



# Our Project

pricing simulation: mimics a market for selling airplane tickets

- goal: compare performance and time consumption of different methods
- implemented several DP methods to calculate optimal solution
- suitable for all stable baselines algorithms
- comprehensive monitoring to analyze pricing strategies and compare RL-based policies with the optimal one



monopoly scenario: agent vs customers

dynamic pricing

problem context:

time horizon: finite (→ take off)

action: price offer

demand: price and time-dependent

rewards: sales revenue

goal: maximize profits



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#### environment:

**state space:** (booking time, current occupancy)

 $(0, 12) \rightarrow (10, 0)$ 

action space: discrete (0, 1, .., 20)

event: tickets sold per step (0, 10)

reward: action \* event (no final reward)

$$p = \left(1 - \frac{a}{20}\right) * (1+t)/T$$

demand: Binomial(10, k, p)

episode: one booking period



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MDP

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### What would a good policy look like?



### A simulation scenario

- optimal solution (full knowledge)
  - → calculated by dynamic programming
- approximate DP solution
- RL solution (limited knowledge)
  - Q-Learning (Ir=0.8, eps=0.5)
  - DQN, DDPG, TD3, A2C, SAC, PPO (default stable baselines parameters)
- setup: training 100, 500 and 1000 episodes per method (n=5)
- evaluation: policy, cumulated reward, initial value of policy



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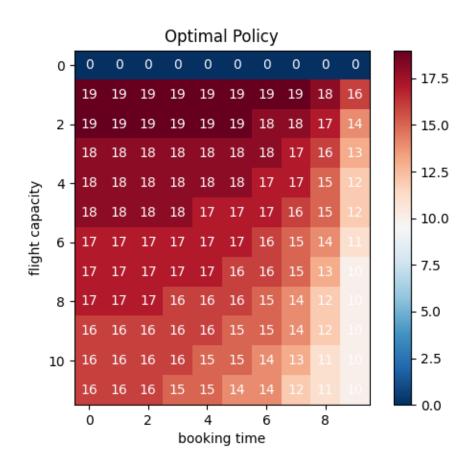
demand: Binomial(10, k, p)

episode: one booking period



### A simulation scenario – optimal policy



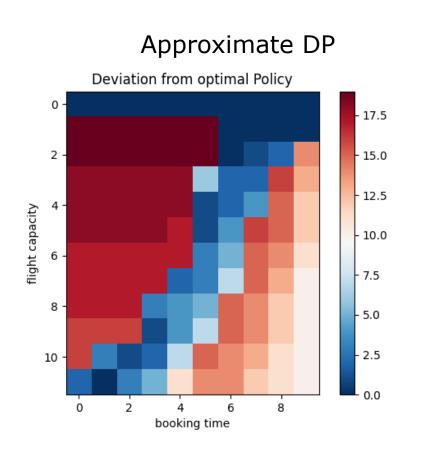


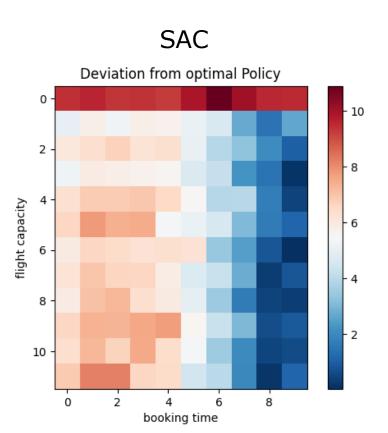
Backward Induction: 0.577s, Policy Iteration: 4.637s, Value Iteration: 6.487s

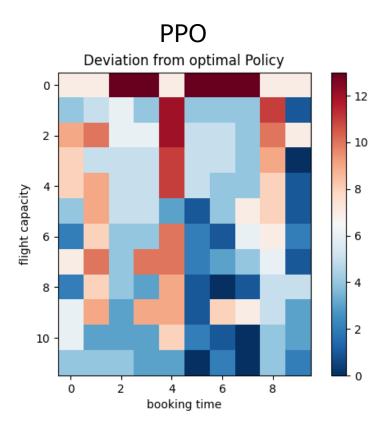


# A simulation scenario – selected policies based on limited knowledge

After 100 Training Episodes



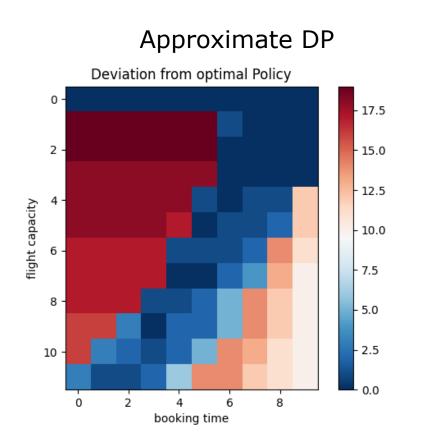


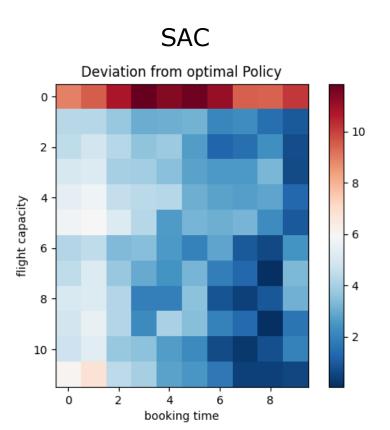


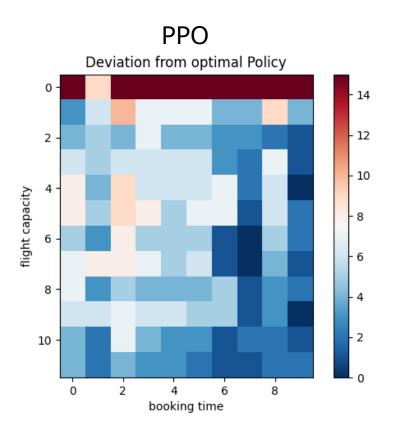


# A simulation scenario – selected policies based on limited knowledge

After 500 Training Episodes



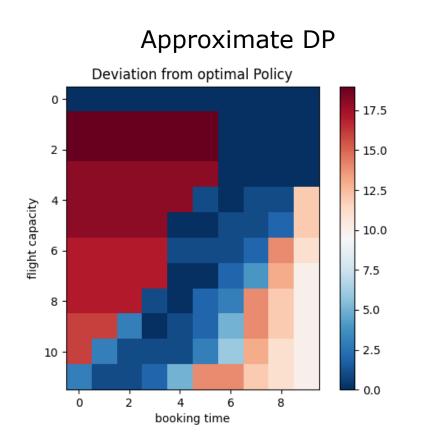


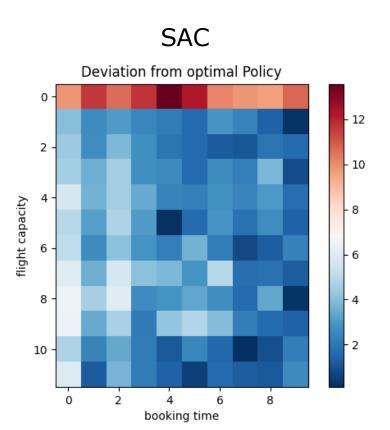


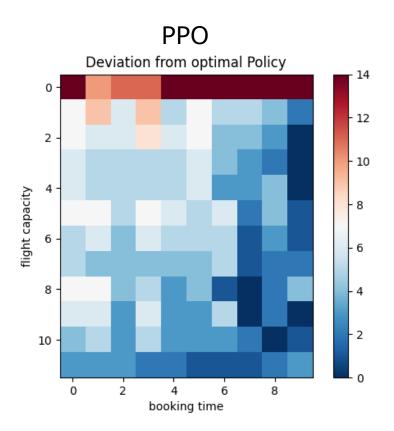


### A simulation scenario – selected policies based on limited knowledge

After 500 Training Episodes

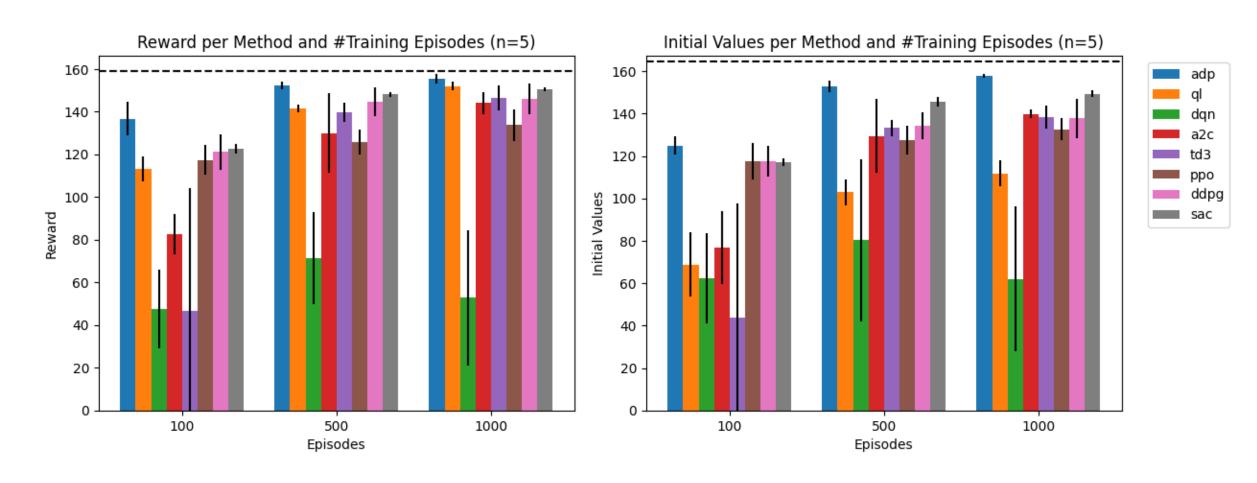








### A simulation scenario – total rewards





# Outlook

- more complex customer behavior (various customer types)
- agent predicts demand based on historical data (regressive)
- multidimensional state space to support multiple flights
  (demand substitution effects)
- introduce competition to agent

What do you think is the most interesting direction?





