

Predicting Relationships Between Variables with Regression



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Overview

Recognize Regression problems in different fields : from Quant Trading to Demand forecasting

Understand how to set up a Regression problem - Dependent and Independent variables

Contrast Classification and Regression and when each technique should be used

Examples of Regression Problems

What will be **the returns** from a stock on a given date?

If waiting time increases, **how does this affect** customer satisfaction?

What will be the **sales** of this product in a given week?

A Regression Problem Statement

**You would like to compute some
Continuous Value**

Stock Returns

Sales

A Regression Problem Statement

You would like to quantify the
relationship between 2 variables

Wait time



**Customer
Satisfaction**

Regression

Regression helps you quantify the relationship between variables



Let's take the example of Stock Returns

**Day of the
week**

**Day of the
month**

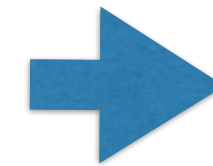
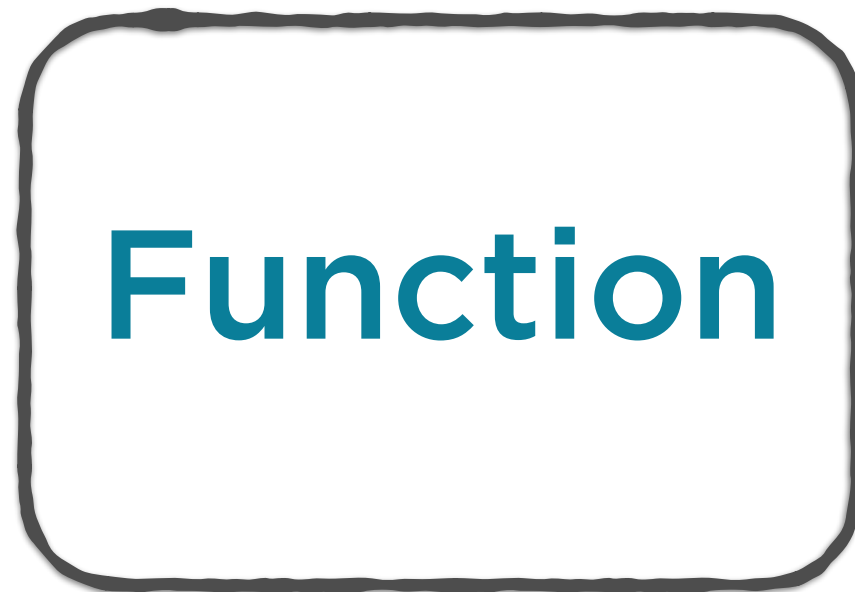
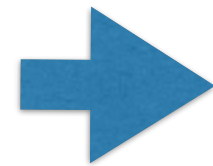
**Daily Stock
returns in the
last 1 week**

**Stock Returns for a given
day might depend on a
number of variables**

Day of the
week

Day of the
month

Daily Stock
returns in the
last 1 week



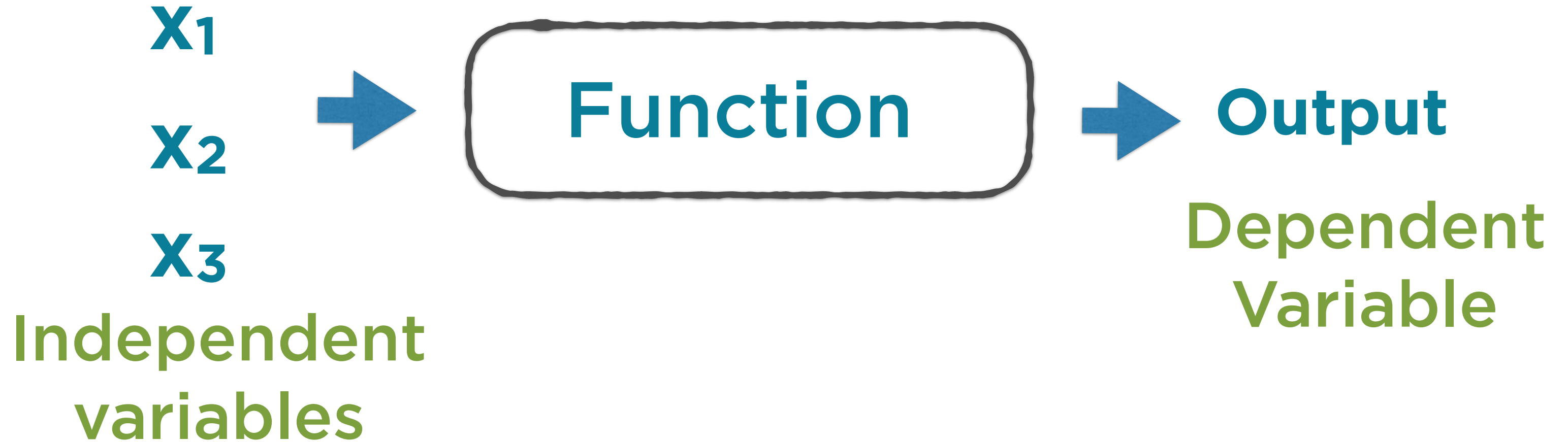
Stock Returns

The Stock Returns
on a given day are
a function of these
variables

Function

**Regression is the
process that identifies
this function**

Regression



Types of Regression

Linear Regression

Polynomial Regression

Non-linear Regression

Demand Forecasting

**Many businesses need to estimate
sales at a future point in time**

Demand Forecasting

**A retail business will
use it for inventory
planning**



Demand Forecasting

A manufacturing business will use it plan production cycles



Demand Forecasting

Sales at a future time might depend on

Sales in the previous week

Expected Marketing spend

Holidays

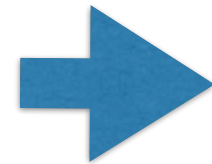
Regression

Sales in the
previous week

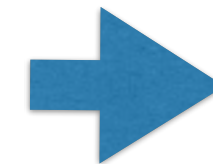
Expected
Marketing spend

Holidays

**Independent
variables**



Function



**Sales in
future week**

**Dependent
Variable**

High Risk, High Reward

A maxim heard quite often in the business world!



The Capital Asset Pricing Model

Used for pricing risky securities

$$R_i = R_f + \beta_i(R_m - R_f)$$

The CAPM Model

$$R_i = R_f + \beta_i(R_m - R_f)$$

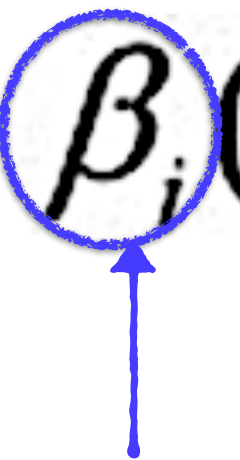
**The return on a
security**

The CAPM Model

$$R_i = R_f + \beta_i (R_m - R_f)$$

The risk free
Rate of Return + a Premium

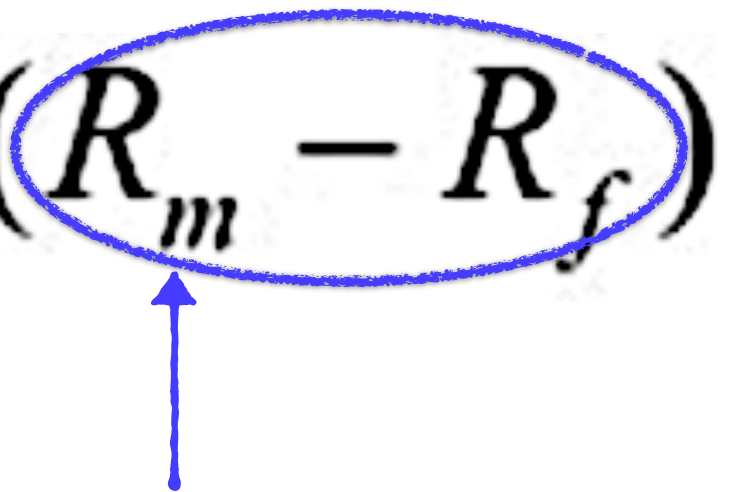
The CAPM Model

$$R_i = R_f + \beta_i (R_m - R_f)$$


The Volatility of the security

A Measure of risk

The CAPM Model

$$R_i = R_f + \beta_i (R_m - R_f)$$


Expected return of the market
over and above the risk free rate

The CAPM Model

$$R_i = R_f + \beta_i (R_m - R_f)$$


**Beta of a security is
an important measure**

**It can tell you how much risk a
security adds to a portfolio**

The CAPM Model

$$R_i = R_f + \beta_i(R_m - R_f)$$

**Beta quantifies the
relationship between Stock
Returns and Market Returns**

The CAPM Model

$$R_i = R_f + \beta_i(R_m - R_f)$$

**Use Regression to find the
value of Beta**

Facial Feature Detection

**Teach a
computer to
identify eyes,
nose, mouth**



Facial Feature Detection

Facial Recognition

**Virtual dressing
rooms**

**Auto-capture
photos**



Facial Feature Detection

**Find the co-ordinates
of the important facial
features**



Facial Feature Detection

Their position depends on

- relative position within the picture
- the properties of surrounding pixels



Facial Feature Detection

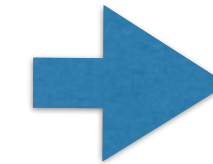
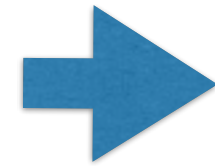
The co-ordinates of each feature can be found using one regression problem



Regression

Size of the
picture

Greyscale value
of each pixel



**Left eye center
co-ordinates**

**Independent
variables**

**Dependent
Variable**

Classification and
Regression are
similar in many ways

Typical Classification Setup

**Problem
Statement**

**Define the problem
statement**

Features

**Represent the
training data and
test data using
numerical
attributes**

Training

**“Train a model”
using the training
data**

Test

**“Test the model”
using test data**

Typical Regression Setup

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**Problem
Statement**

**The problem statement in
Classification**

Assign a category/label

**The problem statement in
Regression**

Compute a continuous value

Typical Regression Setup

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Features

In classification

**The problem instance
represented using
numeric attributes**

In Regression

The Independent Variables

Typical Regression Setup

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Training

In classification

Use training data to
build a classifier

In Regression

Use training data to quantify
the relationship between
variables

Training

Regression
is also a form of
Supervised
learning

Typical Regression Setup

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Test

**“Test the model”
using test data**

Test

In classification

**Assign a label for a
new instance**

In Regression

**Compute output value given
the independent variables**

Classification vs Regression

**A Categorical
output**

**A Continuous
output**

Classification vs Regression

Relationship between Input and Output

Usually a black
box

A mathematical
function

Summary

Recognize Regression problems in different fields : from Quant Trading to Demand forecasting

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