

The logo of the University of Skövde is centered in the background. It features a shield with a lion, a book, and a star, surrounded by a laurel wreath. Below the shield is the year '1977'.

**First-class and high-order functions.
Lazy and eager evaluation**

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First-class functions

- May be called as a literal without an identifier. `(x: Int) => x * x`
- May be contained by a value. `val pow = (x: Int) => x * x`
- May be used as a parameter. `(f: Int => Int, x: Int) => f(x) * f(x)`
- May be used as a return value. `(x: Int) => (y: Int) => x + y`

Functions: def vs val

```
def pow(x: Int): Int = x * x
```



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Functions: def vs val

```
def pow(x: Int): Int = x * x
```

```
val a = pow _
```

```
pow(3) == a(3)
```

Instantiates
a function



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Functions: def vs val

```
val pow = (x: Int) => x * x
```

```
val a = pow
```

```
pow(3) == a(3)
```

The logo of Högskolan i Skövde is a circular emblem. It features a shield in the center with a stylized tree at the bottom, a bird in the middle, and two stars at the top. The shield is surrounded by a laurel wreath. Below the wreath, the year '1977' is inscribed.

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Functions: composition

```
val pow = (x: Int) => x * x
```

```
pow(pow(2)) // = 16
```

```
pow(pow(pow(2))) // = 256
```



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Functions: composition

```
val pow = (x: Int) => x * x
```

```
pow(pow(2)) == (pow andThen pow)(2) // = 16
```

```
pow(pow(pow(2))) = (pow andThen pow andThen pow)(2) // = 256
```

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Functions: composition

```
val pow = (x: Int) => x * x
```

```
val plus1 = (x: Int) => x + 1
```

```
(plus1 andThen pow) (2) // = pow(plus1(2)) = 9
```

```
(plus1 compose pow) (2) // = plus1(pow(2)) = 5
```

```
(plus1 andThen pow) (2) == (pow compose plus1) (2)
```


Functions: composition

```
val times = (x: Int) => (y: Int) => x * y
val add = (x: Int) => (y: Int) => x + y
val subtract = (x: Int) => (y: Int) => y - x

def myAge(shoeSize: Int, year: Int): Int =
  (subtract(year) compose
   (times(5) andThen
    add(50) andThen
    times(20) andThen
    add(1017))) (shoeSize)
```

First class and high-order functions

High-order

```
def sum(x: Int, f: Int => Int): Int =  
    f(x) + f(x)
```

```
def plus1(a: Int): Int = a + 1  
sum(2, plus1)
```

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First class and high-order functions

```
def sum(x: Int, f: Int => Int): Int =  
    f(x) + f(x)
```

```
val plus1 = (a: Int) => a + 1  
sum(2, plus1)
```

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First-class and high-order functions

```
def sum(x: Int, f: Int => Int): Int =  
    f(x) + f(x)
```

```
sum(2, (a: Int) => a + 1)
```

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First-class and high-order functions

```
def sum(x: Int, f: Int => Int): Int =  
    f(x) + f(x)
```

```
sum(2, a => a + 1)
```

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First-class and high-order functions

```
def sum(x: Int, f: Int => Int): Int =  
    f(x) + f(x)
```

```
sum(2, _ + 1)
```

Wildcard = Syntactic sugar



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First-class and high-order functions

```
def compose(x: Int, f: Int => Int): Int = f(f(x))
```

```
val square = (y: Int) => y * y
```

```
compose(2, square)
```

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First class and high-order functions

```
def compose(x: Int, f: Int => Int): Int = f(f(x))
```

```
val square = (y: Int) => y * y
```

```
compose(2, square)
```

```
compose(2, (y: Int) => y * y)(2)
```

```
compose(2, y => y * y)(2)
```

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First class and high-order functions

```
def compose(n: Int, x: Int, f: Int => Int): Int = ???
```

```
val square = (y: Int) => x * x
```

```
def compose(1, 2, square) // = square(2)
```

```
def compose(2, 2, square) // = square(square(2))
```

```
def compose(3, 2, square) // = square(square(square(2)))
```

First class and high-order functions

```
def square(l: List[Int]): List[Int] = l match {  
  case Nil => ???  
  case h :: t => ???  
}  
  
def map(l: List[Int], ???): List[Int] = l match {  
  case Nil => Nil  
  case h :: t => ???  
}
```

First class and high-order functions

```
def sum(l: List[Int]): Int = l match {  
  case Nil => ???  
  case h :: t => ???  
}  
  
def reduce(l: List[Int], ???): Int = l match {  
  case Nil => ???  
  case h :: t => ???  
}
```

First class and high-order functions

```
def squareAndSum(l: List[Int]): Int = l match {  
  case Nil => ???  
  case h :: t => ???  
}  
  
def mapReduce(l: List[Int], ???, ???): Int = l match {  
  case Nil => ???  
  case h :: t => ???  
}
```

First class and high-order functions

```
def add(x: Int): Int => Int =  
  n => n + x
```

```
val add2 = add(2)
```

```
val add3 = add(3)
```

```
add2(5) // = ???
```

```
add3(5) // = ???
```

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First class and high-order functions

```
def pow(n: Int): Int => Int =  
  if (n <= 1) x => x  
  else x => x * pow(n - 1)(x)
```

```
val pow1 = pow(1)
```

```
val pow2 = pow(2)
```

```
val pow3 = pow(3)
```

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First class and high-order functions

```
def compose(f: Int => Int): Int => Int =  
  n => f(f(n))
```

```
val square = (x: Int) => x * x  
compose(square)(2)
```

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First class and high-order functions

```
def compose(f: Int => Int, n: Int): Int => Int = ???
```

```
compose(x => x * x, 2)(2)
```

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Wildcards

```
def apply(x: Int, f: (Int, Int, Int) => Int): Int =  
    f(x, x, x)
```

```
apply(4, (a, b, c) => a + b * c)    // 4 + 4 * 4
```

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Wildcards

```
def apply(x: Int, f: (Int, Int, Int) => Int): Int =  
    f(x, x, x)
```

```
apply(4, _ * _ + _) // 4 + 4 * 4
```

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Wildcards

```
List(1, 2, 3, 4).filter(e => e % 2 == 0)
```

```
List(1, 2, 3, 4).filter(_ % 2 == 0)
```

```
List(1, 2, 3, 4).map(e => e.toString)
```

```
List(1, 2, 3, 4).map(_.toString)
```

```
List(1, 2, 3, 4).reduce((a, b) => a + b)
```

```
List(1, 2, 3, 4).reduce(_ + _)
```

Currying

"Any function of n parameters can be seen as a function that has a single parameter, and given it, it returns a function with $n - 1$ parameters"*

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*Torra, V. (2016). Scala: From a functional programming perspective: An introduction to the programming language (Vol. 9980). Springer.

Currying

"Any function of n parameters can be seen as a function that has a single parameter, and given it, it returns a function with $n - 1$ parameters"*

```
val foo = (a: Int, b: Int, c: Int) => a + b + c
```

*Torra, V. (2016). Scala: From a functional programming perspective: An introduction to the programming language (Vol. 9980). Springer.

Currying

"Any function of n parameters can be seen as a function that has a single parameter, and given it, it returns a function with $n - 1$ parameters"*

```
val foo = (a: Int) =>  
  (b: Int, c: Int) => a + b + c
```

*Torra, V. (2016). Scala: From a functional programming perspective: An introduction to the programming language (Vol. 9980). Springer.

Currying

"Any function of n parameters can be seen as a function that has a single parameter, and given it, it returns a function with $n - 1$ parameters"*

```
val foo = (a: Int) =>  
  (b: Int) =>  
    (c: Int) => a + b + c
```

*Torra, V. (2016). Scala: From a functional programming perspective: An introduction to the programming language (Vol. 9980). Springer.

Lazy and eager evaluation

```
val a = {  
  println("hello!")  
  "hello"  
}
```

```
def b = {  
  println("hello!")  
  "hello"  
}
```

```
lazy val c = {  
  println("hello!")  
  "hello"  
}
```

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Lazy and eager evaluation

Call-by-name

```
def pow2 (a: => Int): Int = a + a
```

```
pow2 ({println("I am lazy"); 5})
```

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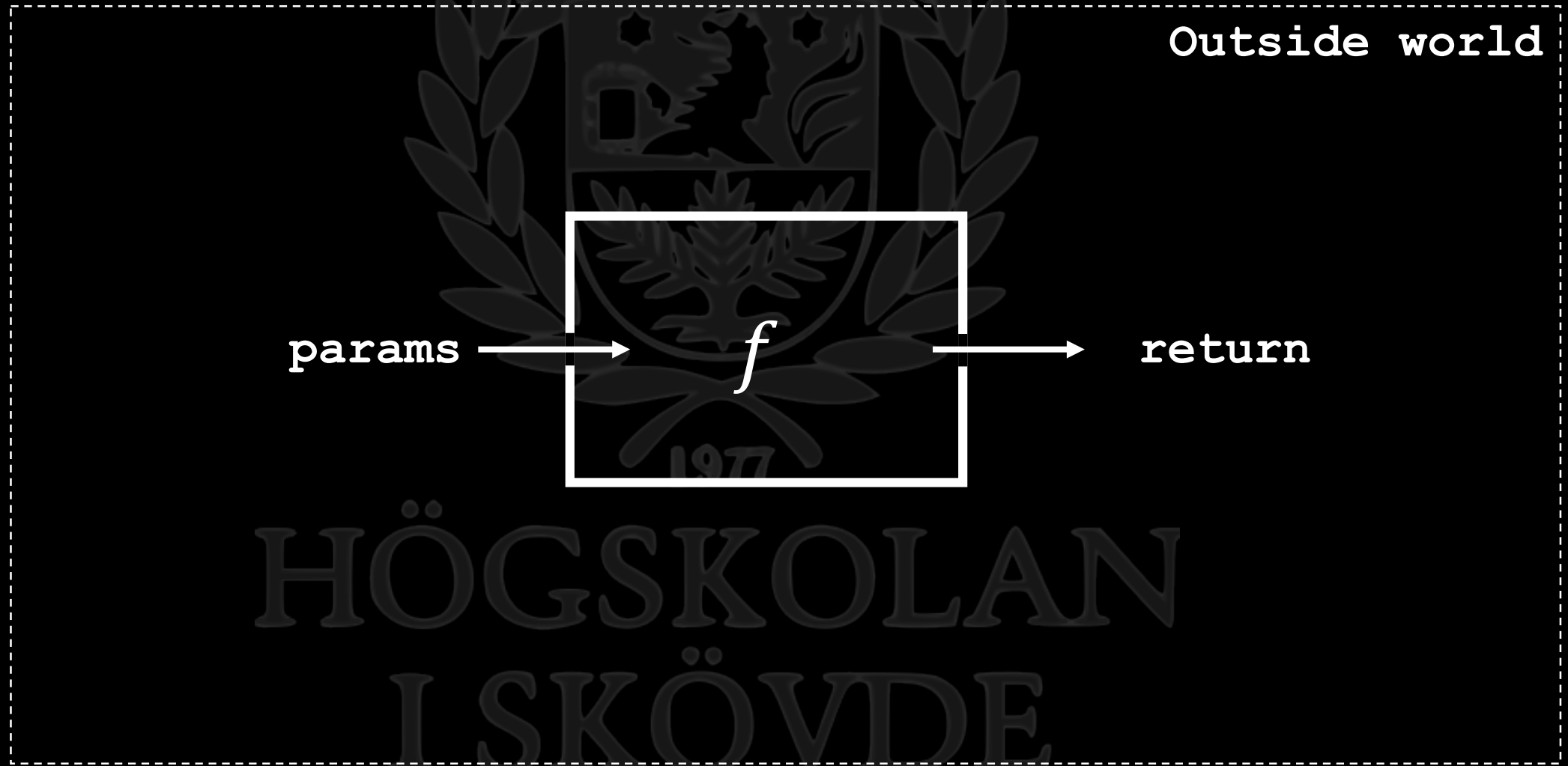
Lazy and eager evaluation

```
def eval(execute: Boolean, code: => Int): Int =  
  if (execute) code  
  else -1
```

```
eval(false, 5 / 0)
```

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Referential transparency



Referential transparency

"A property of functions that are independent of temporal context and have no side effects. For a particular input, an invocation of a referentially transparent function can be replaced by its result without changing the program semantics"*

"An expression e is referentially transparent with regard to a program p if every occurrence of e in p can be replaced by the result of evaluating e without affecting the meaning of p "**

*Odersky, M., Spoon, L., & Venners, B. (2010). Programming in Scala: A comprehensive step-by-step guide, Artima. Inc.,.

**Chiusano, P., & Bjarnason, R. (2014). Functional programming in Scala. Manning Publications Co..

No side effects + independent of context



A function does not
have any direct influence
on external states



A function is only influenced
by its parameters and not by
any other external state

```
var arr = Array(1, 2, 3)
def update(i: Int, x: Int) =
  arr(i) = x
```

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No side effects + independent of context



A function does not
have any direct influence
on external states



A function is only influenced
by its parameters and not by
any other external state

```
var arr = Array(1, 2, 3)
```

```
def update(i: Int, x: Int) =
```

```
arr(i) = x
```

```
def get(i: Int) =
```

```
arr(i)
```

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