

# INTRODUCTION TO LOGISTIC REGRESSION

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# INTRODUCTION TO LOGISTIC REGRESSION

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## LEARNING OBJECTIVES

- ▶ Build a Logistic regression classification model using the sklearn library
- ▶ Describe a sigmoid function, odds, and the odds ratio as well as how they relate to logistic regression
- ▶ Evaluate a model using metrics such as accuracy, precision, and recall.

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## PRE-WORK REVIEW

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- ▶ Implement a linear model (LinearRegression) with sklearn
- ▶ Understand what a coefficient is
- ▶ Recall metrics such as accuracy and misclassification
- ▶ Recall the differences between L1 and L2 regularization

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**OPENING**

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# INTRODUCTION TO LOGISTIC REGRESSION

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## ANSWER THE FOLLOWING QUESTIONS

Read through the following questions and brainstorm answers for each:

1. What are the main differences between linear and KNN models? What is different about how they approach solving the problem?
  - a. For example, what is *interpretable* about linear regression compared to what's *interpretable* in KNN?
1. What would be the advantage of using a linear model like linear regression to solve a classification problem, compared to KNN?
  - a. What are some challenges for using linear regression to solve a classification problem (say, if the values were either 1 or 0)?



EXERCISE

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## INTRODUCTION

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# LOGISTIC REGRESSION

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# LOGISTIC REGRESSION

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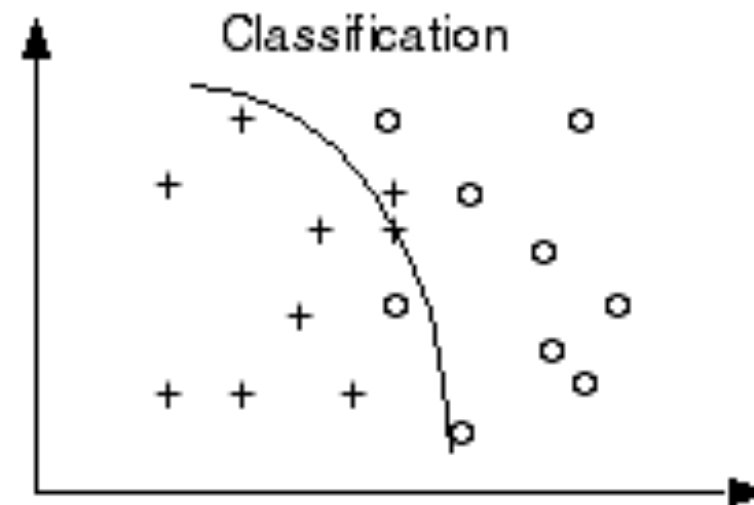
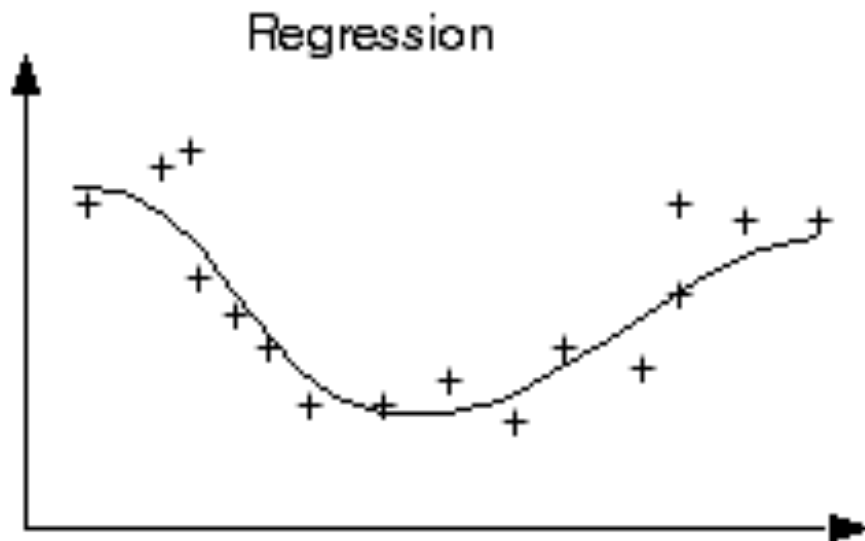
- ▶ Logistic regression is a *linear* approach to solving a *classification* problem.
- ▶ That is, we can use a linear model, similar to Linear regression, in order to solve if an item *belongs* or *does not belong* to a class label.

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# CHALLENGE! LINEAR REGRESSION RESULTS FOR CLASSIFICATION

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- ▶ Regression results can have a value range from  $-\infty$  to  $\infty$ .
- ▶ Classification is used when predicted values (i.e. class labels) are not greater than or less than each other.





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# CHALLENGE! LINEAR REGRESSION RESULTS FOR CLASSIFICATION

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- ▶ But, since most classification problems are binary (0 or 1) and 1 is greater than 0, does it make sense to apply the concept of regression to solve classification?
- ▶ How might we contain those bounds?
- ▶ Let's review some approaches to make classification with regression feasible.

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## **FIX 1: PROBABILITY**

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- ▶ One approach is predicting the probability that an observation belongs to a certain class.

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## **FIX 1: PROBABILITY**

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- ▶ For example, suppose we know that roughly 700 of 2200 people from the Titanic survived. Without knowing anything about the passengers or crew, the probability of survival would be  $\sim 0.32$  (32%).
- ▶ However, we still need a way to use a linear function to either increase or decrease the probability of an observation given the data about it.

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## **FIX 2: LINK FUNCTIONS AND THE SIGMOID FUNCTION**

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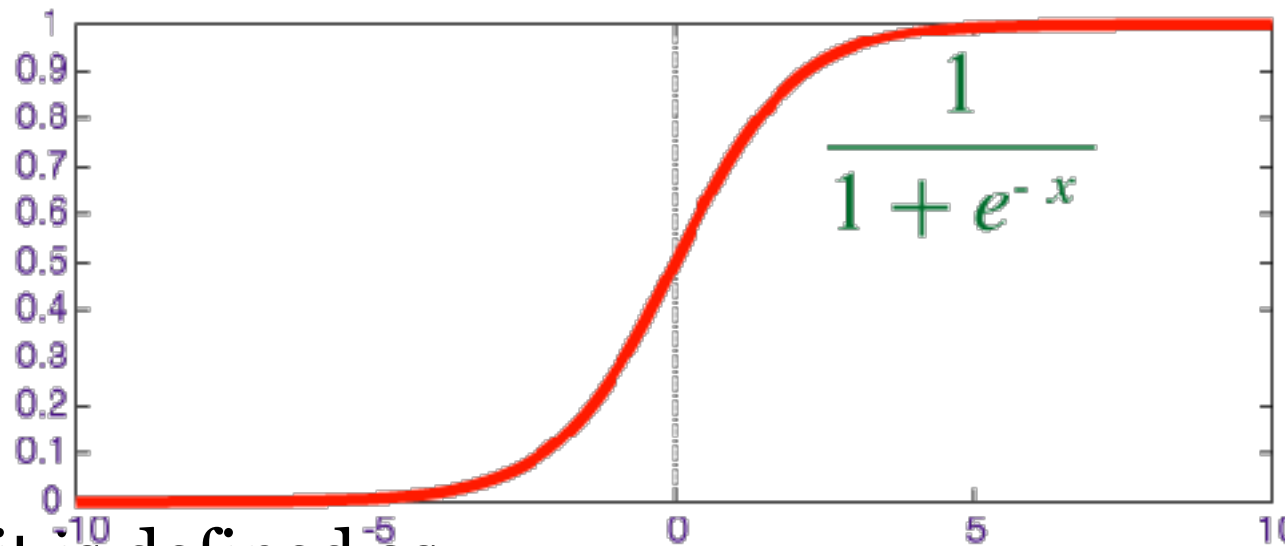
- ▶ We can use a linear model *like* linear regression to output regression *like* values, then convert them into probabilities for classification
- ▶ We use a link function to turn linear regression into something that can be used for classification

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## FIX 2: LINK FUNCTIONS AND THE SIGMOID FUNCTION

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- ▶ A *sigmoid function* is a function that visually looks like an s.



- ▶ Mathematically, it is defined as

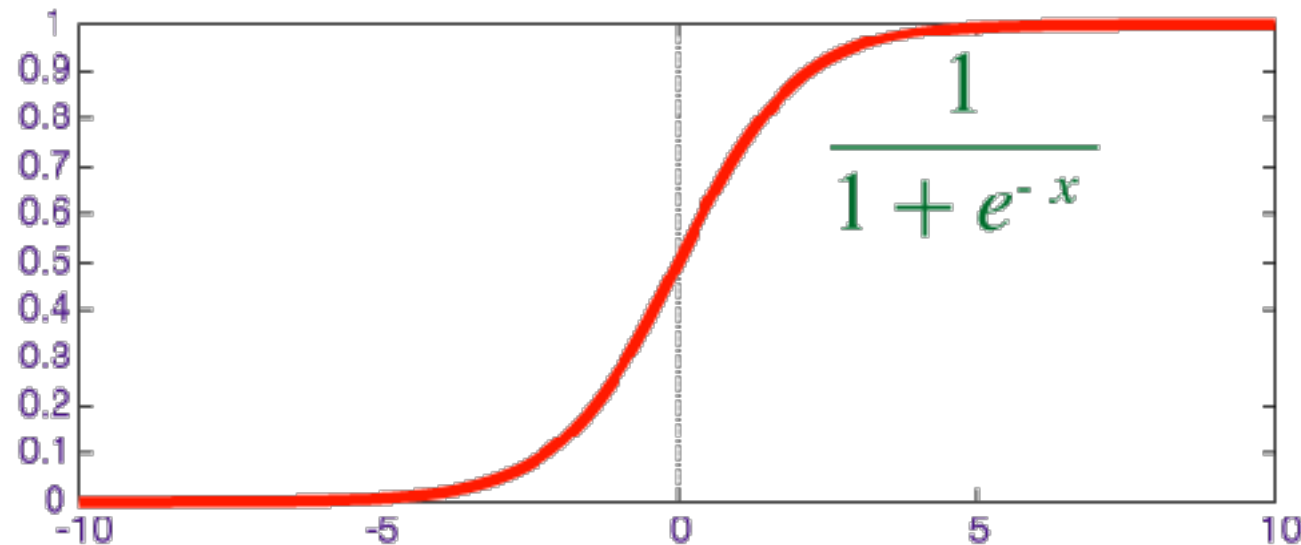
$$f(x) = \frac{1}{1 + e^{-x}}$$

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## FIX 2: LINK FUNCTIONS AND THE SIGMOID FUNCTION

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- ▶ As  $x$  increases, the results is closer to 1. As  $x$  decreases, the result is closer to 0.
- ▶ When  $x = 0$ , the result is 0.5.

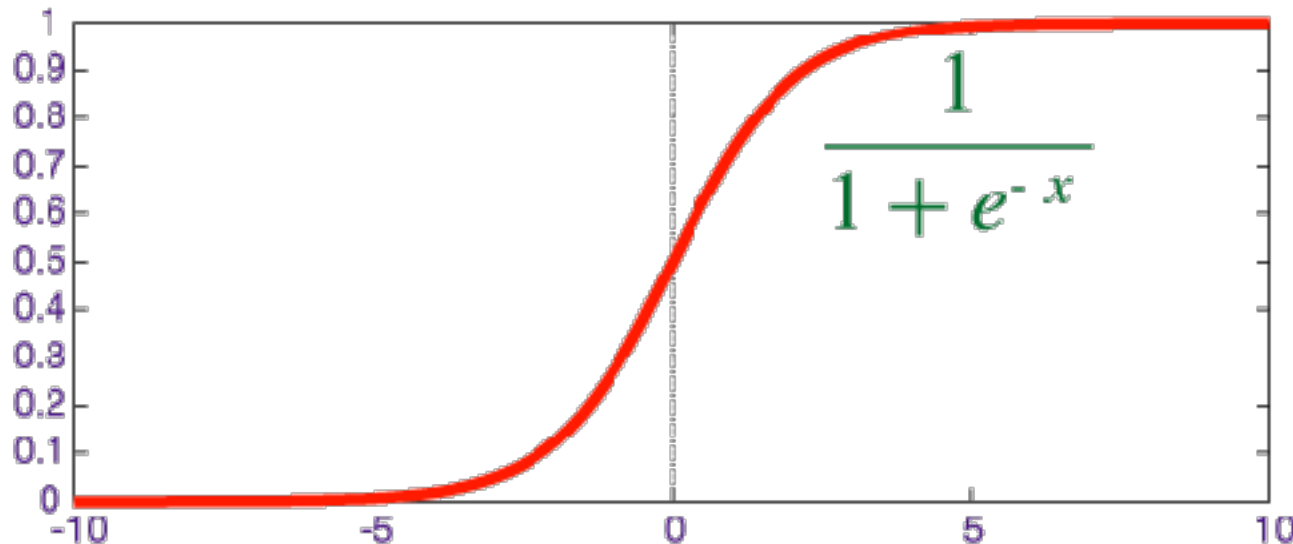


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## FIX 2: LINK FUNCTIONS AND THE SIGMOID FUNCTION

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- ▶ Since  $x$  decides how to much to increase or decrease the value away from 0.5,  $x$  can be interpreted as something like a coefficient.
- ▶  $X$ , here is the value a linear regression would output. Something between negative infinity and infinity



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**DEMO**

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# PLOTTING A SIGMOID FUNCTION



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## Learning check

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- ▶ *Why is sigmoid well suited to turning numbers into a probabilities, especially for binary classification?*

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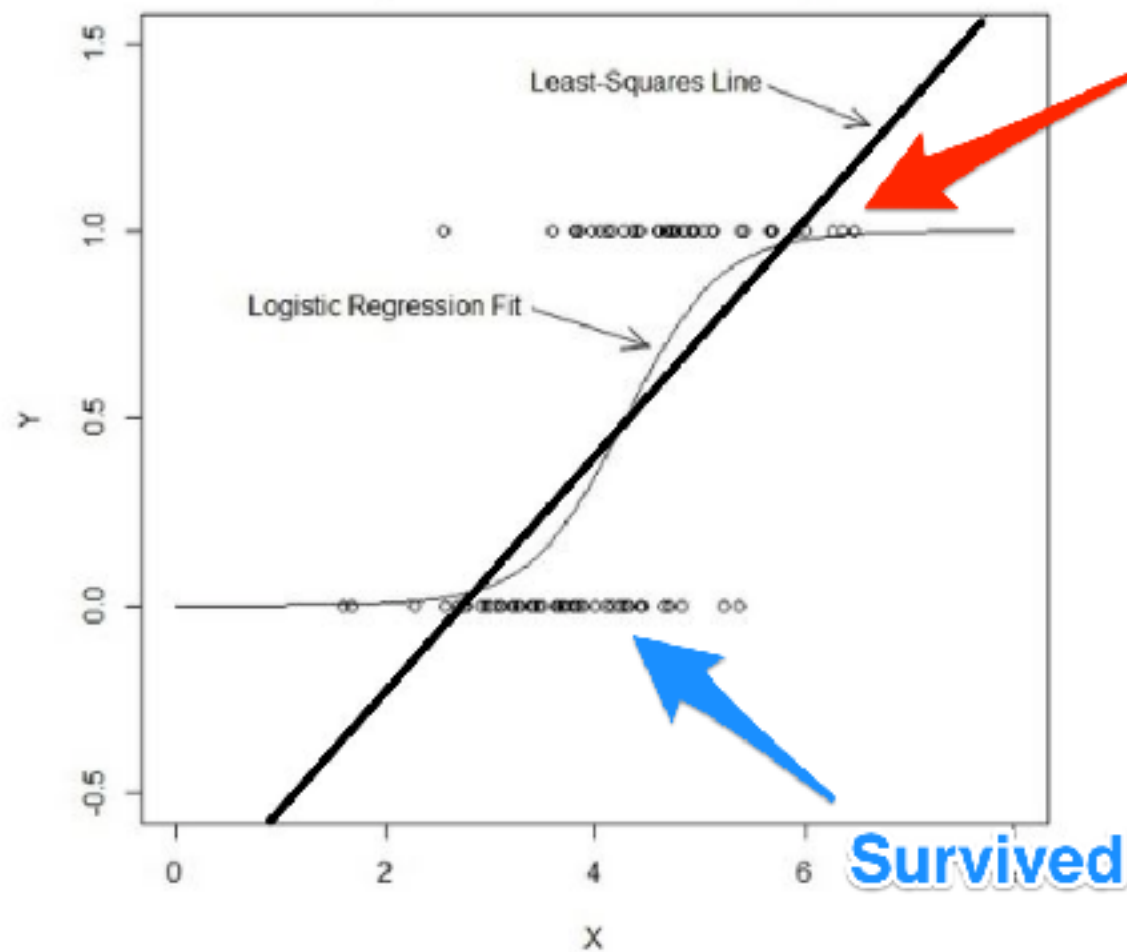
## **FIX 3: ODDS AND LOG-ODDS**

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- ▶ The logit function allows for values between  $-\infty$  and  $\infty$ , but provides us probabilities between 0 and 1.

## FIX 3: ODDS AND LOG-ODDS

### Titanic prediction



- What does that straight, best-fit linear regression-like line represent in terms of classification?

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## FIX 3: ODDS AND LOG-ODDS

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- ▶ While the logit value represents the *coefficients* in the logistic function, we can convert them into odds ratios that make them more easily interpretable.

$$\boxed{\ln\left(\frac{P}{1-P}\right)} = \beta_0 + \beta_1 X_1$$

Log odds



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## FIX 3: ODDS AND LOG-ODDS

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- ▶ While the logit value represents the *coefficients* in the logistic function, we can convert them into odds ratios that make them more easily interpretable.

Odds

$$\ln\left(\frac{P}{1-P}\right) = \beta_0 + \beta_1 X_1$$

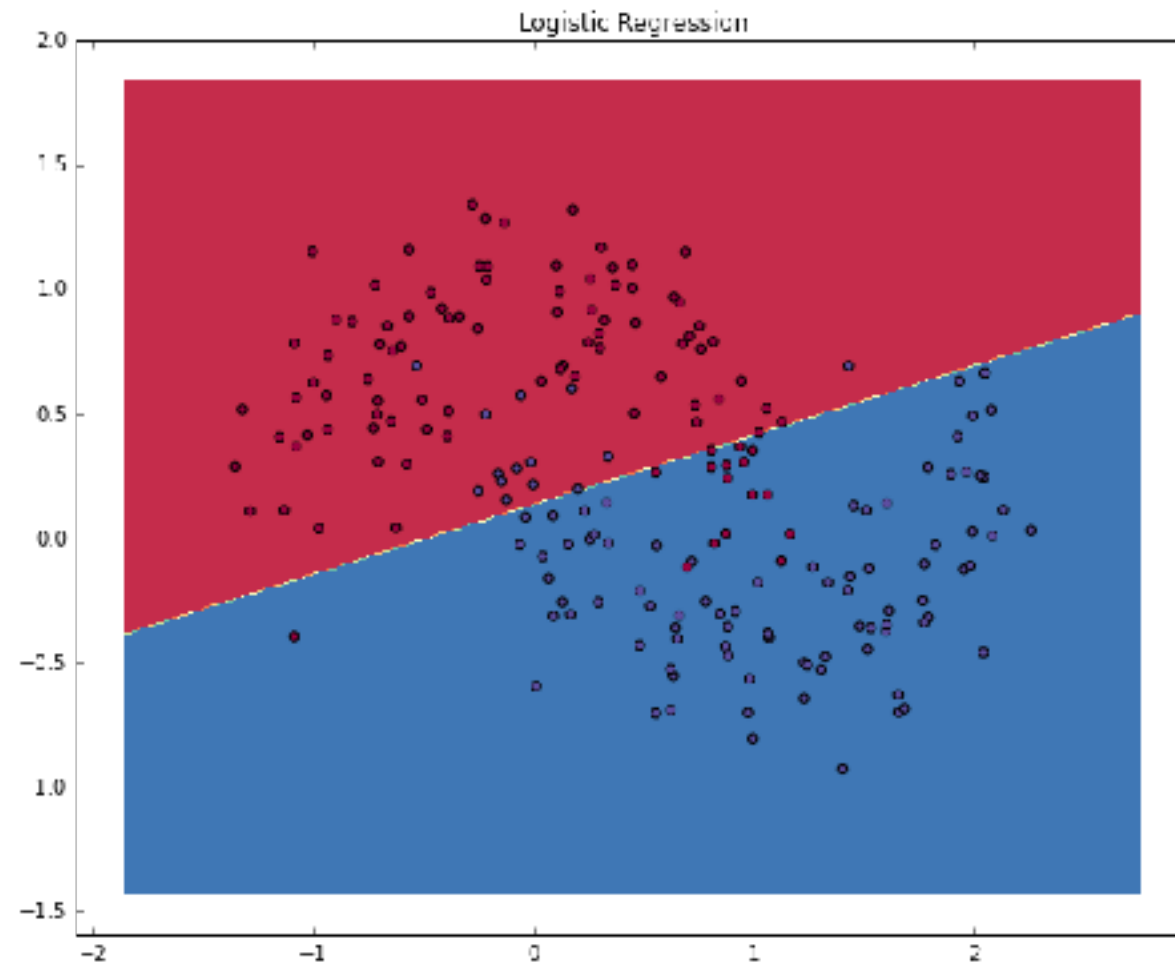
- ▶ So how do we interpret the B1 coefficient? What can we use from what we know about linear regression?

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## FIX 3: ODDS AND LOG-ODDS

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- ▶ With these coefficients, we get our overall probability: the logistic regression draws a linear *decision line* which divides the classes.



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## GUIDED PRACTICE

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**WAGER THOSE  
ODDS!**

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# ACTIVITY: WAGER THOSE ODDS!

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## EXERCISE

### DIRECTIONS (15 minutes)

1. Convert these odds ratios into probability that the favored team wins. Remember the formula for odds, you are going to have to invert it.
  - a. Stanford : Iowa, 5:1
  - b. Alabama : Michigan State, 20:1
  - c. Clemson : Oklahoma, 1.1:1
  - d. Houston : Florida State, 1.8:1
  - e. Ohio State : Notre Dame, 1.6:1

### DELIVERABLE

The desired probabilities



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## INDEPENDENT PRACTICE

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# Logistic Regression in sklearn

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## INTRODUCTION

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# ADVANCED CLASSIFICATION METRICS

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# ADVANCED CLASSIFICATION METRICS

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- ▶ Was it wrong across all labels?
- ▶ Did it just guess one class label for all predictions?
- ▶ It's important to look at other metrics to fully understand the problem.

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# ADVANCED CLASSIFICATION METRICS

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- ▶ We can split up the accuracy of each label by using the *true positive rate* and the *false positive rate*.
- ▶ For each label, we can put it into the category of a true positive, false positive, true negative, or false negative.

		<u>True class</u>	
		<b>p</b>	<b>n</b>
<u>Hypothesized class</u>	<b>Y</b>	True Positives	False Positives
	<b>N</b>	False Negatives	True Negatives
Column totals:		<b>P</b>	<b>N</b>

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# ADVANCED CLASSIFICATION METRICS

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- ▶ **Precision:** “Of everything we classified as positive, what percentage were actually positive”
- ▶ A very precise model doesn’t have many false positives.
- ▶ What situations would you care about a model’s precision?

		<u>True class</u>	
		<b>p</b>	<b>n</b>
<u>Hypothesized class</u>	<b>Y</b>	True Positives	False Positives
	<b>N</b>	False Negatives	True Negatives
Column totals:		<b>P</b>	<b>N</b>

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# ADVANCED CLASSIFICATION METRICS

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- ▶ **Recall:** “Of everything that is *actually positive*, how many did you successfully classify as positive
- ▶ A model with high recall doesn't make false negatives
- ▶ What situations would you care about a model's recall?

		<u>True class</u>	
		<b>p</b>	<b>n</b>
<u>Hypothesized class</u>	<b>Y</b>	True Positives	False Positives
	<b>N</b>	False Negatives	True Negatives
Column totals:		<b>P</b>	<b>N</b>

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## ADVANCED CLASSIFICATION METRICS

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- ▶ A good classifier would have a true positive rate approaching 1 and a false positive rate approaching 0.
- ▶ In our smoking problem, this model would accurately predict *all* of the smokers as smokers and not accidentally predict any of the nonsmokers as smokers.

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## GUIDED PRACTICE

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WHICH METRIC  
SHOULD I USE?



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# ACTIVITY: WHICH METRIC SHOULD I USE?

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## DIRECTIONS (15 minutes)

### Examples:

1. A test is developed for determining if a patient has cancer or not.
2. A newspaper company is targeting a marketing campaign for "at risk" users that may stop paying for the product soon.
3. You build a spam classifier for your email system.

### DELIVERABLE

Answers for each example



EXERCISE

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**CONCLUSION**

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**TOPIC REVIEW**

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## REVIEW QUESTIONS

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- ▶ How is logistic regression different than linear regression?
- ▶ What kind of machine learning problems does logistic regression address?
- ▶ What do the *coefficients* in a logistic regression represent? How does the interpretation differ from ordinary least squares? How is it similar?
- ▶ Why are classification metrics more nuanced than regression metrics?