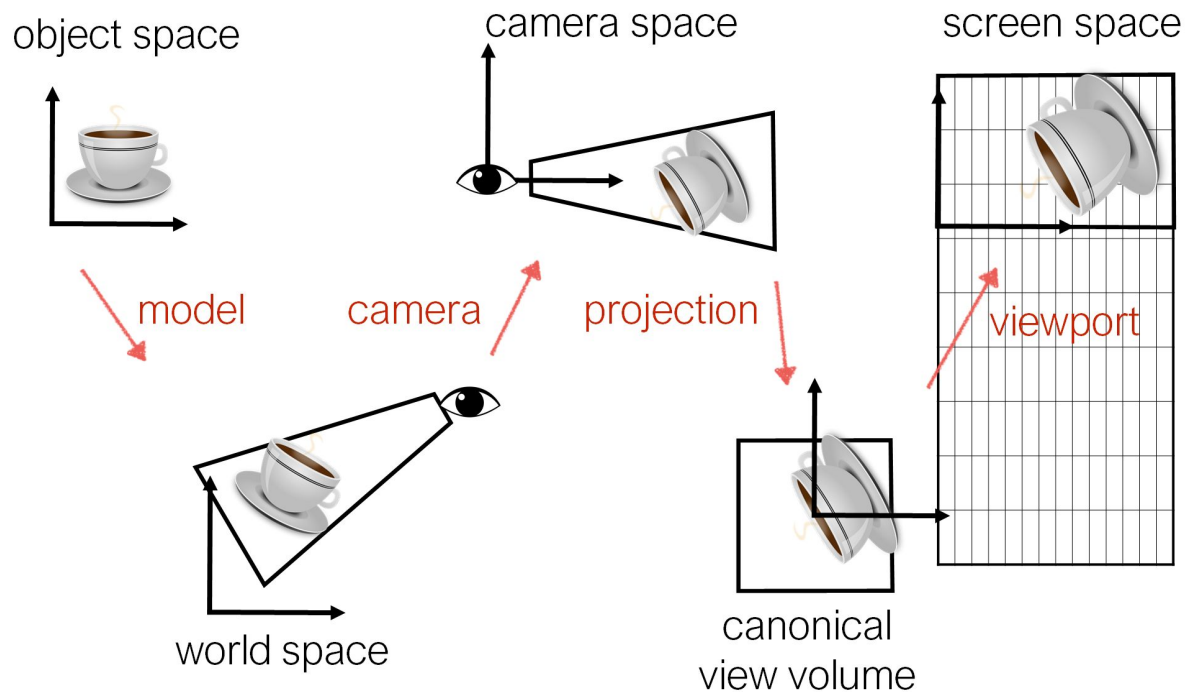


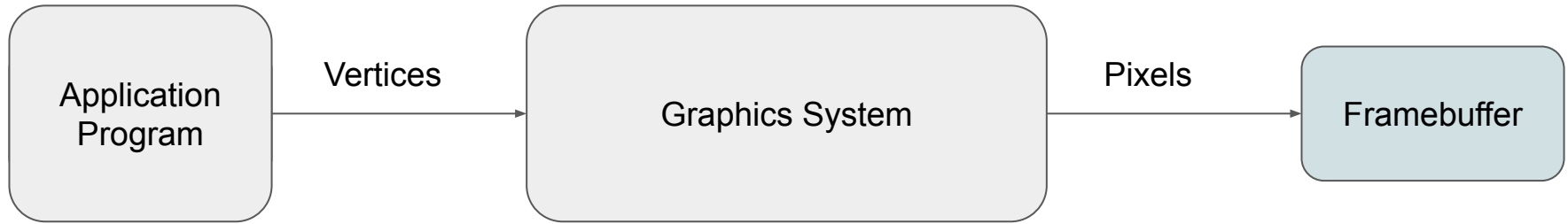
# Rendering Pipeline 1

CS 425: Computer Graphics 1

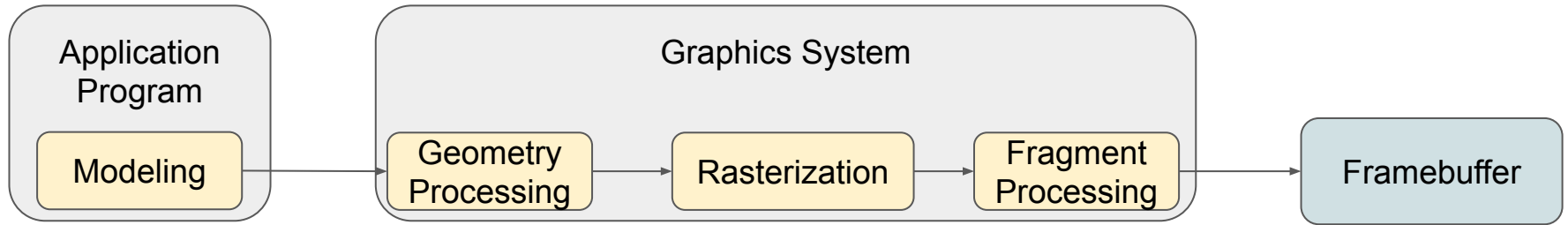
# Recap: Transformations



# Graphics System



# Graphics Pipeline



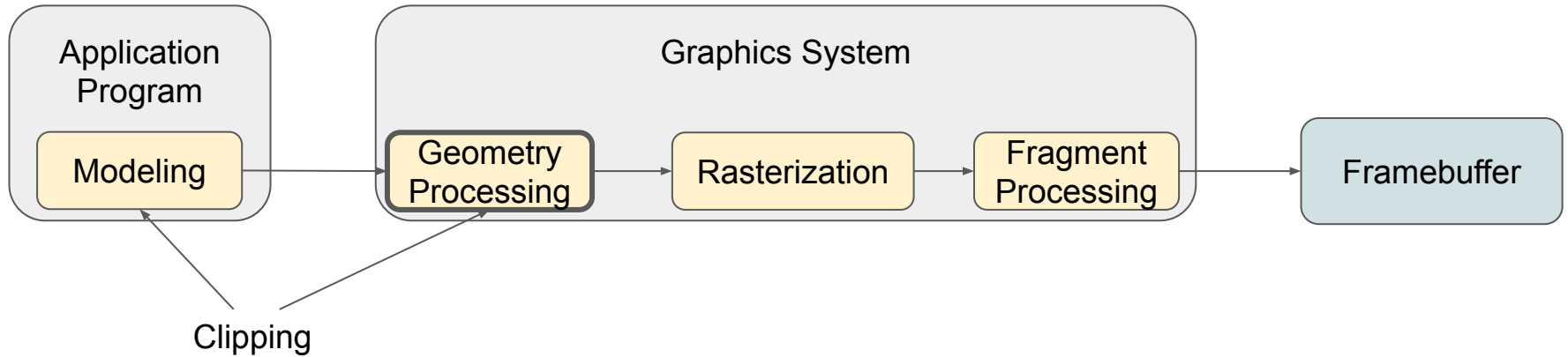
# Geometry Processing

- Change of representation (We saw this in the last class)
- Projection
- Primitive Assembly
- Clipping
- Shading

# Geometry Processing

- **Projection:**
  - Transforming to a normalized view volume.
  - View volume will be a cube of size 2, centered at origin.
  - Eliminates dependency on application specifications as well as display device specifications.
- **Primitive Assembly:**
  - Grouping of vertices to form objects (primitives).
  - Done before clipping.
- **Clipping**
- **Shading**
  - Assignment of colors to vertices and determining how the intermediate vertices are to be colored.

# Clipping



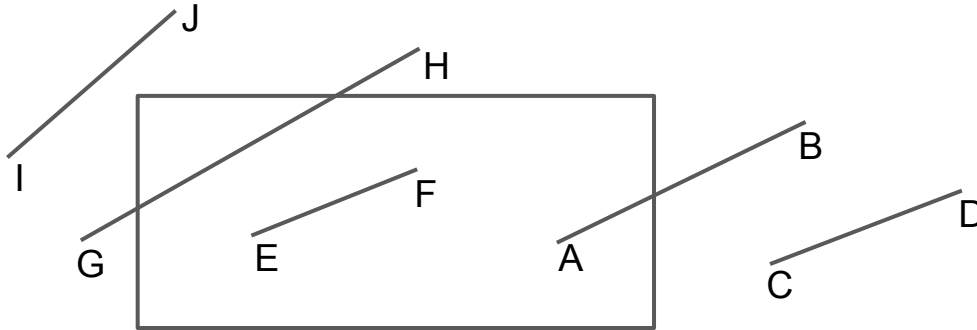
# Clipping

- Rasterization is expensive. Optimize what needs to be rasterized.
- Brute force approach: Clip every primitive against all the four sides of the view window (or six sides of the view volume)
- Computing intersections can be expensive since these calculations involve floating point divisions.



# Clipping: Line segments

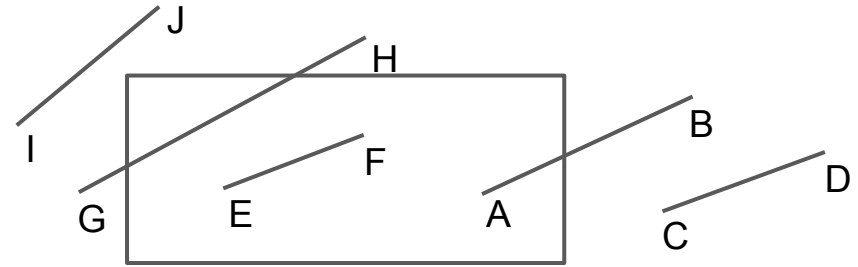
## Cohen-Sutherland Line Clipping



# Clipping: Cohen-Sutherland Line Clipping

	1001	1000	1010
$y = y_{\max}$	0001	0000	0010
$y = y_{\min}$	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	

$\uparrow$   
 $b_0 b_1 b_2 b_3$



$$b_0 = \begin{cases} 1 & \text{if } y > y_{\max} \\ 0 & \text{otherwise} \end{cases}$$

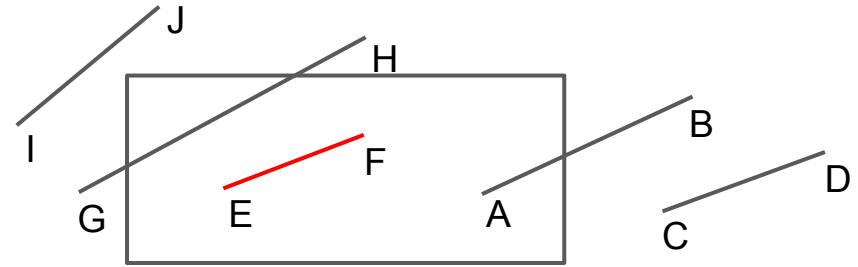
# Clipping: Cohen-Sutherland Line Clipping

```
outcode(x, y):  
    out = 0000  
    if (y > ymax)  
        out = out | 1000  
    else if (y < ymin)  
        out = out | 0100  
    if (x > xmax)  
        out = out | 0010  
    else if (x < xmin)  
        out = out | 0001  
    return out
```

# Clipping: Cohen-Sutherland Line Clipping

Case1:

	1001	1000	1010
$y = y_{\max}$	0001	0000	0010
$y = y_{\min}$	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	



$$o_1 = \text{outcode}(x_1, y_1)$$

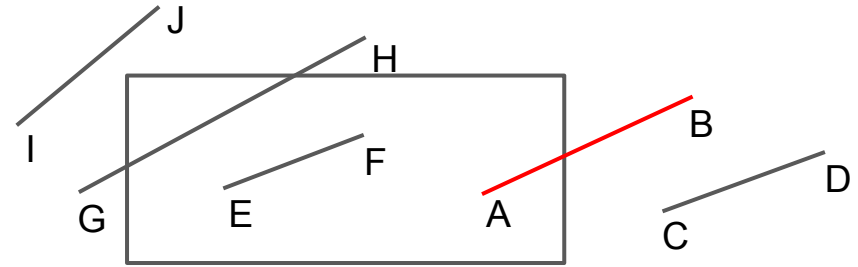
$$o_2 = \text{outcode}(x_2, y_2)$$

$$o_1 = o_2 = 0$$

# Clipping: Cohen-Sutherland Line Clipping

Case2:

	1001	1000	1010
$y = y_{\max}$	0001	0000	0010
$y = y_{\min}$	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	



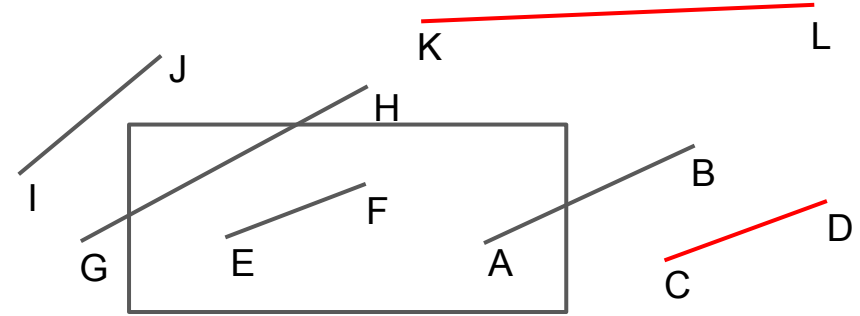
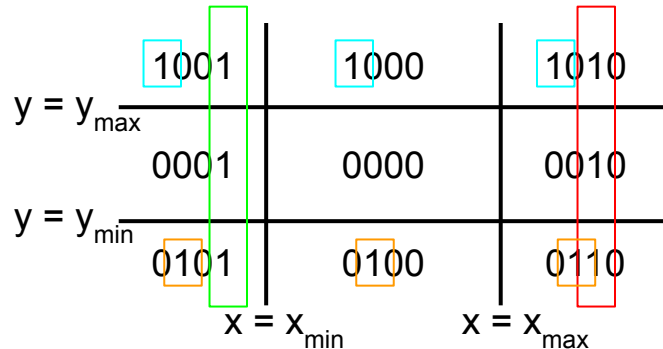
$$o_1 = \text{outcode}(x_1, y_1)$$

$$o_2 = \text{outcode}(x_2, y_2)$$

**$o_1 \neq 0$  and  $o_2 = 0$  or vice versa**

# Clipping: Cohen-Sutherland Line Clipping

Case3:



$o_1 = \text{outcode}(x_1, y_1)$

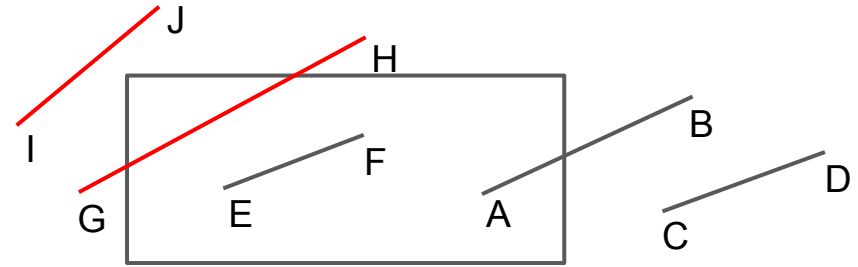
$o_2 = \text{outcode}(x_2, y_2)$

**$o_1 \& o_2 \neq 0$**

# Clipping: Cohen-Sutherland Line Clipping

Case4:

	1001	1000	1010
$y = y_{\max}$			
	0001	0000	0010
$y = y_{\min}$			
	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	



$$o_1 = \text{outcode}(x_1, y_1)$$

$$o_2 = \text{outcode}(x_2, y_2)$$

$$o_1 \& o_2 = 0$$

# Clipping: Cohen-Sutherland Line Clipping

Intersection calculation:

- $y = mx + h$
- $(y - y_1) = ((y_2 - y_1) / (x_2 - x_1)) * (x - x_1)$

Disadvantages:

1. Algorithm is recursively applied (till the clipped result can be accepted or rejected).
2. Vertical lines will have to be treated as a special case.



# Clipping: Liang-Barsky Line Clipping

Algorithm makes use of parametric form of line.

Suppose:

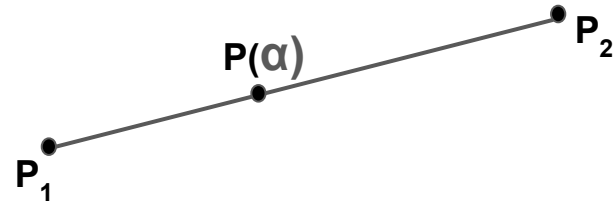
$$\mathbf{P}_1 = [x_1, y_1]^T \text{ and } \mathbf{P}_2 = [x_2, y_2]^T.$$

Then,

$$\mathbf{P}(\alpha) = (1 - \alpha)\mathbf{P}_1 + \alpha\mathbf{P}_2$$

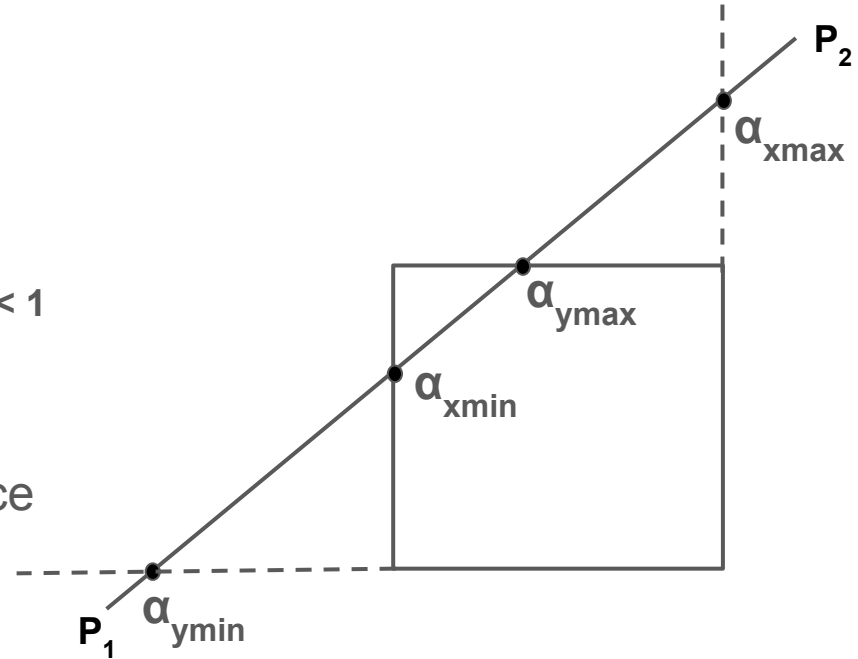
Or

$$x(\alpha) = (1 - \alpha)x_1 + \alpha x_2, y(\alpha) = (1 - \alpha)y_1 + \alpha y_2$$



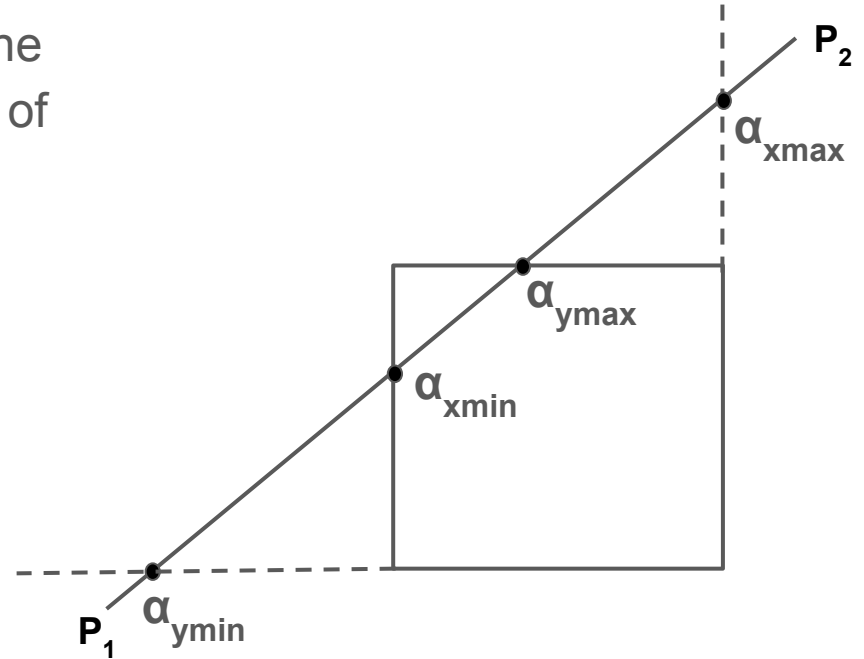
# Clipping: Liang-Barsky Line Clipping

- Compute the four  $\alpha$  values corresponding to four sides of the clipping window
- Compare them to find the order.
  - In this case  $0 < \alpha_{ymin} < \alpha_{xmin} < \alpha_{ymax} < \alpha_{xmax} < 1$
- Between two alpha values corresponding to vertical extremes if there is a horizontal alpha value (or vice versa) it indicates the line passes through the clip window.



# Clipping: Liang-Barsky Line Clipping

- Any  $\alpha$  value that is  $< 0$  or  $> 1$  implies the intersection happens on the extension of the actual line segment.



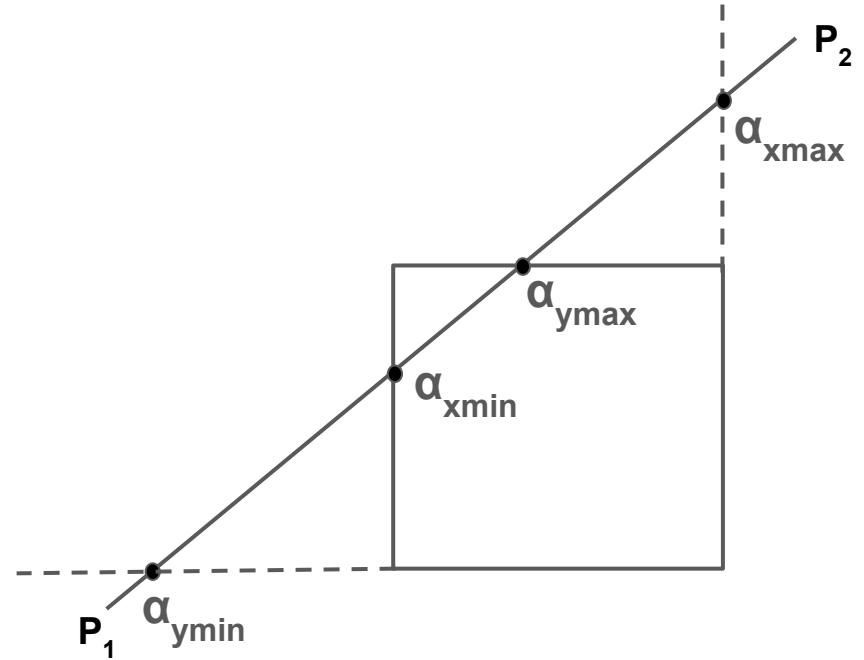
# Clipping: Liang-Barsky Line Clipping

Computing alpha value:

$$\alpha_{ymin} = (y_{min} - y_1) / (y_2 - y_1)$$

or

$$\Delta y \alpha_{ymin} = \Delta y_{min}$$



# Clipping

- Polygons (convex) can be clipped by successively clipping the edges against the clipping window.
- Concave polygons need to be tessellated (broken into smaller convex polygons) and the constituent polygons can be clipped as above.
- The clipping algorithms discussed extend naturally to 3 dimensions.