

COVID-19-Spain-Analysis

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This notebook reports our initial analysis of COVID-19 incidence in Spain and the climatic correlates of incidence. The data have been organized in a package for ease of access and distribution. The name of the package is `covid19env` and if necessary can be installed from the GitHub repository.

Preliminaries

Load packages:

```
library(covid19env)
library(ggthemes)
library(gridExtra)
library(lubridate)
library(sf)
library(spdep)
library(spsur)
library(tidyverse)
library(units)
#library(spatialreg)
#library(systemfit)
#library(plm)
#library(splm)
```

Load data from package `covid19env`

```
data("covid19_spain")
```

Summarize the data:

```
covid19_spain %>%
  select(-geometry) %>%
  summary()
```

##	province	CCAA	ID_INE	
## Albacete	: 30	Castilla y Leon	:270	
## Alicante/Alacant	: 30	Andalucia	:240	
## Almeria	: 30	Castilla - La Mancha	:150	
## Araba/alava	: 30	Cataluña	:120	
## Asturias	: 30	Galicia	:120	
## Avila	: 30	Aragon	: 90	
## (Other)	:1320	(Other)	:510	
##	Date	Cases	Incidence	Population
## Min.	:2020-03-13	Min. : 1.0	Min. : 0.3832	Min. : 88636
## 1st Qu.	:2020-03-20	1st Qu.: 168.0	1st Qu.: 26.6722	1st Qu.: 331549
## Median	:2020-03-27	Median : 547.5	Median : 88.3491	Median : 684202
## Mean	:2020-03-27	Mean : 1485.7	Mean : 153.6087	Mean : 974257

```

## 3rd Qu.:2020-04-04 3rd Qu.: 1290.0 3rd Qu.: 209.6307 3rd Qu.:1149460
## Max. :2020-04-11 Max. :45849.0 Max. :1149.3577 Max. :6663394
##
## Older Median_Age Male2Female GDPpc Transit
## Min. :15.16 Min. :40.19 Min. : 91.59 Min. :16666 Min. :0.0
## 1st Qu.:18.02 1st Qu.:42.35 1st Qu.: 95.43 1st Qu.:18813 1st Qu.:0.0
## Median :19.93 Median :43.70 Median : 98.06 Median :20870 Median :0.0
## Mean :21.03 Mean :44.55 Mean : 97.83 Mean :22506 Mean :0.1
## 3rd Qu.:23.07 3rd Qu.:46.01 3rd Qu.:100.08 3rd Qu.:25901 3rd Qu.:0.0
## Max. :31.36 Max. :50.68 Max. :103.01 Max. :36001 Max. :1.0
##
## Area Altitude Coast Meteo_Station
## Min. :1.979e+09 Min. : 5.0 Min. :0.00 0016A : 30
## 1st Qu.:6.637e+09 1st Qu.: 24.0 1st Qu.:0.00 0076 : 30
## Median :1.001e+10 Median : 215.5 Median :0.00 0367 : 30
## Mean :1.012e+10 Mean : 369.0 Mean :0.42 1024E : 30
## 3rd Qu.:1.377e+10 3rd Qu.: 685.0 3rd Qu.:1.00 1082 : 30
## Max. :2.179e+10 Max. :1131.0 Max. :1.00 1111X : 30
## (Other):1320
## Max_Temp Min_Temp Mean_Temp Mean_Temp_lag8
## Min. : 3.10 Min. : -4.700 Min. : 1.00 Min. : 4.275
## 1st Qu.:14.68 1st Qu.: 4.400 1st Qu.: 9.80 1st Qu.: 9.637
## Median :17.30 Median : 7.600 Median :12.40 Median :11.600
## Mean :17.07 Mean : 7.289 Mean :12.18 Mean :11.779
## 3rd Qu.:19.80 3rd Qu.:10.200 3rd Qu.:14.60 3rd Qu.:13.713
## Max. :27.10 Max. :20.600 Max. :23.20 Max. :20.200
##
## Mean_Temp_lag11 Mean_Temp_lag11w Sunshine_Hours Sunshine_Hours_lag8
## Min. : 5.118 Min. : 4.201 Min. : 0.000 Min. : 0.000
## 1st Qu.: 9.770 1st Qu.: 9.803 1st Qu.: 1.800 1st Qu.: 4.938
## Median :11.795 Median :11.781 Median : 6.100 Median : 6.275
## Mean :11.872 Mean :11.903 Mean : 5.738 Mean : 6.221
## 3rd Qu.:13.598 3rd Qu.:13.941 3rd Qu.: 9.400 3rd Qu.: 7.781
## Max. :20.700 Max. :21.167 Max. :12.400 Max. :10.938
##
## Sunshine_Hours_lag11 Sunshine_Hours_lag11w Precipitation Precipitation_lag8
## Min. : 0.000 Min. : 0.000 Min. :0.0000 Min. :0.0000
## 1st Qu.: 5.164 1st Qu.: 4.771 1st Qu.:0.0000 1st Qu.:0.2500
## Median : 6.273 Median : 6.313 Median :0.0000 Median :0.3750
## Mean : 6.188 Mean : 6.212 Mean :0.4447 Mean :0.3762
## 3rd Qu.: 7.518 3rd Qu.: 7.862 3rd Qu.:1.0000 3rd Qu.:0.5000
## Max. :10.136 Max. :11.041 Max. :1.0000 Max. :1.0000
##
## Precipitation_lag11 Precipitation_lag11w Humidity Humidity_lag8
## Min. :0.0000 Min. :0.0000 Min. : 2.00 Min. :40.24
## 1st Qu.:0.2727 1st Qu.:0.1845 1st Qu.: 71.00 1st Qu.:70.30
## Median :0.3636 Median :0.3963 Median : 78.44 Median :75.98
## Mean :0.3834 Mean :0.3831 Mean : 77.82 Mean :75.00
## 3rd Qu.:0.5455 3rd Qu.:0.5631 3rd Qu.: 85.00 3rd Qu.:80.38
## Max. :1.0000 Max. :1.0000 Max. :100.00 Max. :94.61
##
## Humidity_lag11 Humidity_lag11w geometry
## Min. :42.20 Min. :40.10 MULTIPOLYGON :1500
## 1st Qu.:71.19 1st Qu.:70.94 epsg:4326 : 0

```

```
## Median :76.14 Median :76.99 +proj=long...: 0
## Mean :75.48 Mean :75.84
## 3rd Qu.:80.32 3rd Qu.:81.08
## Max. :93.36 Max. :94.04
##
```

The dataframe is a simple features object with information at the level of the province. The dataframe includes information about the province, including its Autonomous Community (a superior jurisdiction), an identifier, dates, COVID-19 cases and incidence. The period covered is from March 13, 2020 to April 11, 2020. In addition there are some demographic controls, and various climatic variables. Of interest are the lagged variables. The lagged variables are 8-day moving averages calculated using date-minus-12-days to date-minus-5-days, to account for the latency of the infection. More information about the dataset can be obtained by typing `?covid18_spain`.

There are 50 provinces in Spain:

```
nlevels(covid19_spain$province)
```

```
## [1] 50
```

The dataset covers 30 days:

```
T <- max(covid19_spain$Date) - min(covid19_spain$Date) + 1 # To include the starting day
T
```

```
## Time difference of 30 days
```

The order to shelter in place in Spain went into effect on March 16, 2020. March 13 is the first day that every province had at least one reported case of COVID-19.

Calculate population density and convert GDP per capita to thousands of euros:

```
covid19_spain <- covid19_spain %>%
  mutate(GDPpcc = GDPpcc/1000,
         Density = Population/units::set_units(st_area(covid19_spain), km^2))
```

Data exploration

Correlation analysis with Incidence:

```
covid19_spain %>%
  st_drop_geometry() %>%
  group_by(Date) %>%
  summarize(correlation_age = cor(Median_Age, Incidence),
            correlation_older = cor(Older, Incidence),
            correlation_m2f = cor(Male2Female, Incidence),
            correlation_density = cor(Density, Incidence),
            correlation_gdppc = cor(GDPpcc, Incidence),
            correlation_humidity = cor(Humidity_lag11, Incidence),
            correlation_temp = cor(Mean_Temp_lag11, Incidence),
            correlation_sunshine = cor(Sunshine_Hours_lag11, Incidence)) %>%
  summary()
```

```
##      Date      correlation_age correlation_older correlation_m2f
## Min.   :2020-03-13 Min.   : -0.07549 Min.   : -0.2646 Min.   : -0.088806
## 1st Qu.:2020-03-20 1st Qu.: 0.06498 1st Qu.: -0.2298 1st Qu.: -0.037567
## Median :2020-03-27 Median : 0.23377 Median : -0.2160 Median : 0.009642
## Mean   :2020-03-27 Mean   : 0.15994 Mean   : -0.2083 Mean   : 0.013288
## 3rd Qu.:2020-04-03 3rd Qu.: 0.26632 3rd Qu.: -0.1807 3rd Qu.: 0.066967
```

```
## Max. :2020-04-11 Max. : 0.27278 Max. :-0.1204 Max. : 0.106345
## correlation_density correlation_gdppc correlation_humidity correlation_temp
## Min. :-0.08832 Min. :0.2745 Min. :-0.03195 Min. :-0.6211
## 1st Qu.: -0.04832 1st Qu.:0.3354 1st Qu.: 0.04558 1st Qu.: -0.5997
## Median : 0.03670 Median :0.4257 Median : 0.14829 Median : -0.5504
## Mean : 0.03221 Mean :0.4035 Mean : 0.13657 Mean : -0.5160
## 3rd Qu.: 0.10103 3rd Qu.:0.4672 3rd Qu.: 0.20276 3rd Qu.: -0.4505
## Max. : 0.16734 Max. :0.5052 Max. : 0.31221 Max. : -0.2780
## correlation_sunshine
## Min. :-0.25196
## 1st Qu.: -0.12233
## Median : 0.07528
## Mean : 0.02127
## 3rd Qu.: 0.13996
## Max. : 0.24925
```

Correlation analysis with Incidence (log-transformed variables):

```
covid19_spain %>%
  st_drop_geometry() %>%
  group_by(Date) %>%
  summarize(correlation_age = cor(log(Median_Age), log(Incidence)),
            correlation_older = cor(log(Older), log(Incidence)),
            correlation_m2f = cor(log(Male2Female), log(Incidence)),
            correlation_density = cor(log(Density), log(Incidence)),
            correlation_gdppc = cor(log(GDPpc), log(Incidence)),
            correlation_humidity = cor(log(Humidity_lag11), log(Incidence)),
            correlation_temp = cor(log(Mean_Temp_lag11), log(Incidence)),
            correlation_sunshine = cor(log(Sunshine_Hours_lag11 + 0.1), log(Incidence))) %>%
  summary()
```

```
## Date correlation_age correlation_older
## Min. :2020-03-13 Min. : -0.05954 Min. : -0.218157
## 1st Qu.:2020-03-20 1st Qu.: 0.25912 1st Qu.: -0.176906
## Median :2020-03-27 Median : 0.40458 Median : -0.153385
## Mean :2020-03-27 Mean : 0.32729 Mean : -0.148579
## 3rd Qu.:2020-04-03 3rd Qu.: 0.44522 3rd Qu.: -0.137772
## Max. :2020-04-11 Max. : 0.45304 Max. : -0.006352
## correlation_m2f correlation_density correlation_gdppc correlation_humidity
## Min. : -0.127937 Min. : -0.37372 Min. : 0.2595 Min. : -0.056810
## 1st Qu.: -0.072667 1st Qu.: -0.34259 1st Qu.: 0.3314 1st Qu.: 0.004894
## Median : -0.049076 Median : -0.24061 Median : 0.3547 Median : 0.128513
## Mean : -0.047487 Mean : -0.21770 Mean : 0.3541 Mean : 0.133877
## 3rd Qu.: -0.023532 3rd Qu.: -0.14173 3rd Qu.: 0.3800 3rd Qu.: 0.267209
## Max. : 0.004793 Max. : 0.09139 Max. : 0.4123 Max. : 0.324925
## correlation_temp correlation_sunshine
## Min. : -0.7454 Min. : -0.01165
## 1st Qu.: -0.7230 1st Qu.: 0.17008
## Median : -0.6716 Median : 0.23303
## Mean : -0.6133 Mean : 0.21897
## 3rd Qu.: -0.5388 3rd Qu.: 0.29667
## Max. : -0.2716 Max. : 0.35854
```

There are 30 days in the dataset. We can summarize the incidence by week (excluding Canarias):

```

week11.plot <- covid19_spain %>%
  filter(CCAA != "Canarias") %>%
  group_by(province, week = isoweek(Date)) %>%
  summarise(mean_weekly_incidence = mean(Incidence)) %>%
  filter(week == 11) %>%
  ggplot() +
  geom_sf(aes(fill = mean_weekly_incidence)) +
  scale_fill_distiller(name = "Mean Weekly Incidence",
    palette = "Reds",
    direction = 1) +

  theme_tufte() +
  theme(axis.text = element_blank(),
    legend.position = "bottom") +
  facet_wrap(~week)

week12.plot <- covid19_spain %>%
  filter(CCAA != "Canarias") %>%
  group_by(province, week = isoweek(Date)) %>%
  summarise(mean_weekly_incidence = mean(Incidence)) %>%
  filter(week == 12) %>%
  ggplot() +
  geom_sf(aes(fill = mean_weekly_incidence)) +
  scale_fill_distiller(name = "Mean Weekly Incidence",
    palette = "Reds",
    direction = 1) +

  theme_tufte() +
  theme(axis.text = element_blank(),
    legend.position = "bottom") +
  facet_wrap(~week)

week13.plot <- covid19_spain %>%
  filter(CCAA != "Canarias") %>%
  group_by(province, week = isoweek(Date)) %>%
  summarise(mean_weekly_incidence = mean(Incidence)) %>%
  filter(week == 13) %>%
  ggplot() +
  geom_sf(aes(fill = mean_weekly_incidence)) +
  scale_fill_distiller(name = "Mean Weekly Incidence",
    palette = "Reds",
    direction = 1) +

  theme_tufte() +
  theme(axis.text = element_blank(),
    legend.position = "bottom") +
  facet_wrap(~week)

week14.plot <- covid19_spain %>%
  filter(CCAA != "Canarias") %>%
  group_by(province, week = isoweek(Date)) %>%
  summarise(mean_weekly_incidence = mean(Incidence)) %>%
  filter(week == 14) %>%
  ggplot() +
  geom_sf(aes(fill = mean_weekly_incidence)) +
  scale_fill_distiller(name = "Mean Weekly Incidence",

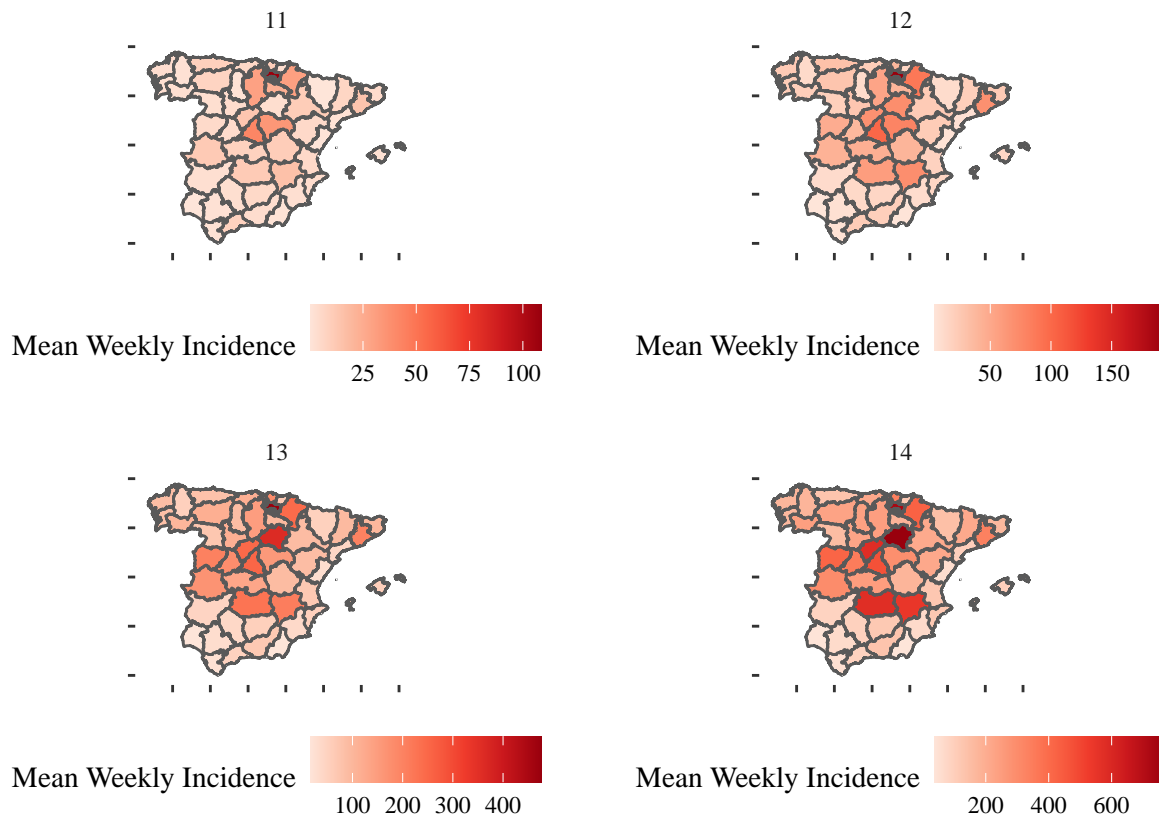
```

```

        palette = "Reds",
        direction = 1) +
theme_tufte() +
theme(axis.text = element_blank(),
      legend.position = "bottom") +
facet_wrap(~week)

grid.arrange(week11.plot, week12.plot, week13.plot, week14.plot, nrow = 2)

```

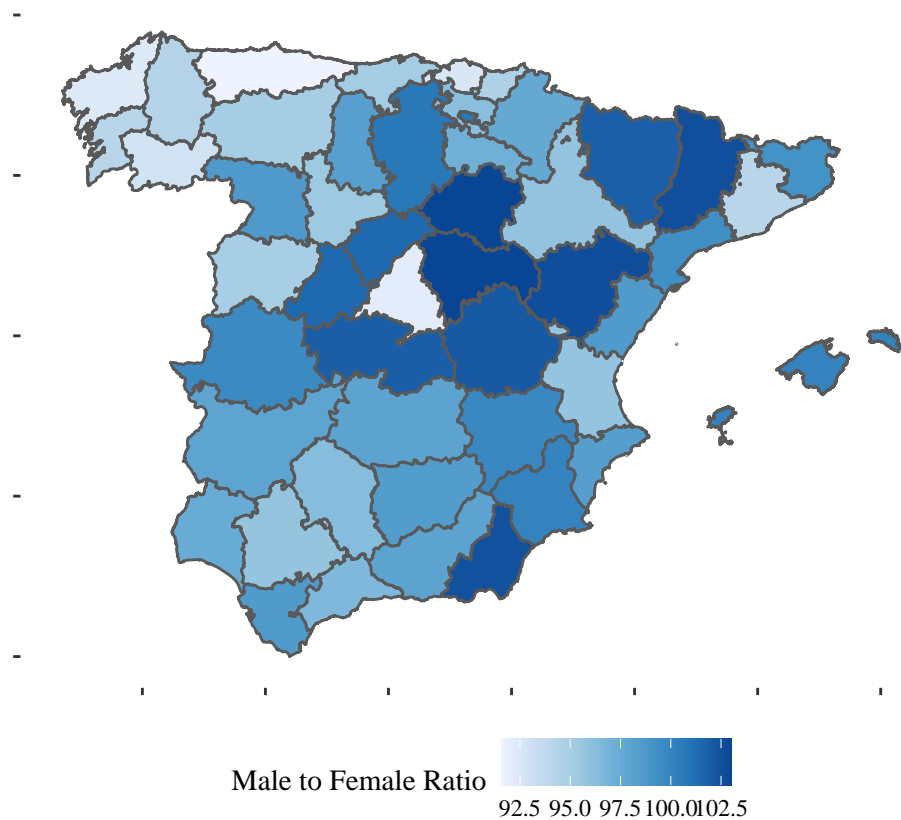


We consider some control variables: ratio of male to female in the province, median age of the population, population density:

```

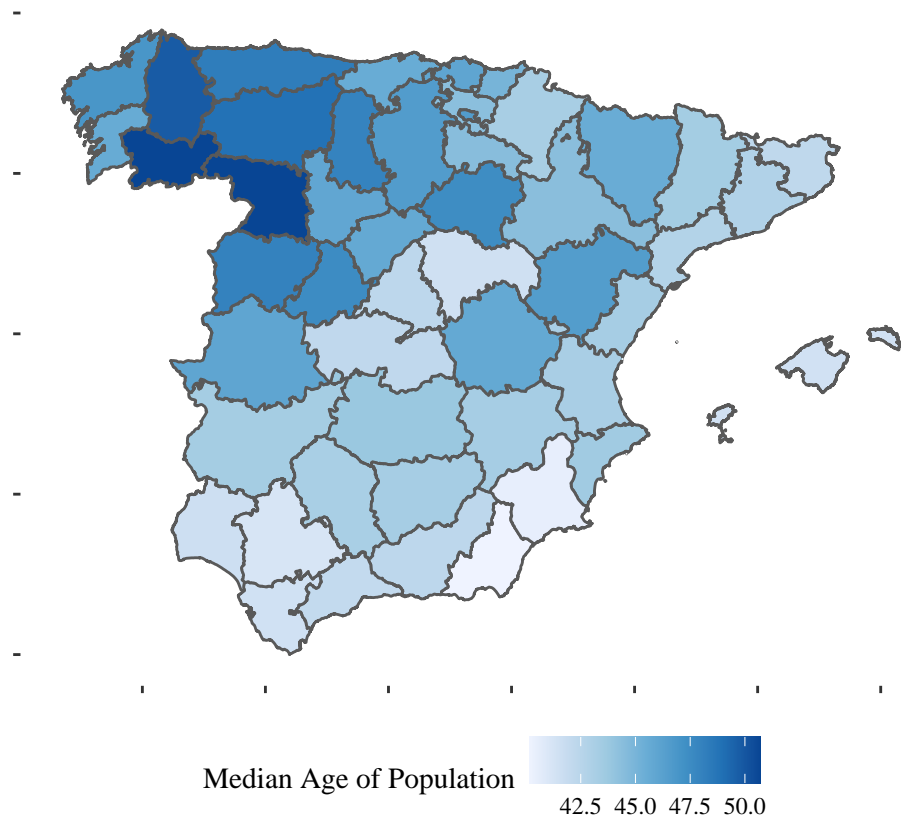
covid19_spain %>%
  filter(CCAA != "Canarias", Date == "2020-03-13") %>%
  ggplot() +
  geom_sf(aes(fill = Male2Female)) +
  scale_fill_distiller(name = "Male to Female Ratio",
                      palette = "Blues",
                      direction = 1) +
  theme_tufte() +
  theme(axis.text = element_blank(),
        legend.position = "bottom")

```



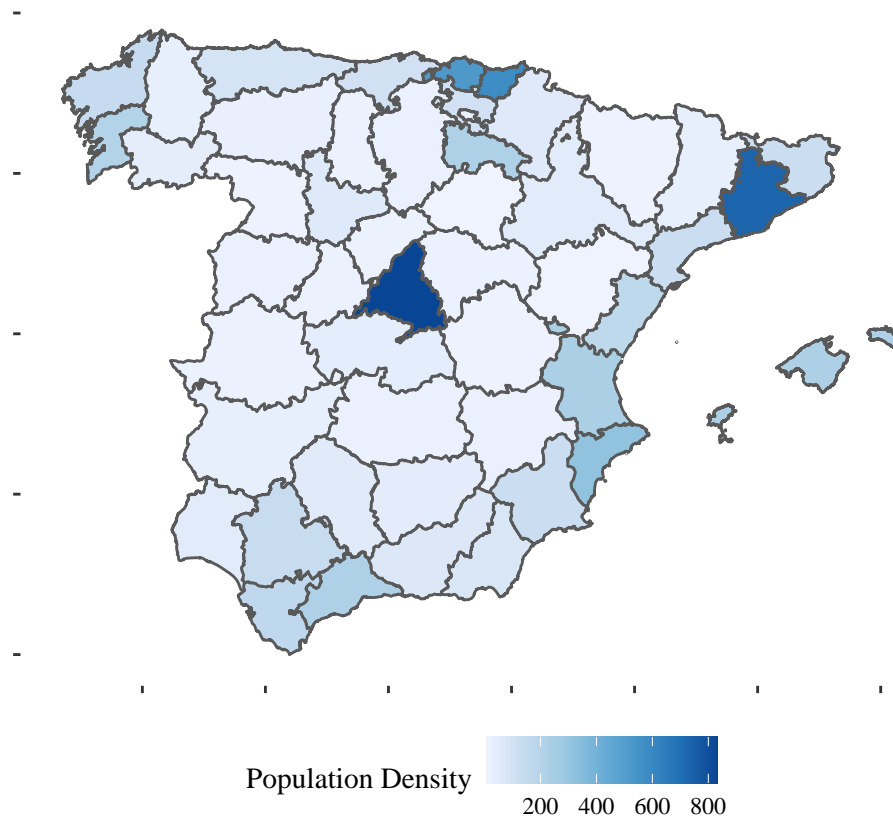
Median age of the population:

```
covid19_spain %>%
  filter(CCAA != "Canarias", Date == "2020-03-13") %>%
  ggplot() +
  geom_sf(aes(fill = Median_Age)) +
  scale_fill_distiller(name = "Median Age of Population",
    palette = "Blues",
    direction = 1) +
  theme_tufte() +
  theme(axis.text = element_blank(),
    legend.position = "bottom")
```



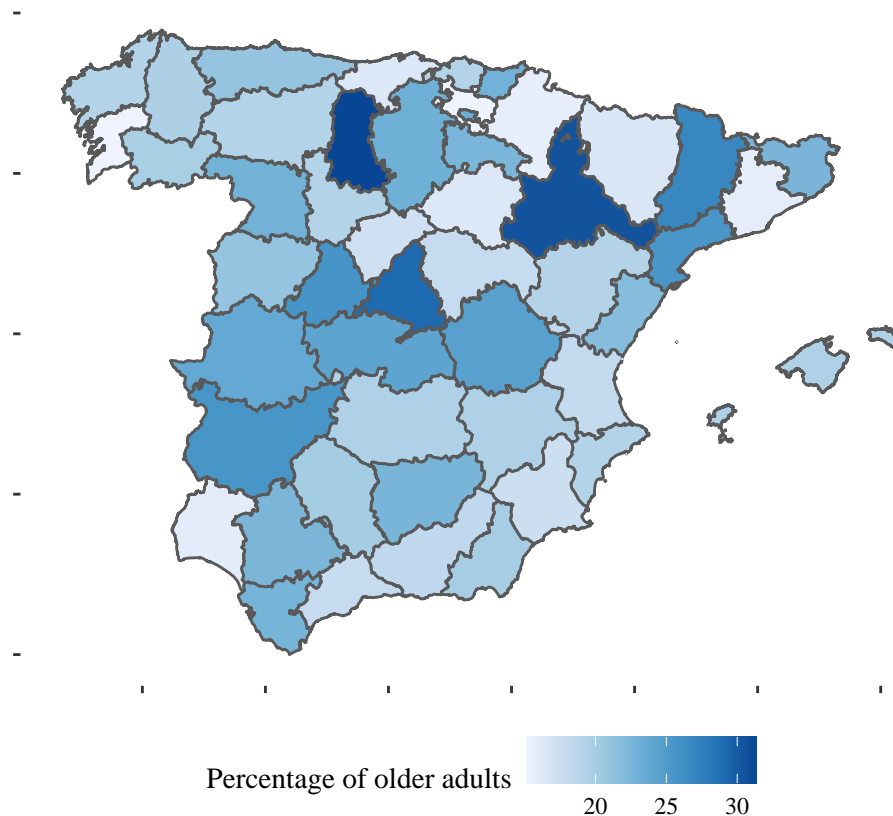
Population density:

```
covid19_spain %>%
  filter(CCAA != "Canarias", Date == "2020-03-13") %>%
  ggplot() +
  geom_sf(aes(fill = as.numeric(Density))) +
  scale_fill_distiller(name = "Population Density",
    palette = "Blues",
    direction = 1) +
  theme_tufte() +
  theme(axis.text = element_blank(),
    legend.position = "bottom")
```

Older people:

```
covid19_spain %>%
  filter(CCAA != "Canarias", Date == "2020-03-13") %>%
  ggplot() +
  geom_sf(aes(fill = as.numeric(Older))) +
  scale_fill_distiller(name = "Percentage of older adults",
    palette = "Blues",
    direction = 1) +
  theme_tufte() +
  theme(axis.text = element_blank(),
    legend.position = "bottom")
```



We are also interested in the climatic variables. To visualize the distribution of temperature by CCAA, we want to sort the communities by latitude, from north to south:

```
# Autonomous communities
ccaa.sf <- covid19_spain %>%
  filter(Date == "2020-03-13") %>%
  group_by(CCAA) %>%
  summarize(provinces = n())

# Extract coordinates of autonomous communities
ccaa.coords <- ccaa.sf %>%
  st_centroid() %>%
  st_coordinates() %>%
  as.data.frame()

## Warning in st_centroid.sf(.): st_centroid assumes attributes are constant over
## geometries of x

## Warning in st_centroid.sfc(st_geometry(x), of_largest_polygon =
## of_largest_polygon): st_centroid does not give correct centroids for longitude/
## latitude data

# Join Y coordinate to ccaa.sf
ccaa.sf <- ccaa.sf %>%
  mutate(long = ccaa.coords$Y)

# Sort autonomous communities from north to south
ccaa.levels <- ccaa.sf %>%
```

```

arrange(desc(long)) %>% select(CCAA)

ccaa.levels <- as.character(ccaa.levels$CCAA)

# Relevel autonomous communities
covid19_spain <- covid19_spain %>%
  mutate(CCAA = factor(CCAA, levels = ccaa.levels, ordered = TRUE))

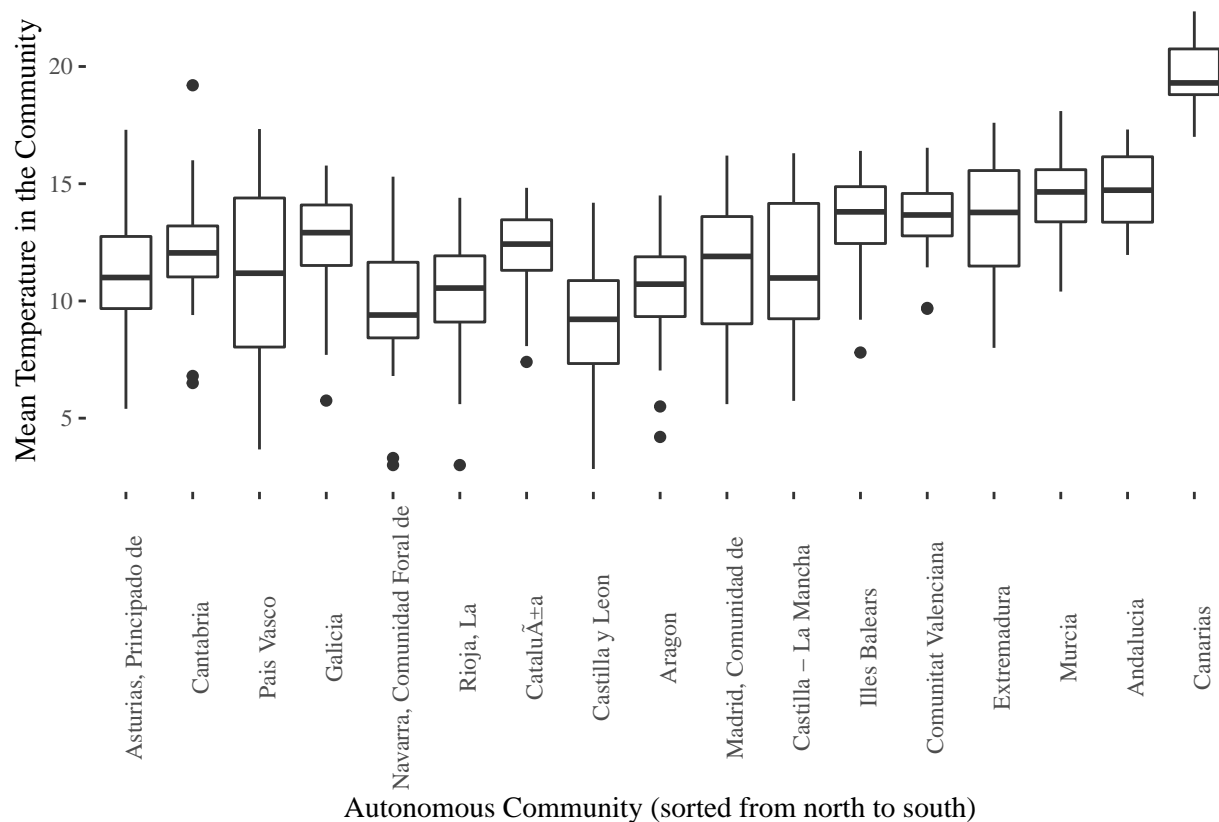
```

The following plot is the distribution of temperature by CCAA, sorted by latitude:

```

# Boxplots of temperatures
covid19_spain %>%
  st_drop_geometry() %>%
  group_by(CCAA, Date) %>%
  summarize(Mean_Temp = mean(Mean_Temp)) %>%
  ggplot(aes(x = CCAA, y = Mean_Temp)) +
  geom_boxplot() +
  theme_tufte() +
  theme(axis.text.x = element_text(angle = 90)) +
  xlab("Autonomous Community (sorted from north to south)") +
  ylab("Mean Temperature in the Community")

```



Multivariate analysis: comparison of approaches

Panel

- 1) Panel clásico

2) Panel Clásico o Dinámico

- Debe ser un modelo de efectos fijos para recoger la heterogeneidad entre las distintas provincias (efectos)
- Debería incluir estructura dinámica ya que la serie tiene una fuerte estructura temporal
- INCONVENIENTE: considera que la influencia del dato del día anterior es constante (se estima un coeficiente constante)
- INCONVENIENTE: No se pueden incluir variables constantes en T. La heterogeneidad entre provincias queda en el efecto fijo. No podemos por tanto incluir datos sobre estructura de la población.
- INCONVENIENTE: No podemos incorporar efectos espaciales. El paquete **splm** no incluye estimación de paneles dinámicos con efectos espaciales. Tendríamos que hacerlo en matlab con los códigos de P.Elhorst.

Spatial SUR

2) SUR espacial

- Hay un coeficiente para cada variable y cada instante de tiempo. Aunque es posible considerar coeficientes constantes para los periodos temporales que consideremos.
- La heterogeneidad espacial debemos incorporarla mediante variables explicativas. -> Estructura de la población relacionada con COVID-19.
- Permite incluir variables constantes en T.
- la dinámica temporal quedará recogida mediante el término independiente y la estructura de correlaciones en los residuos. EN TODO CASO, ENTIENDO QUE NUESTRO OBJETIVO NO ES EXPLICAR ESA TENDENCIA TEMPORAL (solo modelizarla para no incurrir en errores)

Prepare data for SUR analysis

*El modelo debe considerar efectos del 'individuo' y del 'tiempo' (para incorporar tendencia temporal)**

```
# Definición del panel para plm
GPanel <- plm::pdata.frame(covid19_spain %>%
                           st_drop_geometry() %>%
                           select(province,
                                  Date,
                                  Incidence,
                                  Median_Age,
                                  Male2Female,
                                  Older,
                                  GDPpc,
                                  Density,
                                  Transit,
                                  Mean_Temp_lag8,
                                  Humidity_lag8,
                                  Sunshine_Hours_lag8,
                                  Mean_Temp_lag11,
                                  Humidity_lag11,
                                  Sunshine_Hours_lag11,
                                  Mean_Temp_lag11w,
                                  Humidity_lag11w,
                                  Sunshine_Hours_lag11w),
                           c("province", "Date"))
```

Spatial SUR model

Create connectivity matrix:

```

# Extract provinces
provinces <- covid19_spain %>%
  filter(Date == "2020-03-13") %>%
  select(province, CCAA, ID_INE)

# Spatial weights matrix:
Wmat <- provinces %>%
  as("Spatial") %>%
  poly2nb(queen = FALSE) %>%
  nb2mat(zero.policy = TRUE)

Wmat <- (Wmat > 0) * 1

# Join the two provinces in Canarias
Wmat[which(provinces$province == "Palmas(Las)", which(provinces$province == "Santa Cruz de Tenerife")]
Wmat[which(provinces$province == "Santa Cruz de Tenerife", which(provinces$province == "Palmas(Las)")]

# 'Païses Catalans'
#n = 8
Wmat[which(provinces$province == "Barcelona", which(provinces$province == "Balears"))] <- 1
Wmat[which(provinces$province == "Balears", which(provinces$province == "Barcelona"))] <- 1
Wmat[which(provinces$province == "Balears", which(provinces$province == "Castellon/Castello"))] <- 1
Wmat[which(provinces$province == "Castellon/Castello", which(provinces$province == "Balears"))] <- 1
Wmat[which(provinces$province == "Balears", which(provinces$province == "Tarragona"))] <- 1
Wmat[which(provinces$province == "Tarragona", which(provinces$province == "Balears"))] <- 1
miW <- Wmat/rowSums(Wmat)

# Convert to listw
listw <- mat2listw(Wmat, style = "W")

```

Define formulas with three different lagged variables:

```

formula_lag8 <- log(Incidence) ~ log(Male2Female) +
  log(Median_Age) +
  #log(Older) +
  log(Density) +
  Transit +
  log(Humidity_lag8) +
  log(Mean_Temp_lag8)

formula_lag11 <- log(Incidence) ~ log(Male2Female) +
  log(Median_Age) +
  #log(Older) +
  log(Density) +
  Transit +
  log(Humidity_lag11) +
  log(Mean_Temp_lag11)

formula_lag11w <- log(Incidence) ~ log(Male2Female) +
  log(Median_Age) +
  #log(Older) +
  log(Density) +
  Transit +
  log(Humidity_lag11w) +

```

```
log(Mean_Temp_lag11w)
```

Create the terms needed to impose restrictions to the parameters for estimation. In this case we will restrict the two demographic variables and let Density, Transit, and the climatic variables to vary across equations. The rationale is that age and ratio of male to female do not change in the short period of time examined; on the other hand, while density and the presence of transit systems are also constants over the period examined, the behavior changed as a consequence of the lockdown: we expect these variables to be significant early on in the evolution of the pandemic, and become non-significant as the lockdown reduces their importance for the transmission of the virus.

```
# Recall that T is the number of days, i.e., time periods, i.e., equations
k <- 7 # Number of independent variables, including the constant
coef_rest <- 2 # Number of restrictions

# nrow is number of equations (time periods) minus 1, times the number of restrictions
# ncol is number of variables times number of equations
R2 <- matrix(0, nrow = (T - 1) * coef_rest, ncol = k * T)

for (i in 1:(T-1)){
  R2[i, 2] <- 1
  R2[i, (2 + i * k)] <- -1
  R2[(i + T - 1), 3] <- 1
  R2[(i + T - 1), (3 + i * k)] <- -1
  # Use if more restrictions are needed
  #R2[(i + T - 1) * 2, 4] <- 1
  #R2[(i + T - 1) * 2, (4 + i * k)] <- -1
}
b2 <- matrix(0, ncol = 21*coef_rest)
```

Model with a lagged 8-day moving average of climatic variables:

```
sur.slm_lag8 <- spsur::spsurtime(formula = formula_lag8,
                                data=GPanel,
                                time = GPanel$Date,
                                type = "slm",
                                fit_method = "3sls",
                                listw= listw,
                                R = R2,
                                b = b2)
```

```
## Time to fit the model: 0.89 seconds
```

```
summary(sur.slm_lag8)
```

```
## Call:
```

```
## spsur::spsurtime(formula = formula_lag8, data = GPanel, time = GPanel$Date,
##   listw = listw, type = "slm", fit_method = "3sls", R = R2,
##   b = b2)
```

```
##
```

```
##
```

```
## Spatial SUR model type: slm
```

```
##
```

```
## Equation 1
```

```
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_1    13.44984    15.11312  0.8899 0.373747
## log(Male2Female)_1 -1.64613     2.39352 -0.6877 0.491800
```

```

## log(Median_Age)_1      1.18476      1.28365  0.9230 0.356290
## log(Density)_1        0.17688      0.17088  1.0351 0.300918
## Transit_1             0.27409      0.57808  0.4741 0.635524
## log(Humidity_lag8)_1  -1.58699      0.50959 -3.1143 0.001906 **
## log(Mean_Temp_lag8)_1 -1.44960      0.49337 -2.9382 0.003390 **
## rho_1                 0.28975      0.12495  2.3189 0.020636 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.08196
## Equation 2
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_2      9.90840    15.05917  0.6580 0.51074
## log(Density)_2       0.12647     0.14855  0.8514 0.39479
## Transit_2           0.40609     0.50295  0.8074 0.41964
## log(Humidity_lag8)_2 -0.75235     0.38217 -1.9686 0.04932 *
## log(Mean_Temp_lag8)_2 -1.17165     0.38012 -3.0823 0.00212 **
## rho_2              0.18464     0.12882  1.4333 0.15214
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1062
## Equation 3
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_3     11.315709    15.029593  0.7529 0.4517206
## log(Density)_3      0.070084     0.132380  0.5294 0.5966581
## Transit_3           0.440808     0.448411  0.9830 0.3258638
## log(Humidity_lag8)_3 -0.943037     0.341707 -2.7598 0.0059080 **
## log(Mean_Temp_lag8)_3 -1.222653     0.330814 -3.6959 0.0002331 ***
## rho_3              0.235246     0.119393  1.9703 0.0491224 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1334
## Equation 4
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_4     10.9636059    15.0384801  0.7290 0.466179
## log(Density)_4      0.0067185     0.1175162  0.0572 0.954422
## Transit_4           0.5353207     0.3968522  1.3489 0.177722
## log(Humidity_lag8)_4 -0.7691966     0.2787003 -2.7599 0.005905 **
## log(Mean_Temp_lag8)_4 -1.0781542     0.2730226 -3.9490 8.497e-05 ***
## rho_4              0.1506806     0.1174745  1.2827 0.199957
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.134
## Equation 5
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_5     12.404953    15.018945  0.8260 0.4090613
## log(Density)_5     -0.030689     0.116477 -0.2635 0.7922445
## Transit_5           0.558137     0.395825  1.4101 0.1588868
## log(Humidity_lag8)_5 -0.974416     0.250970 -3.8826 0.0001113 ***
## log(Mean_Temp_lag8)_5 -1.222242     0.254942 -4.7942 1.927e-06 ***
## rho_5              0.187947     0.100177  1.8761 0.0609765 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1609
## Equation 6

```

```

##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_6      10.83049   15.03632  0.7203 0.4715444
## log(Density)_6     -0.10441    0.11948 -0.8739 0.3824357
## Transit_6           0.62866    0.41146  1.5279 0.1269159
## log(Humidity_lag8)_6 -0.68658    0.26991 -2.5438 0.0111423 *
## log(Mean_Temp_lag8)_6 -0.93650    0.24869 -3.7657 0.0001775 ***
## rho_6               0.25533    0.11077  2.3051 0.0214000 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.1304
## Equation 7
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_7      11.651636  15.026137  0.7754 0.438304
## log(Density)_7     -0.118801   0.114560 -1.0370 0.300020
## Transit_7           0.665989   0.391825  1.6997 0.089550 .
## log(Humidity_lag8)_7 -0.689727   0.239975 -2.8742 0.004152 **
## log(Mean_Temp_lag8)_7 -1.024375   0.217865 -4.7019 3.005e-06 ***
## rho_7               0.158391   0.094053  1.6841 0.092533 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.1886
## Equation 8
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_8      10.893160  15.030576  0.7247 0.46881
## log(Density)_8     -0.156578   0.109145 -1.4346 0.15177
## Transit_8           0.682642   0.369031  1.8498 0.06468 .
## log(Humidity_lag8)_8 -0.478301   0.214664 -2.2281 0.02613 *
## log(Mean_Temp_lag8)_8 -0.921982   0.184342 -5.0015 6.908e-07 ***
## rho_8               0.162020   0.081989  1.9761 0.04846 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.2021
## Equation 9
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_9      11.623896  15.014431  0.7742 0.43904
## log(Density)_9     -0.176662   0.110867 -1.5935 0.11143
## Transit_9           0.712788   0.376483  1.8933 0.05866 .
## log(Humidity_lag8)_9 -0.489376   0.198374 -2.4669 0.01382 *
## log(Mean_Temp_lag8)_9 -1.024812   0.179182 -5.7194 1.479e-08 ***
## rho_9               0.109777   0.068468  1.6033 0.10923
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.2419
## Equation 10
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_10      9.986345  15.016763  0.6650 0.50622
## log(Density)_10     -0.134631   0.109370 -1.2310 0.21867
## Transit_10           0.650723   0.369541  1.7609 0.07861 .
## log(Humidity_lag8)_10 -0.170465   0.216446 -0.7876 0.43117
## log(Mean_Temp_lag8)_10 -0.955550   0.186729 -5.1173 3.831e-07 ***
## rho_10              0.113468   0.074239  1.5284 0.12678
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.2302

```



```

## Equation 11
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_11      9.080799  15.041676  0.6037  0.54620
## log(Density)_11     -0.092801  0.099979 -0.9282  0.35357
## Transit_11          0.592621  0.327659  1.8087  0.07086 .
## log(Humidity_lag8)_11 0.178389  0.214850  0.8303  0.40660
## log(Mean_Temp_lag8)_11 -1.140343  0.172870 -6.5965 7.378e-11 ***
## rho_11              0.083585  0.070316  1.1887  0.23489
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.3347
## Equation 12
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_12     11.202061  15.022693  0.7457 0.4560686
## log(Density)_12     -0.102112  0.097964 -1.0423 0.2975502
## Transit_12          0.673300  0.317681  2.1194 0.0343435 *
## log(Humidity_lag8)_12 -0.311162  0.192144 -1.6194 0.1057267
## log(Mean_Temp_lag8)_12 -1.282355  0.154621 -8.2936 4.26e-16 ***
## rho_12              0.220517  0.060935  3.6189 0.0003133 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.3523
## Equation 13
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_13     12.155418  15.019873  0.8093 0.418575
## log(Density)_13     -0.084688  0.094181 -0.8992 0.368796
## Transit_13          0.666850  0.299118  2.2294 0.026048 *
## log(Humidity_lag8)_13 -0.456232  0.196078 -2.3268 0.020210 *
## log(Mean_Temp_lag8)_13 -1.367879  0.137606 -9.9405 < 2.2e-16 ***
## rho_13              0.203890  0.063754  3.1981 0.001435 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.4079
## Equation 14
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_14     12.895542  15.024485  0.8583 0.39097
## log(Density)_14     -0.049838  0.091133 -0.5469 0.58461
## Transit_14          0.626989  0.283113  2.2146 0.02705 *
## log(Humidity_lag8)_14 -0.491212  0.203993 -2.4080 0.01625 *
## log(Mean_Temp_lag8)_14 -1.530018  0.142998 -10.6995 < 2e-16 ***
## rho_14              0.154160  0.067569  2.2815 0.02276 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.4605
## Equation 15
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_15     14.026862  15.050704  0.9320 0.351614
## log(Density)_15     -0.035078  0.090952 -0.3857 0.699830
## Transit_15          0.586001  0.280933  2.0859 0.037283 *
## log(Humidity_lag8)_15 -0.637999  0.195857 -3.2575 0.001168 **
## log(Mean_Temp_lag8)_15 -1.732752  0.152369 -11.3721 < 2.2e-16 ***
## rho_15              0.167322  0.067711  2.4711 0.013664 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

## R-squared: 0.5013
## Equation 16
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_16    13.934761  15.057281   0.9255  0.354994
## log(Density)_16   -0.039661  0.091139  -0.4352  0.663547
## Transit_16        0.578650  0.282035   2.0517  0.040504 *
## log(Humidity_lag8)_16 -0.510355  0.169504  -3.0109  0.002682 **
## log(Mean_Temp_lag8)_16 -1.734221  0.150574 -11.5174 < 2.2e-16 ***
## rho_16            0.096357  0.074489   1.2936  0.196159
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5253
## Equation 17
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_17    15.446165  15.072955   1.0248  0.30577
## log(Density)_17   -0.053942  0.091087  -0.5922  0.55387
## Transit_17        0.564386  0.282279   1.9994  0.04588 *
## log(Humidity_lag8)_17 -0.666153  0.169635  -3.9270 9.296e-05 ***
## log(Mean_Temp_lag8)_17 -1.906077  0.162300 -11.7442 < 2.2e-16 ***
## rho_17            0.059027  0.070555   0.8366  0.40305
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5265
## Equation 18
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_18    15.011625  15.078440   0.9956  0.3197420
## log(Density)_18   -0.082739  0.089698  -0.9224  0.3565743
## Transit_18        0.544969  0.275978   1.9747  0.0486262 *
## log(Humidity_lag8)_18 -0.611894  0.157452  -3.8862 0.0001097 ***
## log(Mean_Temp_lag8)_18 -1.734835  0.153588 -11.2954 < 2.2e-16 ***
## rho_18            0.055856  0.069590   0.8026  0.4224054
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5295
## Equation 19
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_19    14.613467  15.015228   0.9732  0.3307
## log(Density)_19   -0.106579  0.090375  -1.1793  0.2386
## Transit_19        0.577372  0.277696   2.0792  0.0379 *
## log(Humidity_lag8)_19 -0.680824  0.147173  -4.6260 4.306e-06 ***
## log(Mean_Temp_lag8)_19 -1.457869  0.131353 -11.0989 < 2.2e-16 ***
## rho_19            0.079397  0.065463   1.2128  0.2255
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5129
## Equation 20
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_20    14.452286  15.008409   0.9629  0.33585
## log(Density)_20   -0.118009  0.088806  -1.3288  0.18426
## Transit_20        0.581016  0.270686   2.1465  0.03212 *
## log(Humidity_lag8)_20 -0.677635  0.130707  -5.1844 2.708e-07 ***
## log(Mean_Temp_lag8)_20 -1.351665  0.111138 -12.1620 < 2.2e-16 ***
## rho_20            0.066946  0.059594   1.1234  0.26160
## ---

```

```

## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5363
## Equation 21
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_21  14.645791  15.026485   0.9747   0.3300
## log(Density)_21  -0.120054   0.086631  -1.3858   0.1662
## Transit_21       0.598982   0.261444   2.2910   0.0222 *
## log(Humidity_lag8)_21 -0.720607   0.130180  -5.5355 4.132e-08 ***
## log(Mean_Temp_lag8)_21 -1.330940   0.103620 -12.8445 < 2.2e-16 ***
## rho_21           0.060944   0.060018   1.0154   0.3102
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5444
## Equation 22
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_22  14.362926  15.035956   0.9552   0.33973
## log(Density)_22  -0.136579   0.084839  -1.6099   0.10780
## Transit_22       0.631086   0.254599   2.4787   0.01338 *
## log(Humidity_lag8)_22 -0.641103   0.129807  -4.9389 9.453e-07 ***
## log(Mean_Temp_lag8)_22 -1.331418   0.094760 -14.0505 < 2.2e-16 ***
## rho_22           0.071593   0.058724   1.2191   0.22313
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5623
## Equation 23
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_23  12.704871  15.021699   0.8458 0.3979194
## log(Density)_23  -0.156511   0.084842  -1.8447 0.0654226 .
## Transit_23       0.638285   0.255450   2.4987 0.0126531 *
## log(Humidity_lag8)_23 -0.372171   0.105597  -3.5245 0.0004469 ***
## log(Mean_Temp_lag8)_23 -1.109823   0.074116 -14.9740 < 2.2e-16 ***
## rho_23           0.082617   0.058387   1.4150 0.1574346
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5538
## Equation 24
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_24  11.571789  15.011703   0.7709   0.44101
## log(Density)_24  -0.170206   0.085769  -1.9845   0.04752 *
## Transit_24       0.625484   0.259957   2.4061   0.01634 *
## log(Humidity_lag8)_24 -0.149682   0.108526  -1.3792   0.16819
## log(Mean_Temp_lag8)_24 -0.948109   0.062931 -15.0658 < 2e-16 ***
## rho_24           0.054686   0.059617   0.9173   0.35925
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5477
## Equation 25
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_25  11.436057  15.015283   0.7616   0.44649
## log(Density)_25  -0.172359   0.085584  -2.0139   0.04433 *
## Transit_25       0.614354   0.260000   2.3629   0.01836 *
## log(Humidity_lag8)_25 -0.100055   0.104985  -0.9530   0.34084
## log(Mean_Temp_lag8)_25 -0.925930   0.060577 -15.2853 < 2e-16 ***
## rho_25           0.036809   0.059081   0.6230   0.53343

```

```

## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5481
## Equation 26
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_26    11.050804   15.010081    0.7362  0.46180
## log(Density)_26   -0.166193    0.086393   -1.9237  0.05473 .
## Transit_26        0.613206    0.264079    2.3221  0.02046 *
## log(Humidity_lag8)_26 -0.048087    0.106885   -0.4499  0.65290
## log(Mean_Temp_lag8)_26 -0.915772    0.059732  -15.3314 < 2e-16 ***
## rho_26            0.061878    0.061026    1.0139  0.31090
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5477
## Equation 27
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_27    10.796678   15.012907    0.7192  0.47224
## log(Density)_27   -0.161802    0.086764   -1.8649  0.06254 .
## Transit_27        0.600227    0.265952    2.2569  0.02427 *
## log(Humidity_lag8)_27 0.027613    0.123835    0.2230  0.82360
## log(Mean_Temp_lag8)_27 -0.974149    0.066514  -14.6458 < 2e-16 ***
## rho_27            0.078597    0.062158    1.2645  0.20640
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5503
## Equation 28
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_28    11.358787   15.002356    0.7571  0.44918
## log(Density)_28   -0.179155    0.088430   -2.0260  0.04308 *
## Transit_28        0.637865    0.273633    2.3311  0.01998 *
## log(Humidity_lag8)_28 -0.086201    0.134724   -0.6398  0.52245
## log(Mean_Temp_lag8)_28 -1.011799    0.073558  -13.7550 < 2e-16 ***
## rho_28            0.109569    0.061852    1.7715  0.07684 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5377
## Equation 29
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_29    11.229688   14.990840    0.7491  0.45400
## log(Density)_29   -0.191128    0.089164   -2.1435  0.03235 *
## Transit_29        0.654982    0.276520    2.3687  0.01807 *
## log(Humidity_lag8)_29 0.023359    0.163680    0.1427  0.88655
## log(Mean_Temp_lag8)_29 -1.088102    0.082927  -13.1212 < 2e-16 ***
## rho_29            0.103976    0.062366    1.6672  0.09585 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5373
## Equation 30
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_30    11.799601   14.985307    0.7874  0.43126
## log(Density)_30   -0.203147    0.090973   -2.2330  0.02580 *
## Transit_30        0.708676    0.284437    2.4915  0.01291 *
## log(Humidity_lag8)_30 -0.090559    0.192976   -0.4693  0.63899
## log(Mean_Temp_lag8)_30 -1.135063    0.094097  -12.0627 < 2e-16 ***

```

```

## rho_30          0.131120    0.066634    1.9678    0.04942 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5224
##
## Variance-Covariance Matrix of inter-equation residuals:
##  1.1182563 0.9098830 0.7975777 0.6764132 0.6573438 0.6205371 0.5629458
##  0.9098830 0.8489919 0.7087750 0.6044651 0.5715793 0.5567053 0.5205337
##  0.7975777 0.7087750 0.6778503 0.5658804 0.5506614 0.5367463 0.4943378
##  0.6764132 0.6044651 0.5658804 0.5318687 0.5172578 0.5109135 0.4738031
##  0.6573438 0.5715793 0.5506614 0.5172578 0.5299510 0.5303869 0.4931065
##  0.6205371 0.5567053 0.5367463 0.5109135 0.5303869 0.5739233 0.5385649
##  0.5629458 0.5205337 0.4943378 0.4738031 0.4931065 0.5385649 0.5201109
##  0.5080998 0.4685015 0.4540600 0.4345078 0.4543341 0.4914405 0.4790405
##  0.5080792 0.4762366 0.4516895 0.4342009 0.4560982 0.4931051 0.4819448
##  0.4888787 0.4579890 0.4273290 0.4154211 0.4387660 0.4752772 0.4665190
##  0.4064836 0.3808485 0.3588320 0.3390001 0.3667017 0.4083891 0.4025867
##  0.3886870 0.3523288 0.3331740 0.3307107 0.3580395 0.3913384 0.3852520
##  0.3635691 0.3253283 0.3105545 0.3106044 0.3346028 0.3585879 0.3519485
##  0.3102844 0.2690953 0.2657039 0.2648937 0.2857021 0.3011191 0.2981952
##  0.2832341 0.2257763 0.2324307 0.2267824 0.2485109 0.2577685 0.2553555
##  0.2577883 0.2025333 0.2164185 0.2070461 0.2256172 0.2314749 0.2301749
##  0.2512318 0.1960556 0.2171990 0.2034817 0.2206736 0.2303925 0.2296815
##  0.2411016 0.2048401 0.2231717 0.2039157 0.2133636 0.2300124 0.2302032
##  0.2462636 0.2128767 0.2342385 0.2199733 0.2285836 0.2461629 0.2451034
##  0.2348479 0.2038085 0.2268670 0.2176839 0.2276584 0.2446452 0.2430821
##  0.2373443 0.2068991 0.2203575 0.2163976 0.2262305 0.2410271 0.2392672
##  0.2309067 0.2058150 0.2176650 0.2144721 0.2275759 0.2417591 0.2409240
##  0.2434555 0.2250270 0.2281998 0.2275158 0.2396575 0.2567190 0.2560850
##  0.2459870 0.2308055 0.2306944 0.2302194 0.2445972 0.2667857 0.2668520
##  0.2375664 0.2242284 0.2267040 0.2280443 0.2432602 0.2642168 0.2646949
##  0.2329468 0.2160497 0.2231339 0.2271739 0.2447450 0.2622730 0.2631072
##  0.2378358 0.2194221 0.2262530 0.2281592 0.2479629 0.2648656 0.2663098
##  0.2463596 0.2268734 0.2351032 0.2374519 0.2565107 0.2743179 0.2759697
##  0.2657724 0.2413598 0.2502876 0.2466617 0.2634294 0.2819760 0.2829029
##  0.2844912 0.2589161 0.2677859 0.2601064 0.2755990 0.2950404 0.2958718
##
##  0.5080998 0.5080792 0.4888787 0.4064836 0.3886870 0.3635691 0.3102844
##  0.4685015 0.4762366 0.4579890 0.3808485 0.3523288 0.3253283 0.2690953
##  0.4540600 0.4516895 0.4273290 0.3588320 0.3331740 0.3105545 0.2657039
##  0.4345078 0.4342009 0.4154211 0.3390001 0.3307107 0.3106044 0.2648937
##  0.4543341 0.4560982 0.4387660 0.3667017 0.3580395 0.3346028 0.2857021
##  0.4914405 0.4931051 0.4752772 0.4083891 0.3913384 0.3585879 0.3011191
##  0.4790405 0.4819448 0.4665190 0.4025867 0.3852520 0.3519485 0.2981952
##  0.4609818 0.4636371 0.4460184 0.3881292 0.3721895 0.3394506 0.2912645
##  0.4636371 0.4799172 0.4643012 0.4002880 0.3839802 0.3485212 0.2974496
##  0.4460184 0.4643012 0.4615898 0.3951360 0.3831288 0.3501339 0.3033439
##  0.3881292 0.4002880 0.3951360 0.3610488 0.3421241 0.3098382 0.2686876
##  0.3721895 0.3839802 0.3831288 0.3421241 0.3392774 0.3139455 0.2784981
##  0.3394506 0.3485212 0.3501339 0.3098382 0.3139455 0.2998876 0.2730688
##  0.2912645 0.2974496 0.3033439 0.2686876 0.2784981 0.2730688 0.2673035
##  0.2495380 0.2548824 0.2648024 0.2347936 0.2475743 0.2482378 0.2552850
##  0.2266161 0.2309677 0.2410772 0.2120717 0.2246656 0.2272649 0.2410773
##  0.2284788 0.2320303 0.2392739 0.2109035 0.2223194 0.2228242 0.2375652

```

```

## 0.2253434 0.2280957 0.2365653 0.2046085 0.2128612 0.2136131 0.2259514
## 0.2399977 0.2429692 0.2493331 0.2146787 0.2227406 0.2223622 0.2294533
## 0.2370444 0.2405428 0.2467085 0.2125932 0.2216113 0.2214191 0.2255987
## 0.2345275 0.2390049 0.2440450 0.2109345 0.2208199 0.2196407 0.2209132
## 0.2366663 0.2423519 0.2460292 0.2137252 0.2224521 0.2194128 0.2162320
## 0.2512650 0.2577597 0.2607560 0.2268153 0.2330974 0.2266185 0.2157006
## 0.2624037 0.2690936 0.2710753 0.2399336 0.2426413 0.2332263 0.2179459
## 0.2629026 0.2693367 0.2693623 0.2397556 0.2414201 0.2319320 0.2150718
## 0.2633565 0.2695508 0.2694714 0.2393372 0.2427601 0.2338846 0.2176473
## 0.2654196 0.2706231 0.2701444 0.2421062 0.2447460 0.2359340 0.2184462
## 0.2759477 0.2810033 0.2788040 0.2490042 0.2517742 0.2424033 0.2239736
## 0.2826218 0.2878577 0.2847598 0.2543157 0.2558090 0.2458586 0.2282654
## 0.2955134 0.3009646 0.2960788 0.2630423 0.2629472 0.2521501 0.2347855
##
## 0.2832341 0.2577883 0.2512318 0.2411016 0.2462636 0.2348479 0.2373443
## 0.2257763 0.2025333 0.1960556 0.2048401 0.2128767 0.2038085 0.2068991
## 0.2324307 0.2164185 0.2171990 0.2231717 0.2342385 0.2268670 0.2203575
## 0.2267824 0.2070461 0.2034817 0.2039157 0.2199733 0.2176839 0.2163976
## 0.2485109 0.2256172 0.2206736 0.2133636 0.2285836 0.2276584 0.2262305
## 0.2577685 0.2314749 0.2303925 0.2300124 0.2461629 0.2446452 0.2410271
## 0.2553555 0.2301749 0.2296815 0.2302032 0.2451034 0.2430821 0.2392672
## 0.2495380 0.2266161 0.2284788 0.2253434 0.2399977 0.2370444 0.2345275
## 0.2548824 0.2309677 0.2320303 0.2280957 0.2429692 0.2405428 0.2390049
## 0.2648024 0.2410772 0.2392739 0.2365653 0.2493331 0.2467085 0.2440450
## 0.2347936 0.2120717 0.2109035 0.2046085 0.2146787 0.2125932 0.2109345
## 0.2475743 0.2246656 0.2223194 0.2128612 0.2227406 0.2216113 0.2208199
## 0.2482378 0.2272649 0.2228242 0.2136131 0.2223622 0.2214191 0.2196407
## 0.2552850 0.2410773 0.2375652 0.2259514 0.2294533 0.2255987 0.2209132
## 0.2624821 0.2566046 0.2517908 0.2376993 0.2356831 0.2296993 0.2221658
## 0.2566046 0.2640318 0.2606083 0.2455221 0.2407362 0.2321358 0.2217893
## 0.2517908 0.2606083 0.2652298 0.2518928 0.2472647 0.2369299 0.2254833
## 0.2376993 0.2455221 0.2518928 0.2534618 0.2515873 0.2404095 0.2254803
## 0.2356831 0.2407362 0.2472647 0.2515873 0.2572028 0.2483143 0.2347442
## 0.2296993 0.2321358 0.2369299 0.2404095 0.2483143 0.2440474 0.2327884
## 0.2221658 0.2217893 0.2254833 0.2254803 0.2347442 0.2327884 0.2271684
## 0.2132450 0.2103830 0.2130556 0.2117976 0.2218485 0.2224014 0.2190310
## 0.2054870 0.2000081 0.2008179 0.2015290 0.2150022 0.2165845 0.2144128
## 0.2028056 0.1943581 0.1945849 0.1964925 0.2120108 0.2135439 0.2107637
## 0.1972612 0.1887374 0.1882220 0.1889529 0.2058000 0.2074861 0.2049809
## 0.2011878 0.1948343 0.1935556 0.1906264 0.2076221 0.2092928 0.2069818
## 0.2018652 0.1951470 0.1930729 0.1884839 0.2046535 0.2066972 0.2047792
## 0.2059062 0.1987343 0.1975735 0.1934682 0.2106335 0.2115829 0.2091759
## 0.2104721 0.2035866 0.2034142 0.2010676 0.2168705 0.2158188 0.2111561
## 0.2169451 0.2106802 0.2108704 0.2096812 0.2245050 0.2224997 0.2163060
##
## 0.2309067 0.2434555 0.2459870 0.2375664 0.2329468 0.2378358 0.2463596
## 0.2058150 0.2250270 0.2308055 0.2242284 0.2160497 0.2194221 0.2268734
## 0.2176650 0.2281998 0.2306944 0.2267040 0.2231339 0.2262530 0.2351032
## 0.2144721 0.2275158 0.2302194 0.2280443 0.2271739 0.2281592 0.2374519
## 0.2275759 0.2396575 0.2445972 0.2432602 0.2447450 0.2479629 0.2565107
## 0.2417591 0.2567190 0.2667857 0.2642168 0.2622730 0.2648656 0.2743179
## 0.2409240 0.2560850 0.2668520 0.2646949 0.2631072 0.2663098 0.2759697
## 0.2366663 0.2512650 0.2624037 0.2629026 0.2633565 0.2654196 0.2759477
## 0.2423519 0.2577597 0.2690936 0.2693367 0.2695508 0.2706231 0.2810033

```

```

## 0.2460292 0.2607560 0.2710753 0.2693623 0.2694714 0.2701444 0.2788040
## 0.2137252 0.2268153 0.2399336 0.2397556 0.2393372 0.2421062 0.2490042
## 0.2224521 0.2330974 0.2426413 0.2414201 0.2427601 0.2447460 0.2517742
## 0.2194128 0.2266185 0.2332263 0.2319320 0.2338846 0.2359340 0.2424033
## 0.2162320 0.2157006 0.2179459 0.2150718 0.2176473 0.2184462 0.2239736
## 0.2132450 0.2054870 0.2028056 0.1972612 0.2011878 0.2018652 0.2059062
## 0.2103830 0.2000081 0.1943581 0.1887374 0.1948343 0.1951470 0.1987343
## 0.2130556 0.2008179 0.1945849 0.1882220 0.1935556 0.1930729 0.1975735
## 0.2117976 0.2015290 0.1964925 0.1889529 0.1906264 0.1884839 0.1934682
## 0.2218485 0.2150022 0.2120108 0.2058000 0.2076221 0.2046535 0.2106335
## 0.2224014 0.2165845 0.2135439 0.2074861 0.2092928 0.2066972 0.2115829
## 0.2190310 0.2144128 0.2107637 0.2049809 0.2069818 0.2047792 0.2091759
## 0.2155609 0.2131507 0.2105506 0.2059294 0.2082041 0.2073625 0.2114568
## 0.2131507 0.2173215 0.2185256 0.2157320 0.2178583 0.2169750 0.2215207
## 0.2105506 0.2185256 0.2252666 0.2238428 0.2252476 0.2243633 0.2292011
## 0.2059294 0.2157320 0.2238428 0.2253841 0.2276629 0.2275096 0.2333216
## 0.2082041 0.2178583 0.2252476 0.2276629 0.2325492 0.2330875 0.2391740
## 0.2073625 0.2169750 0.2243633 0.2275096 0.2330875 0.2357819 0.2418572
## 0.2114568 0.2215207 0.2292011 0.2333216 0.2391740 0.2418572 0.2500889
## 0.2123163 0.2221423 0.2301153 0.2340278 0.2387875 0.2411770 0.2507076
## 0.2166782 0.2265436 0.2345692 0.2385635 0.2424450 0.2445660 0.2546775
##
## 0.2657724 0.2844912
## 0.2413598 0.2589161
## 0.2502876 0.2677859
## 0.2466617 0.2601064
## 0.2634294 0.2755990
## 0.2819760 0.2950404
## 0.2829029 0.2958718
## 0.2826218 0.2955134
## 0.2878577 0.3009646
## 0.2847598 0.2960788
## 0.2543157 0.2630423
## 0.2558090 0.2629472
## 0.2458586 0.2521501
## 0.2282654 0.2347855
## 0.2104721 0.2169451
## 0.2035866 0.2106802
## 0.2034142 0.2108704
## 0.2010676 0.2096812
## 0.2168705 0.2245050
## 0.2158188 0.2224997
## 0.2111561 0.2163060
## 0.2123163 0.2166782
## 0.2221423 0.2265436
## 0.2301153 0.2345692
## 0.2340278 0.2385635
## 0.2387875 0.2424450
## 0.2411770 0.2445660
## 0.2507076 0.2546775
## 0.2554745 0.2615465
## 0.2615465 0.2704584
## Correlation Matrix of inter-equation residuals:
## 1.0000000 0.9395027 0.9327644 0.9094724 0.8917049 0.8317093 0.8062810

```

```

## 0.9395027 1.0000000 0.9469363 0.9179331 0.8810722 0.8387579 0.8356912
## 0.9327644 0.9469363 1.0000000 0.9628235 0.9492536 0.9026160 0.8849747
## 0.9094724 0.9179331 0.9628235 1.0000000 0.9818689 0.9393822 0.9230122
## 0.8917049 0.8810722 0.9492536 0.9818689 1.0000000 0.9666258 0.9502732
## 0.8317093 0.8387579 0.9026160 0.9393822 0.9666258 1.0000000 0.9863324
## 0.8062810 0.8356912 0.8849747 0.9230122 0.9502732 0.9863324 1.0000000
## 0.7802418 0.8082898 0.8695466 0.9086021 0.9370476 0.9638972 0.9837897
## 0.7640322 0.8026225 0.8510437 0.8913394 0.9221923 0.9483977 0.9714496
## 0.7664403 0.8039683 0.8424087 0.8817270 0.9124242 0.9380080 0.9629372
## 0.7208953 0.7596372 0.7996409 0.8203149 0.8628262 0.9096441 0.9424088
## 0.7353983 0.7527048 0.7973631 0.8418122 0.8833505 0.9184453 0.9469511
## 0.7272438 0.7409775 0.7941053 0.8439265 0.8851922 0.9100965 0.9382179
## 0.6788623 0.6882012 0.7577612 0.7990155 0.8405829 0.8562044 0.8916840
## 0.6648600 0.6474126 0.7302037 0.7625425 0.8096666 0.8187746 0.8509940
## 0.6454822 0.6300627 0.7173193 0.7413823 0.7837422 0.7875529 0.8198045
## 0.6408993 0.6264440 0.7172991 0.7353279 0.7762583 0.7860381 0.8185581
## 0.6348248 0.6469200 0.7293641 0.7386143 0.7685933 0.7879704 0.8232600
## 0.6304260 0.6451214 0.7300443 0.7466505 0.7750649 0.7935537 0.8299260
## 0.6078913 0.6208222 0.7099523 0.7379364 0.7688228 0.7885963 0.8261308
## 0.6174739 0.6286410 0.7058095 0.7417513 0.7718430 0.7903930 0.8281807
## 0.6075916 0.6263525 0.7026072 0.7411249 0.7751893 0.7931763 0.8335094
## 0.6110813 0.6402525 0.7065761 0.7485466 0.7788432 0.8006672 0.8426748
## 0.6012068 0.6354145 0.6966112 0.7386988 0.7705922 0.7994248 0.8434175
## 0.5857780 0.6232889 0.6841388 0.7294873 0.7625026 0.7895644 0.8352333
## 0.5767611 0.6096751 0.6751568 0.7235008 0.7588857 0.7817300 0.8277837
## 0.5798275 0.6112650 0.6769316 0.7234152 0.7618892 0.7843567 0.8317006
## 0.5760556 0.6090332 0.6751830 0.7234587 0.7595617 0.7821496 0.8300400
## 0.5865288 0.6159921 0.6861155 0.7302561 0.7637597 0.7859728 0.8335224
## 0.5922902 0.6235134 0.6969794 0.7378387 0.7701497 0.7922736 0.8396815
##
## 0.7802418 0.7640322 0.7664403 0.7208953 0.7353983 0.7272438 0.6788623
## 0.8082898 0.8026225 0.8039683 0.7596372 0.7527048 0.7409775 0.6882012
## 0.8695466 0.8510437 0.8424087 0.7996409 0.7973631 0.7941053 0.7577612
## 0.9086021 0.8913394 0.8817270 0.8203149 0.8418122 0.8439265 0.7990155
## 0.9370476 0.9221923 0.9124242 0.8628262 0.8833505 0.8851922 0.8405829
## 0.9638972 0.9483977 0.9380080 0.9096441 0.9184453 0.9100965 0.8562044
## 0.9837897 0.9714496 0.9629372 0.9424088 0.9469511 0.9382179 0.8916840
## 1.0000000 0.9883266 0.9748732 0.9614730 0.9688993 0.9600488 0.9225595
## 0.9883266 1.0000000 0.9905286 0.9715006 0.9770898 0.9664239 0.9288267
## 0.9748732 0.9905286 1.0000000 0.9732596 0.9802361 0.9716284 0.9392402
## 0.9614730 0.9715006 0.9732596 1.0000000 0.9840528 0.9666545 0.9372570
## 0.9688993 0.9770898 0.9802361 0.9840528 1.0000000 0.9918345 0.9664762
## 0.9600488 0.9664239 0.9716284 0.9666545 0.9918345 1.0000000 0.9830598
## 0.9225595 0.9288267 0.9392402 0.9372570 0.9664762 0.9830598 1.0000000
## 0.8795254 0.8876485 0.9019387 0.8998626 0.9309714 0.9546228 0.9846056
## 0.8505835 0.8588943 0.8719169 0.8665346 0.8943760 0.9192006 0.9570526
## 0.8524389 0.8606125 0.8675610 0.8657234 0.8928664 0.9150909 0.9524498
## 0.8503687 0.8587925 0.8702536 0.8629411 0.8820316 0.9045842 0.9392147
## 0.8574846 0.8650991 0.8745184 0.8663197 0.8864351 0.9105920 0.9398567
## 0.8526263 0.8601422 0.8697341 0.8607284 0.8842414 0.9123496 0.9387097
## 0.8582924 0.8659064 0.8737271 0.8673975 0.8947868 0.9214666 0.9434736
## 0.8672115 0.8760538 0.8808157 0.8753457 0.9025147 0.9272687 0.9433094
## 0.8783801 0.8868807 0.8917530 0.8857702 0.9108205 0.9305232 0.9366862
## 0.8806239 0.8883587 0.8929700 0.8956245 0.9149755 0.9308735 0.9331822

```



```

## 0.8768472 0.8843743 0.8863506 0.8920968 0.9101465 0.9254029 0.9255843
## 0.8725690 0.8790513 0.8803533 0.8841675 0.9055789 0.9217833 0.9226056
## 0.8749532 0.8797090 0.8797228 0.8864620 0.9062280 0.9219001 0.9196489
## 0.8753568 0.8800738 0.8781320 0.8841006 0.9043508 0.9190438 0.9160918
## 0.8799410 0.8851563 0.8821685 0.8898794 0.9084582 0.9211335 0.9196569
## 0.8866000 0.8917948 0.8871679 0.8923803 0.9092806 0.9207068 0.9211770
##
## 0.6648600 0.6454822 0.6408993 0.6348248 0.6304260 0.6078913 0.6174739
## 0.6474126 0.6300627 0.6264440 0.6469200 0.6451214 0.6208222 0.6286410
## 0.7302037 0.7173193 0.7172991 0.7293641 0.7300443 0.7099523 0.7058095
## 0.7625425 0.7413823 0.7353279 0.7386143 0.7466505 0.7379364 0.7417513
## 0.8096666 0.7837422 0.7762583 0.7685933 0.7750649 0.7688228 0.7718430
## 0.8187746 0.7875529 0.7860381 0.7879704 0.7935537 0.7885963 0.7903930
## 0.8509940 0.8198045 0.8185581 0.8232600 0.8299260 0.8261308 0.8281807
## 0.8795254 0.8505835 0.8524389 0.8503687 0.8574846 0.8526263 0.8582924
## 0.8876485 0.8588943 0.8606125 0.8587925 0.8650991 0.8601422 0.8659064
## 0.9019387 0.8719169 0.8675610 0.8702536 0.8745184 0.8697341 0.8737271
## 0.8998626 0.8665346 0.8657234 0.8629411 0.8663197 0.8607284 0.8673975
## 0.9309714 0.8943760 0.8928664 0.8820316 0.8864351 0.8842414 0.8947868
## 0.9546228 0.9192006 0.9150909 0.9045842 0.9105920 0.9123496 0.9214666
## 0.9846056 0.9570526 0.9524498 0.9392147 0.9398567 0.9387097 0.9434736
## 1.0000000 0.9835270 0.9745940 0.9621515 0.9591709 0.9579210 0.9590388
## 0.9835270 1.0000000 0.9944443 0.9826281 0.9753675 0.9686863 0.9650295
## 0.9745940 0.9944443 1.0000000 0.9866377 0.9784295 0.9698561 0.9665505
## 0.9621515 0.9826281 0.9866377 1.0000000 0.9951449 0.9861821 0.9771171
## 0.9591709 0.9753675 0.9784295 0.9951449 1.0000000 0.9947676 0.9875375
## 0.9579210 0.9686863 0.9698561 0.9861821 0.9947676 1.0000000 0.9952038
## 0.9590388 0.9650295 0.9665505 0.9771171 0.9875375 0.9952038 1.0000000
## 0.9522336 0.9543732 0.9557707 0.9651320 0.9780236 0.9888400 0.9962210
## 0.9356944 0.9344477 0.9349513 0.9487098 0.9666954 0.9770207 0.9862938
## 0.9246170 0.9185492 0.9178463 0.9339705 0.9551507 0.9646836 0.9727741
## 0.9129562 0.9077744 0.9067633 0.9206876 0.9435361 0.9527336 0.9611004
## 0.9117168 0.9094989 0.9080059 0.9174796 0.9405607 0.9496166 0.9578649
## 0.9085418 0.9056585 0.9038818 0.9115256 0.9341835 0.9435104 0.9517015
## 0.9029433 0.9004463 0.8996510 0.9069937 0.9298150 0.9366860 0.9442594
## 0.9060328 0.9039426 0.9049590 0.9129075 0.9341304 0.9376010 0.9429922
## 0.9076897 0.9075098 0.9093358 0.9182569 0.9376407 0.9394191 0.9426586
##
## 0.6075916 0.6110813 0.6012068 0.5857780 0.5767611 0.5798275 0.5760556
## 0.6263525 0.6402525 0.6354145 0.6232889 0.6096751 0.6112650 0.6090332
## 0.7026072 0.7065761 0.6966112 0.6841388 0.6751568 0.6769316 0.6751830
## 0.7411249 0.7485466 0.7386988 0.7294873 0.7235008 0.7234152 0.7234587
## 0.7751893 0.7788432 0.7705922 0.7625026 0.7588857 0.7618892 0.7595617
## 0.7931763 0.8006672 0.7994248 0.7895644 0.7817300 0.7843567 0.7821496
## 0.8335094 0.8426748 0.8434175 0.8352333 0.8277837 0.8317006 0.8300400
## 0.8672115 0.8783801 0.8806239 0.8768472 0.8725690 0.8749532 0.8753568
## 0.8760538 0.8868807 0.8883587 0.8843743 0.8790513 0.8797090 0.8800738
## 0.8808157 0.8917530 0.8929700 0.8863506 0.8803533 0.8797228 0.8781320
## 0.8753457 0.8857702 0.8956245 0.8920968 0.8841675 0.8864620 0.8841006
## 0.9025147 0.9108205 0.9149755 0.9101465 0.9055789 0.9062280 0.9043508
## 0.9272687 0.9305232 0.9308735 0.9254029 0.9217833 0.9219001 0.9190438
## 0.9433094 0.9366862 0.9331822 0.9255843 0.9226056 0.9196489 0.9160918
## 0.9522336 0.9356944 0.9246170 0.9129562 0.9117168 0.9085418 0.9029433
## 0.9543732 0.9344477 0.9185492 0.9077744 0.9094989 0.9056585 0.9004463

```

```
## 0.9557707 0.9349513 0.9178463 0.9067633 0.9080059 0.9038818 0.8996510
## 0.9651320 0.9487098 0.9339705 0.9206876 0.9174796 0.9115256 0.9069937
## 0.9780236 0.9666954 0.9551507 0.9435361 0.9405607 0.9341835 0.9298150
## 0.9888400 0.9770207 0.9646836 0.9527336 0.9496166 0.9435104 0.9366860
## 0.9962210 0.9862938 0.9727741 0.9611004 0.9578649 0.9517015 0.9442594
## 1.0000000 0.9945309 0.9833104 0.9749365 0.9726801 0.9684356 0.9615898
## 0.9945309 1.0000000 0.9945642 0.9897989 0.9876032 0.9834079 0.9779959
## 0.9833104 0.9945642 1.0000000 0.9974381 0.9943443 0.9903946 0.9852962
## 0.9749365 0.9897989 0.9974381 1.0000000 0.9983473 0.9959015 0.9926243
## 0.9726801 0.9876032 0.9943443 0.9983473 1.0000000 0.9984008 0.9962314
## 0.9684356 0.9834079 0.9903946 0.9959015 0.9984008 1.0000000 0.9983921
## 0.9615898 0.9779959 0.9852962 0.9926243 0.9962314 0.9983921 1.0000000
## 0.9586247 0.9746107 0.9822450 0.9889078 0.9917670 0.9938476 0.9973189
## 0.9574329 0.9728912 0.9796161 0.9861065 0.9883909 0.9902297 0.9938142
##
## 0.5865288 0.5922902
## 0.6159921 0.6235134
## 0.6861155 0.6969794
## 0.7302561 0.7378387
## 0.7637597 0.7701497
## 0.7859728 0.7922736
## 0.8335224 0.8396815
## 0.8799410 0.8866000
## 0.8851563 0.8917948
## 0.8821685 0.8871679
## 0.8898794 0.8923803
## 0.9084582 0.9092806
## 0.9211335 0.9207068
## 0.9196569 0.9211770
## 0.9060328 0.9076897
## 0.9039426 0.9075098
## 0.9049590 0.9093358
## 0.9129075 0.9182569
## 0.9341304 0.9376407
## 0.9376010 0.9394191
## 0.9429922 0.9426586
## 0.9586247 0.9574329
## 0.9746107 0.9728912
## 0.9822450 0.9796161
## 0.9889078 0.9861065
## 0.9917670 0.9883909
## 0.9938476 0.9902297
## 0.9973189 0.9938142
## 1.0000000 0.9982288
## 0.9982288 1.0000000
##
## R-sq. pooled: 0.809
## Breusch-Pagan: 1.391e+04 p-value: ( 0)
```

Model with 11-day moving average of climatic variables:

```
sur.slm_lag11 <- spsur::spsurtime(formula = formula_lag11,
                                   data=GPanel,
                                   time = GPanel$Date,
                                   type = "slm",
```

```

fit_method = "3sls",
listw= listw,
R = R2,
b = b2)

```

```
## Time to fit the model: 1.47 seconds
```

```
summary(sur.slm_lag11)
```

```

## Call:
## spsur::spsurtime(formula = formula_lag11, data = GPanel, time = GPanel$Date,
##   listw = listw, type = "slm", fit_method = "3sls", R = R2,
##   b = b2)
##
##
## Spatial SUR model type: slm
##
## Equation 1
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_1      14.629030   16.470894  0.8882 0.374697
## log(Male2Female)_1  -0.904527   2.585106 -0.3499 0.726501
## log(Median_Age)_1   -0.017897   1.392574 -0.0129 0.989749
## log(Density)_1       0.136550   0.170853  0.7992 0.424383
## Transit_1           0.360881   0.584452  0.6175 0.537090
## log(Humidity_lag11)_1 -1.516207   0.538466 -2.8158 0.004978 **
## log(Mean_Temp_lag11)_1 -1.472902   0.543854 -2.7083 0.006899 **
## rho_1               0.251350   0.124413  2.0203 0.043666 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.08817
## Equation 2
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_2      12.193542   16.443626  0.7415 0.458573
## log(Density)_2       0.069136   0.150049  0.4608 0.645091
## Transit_2           0.494745   0.513068  0.9643 0.335175
## log(Humidity_lag11)_2 -0.866759   0.452838 -1.9141 0.055947 .
## log(Mean_Temp_lag11)_2 -1.255424   0.469681 -2.6729 0.007663 **
## rho_2               0.130364   0.134642  0.9682 0.333206
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1216
## Equation 3
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_3      13.731007   16.370585  0.8388 0.4018385
## log(Density)_3       0.030904   0.133802  0.2310 0.8173920
## Transit_3           0.532367   0.455176  1.1696 0.2424951
## log(Humidity_lag11)_3 -1.051189   0.404198 -2.6007 0.0094650 **
## log(Mean_Temp_lag11)_3 -1.372328   0.376460 -3.6453 0.0002832 ***
## rho_3               0.159108   0.109729  1.4500 0.1474229
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1558
## Equation 4
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_4      12.501692   16.322466  0.7659 0.4439362

```

```

## log(Density)_4      -0.025680    0.120706 -0.2127 0.8315772
## Transit_4          0.612406    0.404324  1.5146 0.1302341
## log(Humidity_lag11)_4 -0.721221    0.338721 -2.1292 0.0335197 *
## log(Mean_Temp_lag11)_4 -1.073654    0.285975 -3.7544 0.0001856 ***
## rho_4              -0.015448    0.114066 -0.1354 0.8923008
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1983
## Equation 5
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_5    14.142764  16.289745  0.8682 0.385529
## log(Density)_5   -0.055377   0.120579 -0.4593 0.646167
## Transit_5        0.627950   0.404600  1.5520 0.121027
## log(Humidity_lag11)_5 -1.025600   0.323097 -3.1743 0.001556 **
## log(Mean_Temp_lag11)_5 -1.214396   0.264019 -4.5996 4.873e-06 ***
## rho_5            0.096786   0.100526  0.9628 0.335922
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1949
## Equation 6
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_6    11.735140  16.296581  0.7201 0.471662
## log(Density)_6   -0.099212   0.121711 -0.8151 0.415216
## Transit_6        0.654297   0.409765  1.5968 0.110690
## log(Humidity_lag11)_6 -0.539603   0.301328 -1.7907 0.073688 .
## log(Mean_Temp_lag11)_6 -1.113703   0.249873 -4.4571 9.417e-06 ***
## rho_6            0.271843   0.093961  2.8931 0.003911 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1548
## Equation 7
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_7    11.932745  16.296770  0.7322 0.46424
## log(Density)_7   -0.104978   0.115272 -0.9107 0.36271
## Transit_7        0.675328   0.381943  1.7681 0.07740 .
## log(Humidity_lag11)_7 -0.389970   0.291831 -1.3363 0.18181
## log(Mean_Temp_lag11)_7 -1.245946   0.235530 -5.2900 1.556e-07 ***
## rho_7            0.181812   0.088046  2.0650 0.03923 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.2324
## Equation 8
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_8    10.676475  16.296563  0.6551 0.512556
## log(Density)_8   -0.138786   0.108299 -1.2815 0.200365
## Transit_8        0.669846   0.352228  1.9017 0.057542 .
## log(Humidity_lag11)_8 -0.057655   0.259165 -0.2225 0.824006
## log(Mean_Temp_lag11)_8 -1.183232   0.208072 -5.6866 1.779e-08 ***
## rho_8            0.201888   0.076957  2.6234 0.008861 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.2642
## Equation 9
##               Estimate Std. Error t value Pr(>|t|)

```

```

## (Intercept)_9      13.50679    16.29780    0.8287    0.40748
## log(Density)_9     -0.15332    0.10988   -1.3953    0.16329
## Transit_9          0.70830    0.35883    1.9739    0.04872 *
## log(Humidity_lag11)_9 -0.43529    0.26379   -1.6501    0.09928 .
## log(Mean_Temp_lag11)_9 -1.50867    0.21546   -7.0020  5.113e-12 ***
## rho_9              0.16232    0.07286    2.2278    0.02615 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.3066
## Equation 10
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_10      12.969008   16.327996    0.7943    0.42725
## log(Density)_10     -0.110080    0.108645   -1.0132    0.31125
## Transit_10          0.649647    0.352497    1.8430    0.06568 .
## log(Humidity_lag11)_10 -0.367708    0.278671   -1.3195    0.18735
## log(Mean_Temp_lag11)_10 -1.462839    0.219079   -6.6772  4.385e-11 ***
## rho_10              0.176127    0.082495    2.1350    0.03305 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.2938
## Equation 11
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_11      11.769604   16.333387    0.7206    0.47136
## log(Density)_11     -0.052600    0.098948   -0.5316    0.59515
## Transit_11          0.578678    0.308295    1.8770    0.06086 .
## log(Humidity_lag11)_11 0.017457    0.246537    0.0708    0.94357
## log(Mean_Temp_lag11)_11 -1.687958    0.186964   -9.0282 < 2e-16 ***
## rho_11              0.180616    0.072046    2.5070    0.01236 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.4127
## Equation 12
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_12      12.658288   16.302283    0.7765    0.43768
## log(Density)_12     -0.057667    0.097644   -0.5906    0.55496
## Transit_12          0.618549    0.301196    2.0536    0.04031 *
## log(Humidity_lag11)_12 -0.219238    0.221715   -0.9888    0.32303
## log(Mean_Temp_lag11)_12 -1.736247    0.166494  -10.4283 < 2.2e-16 ***
## rho_12              0.279737    0.066705    4.1937  3.032e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.427
## Equation 13
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)_13      12.513851   16.279019    0.7687    0.44228
## log(Density)_13     -0.039997    0.096066   -0.4163    0.67726
## Transit_13          0.602197    0.292599    2.0581    0.03988 *
## log(Humidity_lag11)_13 -0.127564    0.216479   -0.5893    0.55584
## log(Mean_Temp_lag11)_13 -1.759523    0.157667  -11.1597 < 2e-16 ***
## rho_13              0.238324    0.073003    3.2646    0.00114 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.4612
## Equation 14

```

```

##               Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_14      12.3940094  16.2958838   0.7606  0.447130
## log(Density)_14     -0.0091049  0.0945154  -0.0963  0.923279
## Transit_14          0.5808808  0.2846887   2.0404  0.041617 *
## log(Humidity_lag11)_14 -0.0103824  0.2304013  -0.0451  0.964068
## log(Mean_Temp_lag11)_14 -1.9040191  0.1669811 -11.4026 < 2.2e-16 ***
## rho_14              0.2266333  0.0832808   2.7213  0.006635 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.4876
## Equation 15
##               Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_15      14.198401  16.294419   0.8714  0.38380
## log(Density)_15     -0.010121  0.094642  -0.1069  0.91486
## Transit_15          0.562876  0.285864   1.9690  0.04927 *
## log(Humidity_lag11)_15 -0.304009  0.210829  -1.4420  0.14968
## log(Mean_Temp_lag11)_15 -2.067982  0.168936 -12.2412 < 2e-16 ***
## rho_15              0.221668  0.084582   2.6208  0.00893 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5022
## Equation 16
##               Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_16      15.389135  16.255615   0.9467  0.344062
## log(Density)_16     -0.039820  0.093012  -0.4281  0.668677
## Transit_16          0.583757  0.280552   2.0807  0.037755 *
## log(Humidity_lag11)_16 -0.512681  0.187811  -2.7298  0.006468 **
## log(Mean_Temp_lag11)_16 -1.917253  0.144258 -13.2905 < 2.2e-16 ***
## rho_16              0.123229  0.080208   1.5364  0.124821
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5181
## Equation 17
##               Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_17      16.583592  16.283676   1.0184  0.30877
## log(Density)_17     -0.054357  0.090620  -0.5998  0.54878
## Transit_17          0.568251  0.271472   2.0932  0.03662 *
## log(Humidity_lag11)_17 -0.704847  0.176550  -3.9923 7.106e-05 ***
## log(Mean_Temp_lag11)_17 -1.972727  0.134174 -14.7027 < 2.2e-16 ***
## rho_17              0.106902  0.072402   1.4765  0.14018
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5361
## Equation 18
##               Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_18      16.399448  16.310391   1.0055  0.31496
## log(Density)_18     -0.072837  0.088860  -0.8197  0.41262
## Transit_18          0.543271  0.264227   2.0561  0.04008 *
## log(Humidity_lag11)_18 -0.726772  0.164532  -4.4172 1.128e-05 ***
## log(Mean_Temp_lag11)_18 -1.793886  0.126960 -14.1295 < 2.2e-16 ***
## rho_18              0.105993  0.074863   1.4158  0.15719
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5363

```

```

## Equation 19
##
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_19 16.076853 16.278873 0.9876 0.3236
## log(Density)_19 -0.082281 0.088634 -0.9283 0.3535
## Transit_19 0.564585 0.262698 2.1492 0.0319 *
## log(Humidity_lag11)_19 -0.694444 0.149719 -4.6383 4.063e-06 ***
## log(Mean_Temp_lag11)_19 -1.695501 0.116367 -14.5703 < 2.2e-16 ***
## rho_19 0.109702 0.069122 1.5871 0.1129
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.54
## Equation 20
##
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_20 15.160852 16.238739 0.9336 0.35076
## log(Density)_20 -0.103747 0.087976 -1.1793 0.23863
## Transit_20 0.580146 0.259345 2.2370 0.02555 *
## log(Humidity_lag11)_20 -0.561856 0.125979 -4.4599 9.295e-06 ***
## log(Mean_Temp_lag11)_20 -1.473536 0.094878 -15.5308 < 2.2e-16 ***
## rho_20 0.091279 0.063698 1.4330 0.15222
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.556
## Equation 21
##
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_21 13.460221 16.220717 0.8298 0.40687
## log(Density)_21 -0.122404 0.087124 -1.4049 0.16040
## Transit_21 0.609860 0.255052 2.3911 0.01701 *
## log(Humidity_lag11)_21 -0.249241 0.121356 -2.0538 0.04030 *
## log(Mean_Temp_lag11)_21 -1.290527 0.082272 -15.6861 < 2e-16 ***
## rho_21 0.092022 0.060692 1.5162 0.12984
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5565
## Equation 22
##
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_22 13.060770 16.228353 0.8048 0.42115
## log(Density)_22 -0.134818 0.086664 -1.5556 0.12016
## Transit_22 0.619686 0.253088 2.4485 0.01455 *
## log(Humidity_lag11)_22 -0.120788 0.114264 -1.0571 0.29077
## log(Mean_Temp_lag11)_22 -1.270509 0.076472 -16.6141 < 2e-16 ***
## rho_22 0.073698 0.055067 1.3383 0.18114
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5678
## Equation 23
##
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_23 12.615553 16.226275 0.7775 0.43709
## log(Density)_23 -0.153641 0.087418 -1.7575 0.07918 .
## Transit_23 0.627057 0.256737 2.4424 0.01479 *
## log(Humidity_lag11)_23 -0.053045 0.111983 -0.4737 0.63584
## log(Mean_Temp_lag11)_23 -1.173851 0.072147 -16.2702 < 2e-16 ***
## rho_23 0.084021 0.054908 1.5302 0.12634
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

## R-squared: 0.5557
## Equation 24
##
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_24      12.692323   16.225954   0.7822  0.43430
## log(Density)_24      -0.170841    0.088230  -1.9363  0.05316 .
## Transit_24           0.633496    0.260352   2.4332  0.01517 *
## log(Humidity_lag11)_24 -0.092738    0.121198  -0.7652  0.44438
## log(Mean_Temp_lag11)_24 -1.101979    0.070252 -15.6861 < 2e-16 ***
## rho_24               0.089132    0.056186   1.5864  0.11303
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5519
## Equation 25
##
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_25      12.580587   16.218016   0.7757  0.43813
## log(Density)_25      -0.183709    0.089018  -2.0637  0.03934 *
## Transit_25           0.642159    0.264171   2.4308  0.01527 *
## log(Humidity_lag11)_25 -0.110232    0.113168  -0.9741  0.33030
## log(Mean_Temp_lag11)_25 -1.059127    0.068533 -15.4543 < 2e-16 ***
## rho_25               0.121523    0.054240   2.2405  0.02532 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5429
## Equation 26
##
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_26      12.466653   16.207376   0.7692  0.441990
## log(Density)_26      -0.180917    0.089877  -2.0130  0.044433 *
## Transit_26           0.654779    0.268053   2.4427  0.014779 *
## log(Humidity_lag11)_26 -0.073808    0.120675  -0.6116  0.540948
## log(Mean_Temp_lag11)_26 -1.126717    0.071736 -15.7064 < 2.2e-16 ***
## rho_26               0.150934    0.053573   2.8173  0.004954 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5408
## Equation 27
##
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_27      12.4101232  16.2038461   0.7659  0.443962
## log(Density)_27      -0.1845649   0.0906946  -2.0350  0.042158 *
## Transit_27           0.6598972   0.2716998   2.4288  0.015356 *
## log(Humidity_lag11)_27  0.0014789   0.1338886   0.0110  0.991190
## log(Mean_Temp_lag11)_27 -1.2522642   0.0822244 -15.2298 < 2.2e-16 ***
## rho_27               0.1732159   0.0525717   3.2949  0.001025 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5367
## Equation 28
##
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_28      12.731725   16.201815   0.7858  0.4321906
## log(Density)_28      -0.206392    0.092131  -2.2402  0.0253353 *
## Transit_28           0.713556    0.278322   2.5638  0.0105243 *
## log(Humidity_lag11)_28 -0.029016    0.168926  -0.1718  0.8636629
## log(Mean_Temp_lag11)_28 -1.348480    0.096810 -13.9292 < 2.2e-16 ***
## rho_28               0.215247    0.055315   3.8913  0.0001075 ***
## ---

```



```

## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5217
## Equation 29
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_29      11.656206   16.205890    0.7193   0.472179
## log(Density)_29      -0.222011    0.093049   -2.3860   0.017252 *
## Transit_29           0.732949    0.282543    2.5941   0.009646 **
## log(Humidity_lag11)_29  0.285970    0.194118    1.4732   0.141073
## log(Mean_Temp_lag11)_29 -1.436209    0.111171  -12.9189 < 2.2e-16 ***
## rho_29               0.227926    0.056760    4.0156  6.452e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5152
## Equation 30
##
##           Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)_30      10.958075   16.214950    0.6758   0.499350
## log(Density)_30      -0.218312    0.094057   -2.3210   0.020519 *
## Transit_30           0.757977    0.286789    2.6430   0.008369 **
## log(Humidity_lag11)_30  0.454933    0.220223    2.0658   0.039150 *
## log(Mean_Temp_lag11)_30 -1.514856    0.128118  -11.8239 < 2.2e-16 ***
## rho_30               0.263450    0.061766    4.2653  2.22e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5065
##
## Variance-Covariance Matrix of inter-equation residuals:
##  1.1475027 0.9459712 0.8243680 0.6948210 0.6728978 0.6400175 0.5759468
##  0.9459712 0.8860899 0.7360241 0.6265219 0.5936623 0.5827500 0.5384173
##  0.8243680 0.7360241 0.7006135 0.5872736 0.5742111 0.5589726 0.5072724
##  0.6948210 0.6265219 0.5872736 0.5530088 0.5417624 0.5291263 0.4827084
##  0.6728978 0.5936623 0.5742111 0.5417624 0.5540291 0.5430458 0.4959700
##  0.6400175 0.5827500 0.5589726 0.5291263 0.5430458 0.5684697 0.5220800
##  0.5759468 0.5384173 0.5072724 0.4827084 0.4959700 0.5220800 0.4927868
##  0.5128247 0.4813818 0.4618477 0.4371444 0.4498740 0.4690896 0.4462030
##  0.5108911 0.4840856 0.4587561 0.4372861 0.4503483 0.4679342 0.4465727
##  0.4892742 0.4628458 0.4360678 0.4192760 0.4309626 0.4451870 0.4258752
##  0.4068385 0.3792696 0.3639900 0.3384858 0.3537734 0.3742436 0.3607091
##  0.3820028 0.3467427 0.3371239 0.3270007 0.3440396 0.3551543 0.3429197
##  0.3610552 0.3243389 0.3178255 0.3111558 0.3279178 0.3322594 0.3211072
##  0.3104420 0.2760005 0.2774586 0.2691149 0.2841795 0.2843551 0.2783177
##  0.2958734 0.2536809 0.2619170 0.2477010 0.2611792 0.2591141 0.2533047
##  0.2730140 0.2392187 0.2518871 0.2368611 0.2451342 0.2447980 0.2387910
##  0.2619395 0.2322888 0.2489106 0.2321524 0.2386337 0.2411153 0.2341037
##  0.2406643 0.2245810 0.2392124 0.2230869 0.2258198 0.2305345 0.2238939
##  0.2369700 0.2197099 0.2363675 0.2222735 0.2263488 0.2294163 0.2235737
##  0.2335770 0.2183249 0.2331378 0.2257410 0.2310651 0.2346070 0.2294921
##  0.2484429 0.2300240 0.2358040 0.2297301 0.2366515 0.2426036 0.2384358
##  0.2448976 0.2280734 0.2367420 0.2298930 0.2387514 0.2442734 0.2407845
##  0.2493662 0.2343319 0.2440871 0.2379978 0.2463663 0.2525203 0.2481086
##  0.2516294 0.2402526 0.2493924 0.2432851 0.2515291 0.2601659 0.2546535
##  0.2498250 0.2407759 0.2507416 0.2463869 0.2553367 0.2643221 0.2583252
##  0.2584591 0.2477427 0.2575171 0.2517860 0.2599017 0.2677151 0.2615859
##  0.2721754 0.2586502 0.2667379 0.2572619 0.2661811 0.2735846 0.2683381
##  0.2803200 0.2675011 0.2756217 0.2646072 0.2741860 0.2815285 0.2763416

```

```

## 0.2875195 0.2730222 0.2818457 0.2663922 0.2771042 0.2857223 0.2805806
## 0.2913124 0.2774117 0.2853335 0.2672276 0.2779975 0.2869075 0.2814104
##
## 0.5128247 0.5108911 0.4892742 0.4068385 0.3820028 0.3610552 0.3104420
## 0.4813818 0.4840856 0.4628458 0.3792696 0.3467427 0.3243389 0.2760005
## 0.4618477 0.4587561 0.4360678 0.3639900 0.3371239 0.3178255 0.2774586
## 0.4371444 0.4372861 0.4192760 0.3384858 0.3270007 0.3111558 0.2691149
## 0.4498740 0.4503483 0.4309626 0.3537734 0.3440396 0.3279178 0.2841795
## 0.4690896 0.4679342 0.4451870 0.3742436 0.3551543 0.3322594 0.2843551
## 0.4462030 0.4465727 0.4258752 0.3607091 0.3429197 0.3211072 0.2783177
## 0.4182448 0.4196378 0.4001358 0.3425189 0.3263609 0.3048556 0.2678666
## 0.4196378 0.4342935 0.4193143 0.3556265 0.3419202 0.3193643 0.2831647
## 0.4001358 0.4193143 0.4187837 0.3528690 0.3433008 0.3235122 0.2921174
## 0.3425189 0.3556265 0.3528690 0.3183843 0.3041288 0.2846643 0.2592516
## 0.3263609 0.3419202 0.3433008 0.3041288 0.3034095 0.2898443 0.2688822
## 0.3048556 0.3193643 0.3235122 0.2846643 0.2898443 0.2854931 0.2690942
## 0.2678666 0.2831647 0.2921174 0.2592516 0.2688822 0.2690942 0.2691632
## 0.2446956 0.2624041 0.2751465 0.2465272 0.2565476 0.2590334 0.2650294
## 0.2330293 0.2493540 0.2601606 0.2320603 0.2406949 0.2429427 0.2509523
## 0.2297425 0.2459110 0.2534737 0.2257712 0.2321726 0.2316526 0.2381654
## 0.2184833 0.2336505 0.2430515 0.2141635 0.2196505 0.2201652 0.2253949
## 0.2176910 0.2321592 0.2414723 0.2138265 0.2195286 0.2206283 0.2242573
## 0.2224978 0.2364287 0.2447759 0.2161557 0.2219129 0.2227341 0.2214339
## 0.2319958 0.2449481 0.2499614 0.2230349 0.2264610 0.2243139 0.2191466
## 0.2356864 0.2482304 0.2515800 0.2244662 0.2266311 0.2234789 0.2155269
## 0.2431835 0.2548093 0.2576311 0.2281045 0.2295075 0.2250930 0.2146972
## 0.2488495 0.2597065 0.2615561 0.2318144 0.2317359 0.2260882 0.2135880
## 0.2526218 0.2635656 0.2645384 0.2340595 0.2335153 0.2273472 0.2136795
## 0.2566180 0.2677904 0.2687130 0.2373949 0.2370689 0.2311064 0.2177959
## 0.2625434 0.2742090 0.2741232 0.2436770 0.2423278 0.2357414 0.2216917
## 0.2706230 0.2822640 0.2808846 0.2500857 0.2476493 0.2401628 0.2250635
## 0.2745297 0.2868504 0.2848970 0.2555623 0.2513907 0.2430641 0.2282895
## 0.2749170 0.2872001 0.2864592 0.2560468 0.2515311 0.2449467 0.2317085
##
## 0.2958734 0.2730140 0.2619395 0.2406643 0.2369700 0.2335770 0.2484429
## 0.2536809 0.2392187 0.2322888 0.2245810 0.2197099 0.2183249 0.2300240
## 0.2619170 0.2518871 0.2489106 0.2392124 0.2363675 0.2331378 0.2358040
## 0.2477010 0.2368611 0.2321524 0.2230869 0.2222735 0.2257410 0.2297301
## 0.2611792 0.2451342 0.2386337 0.2258198 0.2263488 0.2310651 0.2366515
## 0.2591141 0.2447980 0.2411153 0.2305345 0.2294163 0.2346070 0.2426036
## 0.2533047 0.2387910 0.2341037 0.2238939 0.2235737 0.2294921 0.2384358
## 0.2446956 0.2330293 0.2297425 0.2184833 0.2176910 0.2224978 0.2319958
## 0.2624041 0.2493540 0.2459110 0.2336505 0.2321592 0.2364287 0.2449481
## 0.2751465 0.2601606 0.2534737 0.2430515 0.2414723 0.2447759 0.2499614
## 0.2465272 0.2320603 0.2257712 0.2141635 0.2138265 0.2161557 0.2230349
## 0.2565476 0.2406949 0.2321726 0.2196505 0.2195286 0.2219129 0.2264610
## 0.2590334 0.2429427 0.2316526 0.2201652 0.2206283 0.2227341 0.2243139
## 0.2650294 0.2509523 0.2381654 0.2253949 0.2242573 0.2214339 0.2191466
## 0.2710479 0.2598500 0.2456399 0.2341927 0.2323771 0.2265610 0.2209247
## 0.2598500 0.2606895 0.2492836 0.2390028 0.2358391 0.2281910 0.2211776
## 0.2456399 0.2492836 0.2440073 0.2337979 0.2303254 0.2224138 0.2157905
## 0.2341927 0.2390028 0.2337979 0.2304804 0.2279573 0.2203221 0.2114859
## 0.2323771 0.2358391 0.2303254 0.2279573 0.2280863 0.2224502 0.2140226
## 0.2265610 0.2281910 0.2224138 0.2203221 0.2224502 0.2222377 0.2161171

```

```

## 0.2209247 0.2211776 0.2157905 0.2114859 0.2140226 0.2161171 0.2148697
## 0.2148773 0.2150988 0.2102286 0.2056243 0.2086567 0.2120742 0.2121143
## 0.2129880 0.2145732 0.2097517 0.2061550 0.2093440 0.2128476 0.2132971
## 0.2104343 0.2120625 0.2075443 0.2052320 0.2090461 0.2133279 0.2139479
## 0.2094623 0.2113090 0.2070865 0.2055051 0.2099095 0.2143108 0.2150719
## 0.2132965 0.2149719 0.2103216 0.2082996 0.2126210 0.2165347 0.2171167
## 0.2167503 0.2165919 0.2117837 0.2088306 0.2135222 0.2173711 0.2183475
## 0.2191634 0.2186296 0.2145043 0.2111816 0.2155300 0.2184963 0.2196417
## 0.2232819 0.2222517 0.2178078 0.2134851 0.2171252 0.2190789 0.2204945
## 0.2281807 0.2272163 0.2210291 0.2170160 0.2201267 0.2214398 0.2219839
##
## 0.2448976 0.2493662 0.2516294 0.2498250 0.2584591 0.2721754 0.2803200
## 0.2280734 0.2343319 0.2402526 0.2407759 0.2477427 0.2586502 0.2675011
## 0.2367420 0.2440871 0.2493924 0.2507416 0.2575171 0.2667379 0.2756217
## 0.2298930 0.2379978 0.2432851 0.2463869 0.2517860 0.2572619 0.2646072
## 0.2387514 0.2463663 0.2515291 0.2553367 0.2599017 0.2661811 0.2741860
## 0.2442734 0.2525203 0.2601659 0.2643221 0.2677151 0.2735846 0.2815285
## 0.2407845 0.2481086 0.2546535 0.2583252 0.2615859 0.2683381 0.2763416
## 0.2356864 0.2431835 0.2488495 0.2526218 0.2566180 0.2625434 0.2706230
## 0.2482304 0.2548093 0.2597065 0.2635656 0.2677904 0.2742090 0.2822640
## 0.2515800 0.2576311 0.2615561 0.2645384 0.2687130 0.2741232 0.2808846
## 0.2244662 0.2281045 0.2318144 0.2340595 0.2373949 0.2436770 0.2500857
## 0.2266311 0.2295075 0.2317359 0.2335153 0.2370689 0.2423278 0.2476493
## 0.2234789 0.2250930 0.2260882 0.2273472 0.2311064 0.2357414 0.2401628
## 0.2155269 0.2146972 0.2135880 0.2136795 0.2177959 0.2216917 0.2250635
## 0.2148773 0.2129880 0.2104343 0.2094623 0.2132965 0.2167503 0.2191634
## 0.2150988 0.2145732 0.2120625 0.2113090 0.2149719 0.2165919 0.2186296
## 0.2102286 0.2097517 0.2075443 0.2070865 0.2103216 0.2117837 0.2145043
## 0.2056243 0.2061550 0.2052320 0.2055051 0.2082996 0.2088306 0.2111816
## 0.2086567 0.2093440 0.2090461 0.2099095 0.2126210 0.2135222 0.2155300
## 0.2120742 0.2128476 0.2133279 0.2143108 0.2165347 0.2173711 0.2184963
## 0.2121143 0.2132971 0.2139479 0.2150719 0.2171167 0.2183475 0.2196417
## 0.2119384 0.2141041 0.2154239 0.2172554 0.2194934 0.2213949 0.2235749
## 0.2141041 0.2184210 0.2204346 0.2229741 0.2254068 0.2267991 0.2297029
## 0.2154239 0.2204346 0.2247718 0.2275977 0.2299114 0.2309842 0.2341061
## 0.2172554 0.2229741 0.2275977 0.2317723 0.2346932 0.2360949 0.2399164
## 0.2194934 0.2254068 0.2299114 0.2346932 0.2389015 0.2411029 0.2454165
## 0.2213949 0.2267991 0.2309842 0.2360949 0.2411029 0.2456608 0.2508164
## 0.2235749 0.2297029 0.2341061 0.2399164 0.2454165 0.2508164 0.2581789
## 0.2246203 0.2306970 0.2348802 0.2406313 0.2466415 0.2528513 0.2611061
## 0.2258415 0.2316181 0.2349563 0.2408898 0.2477457 0.2544744 0.2624436
##
## 0.2875195 0.2913124
## 0.2730222 0.2774117
## 0.2818457 0.2853335
## 0.2663922 0.2672276
## 0.2771042 0.2779975
## 0.2857223 0.2869075
## 0.2805806 0.2814104
## 0.2745297 0.2749170
## 0.2868504 0.2872001
## 0.2848970 0.2864592
## 0.2555623 0.2560468
## 0.2513907 0.2515311

```

```

## 0.2430641 0.2449467
## 0.2282895 0.2317085
## 0.2232819 0.2281807
## 0.2222517 0.2272163
## 0.2178078 0.2210291
## 0.2134851 0.2170160
## 0.2171252 0.2201267
## 0.2190789 0.2214398
## 0.2204945 0.2219839
## 0.2246203 0.2258415
## 0.2306970 0.2316181
## 0.2348802 0.2349563
## 0.2406313 0.2408898
## 0.2466415 0.2477457
## 0.2528513 0.2544744
## 0.2611061 0.2624436
## 0.2662557 0.2686619
## 0.2686619 0.2742734
## Correlation Matrix of inter-equation residuals:
## 1.0000000 0.9403010 0.9300692 0.8994038 0.8809872 0.8333785 0.8145938
## 0.9403010 1.0000000 0.9451230 0.9147053 0.8763196 0.8445479 0.8459102
## 0.9300692 0.9451230 1.0000000 0.9596311 0.9456877 0.9074748 0.8945869
## 0.8994038 0.9147053 0.9596311 1.0000000 0.9821768 0.9417065 0.9308477
## 0.8809872 0.8763196 0.9456877 0.9821768 1.0000000 0.9661035 0.9542280
## 0.8333785 0.8445479 0.9074748 0.9417065 0.9661035 1.0000000 0.9864272
## 0.8145938 0.8459102 0.8945869 0.9308477 0.9542280 0.9864272 1.0000000
## 0.7934302 0.8248667 0.8845278 0.9179161 0.9410246 0.9645645 0.9848652
## 0.7784676 0.8199063 0.8676255 0.9018742 0.9259476 0.9482240 0.9714893
## 0.7768570 0.8171291 0.8561703 0.8888107 0.9119296 0.9321095 0.9571347
## 0.7442848 0.7804647 0.8254550 0.8366467 0.8684592 0.9071430 0.9395139
## 0.7486120 0.7636887 0.8148951 0.8461793 0.8817138 0.9086258 0.9380386
## 0.7382592 0.7494037 0.8080259 0.8437762 0.8803482 0.8948261 0.9252693
## 0.6913470 0.6990705 0.7685144 0.7892678 0.8259644 0.8324980 0.8702481
## 0.6783171 0.6683127 0.7456640 0.7543868 0.7919356 0.7953947 0.8312949
## 0.6508286 0.6521413 0.7327843 0.7388498 0.7675616 0.7709440 0.8067292
## 0.6472435 0.6506657 0.7368371 0.7379762 0.7659256 0.7752359 0.8097351
## 0.6231599 0.6472691 0.7278812 0.7290237 0.7501687 0.7636441 0.8000013
## 0.6152894 0.6369406 0.7211861 0.7275795 0.7509058 0.7607418 0.8000051
## 0.5964357 0.6183150 0.7040750 0.7276278 0.7531975 0.7634093 0.8057884
## 0.6144370 0.6327279 0.7071019 0.7344624 0.7615646 0.7756209 0.8203135
## 0.6033917 0.6267515 0.7046451 0.7334138 0.7635871 0.7758999 0.8230020
## 0.6008857 0.6288704 0.7069977 0.7373985 0.7655680 0.7796859 0.8256890
## 0.5954301 0.6290401 0.7062838 0.7382661 0.7656977 0.7844582 0.8284094
## 0.5874905 0.6252978 0.7013041 0.7354738 0.7628092 0.7830552 0.8269958
## 0.5907469 0.6279703 0.7044789 0.7376866 0.7631169 0.7817386 0.8261677
## 0.6005468 0.6360412 0.7114096 0.7406446 0.7673918 0.7862403 0.8327796
## 0.5994880 0.6381143 0.7117454 0.7381428 0.7643387 0.7836068 0.8313935
## 0.6019600 0.6374596 0.7126425 0.7334271 0.7609772 0.7814173 0.8292102
## 0.6043601 0.6399938 0.7159946 0.7327023 0.7603369 0.7802919 0.8270075
##
## 0.7934302 0.7784676 0.7768570 0.7442848 0.7486120 0.7382592 0.6913470
## 0.8248667 0.8199063 0.8171291 0.7804647 0.7636887 0.7494037 0.6990705
## 0.8845278 0.8676255 0.8561703 0.8254550 0.8148951 0.8080259 0.7685144
## 0.9179161 0.9018742 0.8888107 0.8366467 0.8461793 0.8437762 0.7892678

```

```

## 0.9410246 0.9259476 0.9119296 0.8684592 0.8817138 0.8803482 0.8259644
## 0.9645645 0.9482240 0.9321095 0.9071430 0.9086258 0.8948261 0.8324980
## 0.9848652 0.9714893 0.9571347 0.9395139 0.9380386 0.9252693 0.8702481
## 1.0000000 0.9872524 0.9698269 0.9586370 0.9585732 0.9445491 0.8980001
## 0.9872524 1.0000000 0.9886963 0.9692134 0.9704066 0.9554069 0.9118761
## 0.9698269 0.9886963 1.0000000 0.9728683 0.9774846 0.9654889 0.9292461
## 0.9586370 0.9692134 0.9728683 1.0000000 0.9849998 0.9662449 0.9346489
## 0.9585732 0.9704066 0.9774846 0.9849998 1.0000000 0.9905761 0.9647086
## 0.9445491 0.9554069 0.9654889 0.9662449 0.9905761 1.0000000 0.9815494
## 0.8980001 0.9118761 0.9292461 0.9346489 0.9647086 0.9815494 1.0000000
## 0.8573815 0.8765953 0.8991661 0.9077675 0.9377387 0.9590072 0.9870291
## 0.8388685 0.8592064 0.8785570 0.8853611 0.9113854 0.9320214 0.9628294
## 0.8454775 0.8659450 0.8779090 0.8868969 0.9109953 0.9284724 0.9566630
## 0.8336359 0.8531912 0.8696614 0.8750224 0.8963188 0.9164392 0.9421908
## 0.8318174 0.8491759 0.8651720 0.8726399 0.8948032 0.9175166 0.9397118
## 0.8353232 0.8512616 0.8657979 0.8720359 0.8960068 0.9217442 0.9344497
## 0.8535422 0.8678062 0.8772469 0.8910691 0.9122731 0.9320508 0.9385535
## 0.8598676 0.8741539 0.8810623 0.8951990 0.9139824 0.9324138 0.9337565
## 0.8646987 0.8772721 0.8845425 0.8953844 0.9136215 0.9287571 0.9254115
## 0.8664632 0.8772281 0.8839242 0.8962547 0.9124277 0.9255454 0.9187940
## 0.8660732 0.8767575 0.8814021 0.8930071 0.9086975 0.9203510 0.9117737
## 0.8674406 0.8780567 0.8823780 0.8919222 0.9085133 0.9195739 0.9117338
## 0.8729647 0.8830841 0.8851710 0.8969786 0.9116972 0.9209636 0.9114479
## 0.8730731 0.8826834 0.8829803 0.8961935 0.9091018 0.9168390 0.9068177
## 0.8711062 0.8813340 0.8810701 0.8992524 0.9093640 0.9150989 0.9064993
## 0.8696960 0.8792078 0.8804990 0.8953200 0.9051776 0.9124054 0.9071579
##
## 0.6783171 0.6508286 0.6472435 0.6231599 0.6152894 0.5964357 0.6144370
## 0.6683127 0.6521413 0.6506657 0.6472691 0.6369406 0.6183150 0.6327279
## 0.7456640 0.7327843 0.7368371 0.7278812 0.7211861 0.7040750 0.7071019
## 0.7543868 0.7388498 0.7379762 0.7290237 0.7275795 0.7276278 0.7344624
## 0.7919356 0.7675616 0.7659256 0.7501687 0.7509058 0.7531975 0.7615646
## 0.7953947 0.7709440 0.7752359 0.7636441 0.7607418 0.7634093 0.7756209
## 0.8312949 0.8067292 0.8097351 0.8000013 0.8000051 0.8057884 0.8203135
## 0.8573815 0.8388685 0.8454775 0.8336359 0.8318174 0.8353232 0.8535422
## 0.8765953 0.8592064 0.8659450 0.8531912 0.8491759 0.8512616 0.8678062
## 0.8991661 0.8785570 0.8779090 0.8696614 0.8651720 0.8657979 0.8772469
## 0.9077675 0.8853611 0.8868969 0.8750224 0.8726399 0.8720359 0.8910691
## 0.9377387 0.9113854 0.9109953 0.8963188 0.8948032 0.8960068 0.9122731
## 0.9590072 0.9320214 0.9284724 0.9164392 0.9175166 0.9217442 0.9320508
## 0.9870291 0.9628294 0.9566630 0.9421908 0.9397118 0.9344497 0.9385535
## 1.0000000 0.9831822 0.9730299 0.9647761 0.9624896 0.9535798 0.9520438
## 0.9831822 1.0000000 0.9945324 0.9887488 0.9823899 0.9693117 0.9654675
## 0.9730299 0.9945324 1.0000000 0.9910801 0.9839744 0.9706058 0.9686729
## 0.9647761 0.9887488 0.9910801 1.0000000 0.9962581 0.9844877 0.9774150
## 0.9624896 0.9823899 0.9839744 0.9962581 1.0000000 0.9933010 0.9863315
## 0.9535798 0.9693117 0.9706058 0.9844877 0.9933010 1.0000000 0.9949392
## 0.9520438 0.9654675 0.9686729 0.9774150 0.9863315 0.9949392 1.0000000
## 0.9422873 0.9561528 0.9600389 0.9687203 0.9791169 0.9904169 0.9970436
## 0.9311285 0.9465699 0.9500653 0.9615714 0.9729957 0.9837985 0.9914724
## 0.9205113 0.9342096 0.9367633 0.9511323 0.9642509 0.9764346 0.9842044
## 0.9109656 0.9250422 0.9284473 0.9437987 0.9580890 0.9698316 0.9782565
## 0.9097753 0.9239400 0.9277684 0.9417168 0.9556816 0.9660950 0.9742616
## 0.9084550 0.9204068 0.9251137 0.9370175 0.9514985 0.9613106 0.9701545

```

```

## 0.9018086 0.9138225 0.9190250 0.9299441 0.9435707 0.9510063 0.9604634
## 0.9030676 0.9142500 0.9196211 0.9283673 0.9409258 0.9461307 0.9564910
## 0.9051302 0.9168510 0.9211610 0.9300013 0.9413200 0.9446817 0.9536752
##
## 0.6033917 0.6008857 0.5954301 0.5874905 0.5907469 0.6005468 0.5994880
## 0.6267515 0.6288704 0.6290401 0.6252978 0.6279703 0.6360412 0.6381143
## 0.7046451 0.7069977 0.7062838 0.7013041 0.7044789 0.7114096 0.7117454
## 0.7334138 0.7373985 0.7382661 0.7354738 0.7376866 0.7406446 0.7381428
## 0.7635871 0.7655680 0.7656977 0.7628092 0.7631169 0.7673918 0.7643387
## 0.7758999 0.7796859 0.7844582 0.7830552 0.7817386 0.7862403 0.7836068
## 0.8230020 0.8256890 0.8284094 0.8269958 0.8261677 0.8327796 0.8313935
## 0.8598676 0.8646987 0.8664632 0.8660732 0.8674406 0.8729647 0.8730731
## 0.8741539 0.8772721 0.8772281 0.8767575 0.8780567 0.8830841 0.8826834
## 0.8810623 0.8845425 0.8839242 0.8814021 0.8823780 0.8851710 0.8829803
## 0.8951990 0.8953844 0.8962547 0.8930071 0.8919222 0.8969786 0.8961935
## 0.9139824 0.9136215 0.9124277 0.9086975 0.9085133 0.9116972 0.9091018
## 0.9324138 0.9287571 0.9255454 0.9203510 0.9195739 0.9209636 0.9168390
## 0.9337565 0.9254115 0.9187940 0.9117737 0.9117338 0.9114479 0.9068177
## 0.9422873 0.9311285 0.9205113 0.9109656 0.9097753 0.9084550 0.9018086
## 0.9561528 0.9465699 0.9342096 0.9250422 0.9239400 0.9204068 0.9138225
## 0.9600389 0.9500653 0.9367633 0.9284473 0.9277684 0.9251137 0.9190250
## 0.9687203 0.9615714 0.9511323 0.9437987 0.9417168 0.9370175 0.9299441
## 0.9791169 0.9729957 0.9642509 0.9580890 0.9556816 0.9514985 0.9435707
## 0.9904169 0.9837985 0.9764346 0.9698316 0.9660950 0.9613106 0.9510063
## 0.9970436 0.9914724 0.9842044 0.9782565 0.9742616 0.9701545 0.9604634
## 1.0000000 0.9971966 0.9919266 0.9878367 0.9844833 0.9816080 0.9737340
## 0.9971966 1.0000000 0.9966828 0.9946901 0.9921365 0.9887548 0.9825852
## 0.9919266 0.9966828 1.0000000 0.9983613 0.9957869 0.9917328 0.9858061
## 0.9878367 0.9946901 0.9983613 1.0000000 0.9987823 0.9956763 0.9912650
## 0.9844833 0.9921365 0.9957869 0.9987823 1.0000000 0.9982000 0.9952003
## 0.9816080 0.9887548 0.9917328 0.9956763 0.9982000 1.0000000 0.9984662
## 0.9737340 0.9825852 0.9858061 0.9912650 0.9952003 0.9984662 1.0000000
## 0.9697746 0.9783780 0.9810291 0.9862877 0.9910472 0.9955369 0.9984607
## 0.9664299 0.9747081 0.9759380 0.9816672 0.9876462 0.9927364 0.9957063
##
## 0.6019600 0.6043601
## 0.6374596 0.6399938
## 0.7126425 0.7159946
## 0.7334271 0.7327023
## 0.7609772 0.7603369
## 0.7814173 0.7802919
## 0.8292102 0.8270075
## 0.8711062 0.8696960
## 0.8813340 0.8792078
## 0.8810701 0.8804990
## 0.8992524 0.8953200
## 0.9093640 0.9051776
## 0.9150989 0.9124054
## 0.9064993 0.9071579
## 0.9030676 0.9051302
## 0.9142500 0.9168510
## 0.9196211 0.9211610
## 0.9283673 0.9300013
## 0.9409258 0.9413200

```

```
## 0.9461307 0.9446817
## 0.9564910 0.9536752
## 0.9697746 0.9664299
## 0.9783780 0.9747081
## 0.9810291 0.9759380
## 0.9862877 0.9816672
## 0.9910472 0.9876462
## 0.9955369 0.9927364
## 0.9984607 0.9957063
## 1.0000000 0.9977870
## 0.9977870 1.0000000
##
```

```
## R-sq. pooled: 0.8143
## Breusch-Pagan: 1.485e+04 p-value: ( 0)
```

Model with 11-day weighted moving average of climatic variables:

```
sur.slm_lag11w <- spsur::spsurtime(formula = formula_lag11w,
                                   data=GPanel,
                                   time = GPanel$Date,
                                   type = "slm",
                                   fit_method = "3sls",
                                   listw= listw,
                                   R = R2,
                                   b = b2)
```

```
## Time to fit the model: 1.64 seconds
```

```
summary(sur.slm_lag11w)
```

```
## Call:
## spsur::spsurtime(formula = formula_lag11w, data = GPanel, time = GPanel$Date,
##   listw = listw, type = "slm", fit_method = "3sls", R = R2,
##   b = b2)
##
##
## Spatial SUR model type: slm
##
## Equation 1
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_1      14.554168   16.324921  0.8915 0.3728960
## log(Male2Female)_1  -2.638713    2.587019 -1.0200 0.3080262
## log(Median_Age)_1    0.660383    1.387171  0.4761 0.6341505
## log(Density)_1       0.140058    0.165892  0.8443 0.3987521
## Transit_1           0.415219    0.587334  0.7070 0.4797876
## log(Humidity_lag11w)_1 -0.325417    0.350619 -0.9281 0.3536073
## log(Mean_Temp_lag11w)_1 -1.261928    0.374942 -3.3657 0.0007977 ***
## rho_1                0.082886    0.094143  0.8804 0.3788775
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1175
## Equation 2
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_2      15.838472   16.327362  0.9701 0.3322930
## log(Density)_2       0.043362    0.147671  0.2936 0.7691050
## Transit_2           0.520514    0.521163  0.9988 0.3181970
```

```

## log(Humidity_lag11w)_2 -0.453234 0.312544 -1.4501 0.1473867
## log(Mean_Temp_lag11w)_2 -1.143469 0.344582 -3.3184 0.0009436 ***
## rho_2 0.012987 0.112679 0.1153 0.9082689
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1156
## Equation 3
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_3 17.6407798 16.3059558 1.0819 0.279620
## log(Density)_3 -0.0066955 0.1340647 -0.0499 0.960180
## Transit_3 0.5294317 0.4671280 1.1334 0.257375
## log(Humidity_lag11w)_3 -0.6901422 0.3096880 -2.2285 0.026107 *
## log(Mean_Temp_lag11w)_3 -1.3894258 0.3142432 -4.4215 1.107e-05 ***
## rho_3 0.2486656 0.0957495 2.5970 0.009565 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1141
## Equation 4
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_4 18.339056 16.274836 1.1268 0.260129
## log(Density)_4 -0.064726 0.122408 -0.5288 0.597100
## Transit_4 0.617087 0.418361 1.4750 0.140578
## log(Humidity_lag11w)_4 -0.814269 0.289950 -2.8083 0.005094 **
## log(Mean_Temp_lag11w)_4 -1.115189 0.263133 -4.2381 2.5e-05 ***
## rho_4 0.099650 0.114594 0.8696 0.384767
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.119
## Equation 5
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_5 21.09681 16.25543 1.2978 0.1946960
## log(Density)_5 -0.09712 0.12218 -0.7949 0.4269077
## Transit_5 0.66260 0.41738 1.5875 0.1127654
## log(Humidity_lag11w)_5 -1.43811 0.31764 -4.5275 6.817e-06 ***
## log(Mean_Temp_lag11w)_5 -1.28435 0.24312 -5.2828 1.616e-07 ***
## rho_5 0.34809 0.10404 3.3456 0.0008571 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.1057
## Equation 6
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_6 20.437214 16.274612 1.2558 0.20954
## log(Density)_6 -0.147072 0.124447 -1.1818 0.23761
## Transit_6 0.706096 0.427619 1.6512 0.09906 .
## log(Humidity_lag11w)_6 -1.453751 0.317217 -4.5828 5.272e-06 ***
## log(Mean_Temp_lag11w)_6 -1.087508 0.225546 -4.8217 1.685e-06 ***
## rho_6 0.559112 0.093426 5.9845 3.193e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.06339
## Equation 7
## Estimate Std. Error t value Pr(>|t|)
## (Intercept)_7 17.699173 16.258438 1.0886 0.27663
## log(Density)_7 -0.145179 0.118039 -1.2299 0.21907

```



```

## Transit_7          0.701220    0.398153  1.7612    0.07857 .
## log(Humidity_lag11w)_7 -0.669352    0.281104 -2.3812    0.01748 *
## log(Mean_Temp_lag11w)_7 -1.079390    0.191500 -5.6365  2.358e-08 ***
## rho_7              0.369272    0.088447  4.1751  3.285e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.1353
## Equation 8
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_8      14.852652   16.267021  0.9131  0.361473
## log(Density)_8      -0.131410    0.108462 -1.2116  0.226009
## Transit_8           0.620235    0.353692  1.7536  0.079858 .
## log(Humidity_lag11w)_8 0.070772    0.230742  0.3067  0.759136
## log(Mean_Temp_lag11w)_8 -1.083051    0.157674 -6.8689  1.247e-11 ***
## rho_8               0.291451    0.080148  3.6364  0.000293 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.2265
## Equation 9
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_9      17.007533   16.266369  1.0456  0.29606
## log(Density)_9      -0.118055    0.107395 -1.0993  0.27196
## Transit_9           0.611517    0.346796  1.7633  0.07820 .
## log(Humidity_lag11w)_9 -0.108443    0.212138 -0.5112  0.60935
## log(Mean_Temp_lag11w)_9 -1.395297    0.163975 -8.5092 < 2e-16 ***
## rho_9               0.145260    0.078277  1.8557  0.06384 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.3292
## Equation 10
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_10     17.7939316  16.2921078  1.0922  0.2751
## log(Density)_10     -0.0557625  0.1044033 -0.5341  0.5934
## Transit_10          0.5349894  0.3314853  1.6139  0.1069
## log(Humidity_lag11w)_10 -0.1648338  0.2073770 -0.7949  0.4269
## log(Mean_Temp_lag11w)_10 -1.4467523  0.1828892 -7.9105  7.93e-15 ***
## rho_10              -0.0047427  0.0863958 -0.0549  0.9562
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.369
## Equation 11
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_11     19.413174  16.375649  1.1855  0.23615
## log(Density)_11      0.015690  0.092900  0.1689  0.86593
## Transit_11          0.468960  0.279075  1.6804  0.09324 .
## log(Humidity_lag11w)_11 -0.284816  0.217909 -1.3070  0.19155
## log(Mean_Temp_lag11w)_11 -1.888650  0.183074 -10.3163 < 2e-16 ***
## rho_11              -0.020214  0.075568 -0.2675  0.78916
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5022
## Equation 12
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_12     20.2410843  16.3520827  1.2378  0.21612

```

```

## log(Density)_12      -0.0032294  0.0936825  -0.0345  0.97251
## Transit_12           0.4990389  0.2812001   1.7747  0.07631 .
## log(Humidity_lag11w)_12 -0.4751547  0.2108093  -2.2540  0.02445 *
## log(Mean_Temp_lag11w)_12 -1.8985167  0.1815122 -10.4594 < 2e-16 ***
## rho_12               0.0554432  0.0673400   0.8233  0.41055
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5095
## Equation 13
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_13    20.8592957  16.3667231   1.2745  0.20284
## log(Density)_13    -0.0045116  0.0948780  -0.0476  0.96209
## Transit_13         0.4767877  0.2843001   1.6771  0.09390 .
## log(Humidity_lag11w)_13 -0.5374704  0.2305463  -2.3313  0.01997 *
## log(Mean_Temp_lag11w)_13 -1.9128271  0.1938183  -9.8692 < 2e-16 ***
## rho_13             0.0216867  0.0699628   0.3100  0.75666
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5166
## Equation 14
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_14     21.94198665  16.36701075   1.3406  0.18040
## log(Density)_14     -0.01078203  0.09735226  -0.1108  0.91184
## Transit_14          0.49786043  0.29376193   1.6948  0.09048 .
## log(Humidity_lag11w)_14 -0.71739727  0.25242353  -2.8420  0.00459 **
## log(Mean_Temp_lag11w)_14 -1.91970553  0.21110073  -9.0938 < 2e-16 ***
## rho_14              -0.00045764  0.07823028  -0.0058  0.99533
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.4945
## Equation 15
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_15     23.1089564  16.3481938   1.4135  0.1578595
## log(Density)_15     -0.0383552  0.0983285  -0.3901  0.6965807
## Transit_15          0.5179698  0.2995309   1.7293  0.0841226 .
## log(Humidity_lag11w)_15 -0.9451594  0.2508369  -3.7680  0.0001759 ***
## log(Mean_Temp_lag11w)_15 -1.9026082  0.2111780  -9.0095 < 2.2e-16 ***
## rho_15              0.0099609  0.0823096   0.1210  0.9037061
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.4882
## Equation 16
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_16     23.970667  16.337681   1.4672  0.14269
## log(Density)_16     -0.083044  0.095217  -0.8722  0.38336
## Transit_16          0.559813  0.289309   1.9350  0.05332 .
## log(Humidity_lag11w)_16 -1.103027  0.228374  -4.8299 1.619e-06 ***
## log(Mean_Temp_lag11w)_16 -1.763160  0.175321 -10.0568 < 2.2e-16 ***
## rho_16              -0.040169  0.077602  -0.5176  0.60485
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5099
## Equation 17
##               Estimate Std. Error t value Pr(>|t|)

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## (Intercept)_17      22.6654739 16.3166950  1.3891  0.16517
## log(Density)_17     -0.1156848  0.0928365 -1.2461  0.21307
## Transit_17          0.5628069  0.2805805  2.0059  0.04519 *
## log(Humidity_lag11w)_17 -0.9367978  0.2023967 -4.6285 4.255e-06 ***
## log(Mean_Temp_lag11w)_17 -1.5297431  0.1328611 -11.5139 < 2.2e-16 ***
## rho_17              -0.0048497  0.0727149 -0.0667  0.94684
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5165
## Equation 18
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_18      21.356014  16.314577  1.3090  0.19088
## log(Density)_18     -0.139862  0.090413 -1.5469  0.12225
## Transit_18          0.545033  0.270675  2.0136  0.04436 *
## log(Humidity_lag11w)_18 -0.753449  0.174971 -4.3061 1.854e-05 ***
## log(Mean_Temp_lag11w)_18 -1.196928  0.103749 -11.5368 < 2.2e-16 ***
## rho_18              -0.038613  0.074894 -0.5156  0.60629
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5214
## Equation 19
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_19      20.497837  16.300320  1.2575  0.20891
## log(Density)_19     -0.140014  0.089070 -1.5720  0.11633
## Transit_19          0.547951  0.263743  2.0776  0.03805 *
## log(Humidity_lag11w)_19 -0.618105  0.153665 -4.0224 6.271e-05 ***
## log(Mean_Temp_lag11w)_19 -1.112577  0.091164 -12.2042 < 2.2e-16 ***
## rho_19              -0.017861  0.069100 -0.2585  0.79610
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5337
## Equation 20
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_20      19.5711026 16.3005211  1.2006  0.230223
## log(Density)_20     -0.1519017  0.0878278 -1.7295  0.084074 .
## Transit_20          0.5649567  0.2577719  2.1917  0.028671 *
## log(Humidity_lag11w)_20 -0.4201087  0.1483704 -2.8315  0.004742 **
## log(Mean_Temp_lag11w)_20 -1.0901877  0.0886478 -12.2980 < 2.2e-16 ***
## rho_20              0.0092675  0.0691670  0.1340  0.893444
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5522
## Equation 21
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)_21      18.259536  16.287484  1.1211  0.26257
## log(Density)_21     -0.167682  0.087135 -1.9244  0.05464 .
## Transit_21          0.604456  0.254512  2.3750  0.01777 *
## log(Humidity_lag11w)_21 -0.195621  0.138549 -1.4119  0.15834
## log(Mean_Temp_lag11w)_21 -0.966236  0.076808 -12.5799 < 2e-16 ***
## rho_21              0.039914  0.068171  0.5855  0.55837
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5499
## Equation 22

```

```

##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_22      16.869082   16.266026    1.0371  0.30000
## log(Density)_22     -0.178473    0.088163   -2.0244  0.04324 *
## Transit_22          0.603872    0.259168    2.3300  0.02004 *
## log(Humidity_lag11w)_22  0.072958    0.128259    0.5688  0.56962
## log(Mean_Temp_lag11w)_22 -0.871544    0.065566  -13.2926 < 2e-16 ***
## rho_22              0.057434    0.063560    0.9036  0.36645
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5434
## Equation  23
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_23      16.148130   16.265878    0.9928  0.32111
## log(Density)_23     -0.181474    0.088520   -2.0501  0.04066 *
## Transit_23          0.587911    0.260625    2.2558  0.02434 *
## log(Humidity_lag11w)_23  0.243833    0.129613    1.8812  0.06028 .
## log(Mean_Temp_lag11w)_23 -0.850227    0.063858  -13.3144 < 2e-16 ***
## rho_23              0.056880    0.061156    0.9301  0.35259
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5423
## Equation  24
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_24      16.640007   16.266485    1.0230  0.30662
## log(Density)_24     -0.186740    0.089759   -2.0805  0.03778 *
## Transit_24          0.586159    0.265838    2.2050  0.02772 *
## log(Humidity_lag11w)_24  0.172649    0.149311    1.1563  0.24788
## log(Mean_Temp_lag11w)_24 -0.878014    0.071821  -12.2251 < 2e-16 ***
## rho_24              0.049989    0.064605    0.7738  0.43928
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5368
## Equation  25
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_25      17.084677   16.266180    1.0503  0.29387
## log(Density)_25     -0.197042    0.090330   -2.1814  0.02943 *
## Transit_25          0.593680    0.268399    2.2119  0.02724 *
## log(Humidity_lag11w)_25  0.084888    0.156208    0.5434  0.58698
## log(Mean_Temp_lag11w)_25 -0.907508    0.078228  -11.6008 < 2e-16 ***
## rho_25              0.072096    0.061739    1.1678  0.24323
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.5287
## Equation  26
##               Estimate Std. Error  t value Pr(>|t|)
## (Intercept)_26      16.841472   16.260364    1.0357  0.30062
## log(Density)_26     -0.201571    0.091190   -2.2104  0.02734 *
## Transit_26          0.607563    0.272368    2.2307  0.02596 *
## log(Humidity_lag11w)_26  0.165489    0.161248    1.0263  0.30504
## log(Mean_Temp_lag11w)_26 -0.999674    0.085272  -11.7234 < 2e-16 ***
## rho_26              0.110867    0.052886    2.0963  0.03635 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.525

```

```

## Equation 27
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_27      16.683862  16.260128   1.0261 0.3051543
## log(Density)_27     -0.220943   0.093114  -2.3728 0.0178741 *
## Transit_27          0.643343   0.281246   2.2875 0.0224125 *
## log(Humidity_lag11w)_27 0.231966   0.182662   1.2699 0.2044579
## log(Mean_Temp_lag11w)_27 -1.096832   0.103008 -10.6481 < 2.2e-16 ***
## rho_27              0.164174   0.042986   3.8193 0.0001435 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.4981
## Equation 28
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_28      17.129982  16.283996   1.0520 0.293119
## log(Density)_28     -0.256975   0.094750  -2.7122 0.006819 **
## Transit_28          0.720997   0.289387   2.4915 0.012911 *
## log(Humidity_lag11w)_28 0.139481   0.230881   0.6041 0.545921
## log(Mean_Temp_lag11w)_28 -1.173339   0.134399  -8.7303 < 2.2e-16 ***
## rho_28              0.236713   0.040387   5.8611 6.568e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.4656
## Equation 29
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_29      16.570156  16.288578   1.0173 0.309305
## log(Density)_29     -0.285900   0.097174  -2.9422 0.003348 **
## Transit_29          0.765738   0.301134   2.5428 0.011171 *
## log(Humidity_lag11w)_29 0.337152   0.271545   1.2416 0.214724
## log(Mean_Temp_lag11w)_29 -1.239547   0.163297  -7.5907 8.338e-14 ***
## rho_29              0.252609   0.049652   5.0876 4.462e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.4444
## Equation 30
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)_30      16.347737  16.303933   1.0027 0.3162964
## log(Density)_30     -0.295862   0.099639  -2.9693 0.0030679 **
## Transit_30          0.821104   0.312726   2.6256 0.0088037 **
## log(Humidity_lag11w)_30 0.463575   0.298047   1.5554 0.1202278
## log(Mean_Temp_lag11w)_30 -1.358432   0.196783  -6.9032 9.924e-12 ***
## rho_30              0.270852   0.069505   3.8968 0.0001051 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## R-squared:  0.4332
##
## Variance-Covariance Matrix of inter-equation residuals:
##  1.1658557 0.9650778 0.8476086 0.7105957 0.6695102 0.6365497 0.5898090
##  0.9650778 0.9195150 0.7746701 0.6558030 0.6062035 0.5984088 0.5653791
##  0.8476086 0.7746701 0.7401383 0.6264374 0.6023540 0.5952629 0.5468568
##  0.7105957 0.6558030 0.6264374 0.5932867 0.5780217 0.5752731 0.5253834
##  0.6695102 0.6062035 0.6023540 0.5780217 0.5903899 0.5886485 0.5360149
##  0.6365497 0.5984088 0.5952629 0.5752731 0.5886485 0.6196436 0.5648513
##  0.5898090 0.5653791 0.5468568 0.5253834 0.5360149 0.5648513 0.5354713
##  0.5113602 0.4874862 0.4726316 0.4517030 0.4599658 0.4789616 0.4622666

```

```

## 0.4861883 0.4656264 0.4431063 0.4306049 0.4390358 0.4547091 0.4391971
## 0.4504845 0.4278343 0.4044065 0.3969411 0.4035254 0.4150270 0.3972478
## 0.3464279 0.3204449 0.3131653 0.2951366 0.3035501 0.3178943 0.3021311
## 0.3246477 0.2948814 0.2938953 0.2868812 0.2939871 0.3021368 0.2834305
## 0.2985114 0.2675825 0.2754642 0.2711228 0.2813287 0.2851937 0.2659593
## 0.2623961 0.2346907 0.2567166 0.2503579 0.2653174 0.2663450 0.2505222
## 0.2659796 0.2352305 0.2626596 0.2516844 0.2662170 0.2679567 0.2507507
## 0.2715708 0.2549109 0.2764217 0.2599740 0.2652223 0.2701056 0.2534396
## 0.2866774 0.2773128 0.2933992 0.2751753 0.2766015 0.2860181 0.2696955
## 0.2680827 0.2714947 0.2843566 0.2682339 0.2678642 0.2813169 0.2645360
## 0.2618019 0.2642261 0.2745104 0.2626920 0.2639971 0.2752518 0.2596503
## 0.2389386 0.2398939 0.2515531 0.2482208 0.2535289 0.2646990 0.2514831
## 0.2436624 0.2392489 0.2453671 0.2458074 0.2535655 0.2653890 0.2555230
## 0.2447828 0.2394128 0.2480183 0.2484885 0.2598386 0.2722268 0.2658232
## 0.2447508 0.2369619 0.2493884 0.2486010 0.2606525 0.2729879 0.2675498
## 0.2496046 0.2386465 0.2545838 0.2527569 0.2655260 0.2775720 0.2713503
## 0.2530125 0.2431683 0.2599155 0.2575593 0.2701249 0.2818114 0.2744950
## 0.2621731 0.2541286 0.2712009 0.2652812 0.2756978 0.2879822 0.2785601
## 0.2936206 0.2837030 0.2979327 0.2845108 0.2904209 0.3038353 0.2905776
## 0.3080710 0.2998455 0.3128251 0.2936566 0.2968592 0.3114152 0.2972443
## 0.3026432 0.3051248 0.3198693 0.2982096 0.3025901 0.3184799 0.3048624
## 0.3016147 0.3129377 0.3269219 0.3031143 0.3085978 0.3252758 0.3122194
##
## 0.5113602 0.4861883 0.4504845 0.3464279 0.3246477 0.2985114 0.2623961
## 0.4874862 0.4656264 0.4278343 0.3204449 0.2948814 0.2675825 0.2346907
## 0.4726316 0.4431063 0.4044065 0.3131653 0.2938953 0.2754642 0.2567166
## 0.4517030 0.4306049 0.3969411 0.2951366 0.2868812 0.2711228 0.2503579
## 0.4599658 0.4390358 0.4035254 0.3035501 0.2939871 0.2813287 0.2653174
## 0.4789616 0.4547091 0.4150270 0.3178943 0.3021368 0.2851937 0.2663450
## 0.4622666 0.4391971 0.3972478 0.3021311 0.2834305 0.2659593 0.2505222
## 0.4203179 0.4035254 0.3651773 0.2825622 0.2671460 0.2490486 0.2365419
## 0.4035254 0.4034697 0.3740425 0.2898697 0.2767466 0.2591257 0.2459986
## 0.3651773 0.3740425 0.3684464 0.2923025 0.2861095 0.2723694 0.2600248
## 0.2825622 0.2898697 0.2923025 0.2591913 0.2529576 0.2418311 0.2334924
## 0.2671460 0.2767466 0.2861095 0.2529576 0.2631162 0.2596347 0.2545007
## 0.2490486 0.2591257 0.2723694 0.2418311 0.2596347 0.2682500 0.2696019
## 0.2365419 0.2459986 0.2600248 0.2334924 0.2545007 0.2696019 0.2859864
## 0.2341409 0.2440245 0.2574200 0.2312320 0.2530509 0.2689828 0.2884168
## 0.2377377 0.2470303 0.2539845 0.2231479 0.2421594 0.2524120 0.2682478
## 0.2530095 0.2601167 0.2575175 0.2200611 0.2321246 0.2353678 0.2455090
## 0.2462069 0.2515412 0.2476725 0.2092907 0.2185956 0.2200554 0.2256372
## 0.2410053 0.2465488 0.2433776 0.2051998 0.2128872 0.2146695 0.2180616
## 0.2327012 0.2383116 0.2356232 0.1976463 0.2041417 0.2071394 0.2094708
## 0.2374652 0.2415896 0.2351191 0.1967544 0.1993202 0.1994446 0.1999434
## 0.2485610 0.2508259 0.2406272 0.2014079 0.2003984 0.1981560 0.1970845
## 0.2517688 0.2525988 0.2409951 0.2019093 0.1999776 0.1959599 0.1935959
## 0.2553240 0.2548452 0.2427362 0.2028593 0.2024027 0.1993708 0.1976421
## 0.2574943 0.2565109 0.2438463 0.2024474 0.2031877 0.2012699 0.2008005
## 0.2606688 0.2600698 0.2480938 0.2063207 0.2090848 0.2081057 0.2082774
## 0.2696447 0.2685940 0.2558337 0.2139085 0.2186255 0.2177884 0.2175997
## 0.2735122 0.2705425 0.2551998 0.2138599 0.2192767 0.2189430 0.2199613
## 0.2805271 0.2770759 0.2609663 0.2206316 0.2264762 0.2269573 0.2302204
## 0.2878848 0.2838923 0.2679297 0.2272181 0.2326053 0.2338776 0.2393223
##

```

```

## 0.2659796 0.2715708 0.2866774 0.2680827 0.2618019 0.2389386 0.2436624
## 0.2352305 0.2549109 0.2773128 0.2714947 0.2642261 0.2398939 0.2392489
## 0.2626596 0.2764217 0.2933992 0.2843566 0.2745104 0.2515531 0.2453671
## 0.2516844 0.2599740 0.2751753 0.2682339 0.2626920 0.2482208 0.2458074
## 0.2662170 0.2652223 0.2766015 0.2678642 0.2639971 0.2535289 0.2535655
## 0.2679567 0.2701056 0.2860181 0.2813169 0.2752518 0.2646990 0.2653890
## 0.2507507 0.2534396 0.2696955 0.2645360 0.2596503 0.2514831 0.2555230
## 0.2341409 0.2377377 0.2530095 0.2462069 0.2410053 0.2327012 0.2374652
## 0.2440245 0.2470303 0.2601167 0.2515412 0.2465488 0.2383116 0.2415896
## 0.2574200 0.2539845 0.2575175 0.2476725 0.2433776 0.2356232 0.2351191
## 0.2312320 0.2231479 0.2200611 0.2092907 0.2051998 0.1976463 0.1967544
## 0.2530509 0.2421594 0.2321246 0.2185956 0.2128872 0.2041417 0.1993202
## 0.2689828 0.2524120 0.2353678 0.2200554 0.2146695 0.2071394 0.1994446
## 0.2884168 0.2682478 0.2455090 0.2256372 0.2180616 0.2094708 0.1999434
## 0.2977772 0.2797854 0.2556395 0.2362617 0.2275378 0.2179310 0.2065019
## 0.2797854 0.2780645 0.2633922 0.2461683 0.2340312 0.2199813 0.2074181
## 0.2556395 0.2633922 0.2617928 0.2483829 0.2366350 0.2220048 0.2118224
## 0.2362617 0.2461683 0.2483829 0.2430083 0.2343771 0.2218024 0.2118269
## 0.2275378 0.2340312 0.2366350 0.2343771 0.2305286 0.2218777 0.2136522
## 0.2179310 0.2199813 0.2220048 0.2218024 0.2218777 0.2196698 0.2141287
## 0.2065019 0.2074181 0.2118224 0.2118269 0.2136522 0.2141287 0.2141061
## 0.2018712 0.2028700 0.2088572 0.2089401 0.2112810 0.2124535 0.2157441
## 0.1974713 0.1995112 0.2062763 0.2062580 0.2080573 0.2077590 0.2120776
## 0.2014006 0.2040158 0.2102987 0.2097512 0.2105031 0.2088153 0.2126221
## 0.2058782 0.2091225 0.2143770 0.2137552 0.2141435 0.2116780 0.2141843
## 0.2148118 0.2189323 0.2228655 0.2218568 0.2213271 0.2172878 0.2174116
## 0.2250567 0.2304693 0.2333589 0.2306911 0.2285366 0.2218388 0.2193143
## 0.2281125 0.2344635 0.2367336 0.2321201 0.2278654 0.2191560 0.2152865
## 0.2392193 0.2446287 0.2448791 0.2386176 0.2325000 0.2229218 0.2185365
## 0.2489985 0.2520975 0.2491997 0.2421437 0.2353761 0.2260044 0.2213650
##
## 0.2447828 0.2447508 0.2496046 0.2530125 0.2621731 0.2936206 0.3080710
## 0.2394128 0.2369619 0.2386465 0.2431683 0.2541286 0.2837030 0.2998455
## 0.2480183 0.2493884 0.2545838 0.2599155 0.2712009 0.2979327 0.3128251
## 0.2484885 0.2486010 0.2527569 0.2575593 0.2652812 0.2845108 0.2936566
## 0.2598386 0.2606525 0.2655260 0.2701249 0.2756978 0.2904209 0.2968592
## 0.2722268 0.2729879 0.2775720 0.2818114 0.2879822 0.3038353 0.3114152
## 0.2658232 0.2675498 0.2713503 0.2744950 0.2785601 0.2905776 0.2972443
## 0.2485610 0.2517688 0.2553240 0.2574943 0.2606688 0.2696447 0.2735122
## 0.2508259 0.2525988 0.2548452 0.2565109 0.2600698 0.2685940 0.2705425
## 0.2406272 0.2409951 0.2427362 0.2438463 0.2480938 0.2558337 0.2551998
## 0.2014079 0.2019093 0.2028593 0.2024474 0.2063207 0.2139085 0.2138599
## 0.2003984 0.1999776 0.2024027 0.2031877 0.2090848 0.2186255 0.2192767
## 0.1981560 0.1959599 0.1993708 0.2012699 0.2081057 0.2177884 0.2189430
## 0.1970845 0.1935959 0.1976421 0.2008005 0.2082774 0.2175997 0.2199613
## 0.2018712 0.1974713 0.2014006 0.2058782 0.2148118 0.2250567 0.2281125
## 0.2028700 0.1995112 0.2040158 0.2091225 0.2189323 0.2304693 0.2344635
## 0.2088572 0.2062763 0.2102987 0.2143770 0.2228655 0.2333589 0.2367336
## 0.2089401 0.2062580 0.2097512 0.2137552 0.2218568 0.2306911 0.2321201
## 0.2112810 0.2080573 0.2105031 0.2141435 0.2213271 0.2285366 0.2278654
## 0.2124535 0.2077590 0.2088153 0.2116780 0.2172878 0.2218388 0.2191560
## 0.2157441 0.2120776 0.2126221 0.2141843 0.2174116 0.2193143 0.2152865
## 0.2224840 0.2219367 0.2235657 0.2245256 0.2262038 0.2263714 0.2218214
## 0.2219367 0.2251523 0.2284751 0.2295040 0.2306587 0.2307898 0.2268269

```

```

## 0.2235657 0.2284751 0.2342087 0.2357276 0.2368986 0.2369383 0.2329162
## 0.2245256 0.2295040 0.2357276 0.2389926 0.2414025 0.2425121 0.2390910
## 0.2262038 0.2306587 0.2368986 0.2414025 0.2466567 0.2515006 0.2503314
## 0.2263714 0.2307898 0.2369383 0.2425121 0.2515006 0.2637628 0.2683264
## 0.2218214 0.2268269 0.2329162 0.2390910 0.2503314 0.2683264 0.2798254
## 0.2254596 0.2299048 0.2350577 0.2411252 0.2533819 0.2732671 0.2882404
## 0.2289120 0.2327751 0.2369475 0.2431522 0.2559232 0.2761284 0.2919861
##
## 0.3026432 0.3016147
## 0.3051248 0.3129377
## 0.3198693 0.3269219
## 0.2982096 0.3031143
## 0.3025901 0.3085978
## 0.3184799 0.3252758
## 0.3048624 0.3122194
## 0.2805271 0.2878848
## 0.2770759 0.2838923
## 0.2609663 0.2679297
## 0.2206316 0.2272181
## 0.2264762 0.2326053
## 0.2269573 0.2338776
## 0.2302204 0.2393223
## 0.2392193 0.2489985
## 0.2446287 0.2520975
## 0.2448791 0.2491997
## 0.2386176 0.2421437
## 0.2325000 0.2353761
## 0.2229218 0.2260044
## 0.2185365 0.2213650
## 0.2254596 0.2289120
## 0.2299048 0.2327751
## 0.2350577 0.2369475
## 0.2411252 0.2431522
## 0.2533819 0.2559232
## 0.2732671 0.2761284
## 0.2882404 0.2919861
## 0.3035398 0.3121056
## 0.3121056 0.3275075
## Correlation Matrix of inter-equation residuals:
## 1.0000000 0.9379874 0.9250031 0.8845597 0.8531787 0.7828166 0.7890523
## 0.9379874 1.0000000 0.9432042 0.9069482 0.8536291 0.8000407 0.8258215
## 0.9250031 0.9432042 1.0000000 0.9595607 0.9398395 0.8906193 0.8932614
## 0.8845597 0.9069482 0.9595607 1.0000000 0.9797316 0.9341942 0.9367146
## 0.8531787 0.8536291 0.9398395 0.9797316 1.0000000 0.9687127 0.9623908
## 0.7828166 0.8000407 0.8906193 0.9341942 0.9687127 1.0000000 0.9821123
## 0.7890523 0.8258215 0.8932614 0.9367146 0.9623908 0.9821123 1.0000000
## 0.7801616 0.8139427 0.8847691 0.9268585 0.9480139 0.9522867 0.9824530
## 0.7611642 0.8085095 0.8619259 0.9096055 0.9281004 0.9260288 0.9626918
## 0.7404934 0.7983448 0.8359161 0.8849565 0.8955982 0.8874270 0.9275732
## 0.7031373 0.7529635 0.7949013 0.8210927 0.8374520 0.8453767 0.8891337
## 0.6938157 0.7323244 0.7823044 0.8267551 0.8427253 0.8431846 0.8809173
## 0.6625307 0.6985391 0.7584090 0.8068223 0.8253343 0.8193015 0.8568976
## 0.5865399 0.6227271 0.7051897 0.7459415 0.7739575 0.7644061 0.8048498
## 0.5805870 0.6082337 0.6966195 0.7311009 0.7600425 0.7502895 0.7882571

```



```

## 0.5875258 0.6324910 0.7172719 0.7470171 0.7635902 0.7537609 0.7932150
## 0.6133434 0.6613431 0.7472668 0.7740396 0.7891001 0.7846430 0.8245160
## 0.5891854 0.6589881 0.7354894 0.7655843 0.7735802 0.7745894 0.8167938
## 0.5871566 0.6570713 0.7298858 0.7664888 0.7744293 0.7725763 0.8184034
## 0.5605714 0.6246414 0.6992608 0.7483039 0.7615176 0.7627991 0.8119819
## 0.5738797 0.6273394 0.6951366 0.7475714 0.7639841 0.7679579 0.8205112
## 0.5666514 0.6185191 0.6885862 0.7407522 0.7609516 0.7644650 0.8228217
## 0.5628183 0.6140592 0.6868770 0.7377015 0.7578684 0.7621598 0.8218332
## 0.5621140 0.6119331 0.6886107 0.7392501 0.7599507 0.7649095 0.8218147
## 0.5619814 0.6158631 0.6930263 0.7438556 0.7645887 0.7701256 0.8250625
## 0.5614581 0.6214539 0.6981791 0.7448912 0.7635569 0.7700562 0.8238295
## 0.5770687 0.6403654 0.7146370 0.7558302 0.7717631 0.7807760 0.8309718
## 0.5831369 0.6500055 0.7221133 0.7582360 0.7719404 0.7830351 0.8314287
## 0.5800187 0.6476332 0.7185193 0.7504414 0.7641395 0.7757437 0.8241461
## 0.5731895 0.6432597 0.7142658 0.7429018 0.7580899 0.7695268 0.8182496
##
## 0.7801616 0.7611642 0.7404934 0.7031373 0.6938157 0.6625307 0.5865399
## 0.8139427 0.8085095 0.7983448 0.7529635 0.7323244 0.6985391 0.6227271
## 0.8847691 0.8619259 0.8359161 0.7949013 0.7823044 0.7584090 0.7051897
## 0.9268585 0.9096055 0.8849565 0.8210927 0.8267551 0.8068223 0.7459415
## 0.9480139 0.9281004 0.8955982 0.8374520 0.8427253 0.8253343 0.7739575
## 0.9522867 0.9260288 0.8874270 0.8453767 0.8431846 0.8193015 0.7644061
## 0.9824530 0.9626918 0.9275732 0.8891337 0.8809173 0.8568976 0.8048498
## 1.0000000 0.9854929 0.9508048 0.9204559 0.9144786 0.8881591 0.8416554
## 0.9854929 1.0000000 0.9790213 0.9434053 0.9378949 0.9133932 0.8683500
## 0.9508048 0.9790213 1.0000000 0.9661531 0.9670750 0.9478086 0.9046822
## 0.9204559 0.9434053 0.9661531 1.0000000 0.9826385 0.9593351 0.9254305
## 0.9144786 0.9378949 0.9670750 0.9826385 1.0000000 0.9880088 0.9585543
## 0.8881591 0.9133932 0.9478086 0.9593351 0.9880088 1.0000000 0.9817351
## 0.8416554 0.8683500 0.9046822 0.9254305 0.9585543 0.9817351 1.0000000
## 0.8213784 0.8513494 0.8880035 0.9099142 0.9436383 0.9689044 0.9915641
## 0.8305528 0.8629032 0.8915763 0.9043852 0.9353953 0.9529775 0.9712511
## 0.8646611 0.8929602 0.9020994 0.9084057 0.9329315 0.9417951 0.9514245
## 0.8562576 0.8841837 0.8981809 0.9037051 0.9244955 0.9335816 0.9375704
## 0.8567458 0.8824954 0.8968897 0.9028223 0.9229647 0.9351707 0.9351571
## 0.8487431 0.8719846 0.8851862 0.8895773 0.9117337 0.9294617 0.9283379
## 0.8607702 0.8799882 0.8844409 0.8925681 0.9115081 0.9235105 0.9179163
## 0.8665213 0.8836187 0.8830370 0.8923370 0.9061913 0.9148029 0.9058894
## 0.8686822 0.8837883 0.8823950 0.8910491 0.9032299 0.9072460 0.8946687
## 0.8674286 0.8800650 0.8782158 0.8847957 0.8994738 0.9045402 0.8929698
## 0.8687111 0.8798408 0.8753611 0.8785515 0.8946475 0.9004916 0.8907259
## 0.8671239 0.8791766 0.8767521 0.8788312 0.8968807 0.9029718 0.8945516
## 0.8712386 0.8823818 0.8795107 0.8814900 0.9012569 0.9059876 0.8960791
## 0.8700989 0.8793093 0.8727262 0.8751560 0.8952995 0.8986330 0.8894149
## 0.8622002 0.8714066 0.8652155 0.8741515 0.8934001 0.8963535 0.8885212
## 0.8570106 0.8657030 0.8605474 0.8706360 0.8882279 0.8913699 0.8852955
##
## 0.5805870 0.5875258 0.6133434 0.5891854 0.5871566 0.5605714 0.5738797
## 0.6082337 0.6324910 0.6613431 0.6589881 0.6570713 0.6246414 0.6273394
## 0.6966195 0.7172719 0.7472668 0.7354894 0.7298858 0.6992608 0.6951366
## 0.7311009 0.7470171 0.7740396 0.7655843 0.7664888 0.7483039 0.7475714
## 0.7600425 0.7635902 0.7891001 0.7735802 0.7744293 0.7615176 0.7639841
## 0.7502895 0.7537609 0.7846430 0.7745894 0.7725763 0.7627991 0.7679579
## 0.7882571 0.7932150 0.8245160 0.8167938 0.8184034 0.8119819 0.8205112

```

```

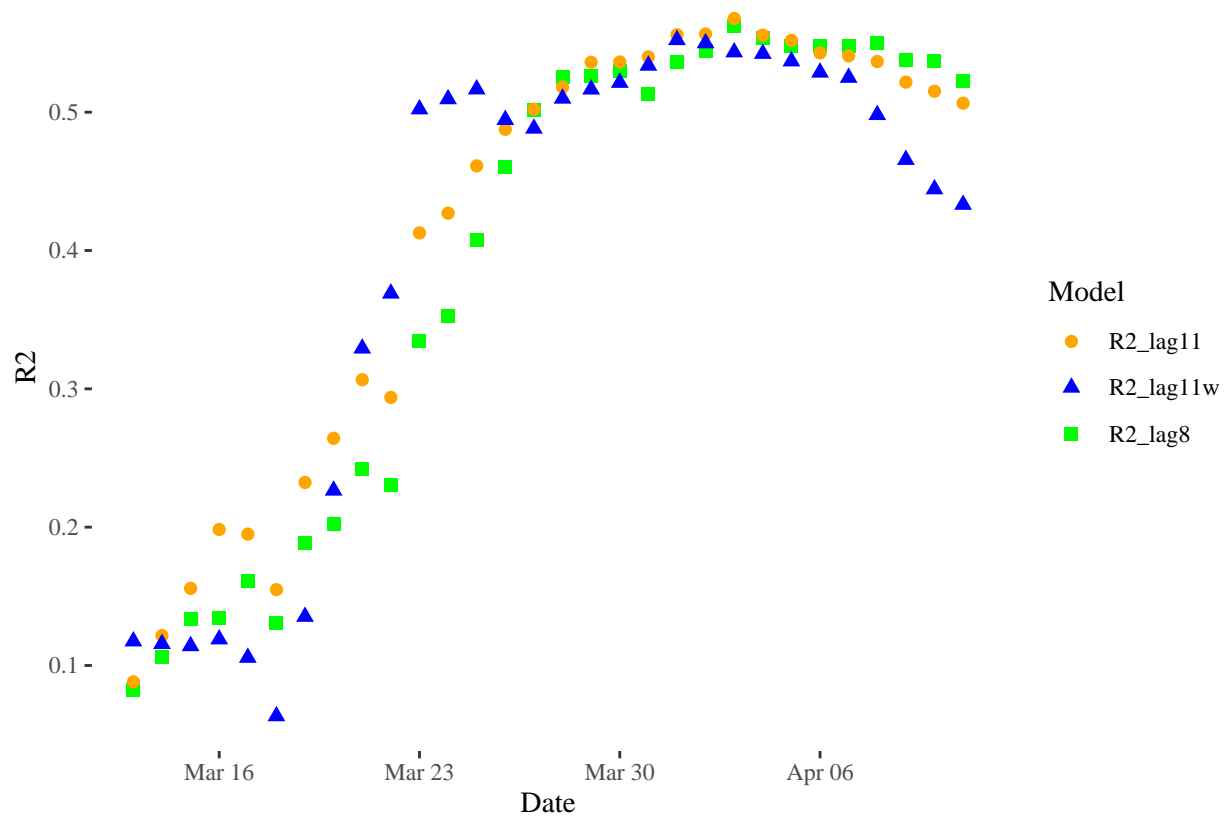
## 0.8213784 0.8305528 0.8646611 0.8562576 0.8567458 0.8487431 0.8607702
## 0.8513494 0.8629032 0.8929602 0.8841837 0.8824954 0.8719846 0.8799882
## 0.8880035 0.8915763 0.9020994 0.8981809 0.8968897 0.8851862 0.8844409
## 0.9099142 0.9043852 0.9084057 0.9037051 0.9028223 0.8895773 0.8925681
## 0.9436383 0.9353953 0.9329315 0.9244955 0.9229647 0.9117337 0.9115081
## 0.9689044 0.9529775 0.9417951 0.9335816 0.9351707 0.9294617 0.9235105
## 0.9915641 0.9712511 0.9514245 0.9375704 0.9351571 0.9283379 0.9179163
## 1.0000000 0.9839611 0.9607635 0.9511781 0.9483157 0.9419053 0.9289310
## 0.9839611 1.0000000 0.9891297 0.9811772 0.9715357 0.9571019 0.9433363
## 0.9607635 0.9891297 1.0000000 0.9909627 0.9809400 0.9656262 0.9582357
## 0.9511781 0.9811772 0.9909627 1.0000000 0.9954529 0.9831865 0.9734395
## 0.9483157 0.9715357 0.9809400 0.9954529 1.0000000 0.9935134 0.9854567
## 0.9419053 0.9571019 0.9656262 0.9831865 0.9935134 1.0000000 0.9947001
## 0.9289310 0.9433363 0.9582357 0.9734395 0.9854567 0.9947001 1.0000000
## 0.9136586 0.9293953 0.9477172 0.9628710 0.9763531 0.9863259 0.9957296
## 0.9005095 0.9181582 0.9383071 0.9540660 0.9681701 0.9753372 0.9863956
## 0.8972921 0.9151055 0.9342633 0.9497850 0.9631966 0.9684468 0.9785738
## 0.8962212 0.9156544 0.9343284 0.9499303 0.9631087 0.9669146 0.9756206
## 0.9020981 0.9232245 0.9396335 0.9548901 0.9663859 0.9678471 0.9736613
## 0.9038870 0.9266262 0.9421046 0.9545208 0.9640023 0.9622743 0.9657700
## 0.8965245 0.9209765 0.9368812 0.9457001 0.9527815 0.9477664 0.9502326
## 0.8957656 0.9184077 0.9325929 0.9390371 0.9450191 0.9391997 0.9419431
## 0.8928874 0.9139739 0.9261067 0.9329272 0.9388790 0.9340141 0.9362134
##
## 0.5666514 0.5628183 0.5621140 0.5619814 0.5614581 0.5770687 0.5831369
## 0.6185191 0.6140592 0.6119331 0.6158631 0.6214539 0.6403654 0.6500055
## 0.6885862 0.6868770 0.6886107 0.6930263 0.6981791 0.7146370 0.7221133
## 0.7407522 0.7377015 0.7392501 0.7438556 0.7448912 0.7558302 0.7582360
## 0.7609516 0.7578684 0.7599507 0.7645887 0.7635569 0.7717631 0.7719404
## 0.7644650 0.7621598 0.7649095 0.7701256 0.7700562 0.7807760 0.7830351
## 0.8228217 0.8218332 0.8218147 0.8250625 0.8238295 0.8309718 0.8314287
## 0.8665213 0.8686822 0.8674286 0.8687111 0.8671239 0.8712386 0.8700989
## 0.8836187 0.8837883 0.8800650 0.8798408 0.8791766 0.8823818 0.8793093
## 0.8830370 0.8823950 0.8782158 0.8753611 0.8767521 0.8795107 0.8727262
## 0.8923370 0.8910491 0.8847957 0.8785515 0.8788312 0.8814900 0.8751560
## 0.9061913 0.9032299 0.8994738 0.8946475 0.8968807 0.9012569 0.8952995
## 0.9148029 0.9072460 0.9045402 0.9004916 0.9029718 0.9059876 0.8986330
## 0.9058894 0.8946687 0.8929698 0.8907259 0.8945516 0.8960791 0.8894149
## 0.9136586 0.9005095 0.8972921 0.8962212 0.9020981 0.9038870 0.8965245
## 0.9293953 0.9181582 0.9151055 0.9156544 0.9232245 0.9266262 0.9209765
## 0.9477172 0.9383071 0.9342633 0.9343284 0.9396335 0.9421046 0.9368812
## 0.9628710 0.9540660 0.9497850 0.9499303 0.9548901 0.9545208 0.9457001
## 0.9763531 0.9681701 0.9631966 0.9631087 0.9663859 0.9640023 0.9527815
## 0.9863259 0.9753372 0.9684468 0.9669146 0.9678471 0.9622743 0.9477664
## 0.9957296 0.9863956 0.9785738 0.9756206 0.9736613 0.9657700 0.9502326
## 1.0000000 0.9963114 0.9907055 0.9876804 0.9842385 0.9746449 0.9589198
## 0.9963114 1.0000000 0.9971643 0.9950611 0.9913376 0.9815724 0.9668104
## 0.9907055 0.9971643 1.0000000 0.9981863 0.9943112 0.9843317 0.9697226
## 0.9876804 0.9950611 0.9981863 1.0000000 0.9979117 0.9897221 0.9771770
## 0.9842385 0.9913376 0.9943112 0.9979117 1.0000000 0.9962266 0.9871007
## 0.9746449 0.9815724 0.9843317 0.9897221 0.9962266 1.0000000 0.9967836
## 0.9589198 0.9668104 0.9697226 0.9771770 0.9871007 0.9967836 1.0000000
## 0.9503182 0.9575911 0.9592391 0.9665462 0.9783303 0.9912121 0.9977870
## 0.9447194 0.9516096 0.9521039 0.9598851 0.9728162 0.9864309 0.9939412

```

```
##
## 0.5800187 0.5731895
## 0.6476332 0.6432597
## 0.7185193 0.7142658
## 0.7504414 0.7429018
## 0.7641395 0.7580899
## 0.7757437 0.7695268
## 0.8241461 0.8182496
## 0.8622002 0.8570106
## 0.8714066 0.8657030
## 0.8652155 0.8605474
## 0.8741515 0.8706360
## 0.8934001 0.8882279
## 0.8963535 0.8913699
## 0.8885212 0.8852955
## 0.8957656 0.8928874
## 0.9184077 0.9139739
## 0.9325929 0.9261067
## 0.9390371 0.9329272
## 0.9450191 0.9388790
## 0.9391997 0.9340141
## 0.9419431 0.9362134
## 0.9503182 0.9447194
## 0.9575911 0.9516096
## 0.9592391 0.9521039
## 0.9665462 0.9598851
## 0.9783303 0.9728162
## 0.9912121 0.9864309
## 0.9977870 0.9939412
## 1.0000000 0.9980244
## 0.9980244 1.0000000
##
## R-sq. pooled: 0.809
## Breusch-Pagan: 1.405e+04 p-value: ( 0)
```

Compare goodness of fit:

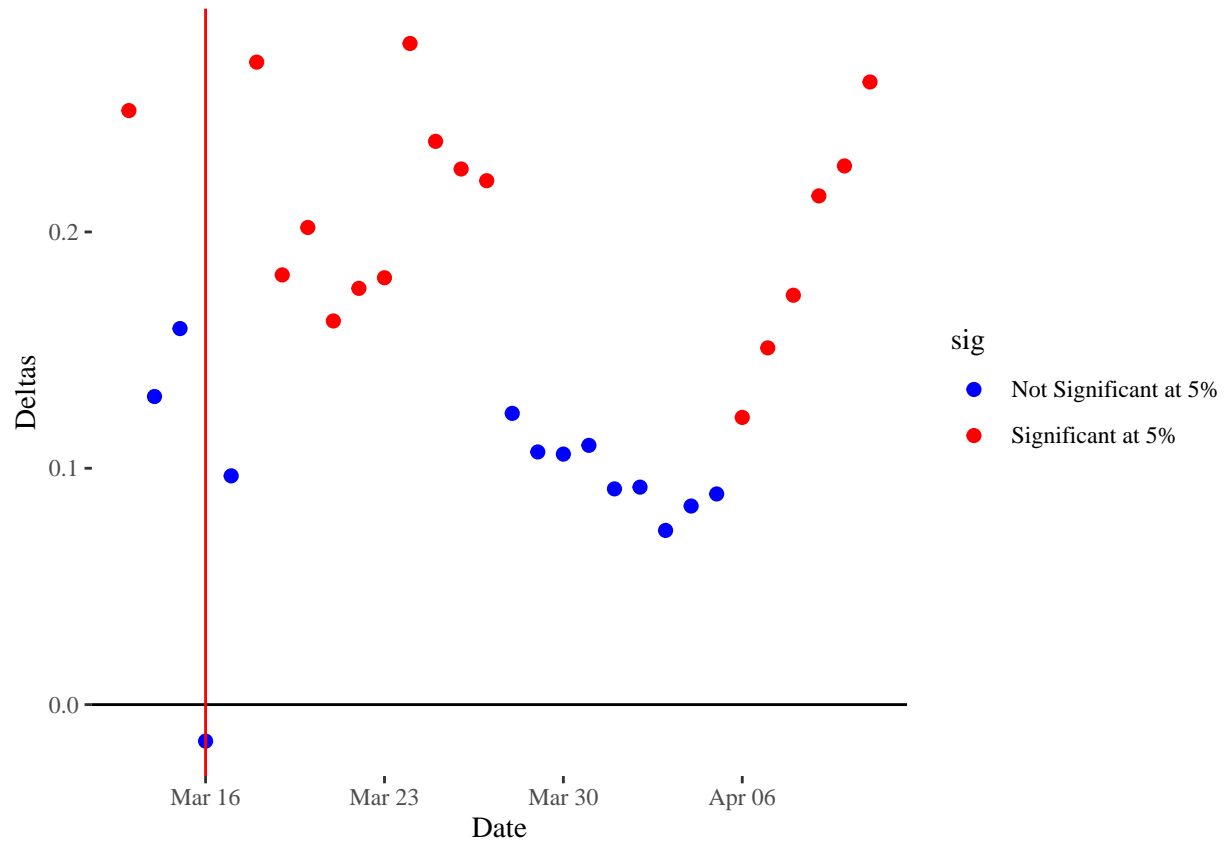
```
data.frame(R2_lag8 = sur.slm_lag8$R2,
           R2_lag11 = sur.slm_lag11$R2,
           R2_lag11w = sur.slm_lag11w$R2) %>%
  slice(2:n()) %>%
  rownames_to_column(var = "Equation") %>%
  mutate(Date = seq(ymd("2020-03-13"),
                    ymd("2020-04-11"),
                    by = "days")) %>%
  pivot_longer(cols = starts_with("R"), names_to = "Model", values_to = "R2") %>%
  ggplot(aes(x = Date, y = R2, color = Model, shape = Model)) +
  geom_point(size = 2) +
  scale_color_manual(values = c("R2_lag11w" = "blue", "R2_lag11" = "orange", "R2_lag8" = "green")) +
  theme_tufte()
```



Spatial evolution of spatial residual autocorrelation

Plot the evolution of the spatial autocorrelation parameter:

```
data.frame(Date = seq(ymd("2020-03-13"),
                      ymd("2020-04-11"),
                      by = "days"),
           Deltas = sur.slm_lag11$deltas,
           tvalue = sur.slm_lag11$deltas/sur.slm_lag11$deltas.se) %>%
mutate(sig = ifelse(abs(tvalue) > 1.64, "Significant at 5%", "Not Significant at 5%")) %>%
ggplot(aes(x = Date, y = Deltas, color = sig)) +
geom_point(size = 2) +
scale_color_manual(values = c("Significant at 5%" = "red", "Not Significant at 5%" = "blue")) +
geom_hline(yintercept = 0) +
geom_vline(xintercept = as_date("2020-03-16"), color = "red") +
theme_tufte()
```



Analysis of autocorrelated residuals

Identify all equations with significant autocorrelation parameters:

```
deltas.sig <- data.frame(Date = seq(ymd("2020-03-13"),
                                   ymd("2020-04-11"),
                                   by = "days"),
                        Deltas = sur.slm_lag11$deltas,
                        tvalue = sur.slm_lag11$deltas/sur.slm_lag11$deltas.se) %>%
  mutate(sig = abs(tvalue) > 1.64)
```

Extract all residuals and calculate the spatially autocorrelated residuals:

```
all_residuais <- data.frame(matrix(unlist(residuals(sur.slm_lag11)),
                                   ncol = length(residuals(sur.slm_lag11)),
                                   byrow = FALSE))

# Spatially lagged residuals
for(i in 1:ncol(all_residuais)){
  all_residuais[,i] <- deltas.sig$Deltas[i] * lag.listw(listw, all_residuais[,i])
}

# Pivot table
all_residuais <- all_residuais %>%
  pivot_longer(everything(),
               names_to = "Date",
```

```

      values_to = "Spatially_Autocorrelated_Residuals") %>%
mutate(Date = rep(seq(dmy("13-03-2020"),
                      dmy("11-04-2020"),
                      by = "days"),
                    50),
      ID_INE = rep(provinces$ID_INE,
                    each = 30))

```

Join to covid19_spain:

```

covid19_spain <- covid19_spain %>%
  left_join(all_residuals, by = c("Date", "ID_INE"))

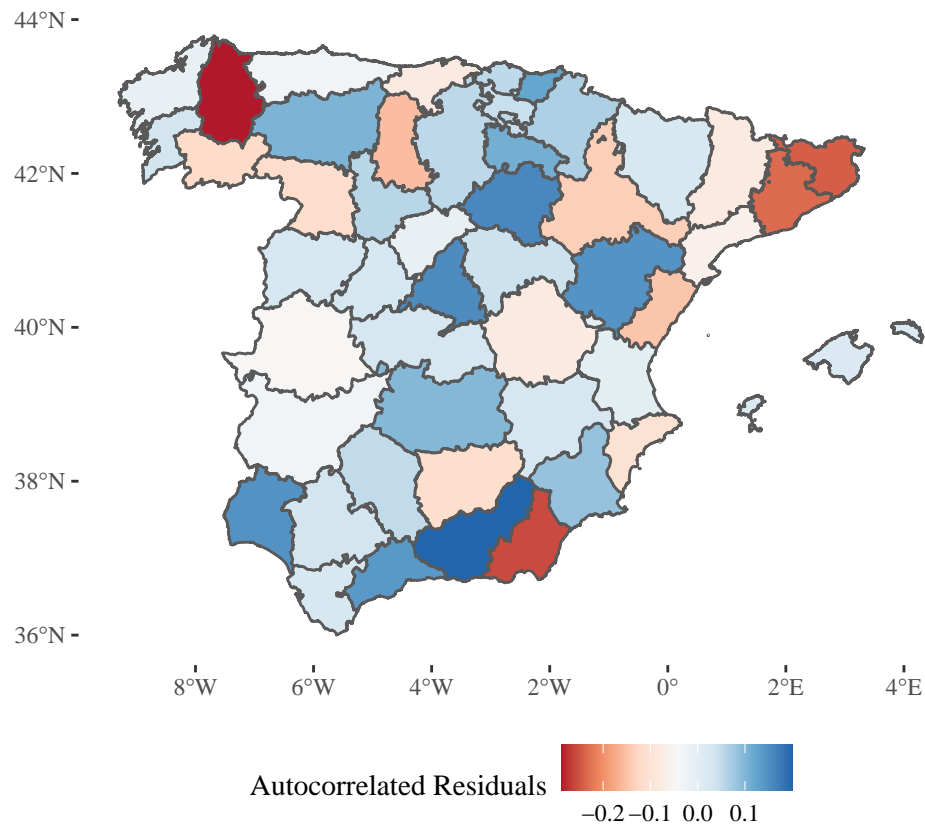
```

Plot residuals on March 13 (positive autocorrelation):

```

covid19_spain %>% filter(Date == "2020-03-13") %>%
  filter(CCAA != "Canarias") %>%
  ggplot() +
  geom_sf(aes(fill = Spatially_Autocorrelated_Residuals)) +
  scale_fill_distiller(name = "Autocorrelated Residuals", palette = "RdBu", direction = 1) +
  theme_tufte() +
  theme(legend.position = "bottom")

```



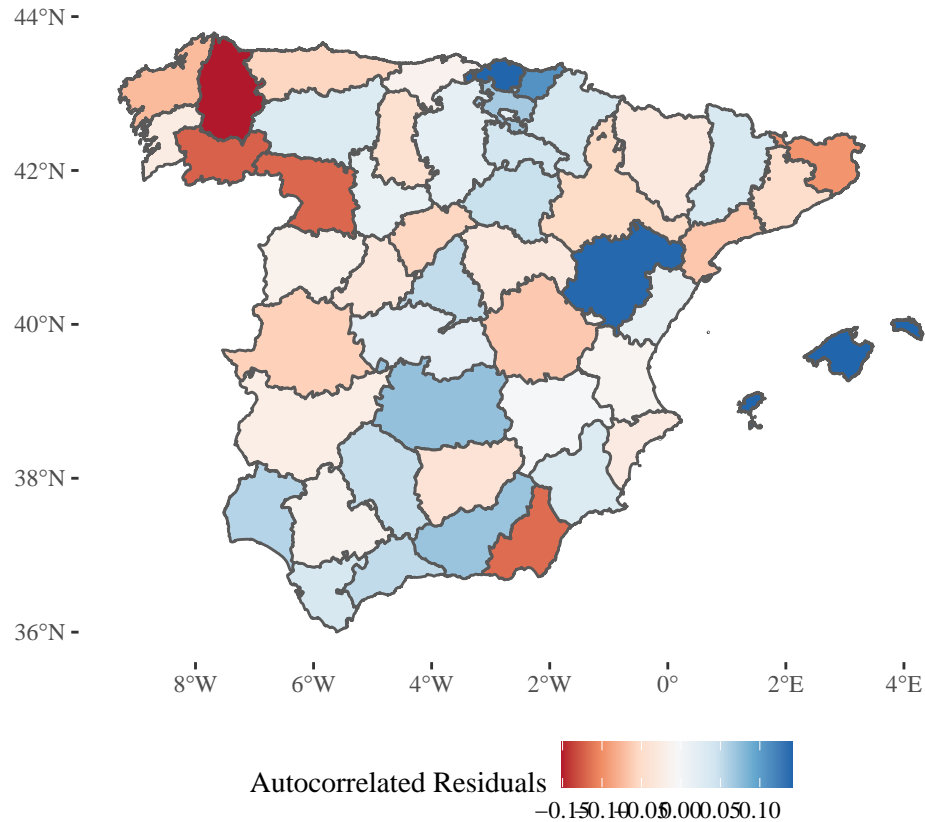
Plot residuals on March 24 (positive autocorrelation):

```

covid19_spain %>% filter(Date == "2020-03-24") %>%
  filter(CCAA != "Canarias") %>%
  ggplot() +

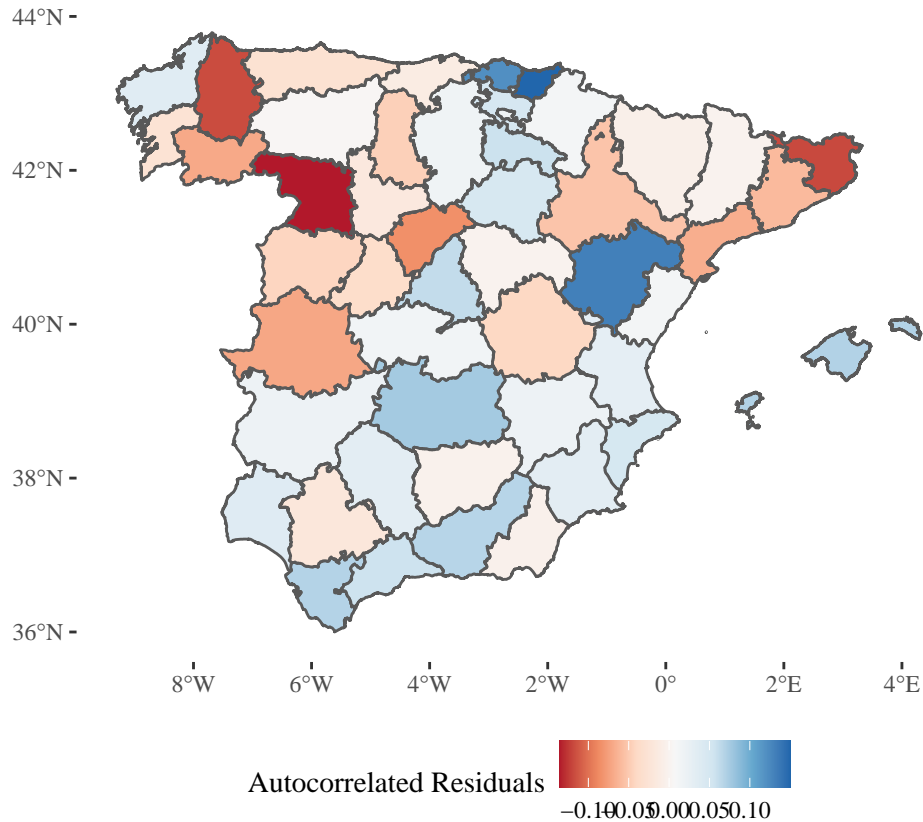
```

```
geom_sf(aes(fill = Spatially_Autocorrelated_Residuals)) +
scale_fill_distiller(name = "Autocorrelated Residuals", palette = "RdBu", direction = 1) +
theme_tufte() +
theme(legend.position = "bottom")
```



Plot residuals on April 11:

```
covid19_spain %>% filter(Date == "2020-04-11") %>%
  filter(CCAA != "Canarias") %>%
  ggplot() +
  geom_sf(aes(fill = Spatially_Autocorrelated_Residuals)) +
  scale_fill_distiller(name = "Autocorrelated Residuals", palette = "RdBu", direction = 1) +
  theme_tufte() +
  theme(legend.position = "bottom")
```



Are these spatially autocorrelated residuals correlated with any other potential control variables? Check the correlations:

```
covid19_spain %>%
  st_drop_geometry() %>%
  group_by(Date) %>%
  summarize(correlation_gdppc = cor(log(GDPPc), Spatially_Autocorrelated_Residuals),
            correlation_older = cor(log(Older), Spatially_Autocorrelated_Residuals),
            correlation_sunshine = cor(log(Sunshine_Hours_lag11 + 0.1), Spatially_Autocorrelated_Residuals),
            summary())
```

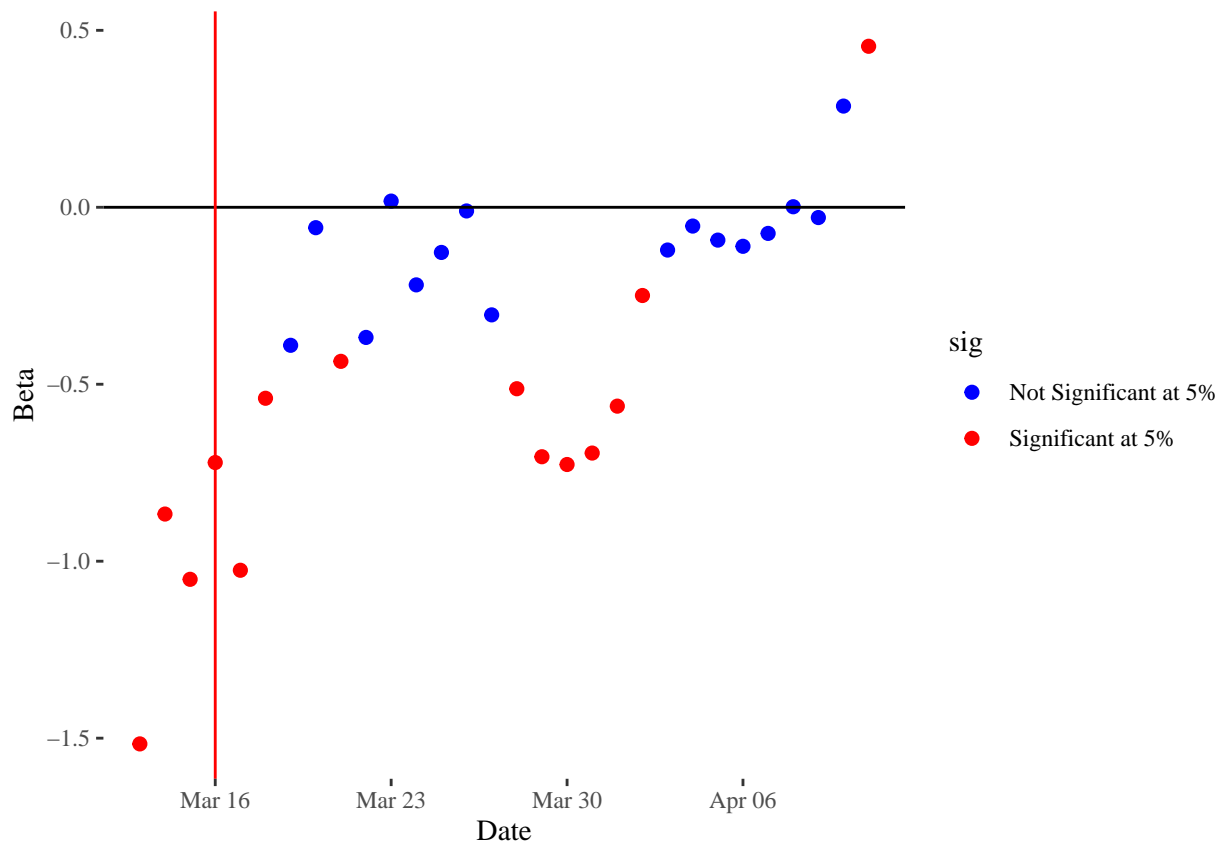
```
##      Date      correlation_gdppc correlation_older
## Min.   :2020-03-13   Min.   : -0.13571   Min.   : -0.30192
## 1st Qu.:2020-03-20   1st Qu.: 0.04029   1st Qu.: -0.18268
## Median :2020-03-27   Median : 0.12926   Median : -0.10704
## Mean   :2020-03-27   Mean   : 0.10492   Mean   : -0.12756
## 3rd Qu.:2020-04-03   3rd Qu.: 0.16818   3rd Qu.: -0.09424
## Max.   :2020-04-11   Max.   : 0.26249   Max.   : 0.28224
## correlation_sunshine
## Min.   : -0.14541
## 1st Qu.: -0.03345
## Median : 0.03646
## Mean   : 0.04495
## 3rd Qu.: 0.12765
## Max.   : 0.23903
```

These two variables are only weakly and inconsistently correlated with the residuals.

Temporal variation of coefficients of climatic variables

Humidity:

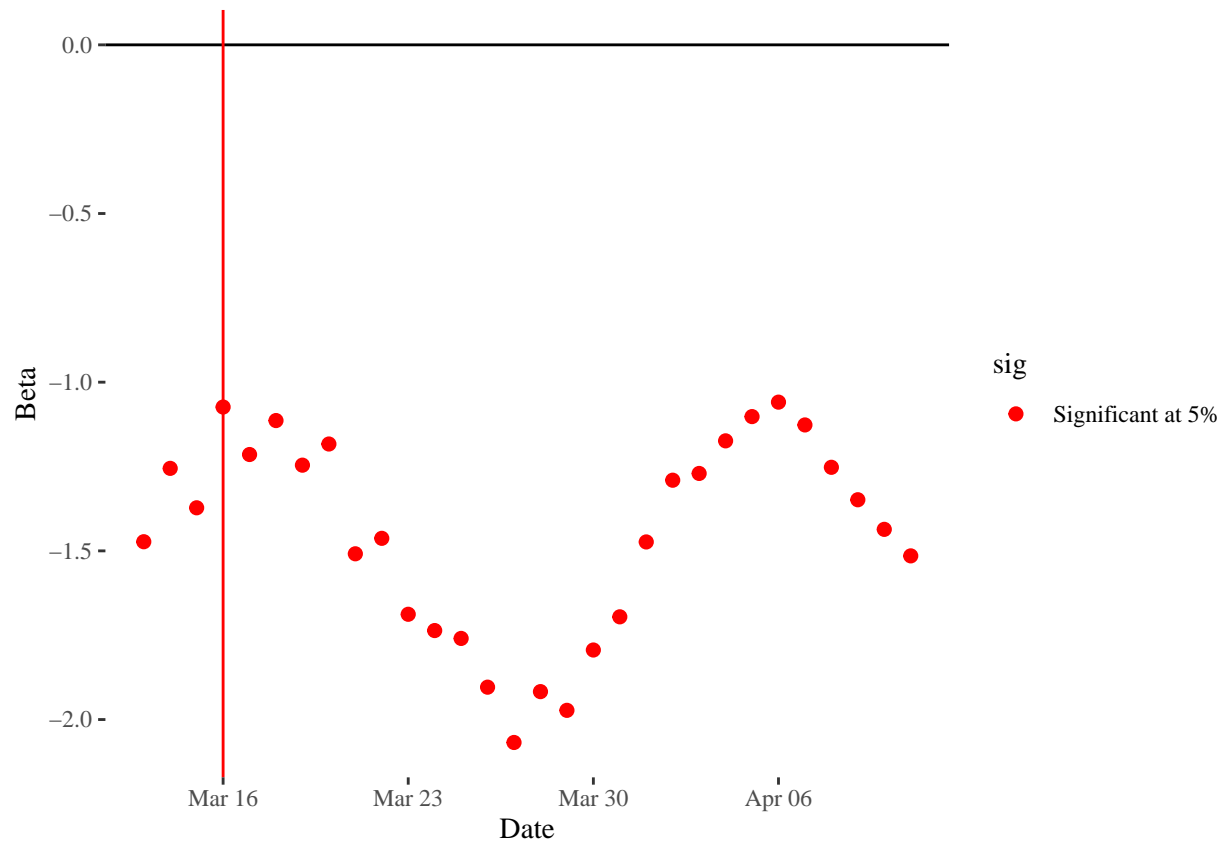
```
n = 4
data.frame(Date = seq(ymd("2020-03-13"),
                      ymd("2020-04-11"),
                      by = "days"),
           Beta = matrix(sur.slm_lag11$coefficients[-c(2,3)], ncol = T)[n,],
           tvalue = matrix(sur.slm_lag11$coefficients[-c(2,3)]/sur.slm_lag11$rest.se[-c(2,3)], ncol = T),
           mutate(sig = ifelse(abs(tvalue) > 1.64, "Significant at 5%", "Not Significant at 5%")) %>%
ggplot(aes(x = Date, y = Beta, color = sig)) +
geom_point(size = 2) +
scale_color_manual(values = c("Significant at 5%" = "red", "Not Significant at 5%" = "blue")) +
geom_hline(yintercept = 0) +
geom_vline(xintercept = as_date("2020-03-16"), color = "red") +
theme_tufte()
```



Temperature:

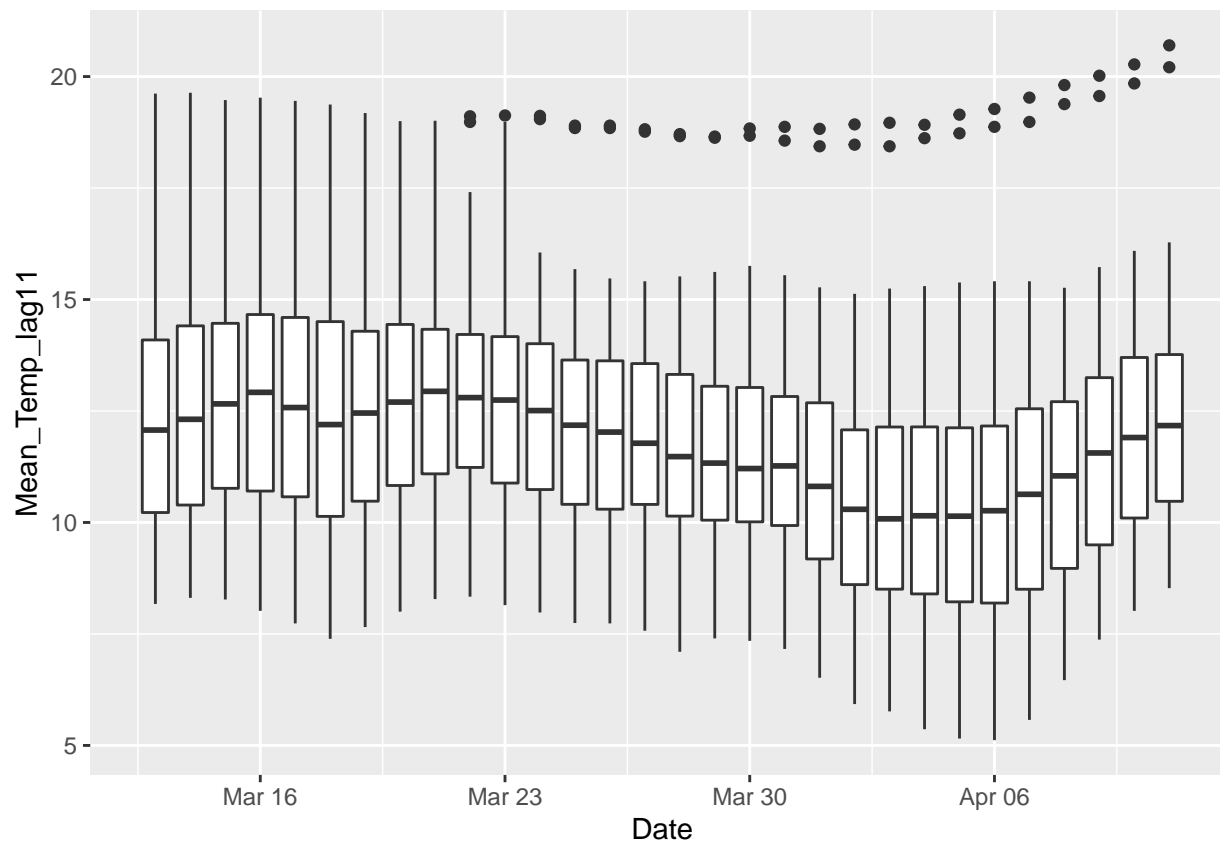
```
n = 5
data.frame(Date = seq(ymd("2020-03-13"),
                      ymd("2020-04-11"),
                      by = "days"),
           Beta = matrix(sur.slm_lag11$coefficients[-c(2,3)], ncol = T)[n,],
           tvalue = matrix(sur.slm_lag11$coefficients[-c(2,3)]/sur.slm_lag11$rest.se[-c(2,3)], ncol = T),
           mutate(sig = ifelse(abs(tvalue) > 1.64, "Significant at 5%", "Not Significant at 5%")) %>%
ggplot(aes(x = Date, y = Beta, color = sig)) +
```

```
geom_point(size = 2) +
scale_color_manual(values = c("Significant at 5%" = "red", "Not Significant at 5%" = "blue")) +
geom_hline(yintercept = 0) +
geom_vline(xintercept = as_date("2020-03-16"), color = "red") +
theme_tufte()
```



Boxplot of temperatures by date

```
ggplot(data = covid19_spain, aes(x = Date, y = Mean_Temp_lag11, group = Date)) +
  geom_boxplot()
```



Intercept

n = 1

```
data.frame(Date = seq(ymd("2020-03-13"),
                      ymd("2020-04-11"),
                      by = "days"),
            Beta = matrix(sur.slm_lag11$coefficients[-c(2,3)], ncol = T)[n,],
            tvalue = matrix(sur.slm_lag11$coefficients[-c(2,3)]/sur.slm_lag11$rest.se[-c(2,3)], ncol = T),
            sig = ifelse(abs(tvalue) > 1.64, "Significant at 5%", "Not Significant at 5%")) %>%
  ggplot(aes(x = Date, y = Beta, color = sig)) +
  geom_point(size = 2) +
  scale_color_manual(values = c("Significant at 5%" = "red", "Not Significant at 5%" = "blue")) +
  geom_hline(yintercept = 0) +
  geom_vline(xintercept = as_date("2020-03-16"), color = "red") +
  theme_tufte()
```

