051200 ***

RADIUS & ANGLE

0.902454450 ***

0.687863968 ***

X & Y

0.566591596 ***

0.702982181 ***

CALPERE

4.000328068 ***

in % vs PERIM:

0.008201700 ***

RADIUS & ANGLE

0.902889796 ***

0.678378402 ***

X & Y

0.560225399 ***

0.708668945 ***

CALPERE

4.000375116 ***

in % vs PERIM:

0.009377900 ***

RADIUS & ANGLE

0.903362702 ***

```
0.668940980 ***
X & Y
0.553859201 ***
0.714300676 ***
CALPERE
4.000422752 ***
in % vs PERIM:
0.010568800 ***
RADIUS & ANGLE
0.903872485 ***
0.659551579 ***
X & Y
0.547493003 ***
0.719877883 ***
CALPERE
4.000470552 ***
in % vs PERIM:
0.011763800 ***
```

X & Y
0.541126806 ***
0.725401051 ***
CALPERE
4.000518120 ***
in % vs PERIM:
0.012953000 ***
RADIUS & ANGLE
0.904999947 ***
0.640916370 ***

RADIUS & ANGLE 0.904418463 *** 0.650210081 ***

X & Y

0.534760608 ***

0.730870638 ***

CALPERE

4.000565080 ***

in % vs PERIM:

0.014127000 ***

RADIUS & ANGLE

0.905616253 ***

0.631670329 ***

X & Y

0.528394410 ***

0.736287080 ***

CALPERE

4.000611100 ***

in % vs PERIM:

0.015277500 ***

RADIUS & ANGLE

0.906266692 ***

0.622471841 ***

X & Y

0.522028212 ***

0.741650789 ***

CALPERE

4.000655856 ***

in % vs PERIM:

0.016396400 ***

RADIUS & ANGLE

0.906950576 ***

0.613320789 ***

0.515662015 *** 0.746962154 *** **CALPERE** 4.000699064 *** in % vs PERIM: 0.017476600 *** **RADIUS & ANGLE** 0.907667215 *** 0.604217052 *** -----X & Y 0.509295817 *** 0.752221542 *** CALPERE 4.000740440 *** in % vs PERIM: 0.018511000 *** **RADIUS & ANGLE** 0.908415916 *** 0.595160507 *** X & Y 0.502929619 *** 0.757429298 *** **CALPERE** 4.000779744 *** in % vs PERIM: 0.019493600 *** **RADIUS & ANGLE** 0.909195988 *** 0.586151030 *** X & Y

X & Y

0.496563422 *** 0.762585748 *** **CALPERE** 4.000816744 *** in % vs PERIM: 0.020418600 *** **RADIUS & ANGLE** 0.910006733 *** 0.577188492 *** X & Y 0.490197224 *** 0.767691194 *** **CALPERE** 4.000851224 *** in % vs PERIM: 0.021280600 *** **RADIUS & ANGLE** 0.910847455 *** 0.568272761 *** X & Y 0.483831026 *** 0.772745923 *** **CALPERE** 4.000883004 *** in % vs PERIM: 0.022075100 *** **RADIUS & ANGLE** 0.911717458 *** 0.559403698 *** X & Y 0.477464829 ***

0.777750203 *** **CALPERE** 4.000911916 *** in % vs PERIM: 0.022797900 *** **RADIUS & ANGLE** 0.912616042 *** 0.550581161 *** X & Y 0.471098631 *** 0.782704277 *** **CALPERE** 4.000937796 *** in % vs PERIM: 0.023444900 *** **RADIUS & ANGLE** 0.913542503 *** 0.541805003 *** X & Y 0.464732433 *** 0.787608376 *** **CALPERE** 4.000960524 *** in % vs PERIM: 0.024013100 *** **RADIUS & ANGLE** 0.914496139 *** 0.533075070 *** X & Y 0.458366235 *** 0.792462713 ***

CALPERE 4.000979972 *** in % vs PERIM: 0.024499300 *** **RADIUS & ANGLE** 0.915476246 *** 0.524391202 *** X & Y 0.452000038 *** 0.797267478 *** CALPERE 4.000996044 *** in % vs PERIM: 0.024901100 *** **RADIUS & ANGLE** 0.916482114 *** 0.515753235 *** X & Y 0.445633840 *** 0.802022846 *** **CALPERE** 4.001008652 *** in % vs PERIM: 0.025216300 *** **RADIUS & ANGLE** 0.917513033 *** 0.507160997 *** X & Y 0.439267642 *** 0.806728980 ***

CALPERE

```
4.001017728 ***
in % vs PERIM:
0.025443200 ***
RADIUS & ANGLE
0.918568293 ***
0.498614307 ***
X & Y
0.432901445 ***
0.811386019 ***
CALPERE
4.001023220 ***
in % vs PERIM:
0.025580500 ***
RADIUS & ANGLE
0.919647178 ***
0.490112982 ***
-----
X & Y
0.426535247 ***
0.815994091 ***
CALPERE
4.001025092 ***
in % vs PERIM:
0.025627300 *** Worst of all
RADIUS & ANGLE
0.920748974 ***
0.481656826 ***
-----
X & Y
0.420169049 ***
0.820553300 ***
CALPERE
4.001023308 ***
```

in % vs PERIM: 0.025582700 *** **RADIUS & ANGLE** 0.921872957 *** 0.473245642 *** -----X & Y 0.413802852 *** 0.825063741 *** CALPERE 4.001017860 *** in % vs PERIM: 0.025446500 *** **RADIUS & ANGLE** 0.923018405 *** 0.464879221 *** -----X & Y 0.407436654 *** 0.829525492 *** **CALPERE** 4.001008760 *** in % vs PERIM: 0.025219000 *** **RADIUS & ANGLE** 0.924184596 *** 0.456557347 *** -----X & Y 0.401070456 *** 0.833938609 *** **CALPERE** 4.000996016 ***

in % vs PERIM:

0.024900400 ***
RADIUS & ANGLE
0.925370799 ***
0.448279800 ***

X & Y

0.394704258 ***

0.838303140 ***

CALPERE

4.000979660 ***

in % vs PERIM:

0.024491500 ***

RADIUS & ANGLE

0.926576282 ***

0.440046346 ***

X & Y

0.388338061 ***

0.842619108 ***

CALPERE

4.000959732 ***

in % vs PERIM:

0.023993300 ***

RADIUS & ANGLE

0.927800307 ***

0.431856751 ***

X & Y

0.381971863 ***

0.846886528 ***

CALPERE

4.000936296 ***

in % vs PERIM:

0.023407400 ***

0.369239468 *** 0.855275685 ***

CALPERE

4.000879168 ***

in % vs PERIM:

0.021979200 ***

RADIUS & ANGLE

0.931576235 ***

0.407548602 ***

X & Y

0.362873270 ***

0.859397363 ***

CALPERE

4.000845660 ***

in % vs PERIM:

0.021141500 ***

RADIUS & ANGLE

0.932866999 *** 0.399531893 *** X & Y 0.356507072 *** 0.863470377 *** **CALPERE** 4.000809004 *** in % vs PERIM: 0.020225100 *** **RADIUS & ANGLE** 0.934172567 *** 0.391557729 *** -----X & Y 0.350140875 *** 0.867494652 *** **CALPERE** 4.000769304 *** in % vs PERIM: 0.019232600 *** RADIUS & ANGLE 0.935492172 *** 0.383625826 *** 0.343774677 *** 0.871470107 *** 4.000726716 ***

-----X & Y **CALPERE** in % vs PERIM: 0.018167900 *** **RADIUS & ANGLE** 0.936825051 ***

X & Y
0.331042281 ***
0.879274103 ***
CALPERE
4.000633432 ***
in % vs PERIM:
0.015835800 ***
RADIUS & ANGLE
0.939527509 ***
0.360080689 ***

...

X & Y 0.324676084 *** 0.883102388 *** CALPERE 4.000583084 *** in % vs PERIM: 0.014577100 *** RADIUS & ANGLE 0.940895524 *** 0.352314798 *** -----

X & Y

0.318309886 ***

0.886881326 ***

CALPERE

4.000530516 ***

in % vs PERIM:

0.013262900 ***

RADIUS & ANGLE

0.942273670 ***

0.344589613 ***

X & Y

0.311943688 ***

0.890610741 ***

CALPERE

4.000475928 ***

in % vs PERIM:

0.011898200 ***

RADIUS & ANGLE

0.943661145 ***

0.336904797 ***

X & Y

0.305577491 ***

0.894290437 ***

CALPERE

4.000419524 ***

in % vs PERIM:

0.010488100 ***

RADIUS & ANGLE

0.945057135 ***

0.329260007 ***

0.299211293 *** 0.897920203 *** **CALPERE** 4.000361552 *** in % vs PERIM: 0.009038800 *** **RADIUS & ANGLE** 0.946460822 *** 0.321654889 *** -----X & Y 0.292845095 *** 0.901499803 *** **CALPERE** 4.000302252 *** in % vs PERIM: 0.007556300 *** **RADIUS & ANGLE** 0.947871375 *** 0.314089084 *** -----X & Y 0.286478898 *** 0.905028982 *** **CALPERE** 4.000241880 *** in % vs PERIM: 0.006047000 *** **RADIUS & ANGLE** 0.949287953 *** 0.306562221 *** X & Y

X & Y

0.280112700 *** 0.908507468 *** **CALPERE** 4.000180708 *** in % vs PERIM: 0.004517700 *** **RADIUS & ANGLE** 0.950709705 *** 0.299073922 *** X & Y 0.273746502 *** 0.911934959 *** **CALPERE** 4.000119024 *** in % vs PERIM: 0.002975600 *** **RADIUS & ANGLE** 0.952135766 *** 0.291623801 *** X & Y 0.267380304 *** 0.915311139 *** **CALPERE** 4.000057124 *** in % vs PERIM: 0.001428100 *** **RADIUS & ANGLE** 0.953565262 *** 0.284211462 *** X & Y 0.261014107 ***

0.918635664 *** CALPERE 3.999995335 *** in % vs PERIM: -0.000116625 *** **RADIUS & ANGLE** 0.954997302 *** 0.276836501 *** X & Y 0.254647909 *** 0.921908166 *** **CALPERE** 3.999933972 *** in % vs PERIM: -0.001650700 *** **RADIUS & ANGLE** 0.956430982 *** 0.269498504 *** X & Y 0.248281711 *** 0.925128252 *** **CALPERE** 3.999873384 *** in % vs PERIM: -0.003165400 *** **RADIUS & ANGLE** 0.957865383 *** 0.262197050 *** X & Y 0.241915514 *** 0.928295503 ***

CALPERE
3.999813918 ***
in % vs PERIM:
-0.004652050 ***
RADIUS & ANGLE
0.959299566 ***
0.254931705 ***
-----X & Y
0.235549316 ***
0.931409473 ***
CALPERE
3.999755950 ***
in % vs PERIM:
-0.006101250 ***

RADIUS & ANGLE 0.960732579 *** 0.247702030 ***

X & Y 0.229183118 *** 0.934469686 *** CALPERE 3.999699847 *** in % vs PERIM: -0.007503825 *** RADIUS & ANGLE 0.962163446 *** 0.240507572 ***

X & Y 0.222816921 ***

0.937475635 *** CALPERE

3.999646000 *** in % vs PERIM: -0.008850000 *** **RADIUS & ANGLE** 0.963591172 *** 0.233347872 *** X & Y 0.216450723 *** 0.940426783 *** **CALPERE** 3.999594809 *** in % vs PERIM: -0.010129775 *** **RADIUS & ANGLE** 0.965014741 *** 0.226222459 *** -----X & Y 0.210084525 *** 0.943322557 *** **CALPERE** 3.999546680 *** in % vs PERIM: -0.011333000 *** **RADIUS & ANGLE** 0.966433109 *** 0.219130852 *** -----X & Y 0.203718327 *** 0.946162350 *** CALPERE 3.999502011 ***

in % vs PERIM: -0.012449725 *** **RADIUS & ANGLE** 0.967845210 *** 0.212072558 *** -----X & Y 0.197352130 *** 0.948945516 *** **CALPERE** 3.999461221 *** in % vs PERIM: -0.013469475 *** **RADIUS & ANGLE** 0.969249945 *** 0.205047075 *** X & Y 0.190985932 *** 0.951671371 *** **CALPERE** 3.999424731 *** in % vs PERIM: -0.014381725 *** RADIUS & ANGLE 0.970646189 *** 0.198053888 *** -----X & Y 0.184619734 *** 0.954339186 *** **CALPERE** 3.999392940 ***

in % vs PERIM:

-0.015176500 ***
RADIUS & ANGLE
0.972032781 ***
0.191092471 ***

X & Y

0.178253537 ***

0.956948186 ***

CALPERE

3.999366256 ***

in % vs PERIM:

-0.015843600 ***

RADIUS & ANGLE

0.973408524 ***

0.184162285 ***

X & Y

0.171887339 ***

0.959497552 ***

CALPERE

3.999345088 ***

in % vs PERIM:

-0.016372800 ***

RADIUS & ANGLE

0.974772184 ***

0.177262780 ***

X & Y

0.165521141 ***

0.961986408 ***

CALPERE

3.999329799 ***

in % vs PERIM:

-0.016755025 ***

RADIUS & ANGLE 0.976122481 *** 0.170393388 ***

X & Y

0.159154944 ***

0.964413822 ***

CALPERE

3.999320753 ***

in % vs PERIM:

-0.016981175 ***

RADIUS & ANGLE

0.977458090 ***

0.163553533 ***

X & Y

0.152788746 ***

0.966778805 ***

CALPERE

3.999318288 ***

in % vs PERIM:

-0.017042800 ***

RADIUS & ANGLE

0.978777635 ***

0.156742618 ***

X & Y

0.146422548 ***

0.969080299 ***

CALPERE

3.999322698 ***

in % vs PERIM:

-0.016932550 ***

RADIUS & ANGLE

0.980079684 *** 0.149960035 *** -----X & Y 0.140056350 ***

0.971317175 ***

CALPERE

3.999334230 ***

in % vs PERIM:

-0.016644250 ***

RADIUS & ANGLE

0.981362744 ***

0.143205156 ***

X & Y

0.133690153 ***

0.973488228 ***

CALPERE

3.999353086 ***

in % vs PERIM:

-0.016172850 ***

RADIUS & ANGLE

0.982625253 ***

0.136477336 ***

X & Y

0.127323955 ***

0.975592168 ***

CALPERE

3.999379398 ***

in % vs PERIM:

-0.015515050 ***

RADIUS & ANGLE

0.983865574 ***

```
0.129775912 ***
------
X & Y
```

0.120957757 *** 0.977627608 ***

CALPERE

3.999413205 ***

in % vs PERIM:

-0.014669875 ***

RADIUS & ANGLE

0.985081986 ***

0.123100201 ***

X & Y

0.114591560 ***

0.979593062 ***

CALPERE

3.999454466 ***

in % vs PERIM:

-0.013638350 ***

RADIUS & ANGLE

0.986272676 ***

0.116449496 ***

X & Y

0.108225362 ***

0.981486927 ***

CALPERE

3.999503012 ***

in % vs PERIM:

-0.012424700 ***

RADIUS & ANGLE

0.987435728 ***

0.109823069 ***

X & Y

0.101859164 ***

0.983307473 ***

CALPERE

3.999558548 ***

in % vs PERIM:

-0.011036300 ***

RADIUS & ANGLE

0.988569105 ***

0.103220163 ***

X & Y

0.095492966 ***

0.985052825 ***

CALPERE

3.999620591 ***

in % vs PERIM:

-0.009485225 ***

RADIUS & ANGLE

0.989670639 ***

0.096639998 ***

X & Y

0.089126769 ***

0.986720945 ***

CALPERE

3.999688487 ***

in % vs PERIM:

-0.007787825 ***

RADIUS & ANGLE

0.990738010 ***

0.090081759 ***

0.082760571 *** 0.988309615 *** **CALPERE** 3.999761346 *** in % vs PERIM: -0.005966350 *** **RADIUS & ANGLE** 0.991768726 *** 0.083544602 *** -----X & Y 0.076394373 *** 0.989816396 *** **CALPERE** 3.999837994 *** in % vs PERIM: -0.004050150 *** **RADIUS & ANGLE** 0.992760091 *** 0.077027644 *** -----X & Y 0.070028176 *** 0.991238607 *** CALPERE 3.999916953 *** in % vs PERIM: -0.002076175 *** **RADIUS & ANGLE** 0.993709173 *** 0.070529960 *** X & Y

X & Y

0.063661978 *** 0.992573274 *** **CALPERE** 3.999996368 *** in % vs PERIM: -0.000090800 *** **RADIUS & ANGLE** 0.994612765 *** 0.064050583 *** X & Y 0.057295780 *** 0.993817076 *** **CALPERE** 4.000073920 *** in % vs PERIM: 0.001848000 *** **RADIUS & ANGLE** 0.995467321 *** 0.057588492 *** X & Y 0.050929583 *** 0.994966273 *** **CALPERE** 4.000146776 *** in % vs PERIM: 0.003669400 *** **RADIUS & ANGLE** 0.996268893 *** 0.051142610 *** X & Y 0.044563385 ***

0.996016603 *** CALPERE 4.000211464 *** in % vs PERIM: 0.005286600 *** **RADIUS & ANGLE** 0.997013023 *** 0.044711790 *** X & Y 0.038197187 *** 0.996963147 *** **CALPERE** 4.000263788 *** in % vs PERIM: 0.006594700 *** **RADIUS & ANGLE** 0.997694613 *** 0.038294809 *** X & Y 0.031830989 *** 0.997800119 *** **CALPERE** 4.000298660 *** in % vs PERIM: 0.007466500 *** **RADIUS & ANGLE** 0.998307713 *** 0.031890353 *** X & Y 0.025464792 *** 0.998520551 ***

CALPERE 4.000309992 *** in % vs PERIM: 0.007749800 *** **RADIUS & ANGLE** 0.998845207 *** 0.025496995 *** X & Y 0.019098594 *** 0.999115754 *** **CALPERE** 4.000290628 *** in % vs PERIM: 0.007265700 *** **RADIUS & ANGLE** 0.999298277 *** 0.019113169 *** X & Y 0.012732396 *** 0.999574289 *** **CALPERE** 4.000232616 *** in % vs PERIM: 0.005815400 *** **RADIUS & ANGLE** 0.999655377 *** 0.012737130 *** X & Y 0.006366199 *** 0.999879555 *** **CALPERE**

4.000129276 ***
in % vs PERIM:
0.003231900 ***
RADIUS & ANGLE
0.999899821 ***
0.006366880 ***

X & Y

0.000000001 ***

1.000000000 ***

CALPERE

4.000000000 ***

in % vs PERIM:

0.000000000 ***

RADIUS & ANGLE

1.000000000 ***

0.000000001 ***
