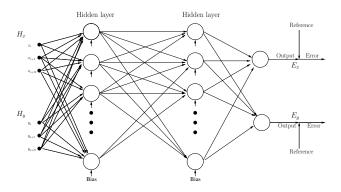
# Machine Learning in Geophysics

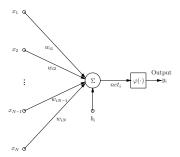
Lecture 7 – Towards neural networks



- Analogy to brain function
- Supervised machine-learning method
- Can be applied to wide range of problems



# Sigmoid neuron



Typical NN consists of many individual neurons, e.g.

$$net_i = \sum_{j=1}^N w_{ij}x_j + b_i$$
  $\varphi(net_i) = tanh\left(\frac{1}{2}net_i\right)$ 

Adaptive noise cancellation

### Linear adaptive filters

- Powerful NN consist of many neurons, layers
- Difficult to understand what exactly is happening (black box)
- Can perform useful tasks with one elementary unit
- Typically called linear adapative combiner, linear adaptive filter
- Used in signal processing, e.g. noise cancelling headphones

### Adaptive noise cancellation

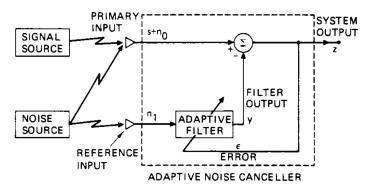
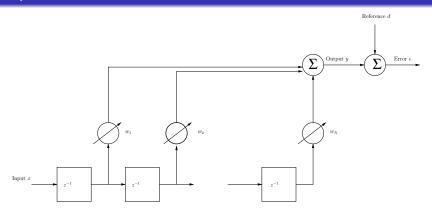


Fig. 1. The adaptive noise cancelling concept.





- We have input x, e.g. noise estimate ( $z^{-1}$  denotes time delay)
- Output is weighted sum
- Compare with reference d, try to minimize error  $\epsilon_{\bullet}$ ,  $\epsilon_{\bullet}$ ,  $\epsilon_{\bullet}$



### LMS Adaptive filter –equations

Start with k = 0,  $\mathbf{w} = 0$ , at step k

$$y_k = \mathbf{x}_k^T \mathbf{w}_k$$
  
$$\epsilon_k = d_k - \mathbf{x}_k^T \mathbf{w}_k$$

#### Question

We want to find **w** that minimize the squared error

$$\epsilon_k^2 = \left( d_k - \mathbf{x_k}^T \mathbf{w_k} \right)^2 \to \min$$

How can we achieve that?

Adaptive noise cancellation

# Adapting w

#### Answer

Calculate derivative

$$\frac{\partial}{\partial \mathbf{w}} \left( d_k - \mathbf{x}_k^T \mathbf{w}_k \right)^2 = 2 \left( d_k - \mathbf{x}_k^T \mathbf{w}_k \right) \mathbf{x}_k = 2 \epsilon \mathbf{x}_k$$

Choose step-length  $\mu$ , adapt weights

$$\mathbf{w}_{k+1} = \mathbf{w}_k + 2\mu\epsilon\mathbf{x}_k$$

Not the most efficient algorithm, but computationally simple

# Step size

- As we saw, the step size is a critical parameter and needs to be chosen "right".
- Can an estimate step size

$$\mu = \frac{\tilde{\mu}}{\delta + \|\mathbf{x}_k\|}$$

with  $\delta$  a small number to avoid division by zero and adaptation constant  $\tilde{\mu} \approx 0.5$ .

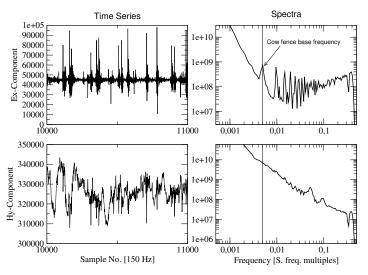
Makes algorithm more robust

$$\begin{pmatrix} E_{x}(\omega) \\ E_{y}(\omega) \end{pmatrix} = \frac{1}{\mu_{0}} \underbrace{\begin{pmatrix} Z_{xx}(\omega) & Z_{xy}(\omega) \\ Z_{yx}(\omega) & Z_{yy}(\omega) \end{pmatrix}}_{\text{complex impedance tensor}} \begin{pmatrix} B_{x}(\omega) \\ B_{y}(\omega) \end{pmatrix}$$

- Inductive, passive electromagnetic method
- Electric field and magnetic field are measured simultaneously
- Recorded data is windowed and transformed into frequency domain
- Local noise sources make far-field assumption invalid



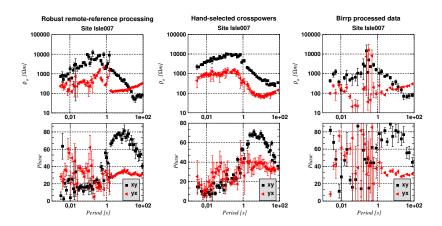
#### Example of contaminated time series and spectra



Strong cow-fence spikes in time series, spectra show strong



#### Remote-reference processing of contaminated data

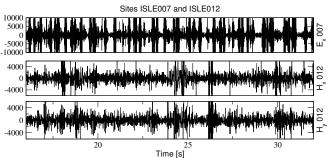


Curves should be smooth with small error bars



#### Basic idea

#### Comparison of time-series



- We have several synchronously recording sites
- Noise free magnetic field is highly correlated but not identical
- Everything is affected by noise to a different degree
- Need to extract the correlated parts

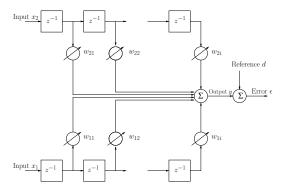


# Noise reduction using adaptive filters

- Adaptive filters are widely used in a range of signal-processing tasks from electrical engineering to medicine
- Provide flexible design that can adjust to problem
- LMS-adaptive linear combiner simplest adaptive filter
- Assume stationary or slowly varying non-stationarity
- Can be extended to non-linear domain ⇒ neural networks

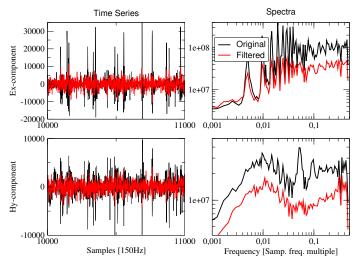
Practical application

### Conceptional diagram of a two-channel LMS-Filter



 $H_X$  and  $H_Y$  of remote site used to clean up local data  $(E_X, E_Y, H_X)$  and  $H_Y$ .

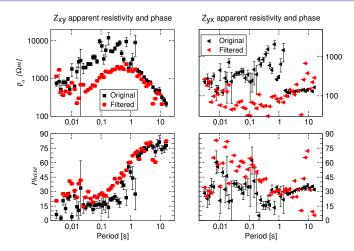
#### Application to a noise contaminated site



Filter removes spikes and reduces spectral signature



### Comparison of transfer functions



Improvement in  $Z_{xy}$ , maybe apparent resistivity  $Z_{yx}$ , suspicious phase  $Z_{yx}$ 

# Summary

- Adaptive combiner is linear part of neural network neuron
- Used as adaptive filter to remove noise
- Implementation relatively simple, some important tuning parameters
- Can be used in noise removal for geophysical time-series