



Quiz 3 - Límites

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$$\textcircled{1} \lim_{x \rightarrow 2} \sqrt{\frac{x^3 + 2x + 3}{x^2 + 5}} = \sqrt{\frac{(2)^3 + 2(2) + 3}{(2)^2 + 5}} = \sqrt{\frac{8 + 4 + 3}{4 + 5}} = \sqrt{\frac{15}{9}} = \sqrt{\frac{5}{3}}$$

$$\textcircled{2} g(x) = \frac{\sqrt{x} - 2}{x - 4}$$

$$g(3) = \frac{\sqrt{3} - 2}{3 - 4} = \frac{\sqrt{3} - 2}{-1} = 0.2679$$

$$g(3.5) = \frac{\sqrt{3.5} - 2}{3.5 - 4} = \frac{\sqrt{3.5} - 2}{-0.5} = 0.2583$$

$$g(3.9) = \frac{\sqrt{3.9} - 2}{3.9 - 4} = \frac{\sqrt{3.9} - 2}{-0.1} = 0.2515$$

$$g(3.99) = \frac{\sqrt{3.99} - 2}{3.99 - 4} = \frac{\sqrt{3.99} - 2}{-0.01} = 0.2501$$

$$g(3.999) = \frac{\sqrt{3.999} - 2}{3.999 - 4} = \frac{\sqrt{3.999} - 2}{-0.001} = 0.2500$$

La función no está definida en ese punto
pero tiende a $0.25 = (1/4)$

$$\begin{aligned} \textcircled{3} \lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x - 4} &= \lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x - 4} \cdot \frac{(\sqrt{x} + 2)}{(\sqrt{x} + 2)} = \lim_{x \rightarrow 4} \frac{x - 4}{\cancel{(x - 4)}(\sqrt{x} + 2)} \\ &= \lim_{x \rightarrow 4} \frac{1}{\sqrt{x} + 2} = \frac{1}{\sqrt{4} + 2} = \frac{1}{2 + 2} = \frac{1}{4} = 0.25 \end{aligned}$$