

DIA project A.Y. 2020/2021 - Pricing and Matching

Scenario. Consider the scenario in which a shop has a number of promo codes to incentivize the customers that buy an item to buy a different item. The customers can belong to different classes and the promo codes can provide different discounts.

Environment. Imagine two items (referred to as first and second items; for each item we have an infinite number of units) and four customers' classes. The daily number of customers of each class is described by a potentially different (truncated) Gaussian probability distribution. Each class is also associated with a potentially different conversion rate returning the probability that the user will buy the first item at a given price.

Once a buyer has bought the item, she/he can decide to buy the second item that can be or not promoted. There are four different promos P0, P1, P2, P3, each corresponding to a different level of discount. P0 corresponds to no discount. Given the total number of customers, the business unit of the shop decides the number of promos as a fraction of the total number of the daily customers and is fixed (use two different settings in your experiments that you are free to choose). Each customers' class is also associated with a potentially different conversion rate returning the probability that the user will buy the second item at a given price after she/he has bought the first. The promos will affect the conversion rate as they actually reduce the price.

Every price available is associated with a margin obtained by the sale that is known beforehand. This holds both for the first and the second item.

The conversion rates will change during time according to some phases due to, e.g., seasonality.

Steps. You need to complete the following steps.

1. Provide a mathematical formulation of the problem in the case in which the daily optimization is performed using the average number of customers per class. Provide an algorithm to find the optimal solution in the offline case in which all the parameters are known. Then, during the day when customers arrive, the shop uses a randomized approach to assure that a fraction of the customers of a given class gets a specified promo according to the optimal solution. For instance, at the optimal solution, a specific fraction of the customers of the first class gets P_0 , another fraction P_1 , and so on. These fractions will be used as probabilities during the day.
2. Consider the online learning version of the above optimization problem, identify the random variables, and choose a model for them when each round corresponds to a single day. Consider a time horizon of one year.
3. Consider the case in which the assignment of promos is fixed and the price of the second item is fixed and the goal is to learn the optimal price of the first item. Assume that the number of users per class is known as well as the conversion rate associated with the second item. Also assume that the prices are the same for all: the classes (assume the same in the following) and that the conversion rates do not change unless specified differently below. Adopt both an upper-confidence bound approach and a Thompson-sampling approach and compare their performance.
4. Do the same as Step 3 when instead the conversion rate associated with the second item is not known. Also assume that the number of customers per class is not known.
5. Consider the case in which prices are fixed, but the assignment of promos to users need to be optimized by using an assignment algorithm. All the parameters need to be learnt.
6. Consider the general case in which the shop needs to optimize the prices and the assignment of promos to the customers in the case all the parameters need to be learnt.
7. Do the same as Step 6 when the conversion rates are not stationary. Adopt a sliding-window approach.
8. Do the same as Step 6 when the conversion rates are not stationary. Adopt a change-detection test approach.

Duties. You are required to:

- Produce the Python code.
- Produce a technical report describing the environment, the algorithms and the plot representing the regret and the reward of every algorithm. Provide also a practical application motivating the scenario.
- Produce a presentation as a summary of the technical report.