

# Getting Started with the sofcFoam Model

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## 1. Introduction

The sofcFoam model is an OpenFOAM (<http://www.openfoam.com/>) application for the simulation of solid oxide fuel cells. It is a single-cell model being developed within the open source **Multi-Scale Integrated Fuel Cell (MuSIC)** project. This document describes how to obtain and use sofcFoam.

To make more sense of what follows, it may be useful to begin with a brief overview of the model. (A more detailed view will be provided later). The model simulates a five region fuel cell, as depicted schematically in Figure 1(a). Between two interconnects we find an air region, an electrolyte, and a fuel region. The model uses a computational domain for each of these regions, and one more global domain for the entire cell. Each domain supports its own fields. Pressure, momentum and species mass fractions, for example, are solved on the air and fuel domains, and temperature is solved on the global domain. Global and regional information is transferred back and forth via grid cell mappings that are established during mesh generation/splitting. Porous cathode and anode zones, shown in Figure 1(b), are incorporated into the air and fuel regions, respectively, using Darcy's Law. Electrochemistry is assumed to occur on the electrode-electrolyte interfaces. The resulting electrochemical mass fluxes give rise to Dirichlet velocity conditions and Neumann mass-fraction conditions on the air and fuel boundaries interfacing the electrolyte.

After an initialization phase, the model enters an iteration loop as follows:

1. global temperature is mapped to the fluid regions, air and fuel
2. fluid densities are calculated
3. pressure and momentum are solved in fluid domains
4. mass diffusivity in fluids is calculated
5. mass fractions of fluid species are solved
6. electrochemistry is calculated
7. regional velocity and thermophysical data fields are mapped to global mesh
8. energy equation is solved for global temperature

9. Steps (1) to (8) are repeated until convergence

## 2. Prerequisites

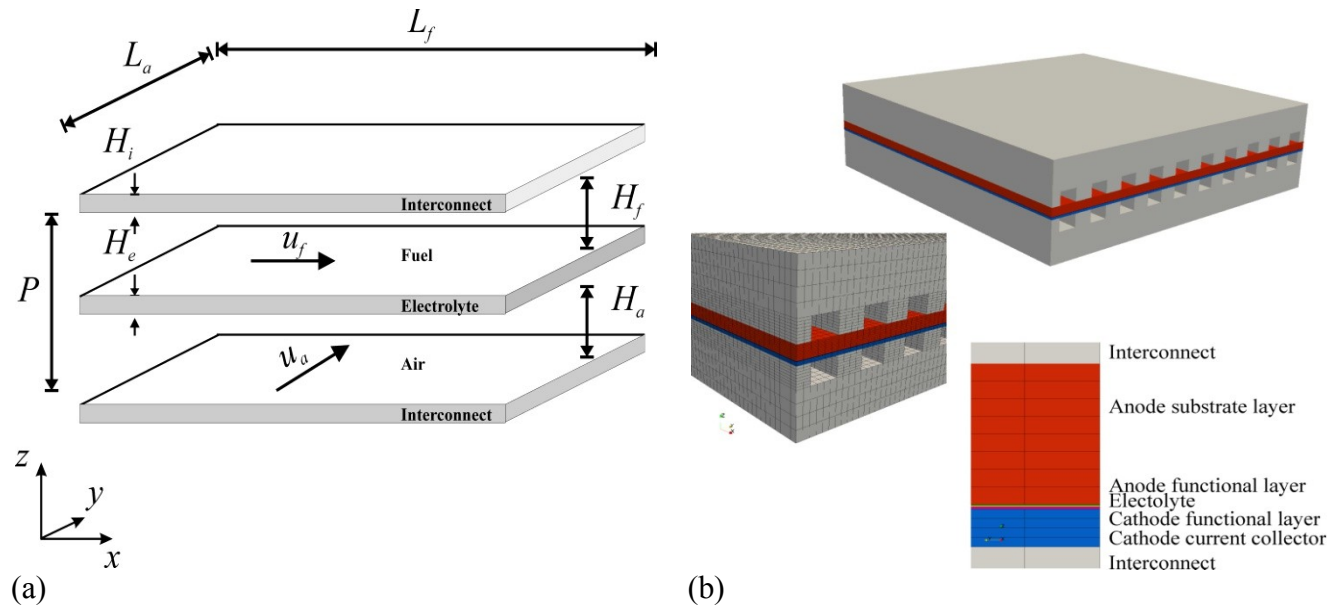
### 2.1 OpenFoam

Since the MuSIC program is being developed with the open source C++ objected oriented software OpenFOAM, it is necessary to have a working installation of OpenFOAM. A number of download options (with instructions) for the latest release of OpenFOAM are available at <http://www.openfoam.org/download/>. At time of writing, the current release is 2.1.1.

Some experience running OpenFoam applications, as might be obtained from OpenFoam tutorials, will be helpful. Instructions for building OpenFOAM come with the download, and further assistance can be obtained from the discussion forum (<http://www.cfd-online.com/Forums/openfoam/>). The WIKKI pages are also useful for supplementary information ([http://openfoamwiki.net/index.php/Main\\_Page](http://openfoamwiki.net/index.php/Main_Page)).

### 2.2 svn

The sofcFoam code is maintained in a Subversion (<http://subversion.apache.org/>) version control system repository at <http://cfd.icpet.nrc.ca/svn/sofcFoam/trunk>. The Subversion command line client tool is *svn*. Graphical tools are also available, e.g. RapidSVN, SmartSVN.



**Figure 1.** (a), left panel, shows five regions as simple rectangular blocks in cross-flow configuration. (b), right panel, shows five regions in coflow (or counterflow) configuration, with air and fuel regions each consisting of a channels zone and two porous zones.

### 3. Obtaining sofFoam

The latest version of sofFoam can be downloaded from <http://cfd.icpet.nrc.ca/svn/sofFoam/trunk/>. Using the svn command line tool, one simply types

```
svn co http://cfd.icpet.nrc.ca/svn/sofFoam/trunk/
```

at the prompt. The check-out delivers the directory structure shown in Figure 2(a) to the current working directory.

### 4. Directories

From Figure 2(a), the left panel of Figure 2, we see that the `trunk/` directory has two main subdirectories, `run/` and `src/`. The `run/` directory contains examples of cases that can be simulated with the model, while the `src/` directory contains the model source code.

#### 4.1 *trunk/src/*

The `src/` directory contains the major subdirectories `libSrc/` and `appSrc/`. In `libSrc/`, we find C++ classes that have been specifically developed or modified for sofFoam and are used in the sofFoam model. The `appSrc/` directory contains the sofFoam model source files, which instantiate objects from both `libSrc/` and `OpenFoam/src` as needed, to implement the sofFoam algorithm. As is typical for OpenFoam applications, the sofFoam application is built by including blocks of code (\*.H files) into a main program (\*.C file).

#### 4.2 *trunk/run/*

The `run` directory contains case directories, or cases. The cases `coFlow`, `counterFlow`, and `crossFlow` exercise the model on co-flow, counter-flow, and cross-flow configurations, respectively. The case `quickTest` is similar to the `coFlow` case, but reduced from twelve to three channels. In each configuration, the fuel velocity is in the +x direction, while the air velocity is in the direction of +x, -x, and +y for co-flow, counter-flow and cross-flow, respectively.

<code>trunk/</code> <code>run/</code> <code>coFlow/</code> <code>0/</code> <code>air/</code> <code>fuel/</code> <code>system/</code> <code>air/</code> <code>electrolyte/</code> <code>fuel/</code> <code>interconnect0/</code> <code>interconnect1/</code> <code>config/</code> <code>constant/</code> <code>polyMesh/</code> <code>air/</code>	<code>0/</code> <code>k</code> <code>T</code> <code>air/</code> <code>p</code> <code>U</code> <code>YN2</code> <code>YO2</code> <code>fuel/</code> <code>p</code> <code>U</code> <code>YH2</code> <code>YH2O</code> <code>Allclean</code> <code>config/</code> <code>make.faceAir</code>
---	---

<pre> electrolyte/ fuel/ interconnect0/ interconnect1/ counterFlow/ &lt;...like coFlow...&gt; crossFlow/ &lt;...like coFlow...&gt; quickTest/ &lt;...like coFlow...&gt; src/ appSrc/   Make/ libSrc/   continuityErrs/   diffusivityModels/     diffusivityModel/     binaryFSG     fixedDiffusivity/     fsgDiffusionVolumes/     fsgMolecularWeights/     knudsen/     porousFSG/   Make/   MeshWave/   polyToddYoung/   regionProperties/   smearPatchToMesh/   sofcSpecie/ </pre>	<pre> make.faceFuel make.faceSet make.setAir make.setFuel make.setSet constant/   cellProperties   rxnProerties   air/     airProperties     porousZones     sofcSpeciesProperties   electrolyte/     electrolyteProperties   fuel/     fuelProperties     porousZones     sofcSpeciesProperties   interconnect0/     interconnectProperties   interconnect1/     interconnectProperties   polyMesh/     blockMeshDict Makefile runscript system/   controlDict.mesh   controlDict.run   controlDict   fvSchemes   fvSolution   decomposeParDict   createPatchDict   air/     fvSchemes     fvSolution   fuel/     fvSchemes     fvSolution   electrolyte/     fvSchemes     fvSolution   interconnect0/     fvSchemes     fvSolution   interconnect1/     fvSchemes     fvSolution </pre>
(a)	(b)

**Figure 2.** (a), left panel, directory structure from svn check out. (b), right panel, files in a case directory after checkout and before meshing.

Like any other OpenFoam case directory, the four cases here contain major subdirectories 0/, constant/, and system/. With only a single mesh, these 0/, constant/ and system/ directories would be populated by files only, but with multiple meshes they have a subdirectory for each region, and the files for each domain are placed in the appropriate directory or subdirectory. Thus initial global temperature T is found in 0/T, initial air velocity U in 0/air/U, initial fuel pressure p in 0/fuel/p, etc. Similarly, global cell properties are found in

`constant/cellProperties`, whereas air properties are found in `constant/air/airProperties`. See Figure 2(b) for more complete listings.

## 5. Installation

In your chosen parent directory for the `sofcFoam` model, e.g. your OpenFoam work space `$WM_PROJECT_USER_DIR/applications/`, check out the `trunk/` directory from the Subversion repository using your favourite graphical svn tool, or the command

```
co http://cfd.icpet.nrc.ca/svn/sofcFoam/trunk/
```

This creates directory `trunk/` in the current working directory.

### 5.1 *src*

To compile the library and application source code, go to `trunk/src/` directory and run the *Allwmake* script. Type `./Allwmake` at the prompt. This should generate shared object library *libsofcFoam.so* in the `$FOAM_USER_LIBBIN` directory and application executable *sofcFoam* in the `$FOAM_USER_APPBIN` directory. A `lnInclude/` directory, containing links to all of the `libSrc` class files, will appear in the `libSrc/` directory.

### 5.2 *cases*

As can be seen in Figure 2(b), a case directory contains only one `polyMesh/` directory immediately after checkout, and it contains only the dictionary file `blockMeshDict`. This dictionary, together with the *setSet* batch command files in the `<case>/config/` directory, describes the global and regional meshes. After the global mesh is made by the OpenFOAM utility *blockMesh*, the utility *splitMeshRegions* generates the required regional meshes and map files. For more information on the *blockMesh*, *setSet*, and *setsToZones* utilities, see Chapter 5 “Mesh generation and conversion” and Section 3.6 “Standard utilities” in the OpenFOAM User Guide (<http://www.openfoam.com/docs/user/>).

Making the global and regional meshes is handled in `sofcFoam` by the `Makefile` in the case directory. See, for example, `run/coFlow/Makefile`. The command

```
make mesh
```

issued from the case directory, will generate the global mesh and the region meshes. During model execution, various material property and other field values will be mapped from the region meshes to the global mesh. Cells that began life labeled as a fluid in the global mesh may have become a solid, and some of these may have boundary faces on the original fluid inlet or outlet patches. Accordingly, the fluid inlet and outlet patches may need to be redefined for the new reality. The redefinitions are specified by the `make.face[Air|Fuel|Set]` files in the `config` directory. See Appendix A for a description of the steps required to specify a new geometry.

## 6. Running the model

With the application already compiled, the command

```
make run
```

will run the executable from the command line, using the available case data. The model can also be run by typing the executable name, and the output directed to Standard Out can be redirected to a file:

```
sofcFoam | tee log.run
```

Instead of running the model from the command line, a runscript is available to submit a job to a queue. The script usage line may need editing for your queuing system.

After the model has run to completion, VTK files for visualization, e.g. with *paraview*, can be prepared easily using the Makefile. Typing

```
make view
```

will generate VTK files for the last output step, whereas

```
make viewAll
```

will generate VTK files for all output directories.

## 7. Mesh files

Before making the meshes the only mesh file is `constant/polyMesh/blockMeshDict`. Making the meshes introduces new directories and files as shown in Figure 3. In addition to the standard `boundary`, `faces`, `neighbour`, `owner` and `points` files, each domain has a `cellZones` file. The original `polyMesh` directory, `constant/polyMesh/`, has a `sets/` subdirectory containing *cellSet* information for each subregion. The regional `polyMesh/` directories contain `faceZones` and `cellZones`, as well as addressing files relating their domains to the global domain. The fluid regions, i.e., air and fuel, also have a `sets/` subdirectory, which contains *cellSet* information for their entire region and for their porous zones.

<b>constant</b> cellToRegion <b>constant/polyMesh</b> blockMeshDict boundary cellZones	<b>constant/&lt;fluid&gt;/polyMesh</b> boundary boundaryRegionAddressing cellRegionAddressing	<b>constant/&lt;solid&gt;/polyMesh</b> boundary boundaryRegionAddressing cellRegionAddressing
---	--	--

faces neighbour owner points sets/ air electrolyte fuel interconnect0 interconnect1	cellZones faceRegionAddressing faces faceZones neighbour owner pointRegionAddressing points pointZones sets/  constant/air/polyMesh/sets air cathode cfl  constant/fuel/polyMesh/sets afl anode fuel	cellZones faceRegionAddressing faces faceZones neighbour owner pointRegionAddressing points pointZones
--	---	--

**Figure 3. Mesh files. Left:** new files in constant, constant/polyMesh/ and constant/polyMesh/sets after generating the meshes. **Centre:** files from meshing in the new constant/<fluid>/polyMesh/ directories, for fluids air and fuel, with additional file details for constant/air/polyMesh/sets/ and constant/fuel/polyMesh/sets/ subdirectories. **Right:** files from meshing in the new constant/<solid>/polyMesh/ directories, for solids electrolyte, interconnect0, and interconnect1.

It should be noted that the generation of the regional submeshes results in the generation of some field files in the constant/<subregion> dictionaries. These files correspond to the field files in the top level of the 0/ directory, k and T. These new constant/<subregion>/[kT] files are not used and can be removed.

## 8. Inputs

Runtime inputs to the model are supplied in dictionaries in the case directory. Among these are the mesh files and mesh mapping files generated during mesh generation, as discussed above. Tables 1 and 2 below show the remaining fields and parameters that must be specified. The specifications supplied for the example coFlow/, counterFlow/, and crossFlow/ cases can be viewed in their respective case files, as indicated by Table 1.



**Table 1.** Input properties and parameters

file <b>constant/cellProperties</b>	
<b><i>parameter</i></b>	<b><i>remarks</i></b>
fuelInletPatch	fuel mesh patch name for the inlet patch
fuelOutletPatch	fuel mesh patch name for the outlet patch
anodePatch	fuel mesh patch name for the fuel/electrolyte interface
airInletPatch	air mesh patch name for the inlet patch
airOutletPatch	air mesh patch name for the outlet patch
cathodePatch	air mesh patch name for the air/electrolyte interface
electrolyteAnodePatch	electrolyte mesh patch name for the electrolyte/fuel interface
electrolyteCathodePatch	electrolyte mesh patch name for the electrolyte/air interface
voltage	initial value for voltage
ibar0	prescribed mean current density
Rhat	voltage correction relaxation coefficient
Tinit	initial internalField temperature for regional temperature fields
file <b>constant/rxnProperties</b>	
<b><i>parameter</i></b>	<b><i>remarks</i></b>
rxnSpecies	list of species name and stoichiometric coefficient pairs
file <b>constant/air/airProperties</b>	
<b><i>parameter</i></b>	<b><i>remarks</i></b>
rho	air mixture density initial value
mu	air molecular viscosity
Cp	air isobaric heat capacity initial value
k	air thermal conductivity
dHyd	hydraulic diameter for Reynolds Number calculation
diffusivity	subdictionary for diffusivity model*
file <b>constant/fuel/fuelProperties</b>	
same as for air properties, but for fuel	
file <b>constant/air/porousZones</b>	
<b><i>parameter</i></b>	<b><i>remarks</i></b>
zone name	e.g. cathode
coordinateSystem	not required for geometry aligned with Cartesian coordinate axes
porosity	porosity value
Cp	zone isobaric heat capacity
k	zone thermal conductivity
Darcy	Darcy-Forchheimer subdictionary
diffusivity	diffusivity model subdictionary*
-- repeat for successive zones	
file <b>constant/fuel/porousZones</b>	
same as for air porousZones, but for fuel	
file <b>constant/electrolyte/electrolyteProperties</b>	

<i>parameter</i>	<i>remarks</i>
rho	electrolyte density
Cp	electrolyte isobaric heat capacity
k	electrolyte thermal conductivity
Hsrc	initial heat source value
file <b>constant/interconnect0/interconnectProperties</b>	
<i>parameter</i>	<i>remarks</i>
rho	interconnect density
Cp	interconnect isobaric heat capacity
k	interconnect thermal conductivity
file <b>constant/interconnect1/interconnectProperties</b>	
same as for interconnect0, but for interconnect1	

\* Diffusivity models and their dictionaries will be described elsewhere.

**Table 2.** Input initial fields.

<b>file</b>	<b>physical field</b>	<b>remarks</b>
0/T	cell temperature	May be changed to suit operating conditions
0/k	cell conductivity	Inlet values = 1e-15 prevents outward diffusion at inlets
0/air/p	air pressure	internalField and outlet boundaries at atmospheric pressure other patches zeroGradient or equivalent
0/air/U	air velocity	internalField <b>0</b> (or initialized to inlet value); inlet specified; outlet zeroGradient; cathodePatch type must allow code to set value (e.g. fixedValue)
0/air/Y <sub>sp</sub>	mass fraction of specie <i>sp</i>	internalField initialized to inlet value cathodePatch must be type fixedGradient Require one such file for each air specie, e.g., YO <sub>2</sub> , YN <sub>2</sub>
0/air/diff <sub>Sp</sub>	diffusivity of specie <i>Sp</i> in mixture	Inlet value = 1e-15 prevents outward diffusion at inlet Not required if outward diffusion at inlet is not an issue Never required for background specie
0/air/rho	air mix density	Optional. Uses zeroGradient BCs if not present. Can use to specify and maintain inlet value, e.g.
0/air/T	air temperature	as for 0/air/rho
0/fuel/p	fuel pressure	as for 0/air/p
0/fuel/U	fuel velocity	as for 0/air/U
0/fuel/Y <sub>sp</sub>	mass fraction of <i>sp</i>	as for 0/air/Y <sub>sp</sub> , e.g., YH <sub>2</sub> , YH <sub>2</sub> O
0/fuel/diff <sub>Sp</sub>	diffusivity of <i>Sp</i> in mixture	as for 0/air/diff <sub>Sp</sub>
0/fuel/rho	fuel mix density	as for 0/air/rho
0/fuel/T	fuel temperature	as for 0/air/T

Numerical Schemes are specified at runtime by `fvSchemes` files in the system directories (`system`, `system/air`, etc). The `fvSchemes` dictionary contains a number of subdictionaries which must be defined for the code to run. In Table 3 we list the `fvSchemes` used by the model and the regions in which the listed schemes are applicable.

**Table 3.** `fvSchemes` settings

operator	scheme	applicable region(s)
<b><i>ddtSchemes</i></b>		
default	steadyState;	all
<b><i>gradSchemes</i></b>		
default	Gauss linear;	all
grad(p)	Gauss linear;	air*, fuel**
<b><i>divSchemes</i></b>		
default	none;	all
div(rhoCpPhi,T)	Gauss upwind;	cell***
div(phi,U)	Gauss GammaV 0.2;	air, fuel
div(phi,y)	Gauss upwind;	air, fuel
<b><i>laplacianSchemes</i></b>		
default	none;	all
laplacian(k,T)	Gauss harmonic corrected;	cell
laplacian(mu,U)	Gauss harmonic corrected;	air, fuel
laplacian((rho A(U)),p)	Gauss linear corrected;	air, fuel
laplacian(diff,y)	Gauss harmonic corrected;	air, fuel
<b><i>interpolationSchemes</i></b>		
default	harmonic;	cell
default	linear;	fluid, solid regions
interpolate(T)	harmonic;	cell, air, fuel
interpolate(rho)	harmonic;	cell, air, fuel
<b><i>snGradSchemes</i></b>		
default	corrected;	all
<b><i>fluxRequired</i></b>		
default	no;	all
p		air, fuel

\*constant/air/fvSchemes    \*\*constant/fuel/fvSchemes    \*\*\*constant/fvSchemes

Solver and other algorithmic controls and tolerances are supplied by the `fvSolution` dictionary files in the system directories, as shown in Table 4. The table shows three subdictionaries in the `fvSolution` files: `solvers`, `PISO`, and `relaxationFactors`. In the `solvers` subdictionary, we find the settings for the linear solvers chosen to solve the discretized finite volume equations for the various fields. The `relaxationFactors` subdictionary contains under-relaxation factors to improve stability. The `PISO` subdictionary controls the PISO algorithm for the simultaneous solution of pressure and momentum. Table 4 also shows which regions (domains) use the

tabulated settings. Note that the `fvSolution` file must exist in the `system` directory, even though it may not need any subdictionaries.

**Table 4.** `fvSolution` settings

<b>solvers dictionary</b>			
<i>field</i>	<i>solver</i>	<i>parameters</i>	<i>region(s)</i>
T	PBiCG	preconditioner DILU; tolerance 1e-10; relTol 0.0; maxIter 5000;	cell
p	PCG	preconditioner DIC; tolerance 1e-09; relTol 0; maxIter 700;	air, fuel
U	PBiCG	preconditioner DILU; tolerance 1e-09; relTol 0; maxIter 700;	air, fuel
Yi	PBiCG	preconditioner DILU; tolerance 1e-09; relTol 0.0; maxIter 700;	
<b>PISO dictionary</b>			air, fuel
<i>parameter</i>	<i>value</i>		
nIteration	0		
nCorrectors	2		
nNonOrthogonalCorrectors	0		
pRefCell	0		
pRefValue	0		
<b>relaxationFactors dictionary</b>			
<i>field</i>	<i>value</i>		
p	0.3		air, fuel
U	0.7		air, fuel

## 9. Outputs

The model writes selected fields to time directories in the case directory, and also writes to Standard Out as it proceeds.

### 9.1 Time directories

The model produces “time” directories in the case directory, in accordance with the settings in the control dictionary (`system/controlDict`). For a steady model like `sofcFoam`, these directory time names (e.g. `50/`, `100/`, etc.) represent iteration count rather than time. Field

IObjects created with the AUTO\_WRITE attribute will be written to these time directories. These include the MUST\_READ fields (which must be present in the 0/ directories), and others, as shown in Table 5.

**Table 5.** Output files at times  $> 0$ .

Those marked \* are MUST\_READ and are thus required at time 0

<u>&lt;case&gt;/</u>	<u>&lt;case&gt;/air/</u>	<u>&lt;case&gt;/fuel/</u>	<u>physical field</u>
	cp	cp	isobaric heat capacity [J/(kg K)]
	diffSp	diffSp	mass diffusivity of specie <i>Sp</i> in mixture
	*p	*p	pressure
	phi	phi	velocity flux
	rho	rho	density
*T	T	T	temperature
	*U	*U	velocity
	Xsp	Xsp	mole fraction of sp
	*Ysp	*Ysp	mass fraction of sp
*k			thermal conductivity
Tsource			Energy eqn source (r.h.s.)
		i	current density [A/m <sup>2</sup> ]

## 9.2 Run log

The model writes considerable information to Standard Out during each “time step”, of the iteration loop. Among these are residuals from linear system solvers, continuity errors, min, mean, and max of various fields, electrochemical information, etc.

## 10. Download, compile, run: Summary

Assuming you have OpenFOAM version 2.1.x with environment variables set, here is all you need to download, compile, and run *sofcFoam*.

```
# obtain the code
cd <myChosenParentDirectory>
svn co http://cfd.icpet.nrc.ca/svn/sofcFoam/trunk/
cd trunk

# compile the model
cd src
./Allwmake

cd ..    #return to trunk directory

# generate meshes
cd run/<caseDirectory>    #coFlow, counterFlow, crossFlow, ...
make mesh
```

```
# run model from the command line with delivered settings
make run

# generate VTK files for final output time
make view
```

## 11. A walk through the model

We follow function `main`, coded in file `sofcFoam.C`, through the model execution. Like all OpenFOAM applications, the model begins by including the OpenFOAM src files `setRootCase.H` to check the case path, and `createTime.H` to read the `system/controlDict` file and instantiate the `Time` object `runTime`. This is followed by the creation of meshes, reading of properties, and creation of fields for the global cell mesh and the region meshes.

### 11.1 Meshes, properties and fields

The first mesh to be created is the mesh for the entire cell. This is accomplished by the included file `$FOAM_SRC/OpenFOAM/lnInclude/createMesh.H`. Mesh data is obtained from the `constant/polyMesh` directory. Global cell properties, or parameters, as listed in Table 1, above, are read from case file `constant/cellProperties` into model variables by appSrc file `readCellProperties.H`. Fields for the entire cell are created as `IOobjects` in appSrc file `createCellFields.H`. Some of the `IOobjects` have the `MUST_READ` attribute and must have a file in the starting time directory. The file name must be the same as the name specified in the `IOobject`. Others have the `READ_IF_PRESENT` attribute. The corresponding files will be read if they are present in the starting time directory. Still others have the `NO_READ` attribute and any file with their name will be ignored at field creation. Fields with `IOobjects` having the `AUTO_WRITE` attribute will write a file in the output time directories, whereas those with the `NO_WRITE` attribute aren't written.

Similarly, meshes, properties, and fields are established for the regions `interconnect0`, `air`, `electrolyte`, `fuel`, and `interconnect1`. The meshes are created by the appSrc files `create<Region>Mesh.H`. These files specify the location of the region's `polyMesh` directory and also create face-, cell-, and patch-maps to the global mesh. Constant properties are read by `read<Region>Properties.H` from case files `constant/<region>/<region>Properties`, and fields are read from case files `0/<region>/<fieldName>` by appSrc file `create<Region>Fields.H`. Note that there are no fields on either of the interconnect meshes, and both interconnects are assumed to have the same properties.

### 11.2 Fluid species and related fields

A number of air and fuel fields are specific to the species that comprise the fluid. The key appSrc files are `createAirSpecies.H` and `createFuelSpecies.H`. The key case files are `constant/air/sofcSpeciesProperties` and `constant/fuel/sofcSpeciesProperties`. See these for details of input data format.

As just indicated, the air species names and associated data are read from the `constant/air/sofcSpeciesProperties` file at run time by `appSrc` file `createAirSpecies.H`. A `speciesTable` object `airSpeciesNames` is instantiated from the list of species following the key word `speciesList` in the `sofcSpeciesProperties` file.

A `pointerList`, `airSpecies`, of pointers to `sofcSpecie` objects is created. The  $i$ -th air species can then be referenced as `airSpecies[i]`. For each specie in the air mixture, the specie properties of name, molar weight, molar charge (for Faraday's law), reaction sign (produced=1, inert=0, consumed=-1), enthalpy of formation, and standard entropy are stored in an `sofcSpecie` object, and can be accessed by class functions `name()`, `MW()`, `ne()`, `rSign()`, `hForm()` and `sForm()`, respectively. The `sofcSpecie` class can be found in `src/libSrc`.

After reading the species data, one of the species is designated as `airInertSpecie`. It is found after the keyword `inertSofcSpecie` in the `sofcSpeciesProperties` file. Note that the `inertSpecie` may well be chemically inert, but need not be. Here "inert" means that the mass fraction of the specie will not be computed from a partial differential equation, but rather calculated by adding the mass fractions of the other components and subtracting that sum from 1. The "inert" nomenclature follows that of OpenFOAM's `thermophysicalModels`.

The `sofcSpeciesProperties` file concludes with a `toddYoung` dictionary of Todd-Young (2002) polynomial coefficients for molar isobaric heat capacity. These are used to create a `pointerList`, `molarCpAir`, of pointers to `polyToddYoung` objects. The `polyToddYoung` class has functions to evaluate the polynomial and to also evaluate definite integrals which correspond to enthalpy and entropy in the case of isobaric heat capacity (see `src/libSrc/polyToddYoung`). Thus, eg, we can evaluate the isobaric heat capacity of the  $i$ -th air species at ambient temperature with the expression `molarCpAir[i].polyVal(Tair.internalField())`.

The specie names are used to create a `pointerList`, `Yair`, to mass fraction fields with names of the form  $Y_{sp}$ , where " $sp$ " is one of the specie names. There is one such file for each specie in the mixture. The mass fraction field `IOobjects` are `MUST_READ`, so must exist as files in the starting time directory.

Mole fraction fields are calculated from the mass fraction fields. Their names have the form  $X_{sp}$ . The read/write attributes are `NO_READ`, `AUTO_WRITE`. Again we have a `pointerList`, `Xair`, so that `Xair[i]` references the mole fraction field of the  $i$ -th air species.

Finally, `createAirSpecies.H` establishes a `pointerlist`, `diffSpAir`, to scalar fields for the diffusivities of the individual species in the mixture. These have `READ_IF_PRESENT` and `AUTO_WRITE` attributes, and are created with initial value 1.

A completely analogous discussion applies to the fuel side.

### 11.3 chemical reaction details

The chemical species involved in the reaction and their stoichiometric coefficients are listed after the `rxnSpecies` keyword in the `constant/rxnProperties` case file. The species “e” must always be in the list. Its coefficient is the number of moles of electrons transferred in the reaction. The list is read by appSrc file `readRxnProperties.H`, where a hash table, `rxnSpCoef`, is created. Thus a specie’s stoichiometric coefficient can be obtained via its name, e.g., `rxnSpCoef["O2"]`, or `rxnSpCoef[airSpecies[i].name()]`.

### 11.4 Global patch Ids

For convenience, global variables are established for the IDs (indices) of a number of patches that are frequently referenced. These patches were assigned to variable names in appSrc file `readCellProperties.H`, reading from case file `constant/cellProperties`. Their IDs are found and assigned in appSrc file `setGlobalPatchIds.H`.

### 11.5 Electrolyte thickness

Electrolyte thickness is used in the calculation of the electrolyte’s volumetric heat source term for the energy equation. It is calculated, in appSrc file `electrolyteThickness.H`, as the electrolyte volume divided by the average area of the anode and cathode interfaces. Average area is used to take into account cylindrical cells.

### 11.6 Patch to patch interpolators

Electrochemistry is assumed to occur on the fuel/electrolyte (anode) interface. Mole fraction patch fields of oxidants on the air side (cathode) interface must be interpolated to fields on the fuel side interface to combine with the fuel reactants. The resulting current density is calculated on the fuel side of the anode interface and must be interpolated to the electrolyte side in order to calculate the electrolyte’s volumetric heat source terms. These interpolations are carried out by OpenFOAM `patchToPatchInterpolation` objects, created in appSrc file `createPatchToPatchInterpolation.H`.

### 11.7 Gas diffusivity models

The diffusivity models are created in appSrc file `createDiffusivityModels.H`. For both air and fuel, a `pointerList` of diffusivity models is declared. On the air side, this is `airDiffModels`. Creation of a new diffusivity model requires a scalar field for the calculated diffusivity values, a label list of cells for which the diffusivity is to be calculated (normally corresponding to a cell zone), and a dictionary specifying the model type along with the corresponding type-specific parameters.

On the air side, a `scalarField`, `airDiff`, is used by each `airDiffusivityModel[m]` to return its calculated values. Then, a diffusivity model is established for each air zone and a pointer to it is added to the `pointerList`. There is one model for the entire air zone. Its dictionary is located in the `constant/air/airProperties` case file. There is also one model for each porous zone within the air region, with dictionaries in the corresponding zone in the case file `constant/air/porousZones`. The `cellZone` `labelLists` are found in the `polyMesh` directory for the air region.

An analogous story holds on the fuel side. How the SOFC model uses the diffusivity models will be described below.



## 11.8 Iteration loop

A number of calculations are repeated until convergence.

### 11.8.1 Mapping global temperature to fluid region meshes

The fluid regions need local temperature fields in order to calculate local fluid density. The mapping is done in appSrc file `mapFromCell.H`, using the cell maps established during mesh creation.

### 11.8.2 Fluid density

Fluid densities  $\rho$  are calculated from pressure  $p$ , temperature  $T$ , constituent mass fractions  $y_i$  and molar weights  $M_i$  as

$$\rho = \frac{p}{RT \sum (y_i/M_i)}$$

where  $R$  is the universal gas constant. The calculations are coded in appSrc files `rhoAir.H` and `rhoFuel.H`.

### 11.8.3 Pressure-momentum solution

Pressure and momentum are solved using the PISO iteration in appSrc files `solveAir.H` and `solveFuel.H`. Following the solution, the Reynolds numbers are calculated in appSrc file `ReynoldsNumber.H`. These are informative only, and require the input of hydraulic diameter in case files `constant/air/airProperties` and `constant/fuel/fuelProperties`.

### 11.8.4 Gas diffusivity calculations

The diffusivities are calculated in appSrc files `diffusivityAir.H` and `diffusivityFuel.H`. The following discussion refers only to air, but applies equally to fuel. Of interest is the diffusivity,  $D(a)$ , of specie  $a$  in the mixture. A diffusivity field is thus calculated for each specie, except for the background “inert” specie. A specie  $a$  can be given a fixed diffusivity value using the `fixedDiffusivity` model, or its diffusivity in the mixture,  $D(a)$ , can be modelled from the pairwise binary diffusivities  $D(a,b)$  of specie  $a$  diffusing in specie  $b$ .

The `sofcFoam` model combines pairwise binary diffusivities following Wilke (1950):

$$D(a) = \frac{1 - x_a}{S_a}$$

where

$$S_a = \sum_{b \neq a} \frac{x_b}{D(a,b)}$$

with mole fractions  $x$  and specie indices  $a, b$ .

The calculation proceeds by first fixing specie  $a$ , stepping through the species  $b$  and accumulating the results to obtain the sum  $S_a$ , which is then used to get  $D(a)$ . The computed diffusivity is stored in `volScalarField diffSpAir[a]`.

The diffusivity calculations have the following algorithmic structure:

```
forAll (airSpecies, a)
{
    if (airSpecies[a].name() != airInertSpecie)
    {
```

```

forAll(airDiffModels, m)
{
    if(airDiffModels[m]->isFixed())
    {
        //obtain fixed diffusivity
    }
    else if(!airDiffModels[m]->isBinary())
    {
        Error: must have fixed or binary: exit
    }
    else
    {
        initialize sumA = 0
        forAll(airSpecies,b)
        {
            if (b != a)
            {
                set specie b in airDiffModel[m]
                calculate binary diffusivity
                accumulate sumA
            }
        }
        obtain diffusivity in mixture using sumA
    } //isBinary
} //m
} //!inert
} //a

```

### 11.8.5 Mass fraction solutions

Mass fractions are computed in appSrc files `YairEqn.H` and `YfuelEqn.H`. For each specie other than the background “inert” specie, a partial differential equation is solved for `Yair[i]`, where *i* is the specie index. The mass fraction of the “inert” specie is obtained by subtracting the sum of all the other species’ mass fractions from 1.

### 11.8.6 Electrochemistry

Electrochemistry is assumed to occur on the anode interface with the electrolyte. It is calculated in appSrc file `solveElectrochemistry.H`. Global temperature is interpolated to the fuel mesh anode patch. Reactant oxidant species mole fractions are computed on the air mesh cathode patch and interpolated to the fuel mesh anode patch. Reactant and product fuel species are also calculated on the fuel mesh anode patch.

With all fields defined on the anode patch, the mole fractions, temperature, and specie properties are used to calculate the Nernst potential, *E*, via included appSrc file `NernstEqn.H`. Area specific resistance, *R*, is modelled by a function in included appSrc file `ASRfunction.H`. Current density *i* is then calculated as

$$i = (E - V)/R,$$

where *V* is the present value of voltage. Voltage is subsequently corrected using the present and prescribed mean current densities.

Electrochemical heating is calculated in included appSrc file `electrochemicalHeating.H`. Specie enthalpies are calculated and combined with enthalpy of formation and Joule heating in the electrolyte volume.

Species electrochemical mass fluxes are calculated and used to set Neumann boundary conditions on the cathode and anode patches for the calculation of air and fuel mass fractions, and Dirichlet conditions for the air and fuel velocities.

#### 11.8.6.1 NernstEquation

For the reaction

$$\text{rxn: } \sum_i a_i R_i = \sum_j b_j P_j,$$

having reactants  $R_i$  with stoichiometric coefficients  $a_i$  and products  $P_j$  with stoichiometric coefficients  $b_j$ , the Nernst potential,  $E$ , is calculated as

$$E = E_0 - \frac{RT}{zF} \ln Q,$$

where

$R$  is the universal gas constant,  $F$  is Faraday's constant,  $z$  is the number [moles] of electrons transferred,

$$Q = \frac{\prod_j [P_j]^{b_j}}{\prod_i [R_i]^{a_i}},$$

with  $[\cdot]$  denoting mole fraction, and

$$E_0 = -\Delta G_{\text{rxn}} = -(\Delta H_{\text{rxn}} - T\Delta S_{\text{rxn}}),$$

where

$$\Delta H_{\text{rxn}} = \sum_j b_j \Delta H(P_j) - \sum_i a_i \Delta H(R_i)$$

and

$$\Delta S_{\text{rxn}} = \sum_j b_j \Delta S(P_j) - \sum_i a_i \Delta S(R_i).$$

For a molecule  $X$ ,

$$\Delta H(X) = \int_{T_0}^T C_{p,X}(T) dT \quad \text{and} \quad \Delta S(X) = \int_{T_0}^T C_{p,X}(T)/T dT,$$

where  $T_0$  and  $T$  are reference and ambient temperatures, respectively. Todd-Young polynomials for molar heat capacity are used to evaluate the  $\Delta H$  and  $\Delta S$  integrals, using `polyToddYoung` class functions `polyInt` and `polyIntS`, respectively.

#### 11.8.6.2 Electrochemical heating

Heating sources for the energy solution are comprised of enthalpy of reactions (assumed to occur on the electrolyte/fuel interface), enthalpy changes of gaseous species from reference to ambient temperature,

and resistive heating. It is assumed that there is no reaction on the air side. The volumetric source terms are ascribed to the electrolyte region.

Enthalpy of formation and enthalpy changes, normalized by number of contributing electrons, are calculated by specie, accumulating products and reactants separately for each of air and fuel. The separate (normalized) enthalpy accumulations are then combined according to

$$h_{\text{src}} = (h_{\text{form}} + h_{\text{P,fuel}} - h_{\text{R,fuel}} + h_{\text{P,air}} - h_{\text{R,air}}) \frac{i}{F h_e},$$

where  $i$  is current density,  $F$  is Faraday's constant,  $h_{\text{form}}$  is accumulated enthalpy of formation,  $h_{\text{P,fuel}}$  is accumulated enthalpy change of products on the fuel side,  $h_{\text{R,fuel}}$  is accumulated enthalpy change of reactants on the fuel side, and similarly for the air side. The final source for the energy equation then becomes

$$S_{\text{energy}} = -h_{\text{src}} - \frac{iV}{h_e}.$$

#### 11.8.6.3 Electrochemical mass fluxes

An electrochemical mass flux is calculated for each specie taking part in the reaction, in accordance with Faraday's law, and taking into account whether the specie is consumed or produced:

$$\dot{m}'' = \pm \frac{Mi}{\nu F},$$

where  $M$  is molar mass,  $i$  is current density,  $\nu$  is valence, and  $F$  is Faraday's constant. Air species are treated separately from fuel species, and separate sums of air and fuel fluxes are accumulated for later use. The plus sign is used for products and the negative sign for reactants. On the air side, the above calculations are coded at lines 164 to 177 of `solveElectrochemistry.H`.

#### 11.8.6.4 Flux boundary conditions on $Y$

Mass fractions  $Y$  of all species, except the background "inert" specie, are found by solving a partial differential equation. Mass is transferred through the electrode boundaries, so these boundary fields are cast to a `fixedGradient` type, to which a (generally non-uniform) gradient value is assigned. The mass fraction gradient of a specie  $i$  will be due to both mass flux of  $i$  and to the mass fluxes of the other species. Letting  $Y_i$  be the mass fraction boundary field of specie  $i$  on the electrode boundary, we have

$$\frac{\partial Y_i}{\partial n} = \dot{m}_i''(1 - Y_i) - Y_i \sum_{j \neq i} \dot{m}_j''$$

#### 11.8.6.5 Flux boundary conditions on $U$

The mass flux sums are used to calculate Dirichlet velocity boundary conditions for air on the cathode and for fuel on the anode. Note that the calculations take place with fields defined on the anode interface, so `patchToPatchInterpolation` to the air side is required. Then, we have for  $U$  on the boundary

$$U|_{\text{electrode}} = - \frac{\sum \dot{m}''}{\rho} \frac{\mathbf{A}}{\|\mathbf{A}\|},$$

where  $\sum \dot{m}''$  is the accumulated mass flux,  $\rho$  is the fluid density, and  $\mathbf{A}/\|\mathbf{A}\|$  is the unit outward normal.

### 11.8.7 Mapping regional fields to global mesh

In order to solve the energy equation, regional values of thermal conductivity, heat capacity, density, velocity, etc., are required on the global mesh. Prior to any mapping, the internal values of the recipient fields on the global mesh are reset to zero by appSrc file `mapToCell.H`. Regional fields are then mapped to the global mesh by appSrc files `map<Region>ToCell.H` for each of the regions air, fuel, electrolyte, interconnect0 and interconnect1.

In the case of the solids, there is no convective heat transfer, so velocity and heat capacity for the corresponding space within the global mesh will simply be set to zero. Density and thermal conductivity are assumed uniform and are given by the values in their properties files. In the case of the electrolyte, the volumetric energy source terms computed there are also mapped to a global energy source field.

For the fluids, we have both convective and diffusive heat transfer. Mass based heat capacity of the mixture,  $c_p$ , is calculated as a linear combination of the specie molar heat capacities,  $C_{p,i}$ , divided by their molar mass,  $M_i$ , using mass fraction,  $Y_i$ , as the linear coefficients:

$$c_p = \sum_i Y_i C_{p,i} / M_i$$

Thermal conductivity is assumed to be uniform within each fluid zone. In the fluid channels it takes the value read from the fluid properties file, whereas in the porous zones it is a linear combination of the channel value and the porous zone value weighted by porosity. Porosity and porous zone thermal conductivity are obtained from the porous zone dictionary.

Rather than mapping velocity directly, it is the fluxes  $\phi = \rho \mathbf{U} \cdot \mathbf{dA}$  (computed during the pressure-velocity calculation such that mass conservation is satisfied) that are required for the finite volume equations. The fluxes form a surface field on the mesh faces and are mapped onto the global faces corresponding to the regional meshes interior faces and also to the regional mesh boundary patches. At this stage, we have fluxes on the fluid sides of the fluid/electrolyte interfaces, but not on the electrolyte side, the electrolyte being a solid. This can result in heat leaving or entering a fluid through its boundary with the electrolyte, without a corresponding gain or loss within the electrolyte. This situation is remedied by zeroing all fluxes that touch the electrolyte and introducing an additional compensating source term into the energy equation. The zeroing of fluxes is done in `mapElectrolyteToCell.H`. The source term is equivalent to the continuity error introduced by the zeroing of the fluxes on the electrolyte boundaries.

### 11.8.8 Energy solution

After the regional fields are mapped to the corresponding locations in the global mesh, the global energy is computed from a partial differential equation in appSrc file `solveEnergy.H`. The equation is essentially

$$\text{div}(\rho \mathbf{U} c_p T) - S_\phi - \text{div}(k \text{grad} T) = S_q,$$

where  $S_q$  is volumetric heat source and  $S_\phi$  is the source due to the zeroed fluxes on the electrolyte boundary faces. The term  $-S_\phi$  appears in the discrete equation as

$$\text{fvm::SuSp}(-\text{fvc::div}(\rho \mathbf{U} c_p \Phi_{\text{Cell}}), T_{\text{cell}})$$

where  $\rho_{c_p \phi_{cell}}$  is equal to the face interpolated  $c_p$  multiplied by the surface scalar field  $\phi_{cell}$ . Note that  $\phi$  already incorporates  $\rho$ . The finite volume matrix operator  $SuSp$  linearizes the source term and adds the linear part to the matrix diagonal or to the source in such a way as to maximize diagonal dominance of the matrix.

## References

Todd, B. and J.B. Young, *Thermodynamic and transport properties of gases for use in solid oxide fuel cell modelling*, Journal of Power Sources, 110 (2002), pp186-200.

Wilke, C.R., *A Viscosity Equation for Gas Mixtures*, Journal of Chemical Physics, v18, n4, April 1950, pp 517-519.

## Appendix A. Specifying meshes for a new geometry

Figure A1 shows the proposed geometry we intend to model. The associated dimensions of the components are given in Table A1. The vertical structure can be captured by seven blocks, as shown in Figure A2, (the block containing the electrolyte is too thin to be discernible). The blocks containing the air and fuel channels can then be split horizontally to separate the channels from the ribs, the latter being part of the interconnects.

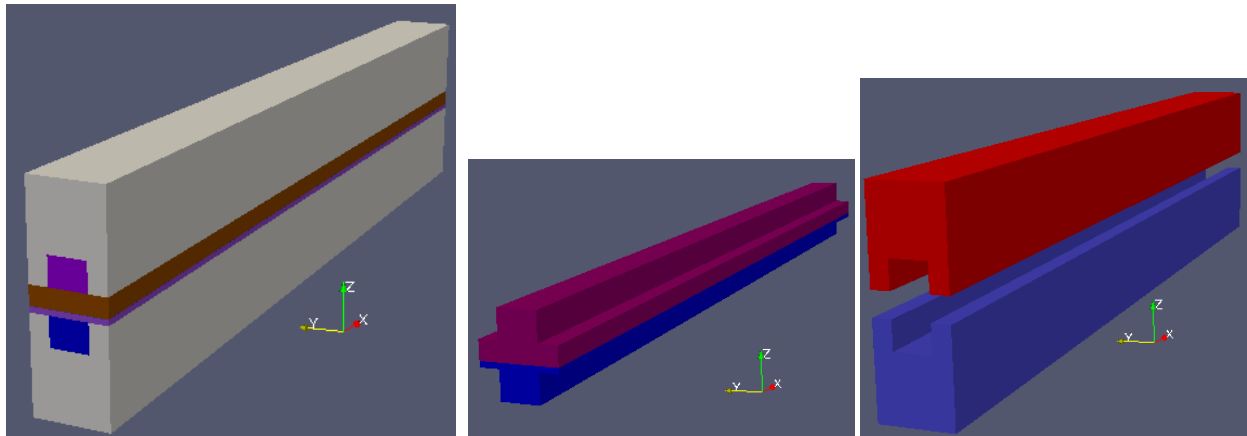


Figure A1. A fuel cell with one air channel and one fuel channel. Left panel shows air (blue) and fuel (purple) inlets, interconnects (grey) and electrode sides. Centre panel shows air (blue) and fuel (purple) volume regions, each comprised of both a channel and a porous electrode zone. Right panel shows lower (blue) and upper (red) interconnect regions.

Table A1. Dimensions and extents of the cell components.

	interconnect0	air channel	cathode	electrolyte	anode	fuel channel	interconnect1
xlow	0	0	0	0	0	0	0
xhigh	50	50	50	50	50	50	50
length [mm]	50	50	50	50	50	50	50
ylow	0	1	0	0	0	1	0
yhigh	4	3	4	4	4	3	4
width [mm]	4	2	4	4	4	2	4
zlow	0	3.5	5.00	5.29	5.3	6.3	6.3
zhigh	5	5.0	5.29	5.30	6.3	7.8	11.3
height [mm]	5	1.5	0.29	0.01	1	1.5	5

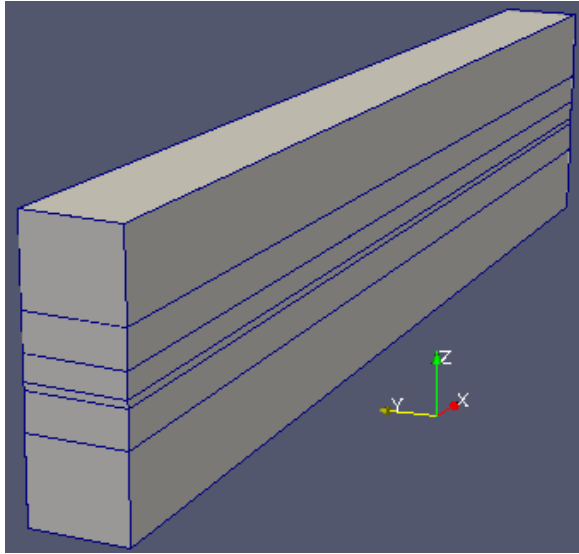


Figure A2. Vertical block structure. Bottom to top: interconnect0, air, cathode, electrolyte (too thin to discern), anode, fuel, and interconnect1.

We begin with a `blockMeshDict` dictionary that will create a parent mesh consisting of the seven vertical blocks (Figure A2), which for convenience, going from bottom to top, we refer to as interconnect0, air, cathode, electrolyte, anode, fuel, and interconnect1. Although the geometry shows symmetry about the  $y = 2$  plane, we construct the entire domain for illustrative purposes. Here is the list of points for the `blockMeshDict` file:

```
blockMeshDict
convertToMeters 0.001;

vertices
(
// ... From Bottom To Top
// Interconnect0
( 0 0 0) // 0
(50 0 0) // 1
(50 4 0) // 2
```

```

    ( 0 4 0)          // 3
// Interconnect0_to_Air
    ( 0 0 3.5)        // 4
    (50 0 3.5)        // 5
    (50 4 3.5)        // 6
    ( 0 4 3.5)        // 7
// Air_to_cathode
    ( 0 0 5.0)        // 8
    (50 0 5.0)        // 9
    (50 4 5.0)        //10
    ( 0 4 5.0)        //11
// cathode_to_Electrolyte
    ( 0 0 5.29)       //12
    (50 0 5.29)       //13
    (50 4 5.29)       //14
    ( 0 4 5.29)       //15
// Electrolyte_to_anode
    ( 0 0 5.3)        //16
    (50 0 5.3)        //17
    (50 4 5.3)        //18
    ( 0 4 5.3)        //19
// anode_to_Fuel
    ( 0 0 6.3)        //20
    (50 0 6.3)        //21
    (50 4 6.3)        //22
    ( 0 4 6.3)        //23
// fuel_to_Interconnect1
    ( 0 0 7.8)        //24
    (50 0 7.8)        //25
    (50 4 7.8)        //26
    ( 0 4 7.8)        //27
// Interconnect1
    ( 0 0 11.3)       //28
    (50 0 11.3)       //29
    (50 4 11.3)       //30
    ( 0 4 11.3)       //31
);

```

In the vertices section above, each set of four vertices defines a horizontal rectangle representing an interface between the above mentioned blocks (and including the top and bottom surfaces). As can be readily seen, the vertices of a rectangle are arranged so that a traversal from one to the next takes one anticlockwise around the rectangle, starting from  $x=0$ . Note that the coordinates are scaled by 0.001 metres, so the maximum  $x$ -coordinate, for example, is 50 mm. The vertices are numbered by their index in the list, beginning at index 0. Figure A3 shows the location of some of these points on the geometry.

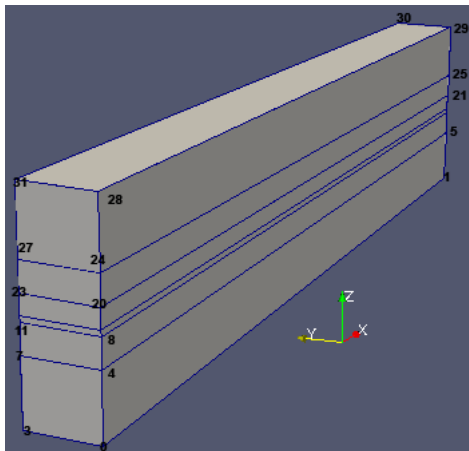


Figure A3. Location on geometry of selected vertices, as numbered by the `blockMeshDict` file.



In the blocks section below, each hexahedral block is defined by two successive sets of four vertices, i.e. the corner vertices of the block. The air block, eg, is defined by: hex (4 5 6 7 8 9 10 11). The number of cells in each coordinate direction and the grading of the mesh are also prescribed here.

```
blocks
(
// Interconnect0
  hex (0 1 2 3 4 5 6 7)      (25 8 7) simpleGrading (1 1 1)
// air
  hex (4 5 6 7 8 9 10 11)    (25 8 3) simpleGrading (1 1 1)
// cathode
  hex (8 9 10 11 12 13 14 15) (25 8 1) simpleGrading (1 1 1)
// electrolyte
  hex (12 13 14 15 16 17 18 19) (25 8 1) simpleGrading (1 1 1)
// anode
  hex (16 17 18 19 20 21 22 23) (25 8 2) simpleGrading (1 1 1)
// fuel
  hex (20 21 22 23 24 25 26 27) (25 8 3) simpleGrading (1 1 1)
// Interconnect1
  hex (24 25 26 27 28 29 30 31) (25 8 7) simpleGrading (1 1 1)
);
```

We have no need to define any edges.

```
edges
(
);
```

A patch consists of one or more outer boundaries of the blocks. These boundaries (rectangles in our case) are described by their corner vertices, arranged so that a traversal from one to the next takes one round the rectangle anticlockwise about the outward normal.

```
patches
(
// ... From Bottom to Top
// Interconnect0
  patch interconnect0Bottom
  (
    (0 3 2 1)
  )
  patch interconnect0Sides
  (
    (0 1 5 4)
    (3 7 6 2)
    (0 4 7 3)
    (1 2 6 5)
  )
// Air
  patch airInlet
  (
    (4 8 11 7)
  )
  patch airOutlet
  (
    (5 6 10 9)
  )
  patch airSides
  (
    (4 5 9 8)
    (7 11 10 6)
  )
// Cathode
```

```

    patch cathodeSides
    (
        (8 9 13 12)
        (11 15 14 10)
        (8 12 15 11)
        (9 10 14 13)
    )

// Electrolyte
    patch electrolyteSides
    (
        (12 13 17 16)
        (15 19 18 14)
        (12 16 19 15)
        (13 14 18 17)
    )

// Anode
    patch anodeSides
    (
        (16 17 21 20)
        (19 23 22 18)
        (16 20 23 19)
        (17 18 22 21)
    )

// Fuel
    patch fuelInlet
    (
        (20 24 27 23)
    )
    patch fuelOutlet
    (
        (21 22 26 25)
    )
    patch fuelSides
    (
        (20 21 25 24)
        (23 27 26 22)
    )

// interconnect1
    patch interconnect1Sides
    (
        (24 28 31 27)
        (25 26 30 29)
        (24 25 29 28)
        (27 31 30 26)
    )
    patch interconnect1Top
    (
        (28 29 30 31)
    )
);

mergePatchPairs
(
);

// ***** //

```

For more description of the blockMeshDict dictionary and the blockMesh utility, see section 5.3, *Mesh generation with the blockMesh utility*, in the *OpenFoam User Guide*, available at <http://www.openfoam.org/docs/>

We must now define the cellSets that will make up the cells of our five *regions*: interconnect0, air, electrolyte, fuel and interconnect1. Using the cellSets, a mesh will be generated for each region. Note that the cathode and anode *blocks* will become porousZones within the air and fuel *regions*, respectively. A portion of the air *block* contains two ribs that must become part of the interconnect0 *region*, and similarly two ribs contained in the fuel *block* must become part of the interconnect1 *region*. Cells in the electrolyte block will form the electrolyte region, and cells in the interconnect blocks will become part of the interconnect regions.

The cellSets for the regions are specified in `config/make.setSet`. Here each cellSet is defined by the diagonally opposite corners of a box bounded by coordinate planes.

The first set specified is the cellSet interconnect0. The specification begins with the cells in the interconnect0 block, which consists of all the cells below  $z=3.5\text{mm}$  (note that the coordinates are given in metres). Then the cells of the ribs are added. One of these extends from  $y=0\text{ mm}$  to  $y=1\text{ mm}$ , and the other from  $y=3\text{ mm}$  to  $y=4\text{ mm}$ . Both extend the full length of  $50\text{ mm}$  in  $x$ , and in height from  $z=3.5\text{ mm}$  to  $z=5\text{ mm}$ .

The specification for the air cellSet begins with the cathode block and adds the channel, which extends the full length of  $50\text{ mm}$  in  $x$ , from  $y=1\text{ mm}$  to  $y=3\text{ mm}$  in width, and from  $y=3.5\text{ mm}$  to  $y=5\text{ mm}$  in height. The remaining sets are similarly specified.

```
make.setSet cellSet interconnect0 new boxToCell (0 0.0e-3 0.0e-3) (50.0e-3 4.0e-3 3.5e-3)
cellSet interconnect0 add boxToCell (0 0.0e-3 3.5e-3) (50.0e-3 1.0e-3 5.0e-3)
cellSet interconnect0 add boxToCell (0 3.0e-3 3.5e-3) (50.0e-3 4.0e-3 5.0e-3)

cellSet air new boxToCell (0 0.0e-3 5.0e-3) (50.0e-3 4.0e-3 5.29e-3)
cellSet air add boxToCell (0 1.0e-3 3.5e-3) (50.0e-3 3.0e-3 5.0e-3)

cellSet electrolyte new boxToCell (0 0 5.29e-3) (50.0e-3 4.0e-3 5.3e-3)

cellSet fuel new boxToCell (0 0.0e-3 5.3e-3) (50.0e-3 4.0e-3 6.3e-3)
cellSet fuel add boxToCell (0 1.0e-3 6.3e-3) (50.0e-3 3.0e-3 7.8e-3)

cellSet interconnect1 new boxToCell (0 0.0e-3 7.8e-3) (50.0e-3 4.0e-3 11.3e-3)
cellSet interconnect1 add boxToCell (0 0.0e-3 6.3e-3) (50.0e-3 1.0e-3 7.8e-3)
cellSet interconnect1 add boxToCell (0 3.0e-3 6.3e-3) (50.0e-3 4.0e-3 7.8e-3)
```

The air and fuel regions are each given a porous zone within the fluid zone, as specified in `config/make.setAir` and `config/make.set fuel`:

#### **make.setAir**

```
cellSet air new boxToCell (0 0.0e-3 5.0e-3) (50.0e-3 4.0e-3 5.29e-3)
cellSet air add boxToCell (0 1.0e-3 3.5e-3) (50.0e-3 3.0e-3 5.0e-3)

cellSet cathode new boxToCell (0 0 5.0e-3) (40.0e-3 4.0e-3 5.29e-3)
```

#### **make.setFuel**

```
cellSet fuel new boxToCell (0 0.0e-3 5.3e-3) (50.0e-3 4.0e-3 6.3e-3)
cellSet fuel add boxToCell (0 1.0e-3 6.3e-3) (50.0e-3 3.0e-3 7.8e-3)

cellSet anode new boxToCell (0 0 5.3e-3) (50.0e-3 4.0e-3 6.3e-3)
```

Clearly, the fluid inlet and outlet patches on the global mesh are incorrect, since their original definitions include faces that are really part of the interconnect ribs. The correction proceeds in three steps. First, faceSets for all of the existing patches of the blockMesh are created using the patchToFace action of the faceSet utility, as specified by the `config/make.faceSet` file:

```
faceSet interconnect0Sides    new patchToFace interconnect0Sides all
faceSet interconnect0Bottom   new patchToFace interconnect0Bottom all

faceSet interconnect1Sides    new patchToFace interconnect1Sides all
faceSet interconnect1Top      new patchToFace interconnect1Top    all

faceSet electrolyteSides     new patchToFace electrolyteSides all

faceSet cathodeSides         new patchToFace cathodeSides all
faceSet airSides             new patchToFace airSides    all
faceSet airInlet             new patchToFace airInlet    all
faceSet airOutlet            new patchToFace airOutlet   all

faceSet anodeSides           new patchToFace anodeSides all
faceSet fuelSides            new patchToFace fuelSides   all
faceSet fuelInlet            new patchToFace fuelInlet   all
faceSet fuelOutlet           new patchToFace fuelOutlet  all

faceSet interconnect0Sides    add patchToFace airInlet   all
faceSet interconnect0Sides    add patchToFace airOutlet  all
faceSet interconnect0Sides    add patchToFace airSides   all

faceSet interconnect1Sides    add patchToFace fuelInlet  all
faceSet interconnect1Sides    add patchToFace fuelOutlet all
faceSet interconnect1Sides    add patchToFace fuelSides  all

faceSet airSides             clear
faceSet airInlet             clear
faceSet airOutlet            clear

faceSet fuelSides            clear
faceSet fuelInlet            clear
faceSet fuelOutlet           clear
```

Note that the `make.faceset` file also specifies some manipulations, adding faceSets `airInlet`, `airOutlet`, and `airSides` to the faceSet `interconnect0`, and similary on the fuel side. After being added, they are subsequently cleared. Next, the inlet and outlet faceSets are corrected using new specifications in `config/make.faceAir` and `config/make.faceFuel`:

#### **make.faceAir**

```
faceSet airInlet new boxToFace (-1e-6 1.0e-3 3.5e-3) (1e-6 3.0e-3 5.0e-3)

faceSet airOutlet new boxToFace (39.999e-3 1.0e-3 3.5e-3) (40.001e-3 3.0e-3 5.0e-3)

faceSet interconnect0Sides delete faceToFace airInlet all
faceSet interconnect0Sides delete faceToFace airOutlet all
```

#### **make.faceFuel**

```
faceSet fuelInlet new boxToFace (-1e-6 1e-3 6.3e-3) (1e-6 3.0e-3 7.8e-3)

faceSet fuelOutlet new boxToFace (39.999e-3 1e-3 6.3e-3) (40.001e-3 3.0e-3 7.8e-3)

faceSet interconnect1Sides delete faceToFace fuelInlet all
faceSet interconnect1Sides delete faceToFace fuelOutlet all
```

The new inlet and outlet patches are defined by a bounding box for the new patch. Here the new `airInlet`, eg, is normal to the  $x$ -direction and is bounded by a box which is shallow in  $x$ , extending

1e-6 m in front of and behind the prescribed  $x$ -coordinate location. The lateral extents of the box in the other two directions correspond to the lateral extent of the inlet in those directions. Faces with face centre within the box will be selected, so the box must not extend to the adjacent grid cell. The fuelInlet and the two outlets are similarly defined. The new inlets and outlets are then removed from the interconnect faceSets.

Finally, the faceSets are used to create new patches using the createPatch utility, which is controlled by the `system/createPatchDict` file. Here is an excerpt for the airInlet patch:

```
patchInfo
(
    {
        name airInlet;
        // Type of new patch
        dictionary
        {
            type patch;
        }
        constructFrom set;
        patches ();
        set airInlet;
    }
    . . .
);
```

We will find the following entry (with additional face numbering information) for the airInlet in the mesh boundary file.

```
airInlet
{
    type          patch;
}
```

The remaining patches are formed in the same way. The complete patch list is:

```
interconnect0Bottom
interconnect0Sides
airInlet
airOutlet
cathodeSides
electrolyteSides
anodeSides
fuelInlet
fuelOutlet
interconnect1Sides
interconnect1Top
```