

# Performance Evaluations of Computer Networks with Graph Neural Networks

**Fabien Geyer**

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Airbus Central R&T  
Munich  
[fabien.geyer\(at\)airbus.com](mailto:fabien.geyer(at)airbus.com)

Chair of Network Architectures and Services  
Technical University of Munich (TUM)  
[fabien.geyer\(at\)tum.de](mailto:fabien.geyer(at)tum.de)



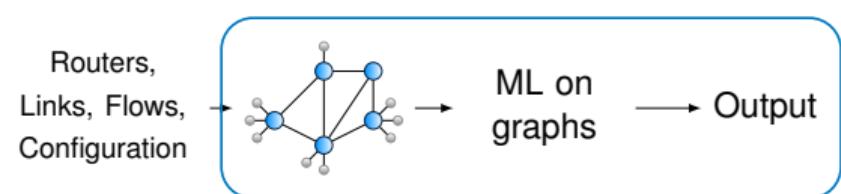
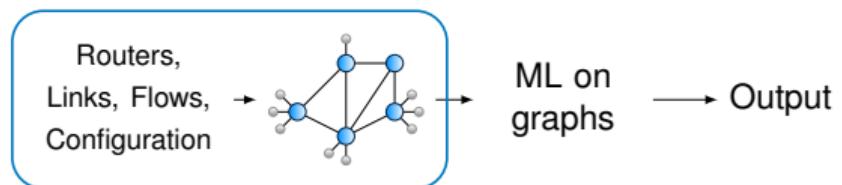
# Outline

Graphs for computer networks

Graph Neural Networks

Application of GNNs for performance evaluation

Conclusions



# Motivation

## Machine Learning and Networking

### Trends in networking and ML research

- Softwarization of networks → *SDN, OpenFlow, P4, ...*
  - Hardware for flexible and customized line-rate processing → *DPDK, PISA switches, SmartNICs, RDMA, ...*
  - Hardware and tools for machine learning
- **Research towards autonomous / self-driving networks**

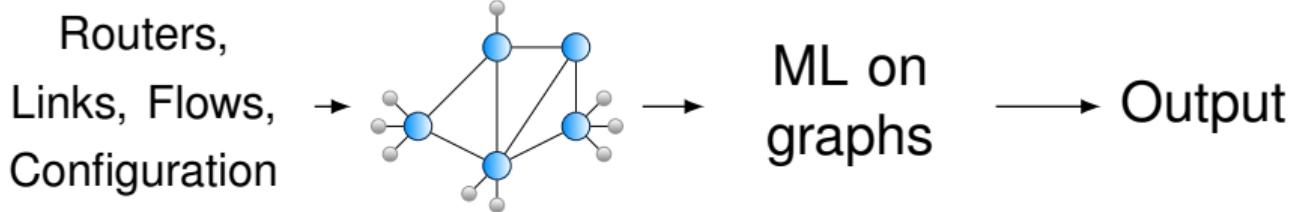
### Various promises of ML for networks

- Minimize human intervention in networks
  - Use data-driven approach on monitoring data to optimize networks
- **Self-\* networks:** self-repairing, self-configuring, self-stabilizing, self-adjusting, ...

## Motivation

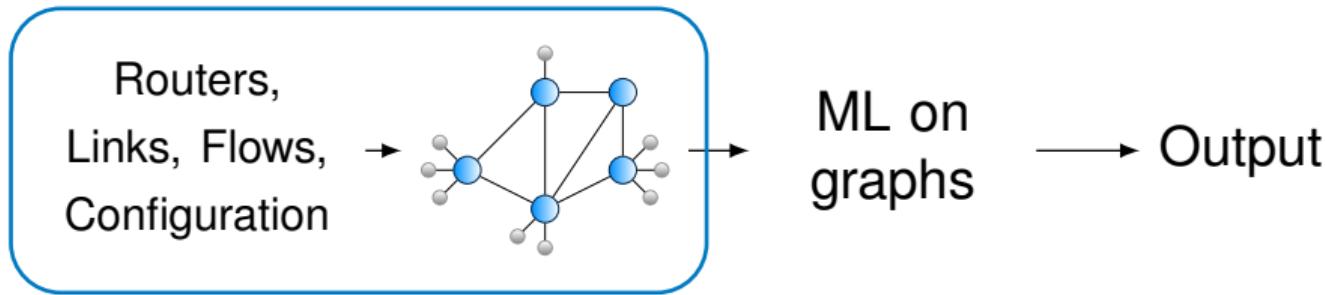
### Abstracting Computer Networks for ML

#### Machine learning workflow



- Need abstraction which has a dynamic size and which can scale (independent of network size)
  - **Graphs as abstraction for representing networks**
  - **Use of machine learning frameworks which can learn on graphs**

## Graphs for computer networks



# Graphs for computer networks

## Routing [Geyer and Carle, 2018]

**Goal:** Given a destination, routers need to know the next hop, i.e. which output interface to use

Transformation from topology to graph

- Nodes: routers and their interfaces
- Edges correspond to physical links

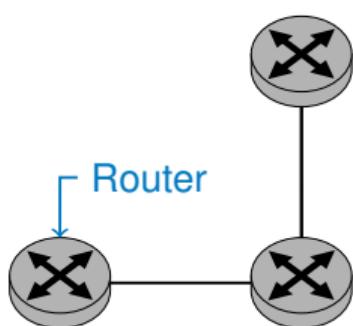


Figure 1: Network topology

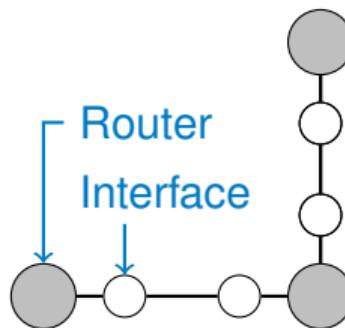


Figure 2: Graph encoding of topology

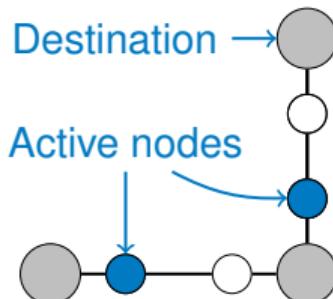


Figure 3: Output for routing  
(classification task)

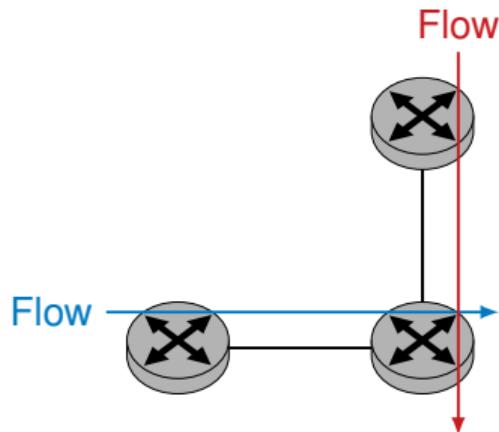
## Graphs for computer networks

Performance evaluation of flows [Geyer, 2018]

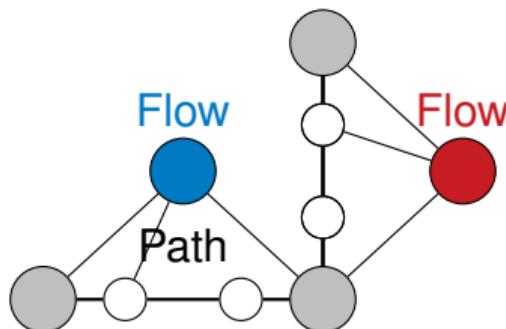
**Goal:** Given a network, predict the performance of flows (e.g. *latency*, *bandwidth*) (regression task)

## Transformation from topology to graph

- Nodes: routers, their interfaces, and flows
  - Edges correspond to physical links between routers
  - Edges also represent the path of flows



**Figure 4:** Network topology



**Figure 5:** Graph encoding of topology

# Graphs for computer networks

MPLS Networks [Geyer and Schmid, 2019]

**Goal:** Given a network and its MPLS configuration, predict properties such as reachability (classification task)

Transformation from topology to graph

- Nodes: routers, their interfaces, and MPLS rules

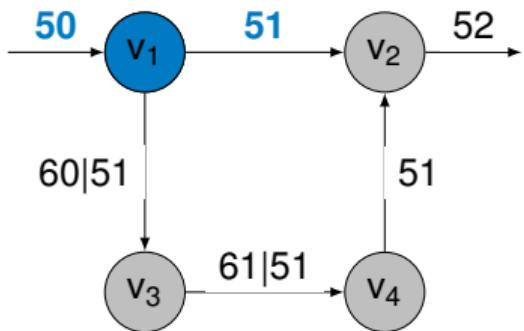


Figure 6: MPLS network, MPLS labels and rules

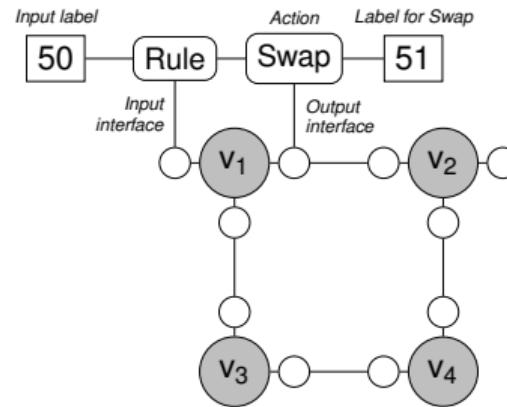
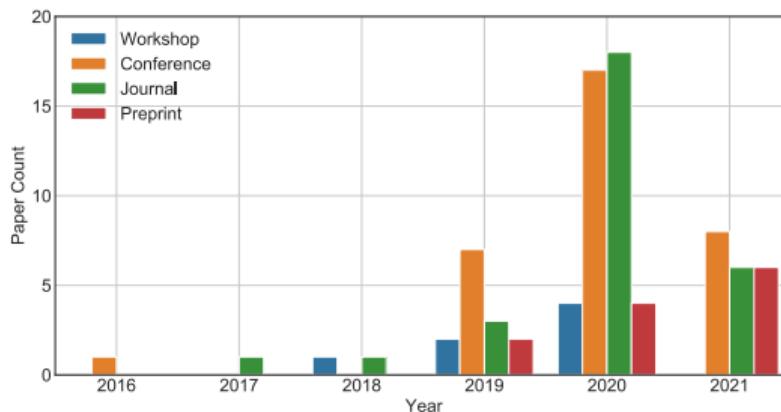


Figure 7: Graph encoding of topology and rules

## Graphs for computer networks

### Other examples for communication networks

- Learning **queueing theory** [Rusek and Cholda, 2018]
- Optimization in **Software Defined Networking** [Rusek et al., 2019]
- **Wireless networks**: analysis [Lee et al., 2019] of scheduling and interference [Shen et al., 2019]
- Speed-up of **formal verification** of end-to-end latencies (network calculus) [Geyer and Bondorf, 2019]
- Graph Neural Networking Challenge organized by UPC [Suárez-Varela et al., 2021]
- Recent survey showed **81 papers** ranging from 2016 to 2021 [Jiang, 2022]



Papers count on GNNs for networking (source: [Jiang, 2022])

# Graphs for computer networks

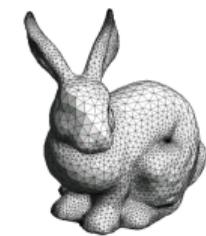
## Other examples outside computer networks

And in other fields also

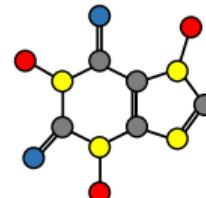
- Analysis of source code and automatic bug-fixing
- Chemistry and molecule analysis (*AlphaFold*)
- Discrete optimization
- Knowledge graphs
- ...



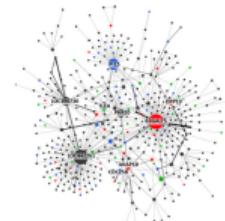
Social networks



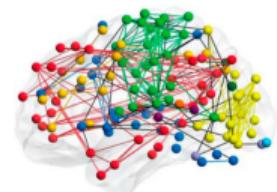
Meshes



Molecules



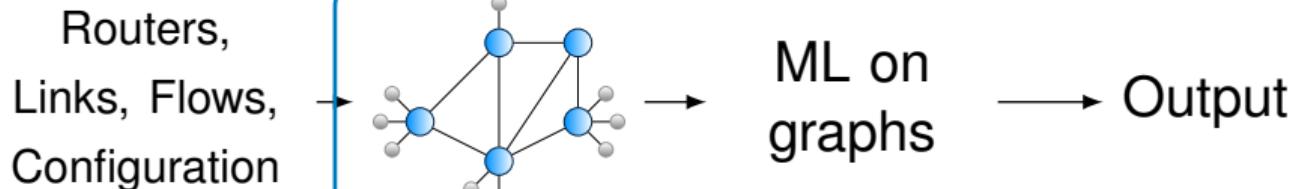
Interaction networks



Functional networks

(source: [Bronstein et al., 2021])

# Graph Neural Networks

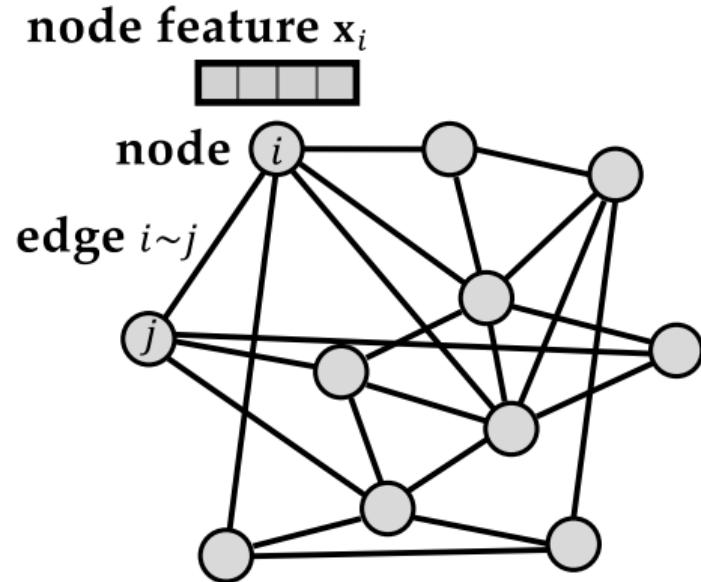


Focus of today's talk: **Graph Neural Networks**

(Disclaimer: some illustrations were taken from Bronstein et al.'s talk [Bronstein et al., 2021])

# Graph Neural Networks

## Key properties of graphs

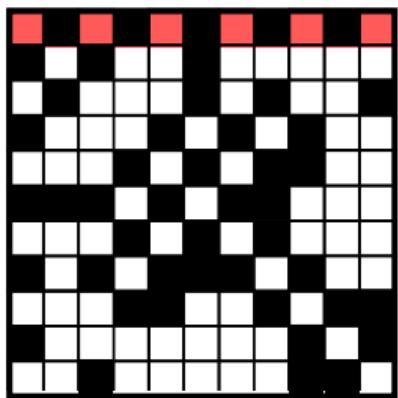


(source: [Bronstein et al., 2021])

# Graph Neural Networks

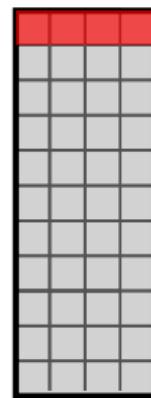
Key properties of graphs: arbitrary ordering

Adjacency  
matrix  $n \times n$

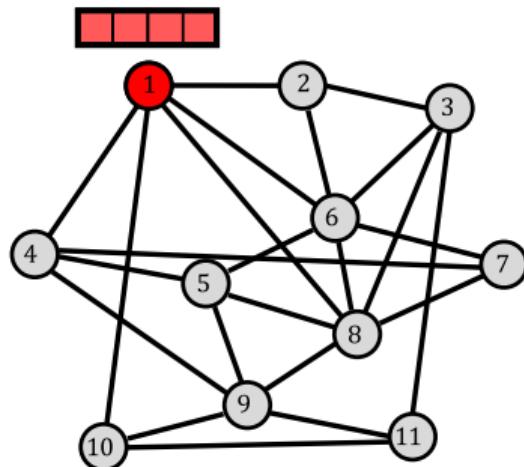


**A**

Feature  
matrix  $n \times d$



**X**

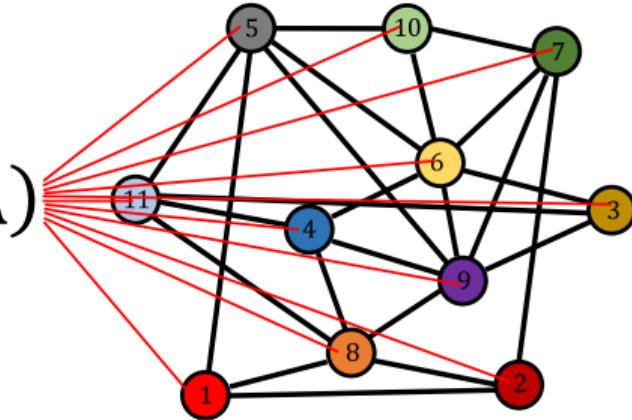


(source: [Bronstein et al., 2021])

# Graph Neural Networks

## Invariant graph function

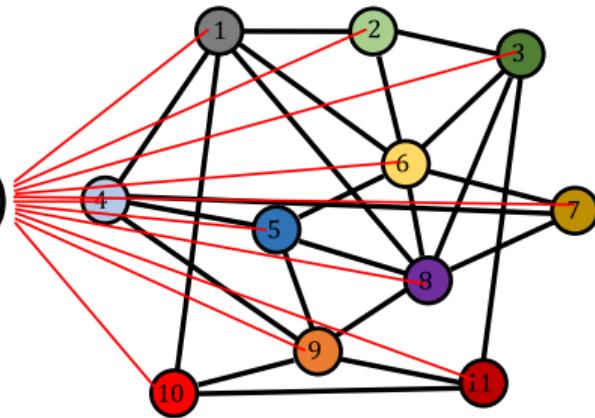
graph function  $f(\mathbf{X}, \mathbf{A})$



(source: [Bronstein et al., 2021])

permutation-invariant

$$f(\mathbf{P}\mathbf{X}, \mathbf{P}\mathbf{A}\mathbf{P}^T) = f(\mathbf{X}, \mathbf{A})$$



(source: [Bronstein et al., 2021])

# Graph Neural Networks

## Introduction

**Graph Neural Networks** [Scarselli et al., 2009] and related neural network architectures are able to process general graphs and predict feature of nodes  $\mathbf{o}_v$

## Principle

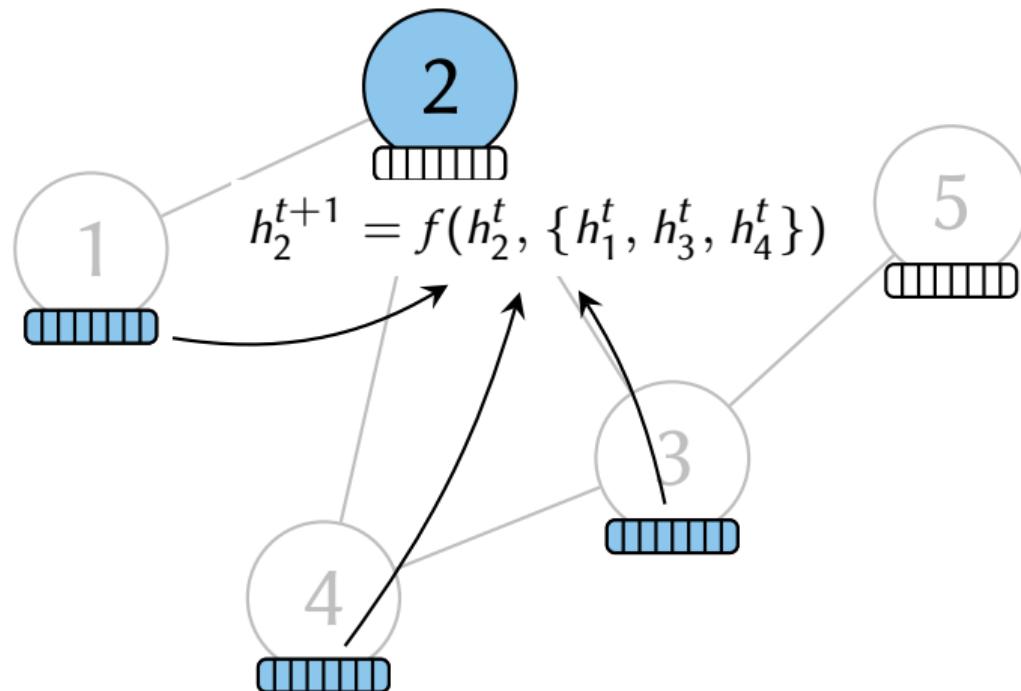
- Each node has a *hidden* vector  $\mathbf{h}_v \in \mathbb{R}^k$
- ...computed according to the vector of its neighbors
- ...and are propagated through the graph
- Once the propagation is done, a prediction is made
  - Node prediction (*classification or regression*)
  - Edge prediction

## Iterative algorithm

- Initialize  $\mathbf{h}_v^{(0)}$  according to features of nodes ( $\mathbf{X}$ )
- for  $t = 1, \dots, T$  do
  - $\mathbf{a}_v^{(t)} = \text{AGGREGATE} \left( \left\{ \mathbf{h}_u^{(t-1)} \mid u \in \text{Nbr}(v) \right\} \right)$
  - $\mathbf{h}_v^{(t)} = \text{COMBINE} \left( \mathbf{h}_v^{(t-1)}, \mathbf{a}_v^{(t)} \right)$
- return  $\text{READOUT} \left( \mathbf{h}_v^{(T)} \right)$

# Graph Neural Networks

## Illustration



# Graph Neural Networks

## Implementation

### Implementation (simplified)

- Initialize  $\mathbf{h}_v^{(0)}$  according to features of nodes
- for  $t = 1, \dots, T$  do
  - *AGGREGATE*  $\rightarrow \mathbf{a}_v^{(t)} = \sum_{u \in Nbr(v)} \mathbf{h}_u^{(t-1)}$
  - *COMBINE*  $\rightarrow \mathbf{h}_v^{(t)} = \text{Neural Network}(\mathbf{h}_v^{(t-1)}, \mathbf{a}_v^{(t)})$
- *READOUT*  $\rightarrow$  return *Neural Network*  $(\mathbf{h}_v^{(T)})$

### Training

- Using standard gradient descent techniques

### Different approaches

- **Gated-Graph Neural Network** [Li et al., 2016]
- Graph Convolution Network
- Graph Attention Networks
- Graph Spatial-Temporal Networks
- ...

→ Hot area of research in the ML community

→ Various open-source libraries implementing GNNs

# Graph Neural Networks

## History of Graph Neural Networks according to Machine Learners



A. Sperduti



C. Goller



A. Küchler



M. Gori



F. Scarselli



Y. Li

Labeling RAAM

1994

Backprop through structure

1996

Graph Neural Networks

2005, 2008

Gated GNN

2015

(source: [Bronstein et al., 2021])

## Some references (non-exhaustive list)

### Introductions / Theory / Books

- [Gilmer et al., 2017]
- [Battaglia et al., 2018]
- [Wang et al., 2018]
- <https://geometricdeeplearning.com>
- [https://www.cs.mcgill.ca/~wlh/grl\\_book/](https://www.cs.mcgill.ca/~wlh/grl_book/)
- <https://distill.pub/2021/gnn-intro/>

### Libraries

- pytorch-geometric (*used for today's talk*)
- TensorFlow GNN
- DGL
- DeepMind's Graph Nets and jgraph
- Spektral
- Keras

### Talks and keynotes on YouTube

- ICLR 2021 Keynote - "Geometric Deep Learning: The Erlangen Programme of ML" - M. Bronstein
- Intro to graph neural networks - P. Veličković
- Beyond the Patterns 28 - Petar Veličković - Geometric Deep Learning

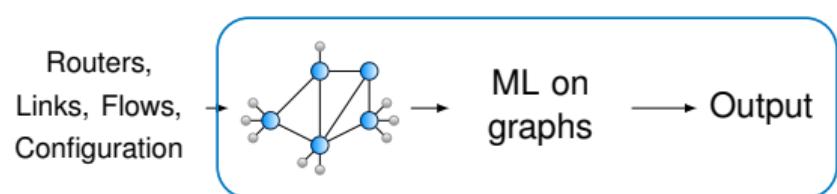
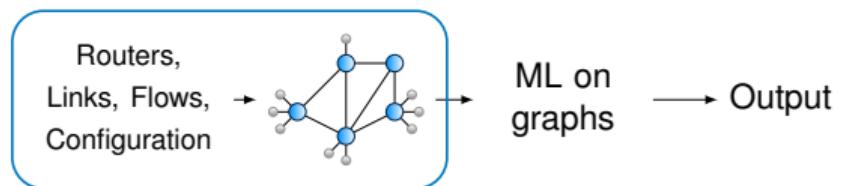
# Application of GNNs for performance evaluation

Graphs for computer networks

Graph Neural Networks

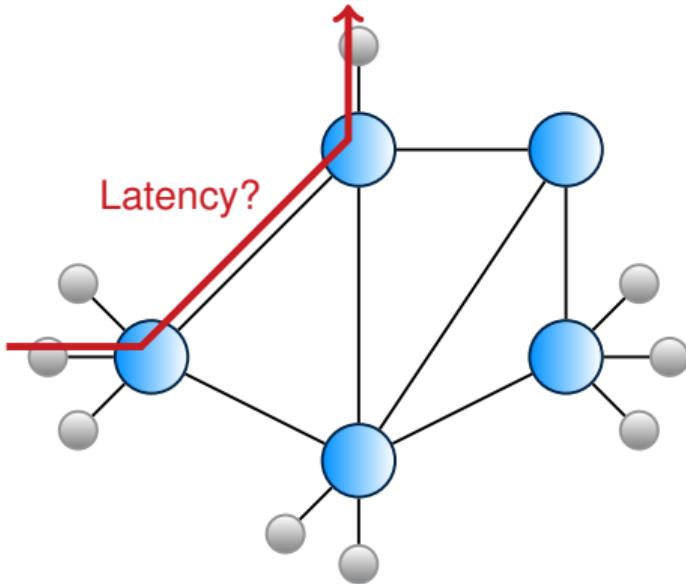
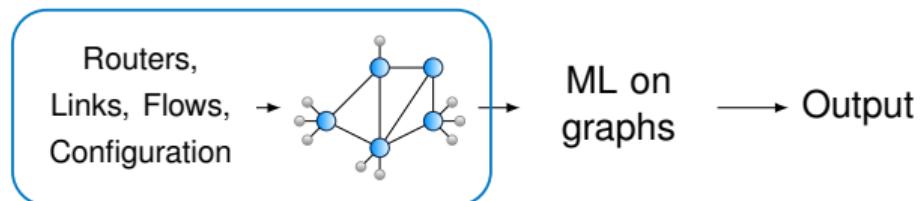
Application of GNNs for performance evaluation

Conclusions



# Application of GNNs for performance evaluation

## Introduction



Focus for the remaining slides: **Network calculus**

# Application of GNNs for performance evaluation

## Introduction to network calculus

Network calculus is a set of mathematical results which give insights into man-made systems such as concurrent programs, digital circuits and communication networks. [Le Boudec and Thiran, 2001]

### Flows

- Flows represent unidirectional transfer of data in a network
- Modeled as cumulative function  $A$ , where  $A(t)$  represents the amount of data sent in the interval  $[0, t]$
- Token buckets are often used as envelope:  $A(t) - A(s) \leq \text{rate} \cdot (t - s) + \text{burst}$

### Servers

- Servers represent entities processing the data in the network: queues, schedulers, links, etc.
- They model the relation between some arrival cumulative curve  $A$  and some departure cumulative curve  $D$ .
- Rate-latency curves are often used as envelope:  $D(t) - A(s) \leq \text{rate} \cdot [(t - s) - \text{latency}]^+$

# Application of GNNs for performance evaluation

## Introduction to network calculus

### Bounds

- Based on this model and the envelopes it is possible to compute bounds
- **Latency bound**, representing an upper bound on the end-to-end delay
- **Backlog bound**, representing an upper bound on the queue size

### Mathematics and methods

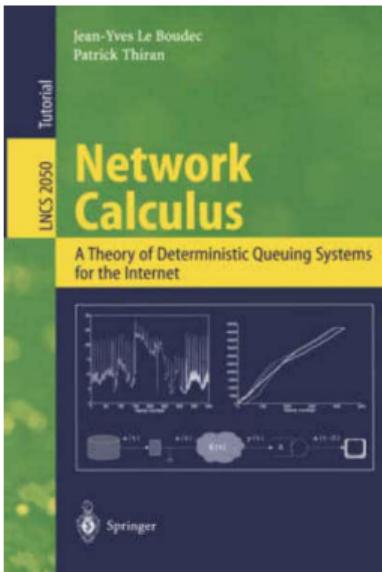
- The **(min,plus) algebra** can be defined for working with the envelopes
- Interesting properties result from the algebra: *server concatenation, pay burst / multiplexing only once*

### Applications

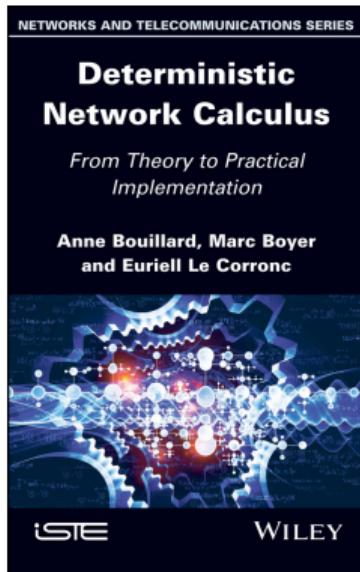
- Industrial networks where real time guarantees are important (eg. aircraft)
- IEEE Time Sensitive Networking (TSN)

# Application of GNNs for performance evaluation

## Introduction to network calculus – References



by Jean-Yves Le Boudec and Patrick Thiran  
Download: <https://leboudec.github.io/netcal/>



by Anne Bouillard, Marc Boyer, and Euriell Le Corronc

# Application of GNNs for performance evaluation

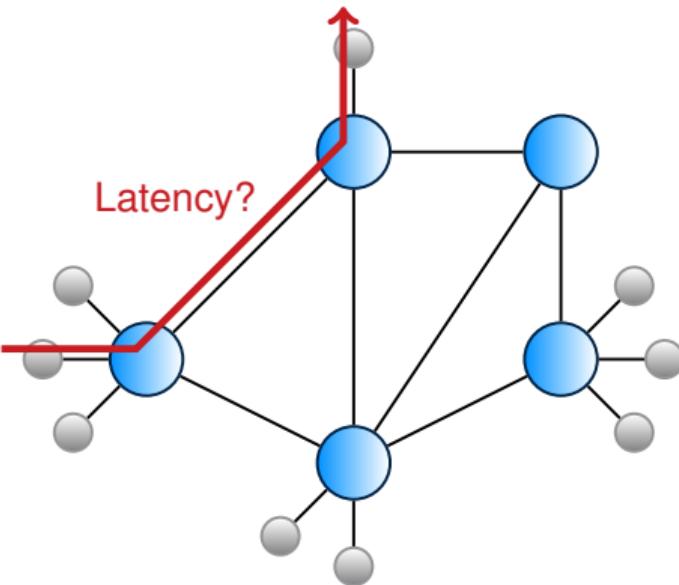
[Back to ML and GNNs](#)

## Inputs

- Network topology, with the queues, links and their properties
  - Flows, with their path in the network, and their traffic envelopes
- **Modeled as graph**

## Target

- Predict end-to-end delay bounds
- **Regression task for each flow in the network**



# Application of GNNs for performance evaluation

Code



<https://github.com/fabgeyer/ainet-summer-school-2022>  
(code and slides located there)

Libraries used:

- pytorch
- pytorch-geometric
- networkx

## Step 1: Getting and understanding the dataset

We will use the dataset from [Geyer et al., 2021], with instructions on <https://github.com/fabgeyer/dataset-rtas2021>

```
$ wget -r ftp://m1596901:m1596901@dataserv.ub.tum.de/
$ mv dataset.ub.tum.de dataset
$ tree dataset
dataset
checksums.sha512
dataset-evaluation-large.pbz
dataset-evaluation.pbz
dataset_structure.proto
dataset-train.pbz
```

We will read the dataset using <https://github.com/fabgeyer/pbzlib-py>

```
$ pip install pbzlib
```

## Step 1: Getting and understanding the dataset

```
import pbzlib
for network in pbzlib.open_pbz("dataset/dataset-train.pbz"):
    print(network)
    break
```

```
server {
    id: 0
    rate: 0.652298881523439
    latency: 0.5384246880613892
}
server {
    id: 1
    rate: 0.1981014874337499
    latency: 0.14038693814170045
}
...
```

```
flow {
    id: 0
    rate: 0.00031810534748519687
    burst: 0.968261581700407
    path: 5
    path: 4
    ...
    pmoo {
        delay_bound: 41.661718156913125
    }
    ...
}
flow {
    id: 1
```

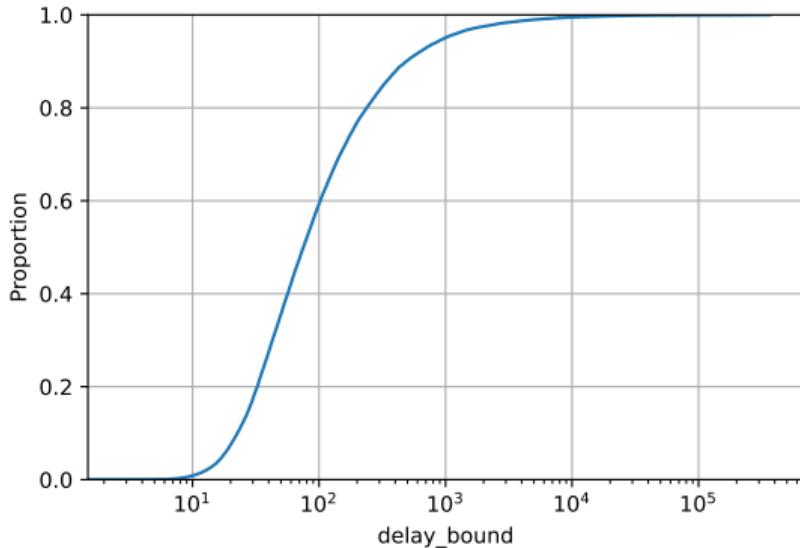
## Step 1: Getting and understanding the dataset

Let's understand the distribution of delay bounds:

```
import seaborn
from pbzlib import open_pbz

delays = []
for network in open_pbz("dataset/dataset-
    train.pbz"):
    for flow in network.flow:
        if flow.pmoo.delay_bound > 0:
            delays.append(flow.pmoo.delay_bound)

seaborn.ecdfplot(delays)
plt.xscale("log")
```



### First lesson

- The delay bounds range over multiple orders of magnitude!
- We will need to scale it for training the GNN → sklearn.preprocessing package

## Step 2: Graph transformation

rows → nodes	targets	mask
	$s_1$	
	$s_2$	
	$s_3$	
	$f_1$	0
	$f_2$	
1		
2		
2		1
1		0

Steps for transforming a network to graph:

- Each server → node in the graph
- Each link between servers → edges between servers
- Each flow → node in the graph
- **How to represent the path?**
  - Edges connecting the flow with the servers it traverses
  - Order is important, so add so-called *path order* nodes

→ **Matrix representation of the graph**

→ **Matrix representation of the targets and mask**

→ **Edges represented as adjacency list**

network2graph and graph2torch functions in the code

## Step 3: Build the GNN

```
import torch_geometric.nn as gnn
class GNNModel(gnn.MessagePassing):
    def __init__(self, num_features, num_classes, hidden_size):
        super(GNNModel, self).__init__()
        self.fcin = nn.Sequential(nn.Linear(num_features, hidden_size), nn.LeakyReLU())
        self.cell = gnn.GatedGraphConv(hidden_size, 1)
        self.fcout = nn.Sequential(
            nn.Linear(hidden_size, hidden_size),
            nn.LeakyReLU(),
            nn.Linear(hidden_size, num_classes))

    def forward(self, x, edge_index, nunroll):
        h = self.fcin(x)
        for _ in range(nunroll):
            h = self.cell(h, edge_index)
        h = self.fcout(h)
        return h
```

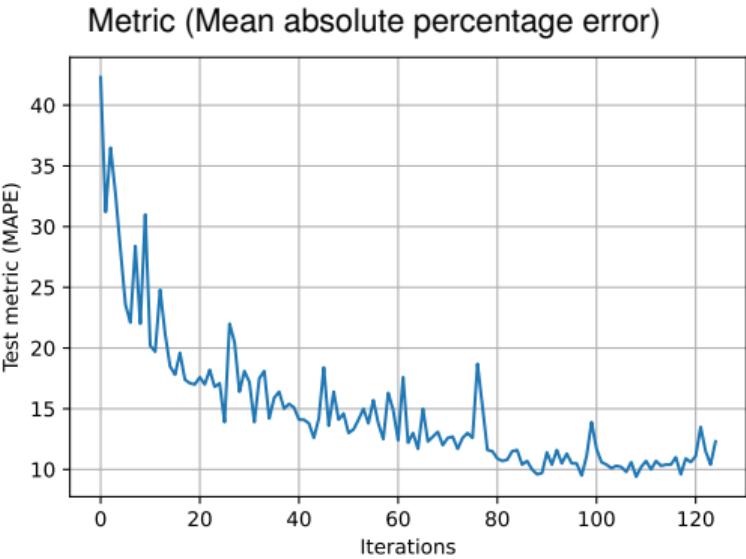
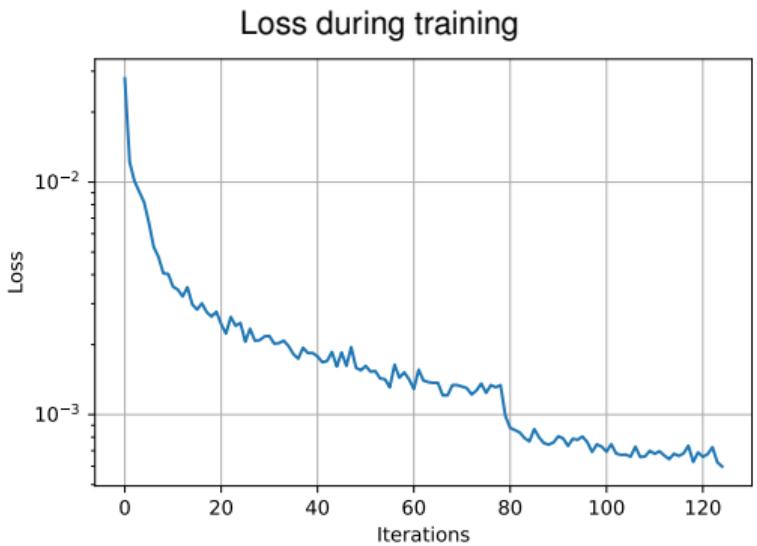
## Step 4: Train the GNN

### Main training loop

```
model = GNNModel(...)  
optimizer = torch.optim.AdamW(model.parameters())  
criterion = nn.MSELoss()  
  
for dt in loader:  
    optimizer.zero_grad()  
    output = model(dt.x, dt.edge_index)  
    nodes_of_interest = torch.where(dt.mask)[0]  
    output = torch.index_select(output, 0, nodes_of_interest)  
    target = torch.index_select(dt.y, 0, nodes_of_interest)  
    loss = criterion(output, target)  
    loss.backward()  
    optimizer.step()
```

The loss function is only applied to a subset of nodes

## Step 4: Train the GNN



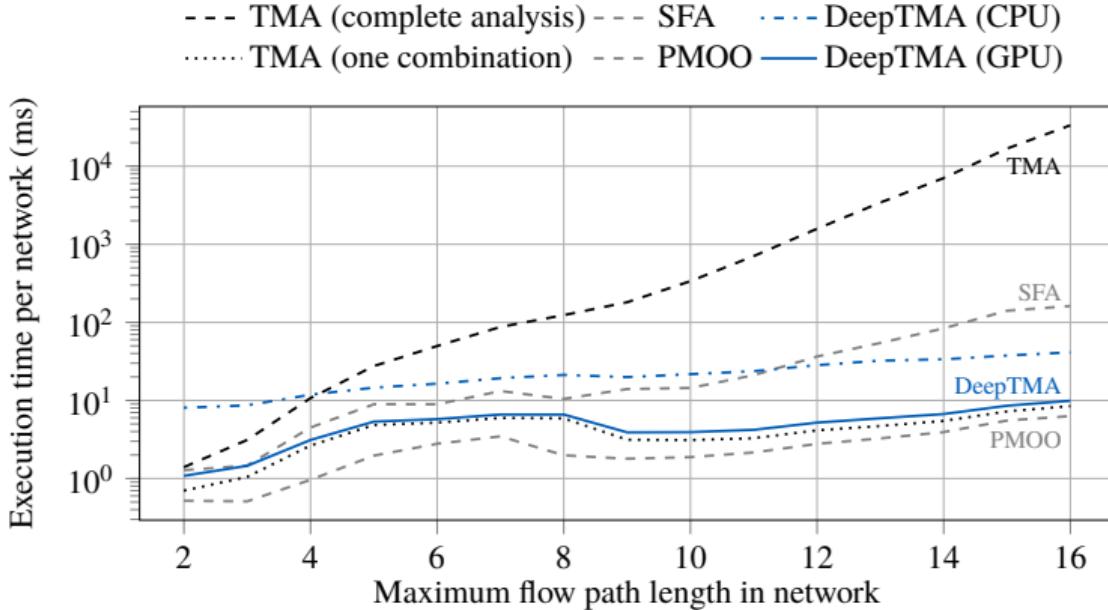
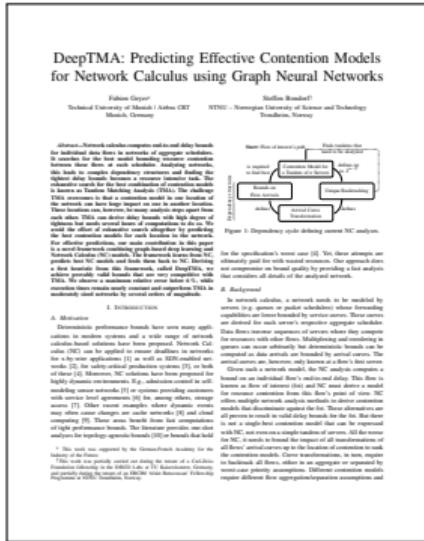
### Improve the training performance

Hyper-parameter optimization is often needed to find the best training parameters (eg. learning rate)  
Various tools available (eg. <https://nni.readthedocs.io> used in the code)

# GNNs and network calculus

This tutorial is only a **toy example**.

Applications of GNNs for network calculus: **speeding up the analysis by avoiding exhaustive searches**



# Conclusions

Graphs for computer networks

Graph Neural Networks

Application of GNNs for performance evaluation

Conclusions

# Conclusions

## Summary of today's talk

- Overview over **Graph Neural Networks**' theory and practice
- Examples of **graph transformations** for networking problems
- A **concrete application** of GNNs for predicting latency bounds in computer networks
- **Code** to play with GNNs and better understand some practical aspects

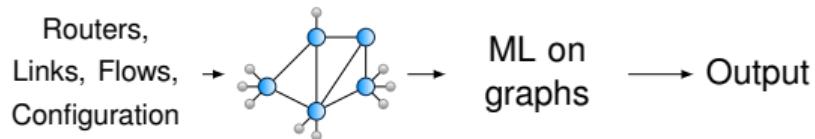
## Next steps for you

- Identify if graphs are the adequate data structure for the challenge you are trying to address
- Better understand the theory behind GNNs
- Play with one of the GNN libraries and your deep learning framework of choice

# Conclusions

## Key messages

- Interesting time for ML applied to computer networks
- **Graphs as abstraction for computer networks for ML**
- Use of **Graph Neural Networks** to make predictions on nodes and edges



## Future work – Collaborations welcome!

- Application to more challenging and dynamic tasks → **self-\* networks**
- **Deployment in real networks** (eg. GNN-based SDN controller)
- Evaluation of most suitable neural network architecture and their scalability

## Conclusions

## Q & A



My personal page  
(contact and publications)



Code and slides

- [Battaglia et al., 2018] Battaglia, P. W., Hamrick, J. B., Bapst, V., Sanchez-Gonzalez, A., Zambaldi, V., Malinowski, M., Tacchetti, A., Raposo, D., Santoro, A., Faulkner, R., Gulcehre, C., Song, F., Ballard, A., Gilmer, J., Dahl, G., Vaswani, A., Allen, K., Nash, C., Langston, V., Dyer, C., Heess, N., Wierstra, D., Kohli, P., Botvinick, M., Vinyals, O., Li, Y., and Pascanu, R. (2018).  
Relational inductive biases, deep learning, and graph networks.  
*arxiv:1806.01261*.
- [Bronstein et al., 2021] Bronstein, M., Bruna, J., Cohen, T., and Veličković, P. (2021).  
Geometric deep learning.  
*African Master in Machine Intelligence – Summer 2021*.
- [Geyer, 2018] Geyer, F. (2018).  
DeepComNet: Performance Evaluation of Network Topologies using Graph-Based Deep Learning.  
*Performance Evaluation*.
- [Geyer and Bondorf, 2019] Geyer, F. and Bondorf, S. (2019).  
DeepTMA: Predicting Effective Contention Models for Network Calculus using Graph Neural Networks.  
*In Proc. IEEE INFOCOM*.
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