

## selection sort

arr [ ] = 

1	7	9	2	3	0
---	---	---	---	---	---

sorted  $\rightarrow$

0	1	2	3	7	9
---	---	---	---	---	---

Round

i. select the **SMALLEST** element and place it to the right place.

Ex: arr:

arr [ ] = 

6	4	25	12	22	11
---	---	----	----	----	----

Round 1:

place

$i = 0$

(64)

element

1st smallest element

(11)

Swap

} 

11	25	12	22	6	4
----	----	----	----	---	---

11	25	12	22	6	4
----	----	----	----	---	---

(after Round 1)

Round 2:

place

$i = 1$

(25)

element

2nd smallest element

(12)

Swap

11	12	25	22	6	4
----	----	----	----	---	---

(after Round 2)

Round 3:

11	12	22	25	6	4
----	----	----	----	---	---

(after Round 3)

Round 4:

11	12	22	25	6	4
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(last element is in the perfect place)

$$\begin{aligned} \therefore \text{Total Round} &= 4 \\ &= (\text{total element} - 1) \\ &= (n - 1) \end{aligned}$$

How many rounds till sorted?

5 elements,  $i \Rightarrow 0$  to 3  
 $\therefore i=0 \ \& \ i < (n-1)$

Round 1  $i=0$  x x x x x  
 Round 2  $i=1$  x x x x x  
 ...  
 Last Round  $i=3$  x x x x x

In 1 Round how many compares?

Round 1  $i=0$  x x x x x  
 $j=1$   $j=2$   $j=3$   $j=4$   
 $j = i+1$ ,  $j \Rightarrow i+1$  to  $(n-1)$   
 $\Rightarrow j = i+1$ ,  $j \Rightarrow (i+1)$  to  $(n-1)$   
 $\Rightarrow j = i+1 \ \& \ j < n$

### Time Efficiency Analysis of Selection Sort

Unsorted elements	Number of comparisons required to select either the smallest or the largest	Number of swapping
n	n-1	1
n-1	n-2	1
...	...	...
3	2	1
2	1	1
1	0	0
	$n(n-1)/2$	n-1

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Note that comparing  $n-1$  times and iterating  $n-1$  times is the most amount of work selection sort does when sorting data

### Time Efficiency Analysis of Selection Sort

- In selection sort ...
    - ... makes  $n-1$  comparisons
    - ... performs 1 swap (i.e., 3 assignments)
- Done in sequence  
 $\rightarrow \max[O(n-1), O(1)] = \max[O(n), O(1)] = O(n)$
- Then 1. and 2. are done in sequence  $n-1$  times  
 $\rightarrow O(n-1) * O(n) = O(n) * O(n) = O(n * n) = O(n^2)$

19

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### Time Efficiency Analysis of Selection Sort

- Is  $O(n^2)$  the time efficiency of the best, worst or average case scenario?
- Would the way the data is organized affect the number of operations selection sort perform (affect its time efficiency)?
  - For example:
    - If the data was already sorted (in the desired sort order, e.g., ascending)?
    - If the data was sorted but in the other sort order (e.g., descending)?
    - If the data was unsorted?
  - Let's check it out! @ <https://www.toptal.com/developers/sorting-algo/>

### Summary – Selection Sort Algorithm

- The way the data is organized **does not** affect the number of operations selection sort perform, i.e., does not affect its time efficiency
- Time efficiency
  - Best case scenario:  $O(n^2)$
  - Worst case scenario:  $O(n^2)$
  - Average case scenario:  $O(n^2)$
- Space efficiency
  - in-place sorting algorithm  $\Rightarrow O(1)$

21