Information Security Definitions

Cryptography

Perfect Secrecy Encryption scheme is perfectly secret if either:

- 1. For random M, C and every $m \in M$, $c \in C$ it holds that $P(M = m) = P(M = m\bar{C} = c)$.
- 2. For M, C, we have that M and C are independent.
- 3. For every m_0, m_1 , we have that $Enc(K, m_0)$ and $Enc(K, m_1)$ have the same distribution.

(Shannon's Theorem) In every perfectly secret encryption scheme, $|K| \ge |M|$.

Semantically Secure / CPA-Secure / IND-CPA In a learning phase, an adversary chooses m'_0, \dots, m'_t and receives c'_0, \dots, c'_t from the oracle.

In a challenge phase, the adversary chooses m_0 , m_1 and the oracle returns $c = Enc(k, m_b)$.

The encryption is CPA-secure if every randomized poly-time adversary guesses b correctly with probability at most $0.5 + \epsilon(n)$, where ϵ is negligible.

(Observation) Every CPA-secure encryption has to be randomized or have a state.

Math

Safe Prime Prime p is safe if $\frac{p-1}{2}$ is also prime.

Quadratic Residue q is a quadratic residue modulo n if there exists an integer x such that $x^2 = q \mod n$.

Security Properties

Confidentiality No improper disclosure of information.

Integrity No improper modification of information.

Availability No improper impairment of functionality/service.

Authenticity Message originated from correct actor.

Non-Repudiation / Accountability Responsibility for actions can be established.

Hash Functions

Collision Resistant

Preimage Resistant Given y, it is infeasible to find x such that H(x) = y.

Second Preimage Resistant Given x, it is infeasible to find $x \neq x'$ such that H(x) = H(x').

Commitments

Hiding After the commit phase, the verifier learns nothing about the locked value of the prover.

Binding After the commit phase, there is only one value that the prover can reveal.

Authentication

Weak Agreement

• b has been running the protocol believing to be communication with a.

Non-Injective Agreement

- Weak agreement is satisfied.
- a and b agree on the contents of all the messages exchanged.

Injective Agreement

- Non-injective agreement is satisfied.
- Each run of A corresponds to a unique run of B.

E-Voting Properties

Coercion Resistance A voter cannot cooperate with a coercer to prove to him that they voted in a certain way.

Coercion resistance implies receipt-freeness.

Receipt-Freeness A voter does not gain any information which can be used to prove to a coercer that they voted in a certain way.

Other Definitions

Intrusion Detection The process of monitoring system/network events for signs of possible incidents, which represent violations of security policies.

Anonymity Set The set of users which appear indistinguishable from each other.

Protocols

Message Authentication Code

Pedersen Commitment Scheme

Perfectly hiding, computationally binding.