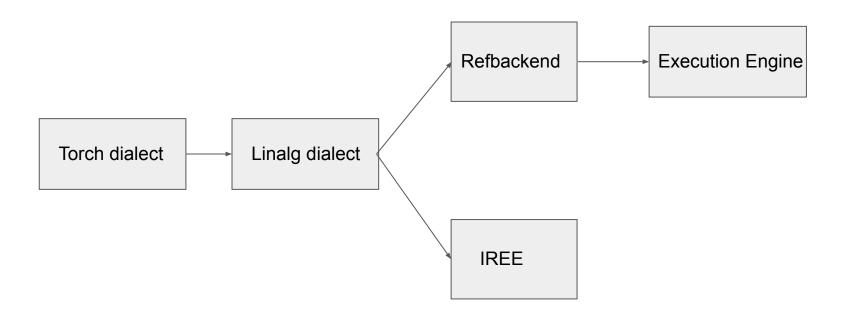
## Anatomy of Linalg.generic

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### End to End Torch Module Execution



### Linalg ops overview

Linalg defines payload carrying operations which implement the **<u>structured</u>** ops.

- Structure ops carry out computations on tensor or buffers like contractions or convolutions.
- Can be further lowered to loops or to affine expressions with computation in the loop body.

### Linalg ops overview

Linalg defines a small set of commonly used named ops

linalg-generalize-named-ops

Named Ops — Linalg.generic Ops

linalg.conv

linalg.batch\_matmul

linalg.pooling

### Example tensor operation

perform a sum reduction along the H,W dimensions of a tensor<NxCxHxW>, resulting in a tensor<NxC>.

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perform a sum reduction along the H,W dimensions of a tensor<NxCxHxW>, resulting in a tensor<NxC>.

```
%6 = linalq.generic {
   indexing maps =
            [affine map<(d0, d1, d2, d3) \rightarrow (d0, d1, d2, d3)]
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", " reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
                                                                    compute payload
      ^bb0(%arg1: f32, %arg2: f32): // no predecessors
          %17 = arith.addf %arg2, %arg1 : f32
          linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

### Components of a generic op

- iterator types
- indexing maps
- input/output tensors
- compute payload

### Iterator types

```
%6 = linalg.generic {
   indexing maps =
           [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
         %17 = arith.addf %arg2, %arg1 : f32
         linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

```
for d0 := ...
for d1 := ...
for d2 := ...
for d3 := ...
```

### Iterator types

```
SmallVector<StringRef, 4> iteratorTypesSum{"parallel", "parallel",
                                                          "reduction", "reduction"};
%6 = linalg.generic {
   indexing maps =
           [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
           affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
         %17 = arith.addf %arg2, %arg1 : f32
         linalg.yield %17 : f32
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```

```
%6 = linalg.generic {
   indexing maps =
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            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1: tensor<?x?x?x?xf32>) outs(%5: tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
         %17 = arith.addf %arg2, %arg1 : f32
         linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

```
affine_map<(d0, d1, d2, d3) -> (d1+1, 2*d2, d3)>

for d0 := ...

for d1 := ...

for d2 := ...

for d3 := ...
```

The left hand side are the induction variables for each nested loops

```
affine_map<(d0, d1, d2, d3) -> (d1+1, 2*d2, d3)>

for d0 := ...

for d1 := ...

for d2 := ...

for d3 := ...
```

```
affine_map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>
                       for d0 := ...
                         for d1 := ...
                          for d2 := ...
                            for d3 := ...
                       a[d0][d1][d2][d3]
affine map<(d0, d1, d2, d3) \rightarrow (d0, d1)>
                        for d0 := ...
                          for d1 := ...
                           for d2 := ...
                             for d3 := ...
                        b[d0][d1]
```

identity map

```
affine_map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>
```

#### input

```
for d0 := ...
for d1 := ...
for d2 := ...
for d3 := ...
```

a[d0][d1][d2][d3]

```
affine_map<(d0, d1, d2, d3) -> (d0, d1)>
```

#### output

```
for d0 := ...
for d1 := ...
for d2 := ...
for d3 := ...
```

b[d0][d1]

## accumulated sum of the inner two dimension:

b[d0][d1] += a[d0][d1][d2][d3]

```
affine_map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>
```

#### output

```
for d0 := ...
for d1 := ...
for d2 := ...
for d3 := ...
```

a[d0][d1][d2][d3]

```
affine_map<(d0, d1, d2, d3) -> (d0, d1)>
```

#### input

```
for d0 := ...
for d1 := ...
for d2 := ...
for d3 := ...
```

b[d0][d1]

#### broadcast the 2 dimensions:

a[d0][d1][d2][d3] = b[d0][d1]

```
affine_map<(d0, d1) -> (d1, d0)>
```

#### input

```
for d0 := ...
for d1 := ...
```

a[d1][d0]

```
affine_map<(d0, d1) -> (d0, d1)>
```

for d0 := ...

for d1 := ...

#### output

#### transpose the input:

b[d0][d1] = a[d1][d0]

```
SmallVector<AffineExpr, 2> ncExprs;
                               ncExprs.push_back(mlir::getAffineDimExpr(0, context));
                               ncExprs.push_back(mlir::getAffineDimExpr(1, context));
                               auto ncIndexingMap = AffineMap::get(
                               SmallVector<AffineMap, 2> indexingMaps = {
                                   rewriter.getMultiDimIdentityMap(4), // input
                                   ncIndexingMap,
%6 = linalg.generic {
   indexing maps =
            [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
          %17 = arith.addf %arg2, %arg1 : f32
          linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

```
SmallVector<AffineExpr, 2> ncExprs;
                              ncExprs.push_back(mlir::getAffineDimExpr(0, context));
                              ncExprs.push_back(mlir::getAffineDimExpr(1, context));
                               auto ncIndexingMap = AffineMap::get(
                                  /*symbolCount=*/0, ncExprs, context);
                              SmallVector<AffineMap. 2> indexingMaps =
                                  rewriter.getMultiDimIdentityMap(4), // input
%6 = linalg.generic {
   indexing maps =
           [affine_map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
            affine map<(d0, d1, d2, d3) -> (d0, d1)>1.
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
         %17 = arith.addf %arg2, %arg1 : f32
         linalg.yield %17 : f32
    } -> tensor<?x?xf32>
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```
SmallVector<AffineExpr, 2> ncExprs;
                               ncExprs.push_back(mlir::getAffineDimExpr(1, context));
                               auto ncIndexingMap = AffineMap::get(
                                   /*svmbolCount=*/0. ncExprs. context):
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                                   rewriter.getMultiDimIdentityMap(4), // input
                                   ncIndexingMap,
%6 = linalg.generic {
   indexing maps =
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   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
          %17 = arith.addf %arg2, %arg1 : f32
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```

```
SmallVector<AffineEvnr 2> ncEvnrs
                               ncExprs.push_back(mlir::getAffineDimExpr(0, context));
                               auto ncIndexingMap = AffineMap::get(
                                   /*symbolCount=*/0, ncExprs, context);
                               SmallVector<AffineMap, 2> indexingMaps = {
                                   rewriter.getMultiDimIdentityMap(4), // input
                                   ncIndexingMap,
%6 = linalg.generic {
   indexing maps =
            [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1)>1.
   iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
          %17 = arith.addf %arg2, %arg1 : f32
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```

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```
SmallVector<AffineExpr, 2> ncExprs;
                            ncExprs.push_back(mlir::getAffineDimExpr(1, context));
                            auto ncindexingmap = Attinemap::get(
                                /*symbolCount=*/0, ncExprs, context);
                            SmallVector<AffineMap, 2> indexingMaps = {
                                rewriter.getMultiDimIdentityMap(4), // input
                                ncIndexingMap,
        [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
         affine map<(d0, d1, d2, d3) \rightarrow (d0, d1)>1.
iterator types = ["parallel", "parallel", "reduction", "reduction"]}
ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
  ^bb0(%arg1: f32, %arg2: f32): // no predecessors
      %17 = arith.addf %arg2, %arg1 : f32
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indexing maps =

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                                ncIndexingMap,
        [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
         affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
iterator types = ["parallel", "parallel", "reduction", "reduction"]}
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      %17 = arith.addf %arg2, %arg1 : f32
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SmallVector<AffineExpr, 2> ncExprs;
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%6 = linalg.generic {
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            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
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          %17 = arith.addf %arg2, %arg1 : f32
          linalg.yield %17 : f32
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```
%6 = linalg.generic {
   indexing maps =
           [affine map<(d0, d1, d2, d3) \rightarrow (d0, d1, d2, d3)]
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                                                                  compute payload
          %17 = arith.addf %arg2, %arg1 : f32
          linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

- Define the iteration space
  - decide the bounds of induction variables

- Define the iteration space
  - decide the bounds of induction variables
- output operands
  - shape-only tensor: decide the Linalg operation result shape

```
ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
    ^bb0(%arg1: f32, %arg2: f32): // no predecessors
        %17 = "some operation" %arg1 : f32
        linalg.yield %17 : f32
} -> tensor<?x?xf32>
```

- Define the iteration space
  - decide the bounds of induction variables
- output operands
  - shape-only tensor: decide the Linalg operation result shape
  - init tensor: used for destructive update

```
ins(%1 : tensor<?x?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
    ^bb0(%arg1: f32, %arg2: f32): // no predecessors
        %17 = arith.addf %arg2, %arg1 : f32
        linalg.yield %17 : f32
    } -> tensor<?x?xf32>
    out[d0][d1] += in[d0][d1][d2][d3]
```

```
%6 = linalg.generic {
   indexing maps =
           [affine map<(d0, d1, d2, d3) \rightarrow (d0, d1, d2, d3)]
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                                                                  compute payload
          %17 = arith.addf %arg2, %arg1 : f32
          linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

```
%6 = linalg.generic {
   indexing_maps =
           [affine map<(d0, d1, d2, d3) \rightarrow (d0, d1, d2, d3)]
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                                                                  compute payload
          %17 = arith.addf %arg2, %arg1 : f32
          linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

```
[&](OpBuilder &b, Location loc, ValueRange args) {
                           Value input = args[0], sum = args[1];
                           Value result = rewriter.create<arith::AddF0p>(
                               loc, sum, input);
                           b.create<linalg::YieldOp>(loc, result);
%6 = linalg.generic {
   indexing maps =
           [affine map<(d0, d1, d2, d3) \rightarrow (d0, d1, d2, d3)]
           affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                                                             compute payload
         %17 = arith.addf %arg2, %arg1 : f32
         linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

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%6 = linalg.generic {
   indexing maps =
           [affine map<(d0, d1, d2, d3) \rightarrow (d0, d1, d2, d3)]
            affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
   iterator types = ["parallel", "parallel", "reduction", "reduction"]}
   ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
     ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                                                                  linalg.index 0 == d0
                                                                  linalg.index 1 == d1
          linalg.index dim: index
    } -> tensor<?x?xf32>
```

```
indexing maps =
                    [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
                     affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
            iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
            ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
               ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                   %17 = arith.addf %arg2, %arg1 : f32
                   linalg.yield %17 : f32
            } -> tensor<?x?xf32>
Value sumPool2d = rewriter
                       .create<linalg::GenericOp>(
                           loc, initTensor0.getType(),
                           /*inputs=*/input, /*outputs=*/initTensor0,
                           /*indexingMaps=*/indexingMaps,
                           /*iteratorTypes=*/iteratorTypesSum,
                           [&](OpBuilder &b, Location loc, ValueRange args)
                             Value input = args[0], sum = args[1];
                             Value result = rewriter.create<arith::AddFOp>(
                                 loc, sum, input);
                             b.create<linalg::YieldOp>(loc, result);
                          })
                       .getResult(0);
```

```
indexing_maps =
                    [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
                     affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
            iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
            ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
               ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                   %17 = arith.addf %arg2, %arg1 : f32
                   linalg.yield %17 : f32
            } -> tensor<?x?xf32>
Value sumPool2d = rewriter
                       .create<linalg::GenericOp>(
                           loc, initTensor0.getType(),
                          /*inputs=*/input. /*outputs=*/initTensor0,
                          /*indexingMaps=*/indexingMaps,
                          /*iteratorTypes=*/iteratorTypesSum,
                           [&](OpBuilder &b, Location loc, ValueRange args)
                             Value input = args[0], sum = args[1];
                             Value result = rewriter.create<arith::AddFOp>(
                                 loc, sum, input);
                             b.create<linalg::YieldOp>(loc, result);
                          })
```

```
indexing maps =
                    [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
                     affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
            iterator types = ["parallel", "parallel", "reduction", "reduction"]}
            ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
               ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                   %17 = arith.addf %arg2, %arg1 : f32
                   linalg.yield %17 : f32
            } -> tensor<?x?xf32>
Value sumPool2d = rewriter
                       .create<linalg::GenericOp>(
                           loc, initTensor0.getType(),
                           /*inputs=*/input, /*outputs=*/initTensor0,
                            *indexingMaps=*/indexingMaps,
                           /*iteratorTypes=*/iteratorTypesSum,
                           [&](OpBuilder &b, Location loc, ValueRange args)
                             Value input = args[0], sum = args[1];
                             Value result = rewriter.create<arith::AddFOp>(
                                 loc, sum, input);
                             b.create<linalg::YieldOp>(loc, result);
                       .getResult(0);
```

```
indexing maps =
                    [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
                     affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
            iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
            ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
               ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                   %17 = arith.addf %arg2, %arg1 : f32
                   linalg.yield %17 : f32
            } -> tensor<?x?xf32>
Value sumPool2d = rewriter
                       .create<linalg::GenericOp>(
                           loc, initTensor0.getType()
                           /*inputs=*/input, /*outputs=*/initTensor0,
                           /*indexingMaps=*/indexingMaps,
                           /*iteratorTypes=*/iteratorTypesSum,
                           [&](OpBuilder &b, Location loc, ValueRange args)
                             Value input = args[0], sum = args[1];
                             Value result = rewriter.create<arith::AddFOp>(
                                 loc, sum, input);
                             b.create<linalg::YieldOp>(loc, result);
                           })
```

```
indexing maps =
                    [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
                     affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
            iterator_types = ["parallel", "parallel", "reduction", "reduction"]}
            ins(%1 : tensor<?x?x?x?xf32>) outs(%5 : tensor<?x?xf32>) {
               ^bb0(%arg1: f32, %arg2: f32): // no predecessors
                   %17 = arith.addf %arg2, %arg1 : f32
                   linalg.yield %17 : f32
            } -> tensor<?x?xf32>
Value sumPool2d = rewriter
                       .create<linalg::GenericOp>(
                           loc, initTensor0.getType(),
                           /*inputs=*/input, /*outputs=*/initTensor0,
                           /*indexingMaps=*/indexingMaps,
                           /*iteratorTypes=*/iteratorTypesSum,
                          [&](OpBuilder &b, Location loc, ValueRange args)
                             Value input = args[0], sum = args[1];
                             Value result = rewriter.create<arith::AddFOp>(
                                 loc, sum, input);
                             b.create<linalg::YieldOp>(loc, result);
                       .getResult(0);
```

```
%6 = linalg.generic {
    indexing maps =
            [affine map<(d0, d1, d2, d3) -> (d0, d1, d2, d3)>,
             affine map<(d0, d1, d2, d3) \rightarrow (d0, d1),
    iterator types = ["parallel", "parallel", "reduction", "reduction"]}
    ins(%1: tensor<?x?x?x?xf32>) outs(%5: tensor<?x?xf32>) {
      ^bb0(%arg1: f32, %arg2: f32): // no predecessors
           %17 = arith.addf %arg2, %arg1 : f32
           linalg.yield %17 : f32
    } -> tensor<?x?xf32>
```

```
Value \mathbb{N} = \text{getDimOp}(\text{rewriter}, \text{loc}, \text{input}, 0);
Value c0 = rewriter.create<arith::ConstantOp>(
Value initTensor0 =
SmallVector<StringRef, 4> iteratorTypesSum{"parallel", "parallel",
Value sumPool2d = rewriter
                             [&](OpBuilder &b, Location loc, ValueRange args)
                               Value result = rewriter.create<arith::AddFOp>(
                               b.create<linalg::YieldOp>(loc. result):
```

tensor operation:

perform a sum reduction along the H,W dimensions of a tensor<NxCxHxW>, resulting in a tensor<NxC>.

# Thank you!