

DESEMPENHO E DIMENSIONAMENTO DE REDES

ASSIGNMENT GUIDE NO. 3

AVAILABILITY PERFORMANCE OF MULTI-HOP WIRELESS NETWORKS WITH MOBILE TERMINALS

Realizado por:

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2. Simulator Development

Funções desenvolvidas:

```
function counter= InitializeCounter(N)
% counter - a row vector with N values to count the number of time slots
%           such that each mobile node has Internet access
% This function creates the row vector 'counter' and initializes it with
% zeros
% in all positions.
    counter = zeros(1,N);
end
```

```
function counter= UpdateCounter(C,counter)
% This function increments the values of the 'counter' positions of the
% mobile nodes that have Internet access.
counter=counter+C;
end
```

```
function L= ConnectedList(pos,W,AP)
% Input:
%   pos - a matrix with N rows and 2 columns; each row identifies the
%         (x,y)
%         coordinates of each mobile node
%   W -   radio range (in meters)
%   AP - coordinates of Access Points (APs)
% Output:
%   L - a matrix with 2 columns; each row identifies a pair of nodes
%       (mobile nodes and AP nodes) with a direct wireless link
%       between them

L = [];
W = W^2;
aux = [pos ; AP];

for k = 1:size(pos,1)
    for l = k+1:size(aux,1)
        elem1 = aux(k,:);
        elem2 = aux(l,:);
        dist = (elem1(1)-elem2(1))^2 + (elem1(2)-elem2(2))^2;

        if dist <= W
            L = [L; [l,k]];
        end
    end
end
end
```

```

function C= ConnectedNodes(L,N,AP)
% Input:
%   L - a matrix with 2 columns; each row identifies a pair of nodes
%        (mobile nodes and AP nodes) with a direct wireless link
%        between them
%   N - no. of mobile nodes
%   AP - coordinates of Access Points (APs)
% Output:
%   C - an array with N values (one for each mobile node) that is 1 in
%        position i if mobile node i has Internet access
%
% NOTE: To develop this function, check MATLAB function 'distances' that
%        computes shortest path distances of a graph.
%

    C = false(1, N);

    num_ap = size(AP,1);
    id_last_ap = N + num_ap;

    tmp1= N+1:id_last_ap;
    tmp2= N+1:id_last_ap;

    col1 = [ L(:,1) ; tmp1(:) ];
    col2 = [ L(:,2) ; tmp2(:) ];

    grap = graph(col1,col2);
    dis= distances(grap,1:N,N+1:id_last_ap);

    for i=1:size(dis,1)
        for j=1:num_ap
            if not(dis(i,j)==Inf)
                C(1,i) = true;
            end
        end
    end
end
end

```

3. Assignment tasks:

Código escrito para recolha de dados:

```
Result = zeros(24,6);
Conf = zeros(24,6);

Case = zeros(10,2);
Aps = [ 250,100;
        150,100;
        350,100;
        50,50;
        250,100;
        450,150];

for ap = 1:3
    for w = 1:3
        for s = 1:2
            for n = 1:4
                for k = 1:10
                    [AvgAvail, MinAvail]= simulatorFunction(n*20, s*3,
w*20 + 20, 1, 7200, Aps(2^(ap-1):2^(ap-1)+ap-1,1:2), 0);
                    Case(k,1) = AvgAvail;
                    Case(k,2) = MinAvail;
                end

                Result((8*w-8)+(4*s-4)+n, 2*ap-1) = mean(Case(:,1));
                Result((8*w-8)+(4*s-4)+n, 2*ap) = mean(Case(:,2));
                Conf((8*w-8)+(4*s-4)+n, 2*ap-1) = 1.645*std(Case(:,
1))/sqrt(10);
                Conf((8*w-8)+(4*s-4)+n, 2*ap) = 1.645*std(Case(:,
2))/sqrt(10);

                Result
                Conf
            end
        end
    end
end
end
```

a)

Para 1 AP:

| Case | N | S (km/h) | W (meters) | Average availability | 90% confidence interval | Minimum availability | 90% confidence interval |
|------|-----|---------------|-----------------|-------------------------|-------------------------------|-------------------------|-------------------------------|
| 1 | 20 | 3 | 40 | 0.0791 | 0.0164 | 0.0014 | 0.0018 |
| 2 | 40 | 3 | 40 | 0.1377 | 0.0104 | 0.0077 | 0.0036 |
| 3 | 60 | 3 | 40 | 0.2387 | 0.0240 | 0.0462 | 0.0148 |
| 4 | 80 | 3 | 40 | 0.4145 | 0.0211 | 0.1903 | 0.0434 |
| 5 | 20 | 6 | 40 | 0.0795 | 0.0066 | 0.0098 | 0.0073 |
| 6 | 40 | 6 | 40 | 0.1344 | 0.0074 | 0.0303 | 0.0160 |
| 7 | 60 | 6 | 40 | 0.2415 | 0.0171 | 0.0623 | 0.0231 |
| 8 | 80 | 6 | 40 | 0.4197 | 0.0129 | 0.1921 | 0.0326 |

| | | | | | | | |
|-----------|----|---|----|--------|--------|--------|--------|
| 9 | 20 | 3 | 60 | 0.2738 | 0.0084 | 0.0825 | 0.0325 |
| 10 | 40 | 3 | 60 | 0.6052 | 0.0239 | 0.3811 | 0.0382 |
| 11 | 60 | 3 | 60 | 0.8782 | 0.0108 | 0.7366 | 0.0268 |
| 12 | 80 | 3 | 60 | 0.9736 | 0.0032 | 0.9102 | 0.0110 |
| 13 | 20 | 6 | 60 | 0.2973 | 0.0242 | 0.1366 | 0.0481 |
| 14 | 40 | 6 | 60 | 0.6025 | 0.0108 | 0.4021 | 0.0585 |
| 15 | 60 | 6 | 60 | 0.8901 | 0.0103 | 0.7859 | 0.0394 |
| 16 | 80 | 6 | 60 | 0.9759 | 0.0033 | 0.9363 | 0.0085 |
| 17 | 20 | 3 | 80 | 0.6082 | 0.0235 | 0.4508 | 0.0365 |
| 18 | 40 | 3 | 80 | 0.9418 | 0.0081 | 0.8574 | 0.0213 |
| 19 | 60 | 3 | 80 | 0.9944 | 0.0017 | 0.9680 | 0.0099 |
| 20 | 80 | 3 | 80 | 0.9995 | 0.0002 | 0.9897 | 0.0036 |
| 21 | 20 | 6 | 80 | 0.6136 | 0.0240 | 0.4230 | 0.0634 |
| 22 | 40 | 6 | 80 | 0.9298 | 0.0077 | 0.8523 | 0.0299 |
| 23 | 60 | 6 | 80 | 0.9946 | 0.0013 | 0.9785 | 0.0031 |
| 25 | 80 | 6 | 80 | 0.9995 | 0.0003 | 0.9933 | 0.0012 |

Para 2 APs:

| Case | <i>N</i> | <i>S</i> (km/h) | <i>W</i> (meters) | Average availability | 90% confidence interval | Minimum availability | 90% confidence interval |
|-----------|----------|--------------------|----------------------|-------------------------|-------------------------------|-------------------------|-------------------------------|
| 1 | 20 | 3 | 40 | 0.1415 | 0.0072 | 0.0314 | 0.0213 |
| 2 | 40 | 3 | 40 | 0.2666 | 0.0118 | 0.0730 | 0.0257 |
| 3 | 60 | 3 | 40 | 0.4255 | 0.0204 | 0.2107 | 0.0325 |
| 4 | 80 | 3 | 40 | 0.6239 | 0.0110 | 0.3541 | 0.0598 |
| 5 | 20 | 6 | 40 | 0.1445 | 0.0070 | 0.0496 | 0.0246 |
| 6 | 40 | 6 | 40 | 0.2637 | 0.0092 | 0.1351 | 0.0384 |
| 7 | 60 | 6 | 40 | 0.4311 | 0.0114 | 0.2228 | 0.0350 |
| 8 | 80 | 6 | 40 | 0.6325 | 0.0098 | 0.4031 | 0.0467 |
| 9 | 20 | 3 | 60 | 0.5027 | 0.0214 | 0.2934 | 0.0646 |
| 10 | 40 | 3 | 60 | 0.7996 | 0.0057 | 0.5945 | 0.0568 |
| 11 | 60 | 3 | 60 | 0.9537 | 0.0038 | 0.8488 | 0.0242 |
| 12 | 80 | 3 | 60 | 0.9877 | 0.0022 | 0.9411 | 0.0120 |
| 13 | 20 | 6 | 60 | 0.4965 | 0.0090 | 0.3916 | 0.0360 |
| 14 | 40 | 6 | 60 | 0.8083 | 0.0113 | 0.6852 | 0.0244 |
| 15 | 60 | 6 | 60 | 0.9464 | 0.0039 | 0.8586 | 0.0361 |
| 16 | 80 | 6 | 60 | 0.9877 | 0.0008 | 0.9590 | 0.0045 |
| 17 | 20 | 3 | 80 | 0.8289 | 0.0092 | 0.6731 | 0.0488 |
| 18 | 40 | 3 | 80 | 0.9778 | 0.0027 | 0.9221 | 0.0130 |
| 19 | 60 | 3 | 80 | 0.9977 | 0.0007 | 0.9780 | 0.0053 |
| 20 | 80 | 3 | 80 | 0.9997 | 0.0001 | 0.9926 | 0.0029 |
| 21 | 20 | 6 | 80 | 0.8351 | 0.0052 | 0.7334 | 0.0277 |
| 22 | 40 | 6 | 80 | 0.9776 | 0.0017 | 0.9353 | 0.0111 |
| 23 | 60 | 6 | 80 | 0.9978 | 0.0004 | 0.9845 | 0.0025 |
| 25 | 80 | 6 | 80 | 0.9997 | 0.0001 | 0.9948 | 0.0017 |

Para 3 APs:

| Case | N | S (km/h) | W (meters) | Average availability | 90% confidence interval | Minimum availability | 90% confidence interval |
|------|-----|---------------|-----------------|-------------------------|-------------------------------|-------------------------|-------------------------------|
| 1 | 20 | 3 | 40 | 0.2215 | 0.0195 | 0.0717 | 0.0253 |
| 2 | 40 | 3 | 40 | 0.3408 | 0.0138 | 0.1634 | 0.0269 |
| 3 | 60 | 3 | 40 | 0.5027 | 0.0140 | 0.2400 | 0.0375 |
| 4 | 80 | 3 | 40 | 0.7094 | 0.0079 | 0.4718 | 0.0683 |
| 5 | 20 | 6 | 40 | 0.2206 | 0.0123 | 0.0757 | 0.0281 |
| 6 | 40 | 6 | 40 | 0.3330 | 0.0112 | 0.1611 | 0.0361 |
| 7 | 60 | 6 | 40 | 0.5142 | 0.0077 | 0.3357 | 0.0439 |
| 8 | 80 | 6 | 40 | 0.7187 | 0.0066 | 0.5748 | 0.0321 |
| 9 | 20 | 3 | 60 | 0.5932 | 0.0190 | 0.3874 | 0.0539 |
| 10 | 40 | 3 | 60 | 0.8811 | 0.0064 | 0.7352 | 0.0375 |
| 11 | 60 | 3 | 60 | 0.9748 | 0.0020 | 0.9018 | 0.0155 |
| 12 | 80 | 3 | 60 | 0.9940 | 0.0006 | 0.9603 | 0.0071 |
| 13 | 20 | 6 | 60 | 0.5851 | 0.0173 | 0.4178 | 0.0556 |
| 14 | 40 | 6 | 60 | 0.8844 | 0.0041 | 0.8010 | 0.0202 |
| 15 | 60 | 6 | 60 | 0.9723 | 0.0016 | 0.9180 | 0.0107 |
| 16 | 80 | 6 | 60 | 0.9942 | 0.0006 | 0.9709 | 0.0079 |
| 17 | 20 | 3 | 80 | 0.9048 | 0.0078 | 0.8173 | 0.0173 |
| 18 | 40 | 3 | 80 | 0.9900 | 0.0015 | 0.9491 | 0.0129 |
| 19 | 60 | 3 | 80 | 0.9984 | 0.0004 | 0.9806 | 0.0045 |
| 20 | 80 | 3 | 80 | 0.9998 | 0.0001 | 0.9926 | 0.0054 |
| 21 | 20 | 6 | 80 | 0.9048 | 0.0044 | 0.8215 | 0.0263 |
| 22 | 40 | 6 | 80 | 0.9897 | 0.0010 | 0.9635 | 0.0048 |
| 23 | 60 | 6 | 80 | 0.9987 | 0.0004 | 0.9904 | 0.0024 |
| 25 | 80 | 6 | 80 | 0.9998 | 0.0001 | 0.9942 | 0.0021 |

a) Não influencia uma vez que a velocidade não tem influencia direta sobre a conexao entre nodes. Esta é apenas alterada devido ao range, à posição e ao número de dispositivos.

b) Quanto maior o range, maior será a disponibilidade média, uma vez que quanto maior for o range, maior será a área na qual os dispositivos se conseguem conectar, ou seja, existirão mais conexões entre estes.

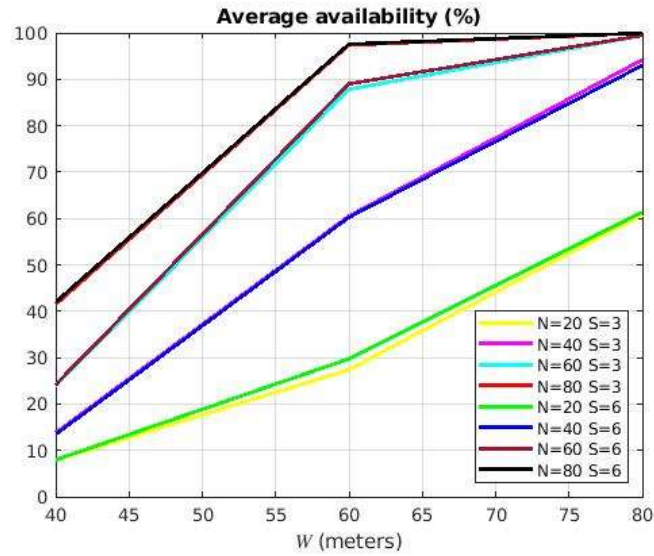


Figura 1 - Disponibilidade média para 1 AP.

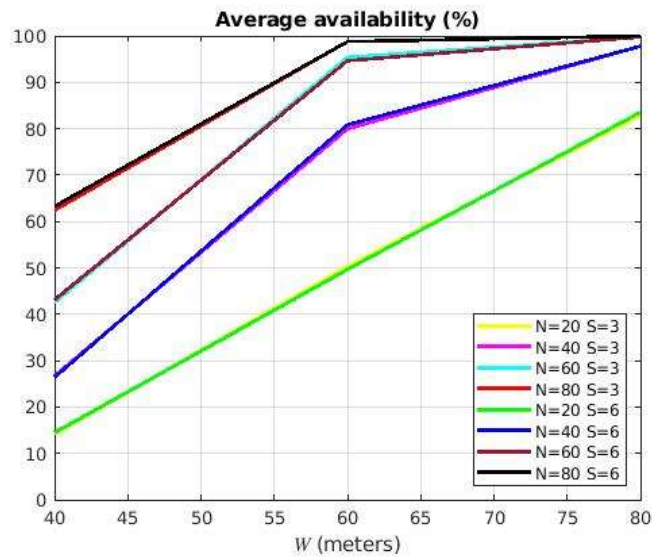


Figura 2 - Disponibilidade média para 2 APs.

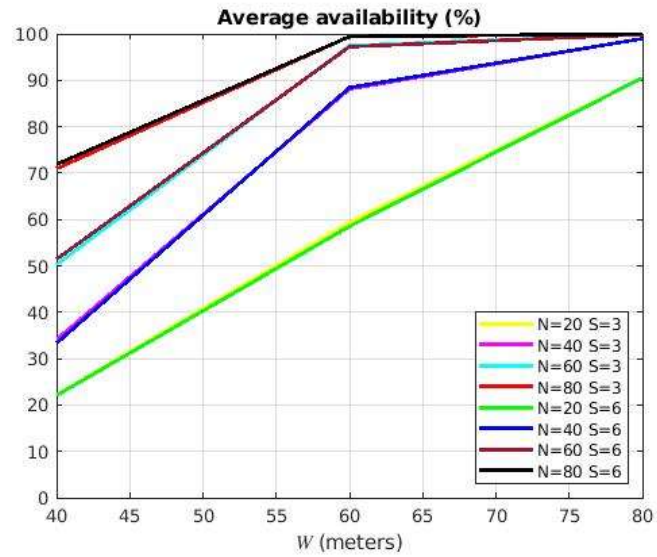


Figura 3 - Disponibilidade média para 3 APs.

```
%1 AP

x = [40, 60, 80];

Y1 = [0.0791, 0.2738, 0.6082].*100;
Y2 = [0.1377, 0.6052, 0.9418].*100;
Y3 = [0.2387, 0.8782, 0.9944].*100;
Y4 = [0.4145, 0.9736, 0.9995].*100;
Y5 = [0.0795, 0.2973, 0.6136].*100;
Y6 = [0.1344, 0.6025, 0.9298].*100;
Y7 = [0.2415, 0.8901, 0.9946].*100;
Y8 = [0.4197, 0.9759, 0.9995].*100;

figure('Name','Radio range')
l=plot(x,Y1,'y-',x,Y2,'m-',x,Y3,'c-',x,Y4,'r-',x,Y5,'g-',x,Y6,'b-',
,x,Y7,'-',x,Y8,'k-');
for k=1:8
    l(k).LineWidth = 2;
end
title('Average availability (%)')
xlabel('W (meters)')
legend('N=20 S=3','N=40 S=3','N=60 S=3','N=80 S=3','N=20 S=6','N=40 S=6',
'N=60 S=6','N=80 S=6','location','southeast')
axis([40 80 0 100])
grid on
```



```
%2 AP
```

```
x = [40, 60, 80];

Y1 = [0.1415, 0.5027, 0.8289].*100;
Y2 = [0.2666, 0.7996, 0.9778].*100;
Y3 = [0.4255, 0.9537, 0.9977].*100;
Y4 = [0.6239, 0.9877, 0.9997].*100;
Y5 = [0.1445, 0.4965, 0.8351].*100;
Y6 = [0.2637, 0.8083, 0.9776].*100;
Y7 = [0.4311, 0.9464, 0.9978].*100;
Y8 = [0.6325, 0.9877, 0.9997].*100;

figure('Name','Radio range')
l=plot(x,Y1,'y-',x,Y2,'m-',x,Y3,'c-',x,Y4,'r-',x,Y5,'g-',x,Y6,'b-',
,x,Y7,'-',x,Y8,'k-');
for k=1:8
    l(k).LineWidth = 2;
end
title('Average availability (%)')
xlabel('W (meters)')
legend('N=20 S=3','N=40 S=3','N=60 S=3','N=80 S=3','N=20 S=6','N=40
S=6','N=60 S=6','N=80 S=6','location','southeast')
axis([40 80 0 100])
grid on
```

```
%3 AP
```

```
x = [40, 60, 80];

Y1 = [0.2215, 0.5932, 0.9048].*100;
Y2 = [0.3408, 0.8811, 0.9900].*100;
Y3 = [0.5027, 0.9748, 0.9984].*100;
Y4 = [0.7094, 0.9940, 0.9998].*100;
Y5 = [0.2206, 0.5851, 0.9048].*100;
Y6 = [0.3330, 0.8844, 0.9897].*100;
Y7 = [0.5142, 0.9723, 0.9987].*100;
Y8 = [0.7187, 0.9942, 0.9998].*100;

figure('Name','Radio range')
l=plot(x,Y1,'y-',x,Y2,'m-',x,Y3,'c-',x,Y4,'r-',x,Y5,'g-',x,Y6,'b-',
,x,Y7,'-',x,Y8,'k-');
for k=1:8
    l(k).LineWidth = 2;
end
title('Average availability (%)')
xlabel('W (meters)')
legend('N=20 S=3','N=40 S=3','N=60 S=3','N=80 S=3','N=20 S=6','N=40
S=6','N=60 S=6','N=80 S=6','location','southeast')
axis([40 80 0 100])
grid on
```

c) Quanto maior for o numero de nodes, maior será a disponibilidade, uma vez que existirão mais conexões entre estes e é mais provavel que um deles tenha conexão a um dos APs.

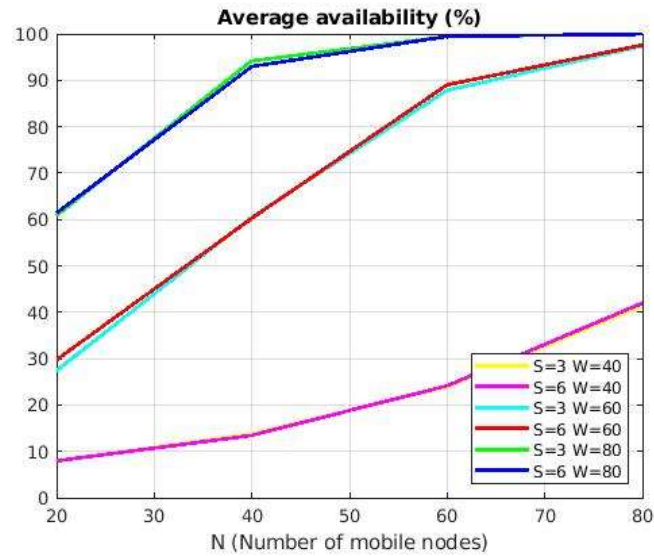


Figura 4 - Disponibilidade média para 1 AP.

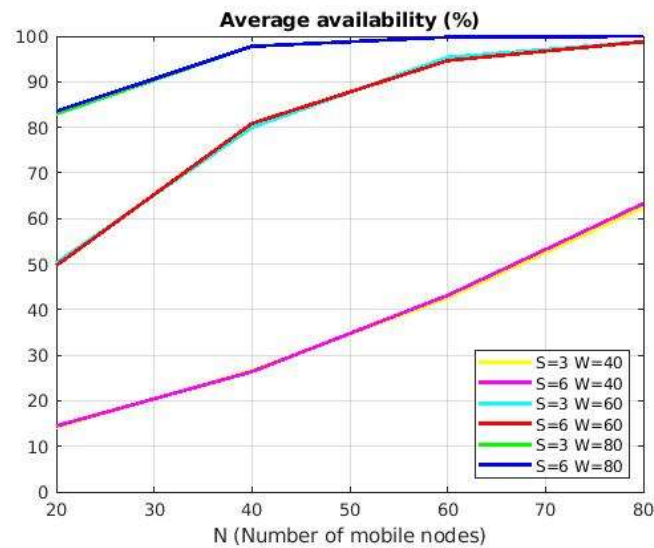


Figura 5 - Disponibilidade média para 2 APs.

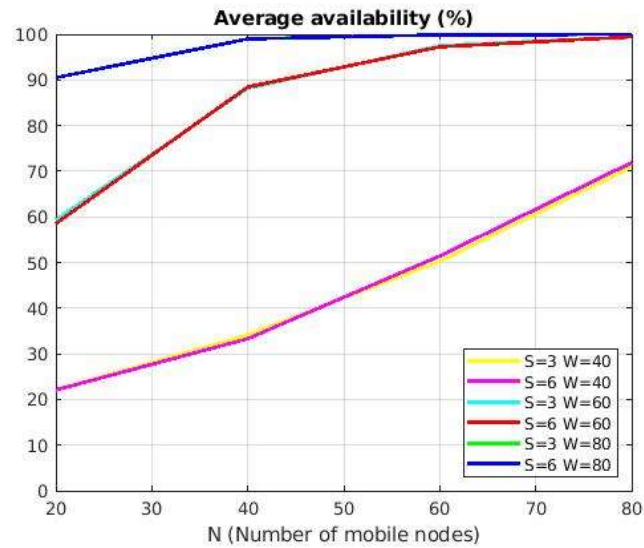


Figura 6- Disponibilidade média para 3 APs.

```
%1 AP
```

```
x = [20, 40, 60, 80];
```

```
Y1 = [0.0791, 0.1377, 0.2387, 0.4145].*100;
```

```
Y2 = [0.0795, 0.1344, 0.2415, 0.4197].*100;
```

```
Y3 = [0.2738, 0.6052, 0.8782, 0.9736].*100;
```

```
Y4 = [0.2973, 0.6025, 0.8901, 0.9759].*100;
```

```
Y5 = [0.6082, 0.9418, 0.9944, 0.9995].*100;
```

```
Y6 = [0.6136, 0.9298, 0.9946, 0.9995].*100;
```

```
figure('Name','Number of mobile nodes')
```

```
l=plot(x,Y1,'y-',x,Y2,'m-',x,Y3,'c-',x,Y4,'r-',x,Y5,'g-',x,Y6,'b-');
```

```
for k=1:6
```

```
    l(k).LineWidth = 2;
```

```
end
```

```
title('Average availability (%)')
```

```
xlabel('N (Number of mobile nodes)')
```

```
legend('S=3 W=40','S=6 W=40','S=3 W=60','S=6 W=60','S=3 W=80','S=6
```

```
W=80','location','southeast')
```

```
axis([20 80 0 100])
```

```
grid on
```

```
%2 AP
```

```
x = [20, 40, 60, 80];
```

```
Y1 = [0.1415, 0.2666, 0.4255, 0.6239].*100;
```

```
Y2 = [0.1445, 0.2637, 0.4311, 0.6325].*100;
```

```
Y3 = [0.5027, 0.7996, 0.9537, 0.9877].*100;
```

```
Y4 = [0.4965, 0.8083, 0.9464, 0.9877].*100;
```

```
Y5 = [0.8289, 0.9778, 0.9977, 0.9997].*100;
```

```
Y6 = [0.8351, 0.9776, 0.9978, 0.9997].*100;
```

```
figure('Name','Number of mobile nodes')
```

```
l=plot(x,Y1,'y-',x,Y2,'m-',x,Y3,'c-',x,Y4,'r-',x,Y5,'g-',x,Y6,'b-');
```

```
for k=1:6
```

```
    l(k).LineWidth = 2;
```

```
end
```

```
title('Average availability (%)')
```

```
xlabel('N (Number of mobile nodes)')
```

```
legend('S=3 W=40','S=6 W=40','S=3 W=60','S=6 W=60','S=3 W=80','S=6 W=80','location','southeast')
```

```
axis([20 80 0 100])
```

```
grid on
```

```
%3 AP
```

```
x = [20, 40, 60, 80];
```

```
Y1 = [0.2215, 0.3408, 0.5027, 0.7094].*100;
```

```
Y2 = [0.2206, 0.3330, 0.5142, 0.7187].*100;
```

```
Y3 = [0.5932, 0.8811, 0.9748, 0.9940].*100;
```

```
Y4 = [0.5851, 0.8844, 0.9723, 0.9942].*100;
```

```
Y5 = [0.9048, 0.9900, 0.9984, 0.9998].*100;
```

```
Y6 = [0.9048, 0.9897, 0.9987, 0.9998].*100;
```

```
figure('Name','Number of mobile nodes')
```

```
l=plot(x,Y1,'y-',x,Y2,'m-',x,Y3,'c-',x,Y4,'r-',x,Y5,'g-',x,Y6,'b-');
```

```
for k=1:6
```

```
    l(k).LineWidth = 2;
```

```
end
```

```
title('Average availability (%)')
```

```
xlabel('N (Number of mobile nodes)')
```

```
legend('S=3 W=40','S=6 W=40','S=3 W=60','S=6 W=60','S=3 W=80','S=6 W=80','location','southeast')
```

```
axis([20 80 0 100])
```

```
grid on
```

d) Quanto mais APs, maior será a disponibilidade média uma vez que existirão mais pontos com ligação à internet, permitindo que nós que não conseguiam alcançar um AP agora possam alcançar outro. Porém, existe uma grande dependência da posição em que são colocados (Pouca melhoria caso estejam aglomerados; Muita melhoria caso estejam dispersos).

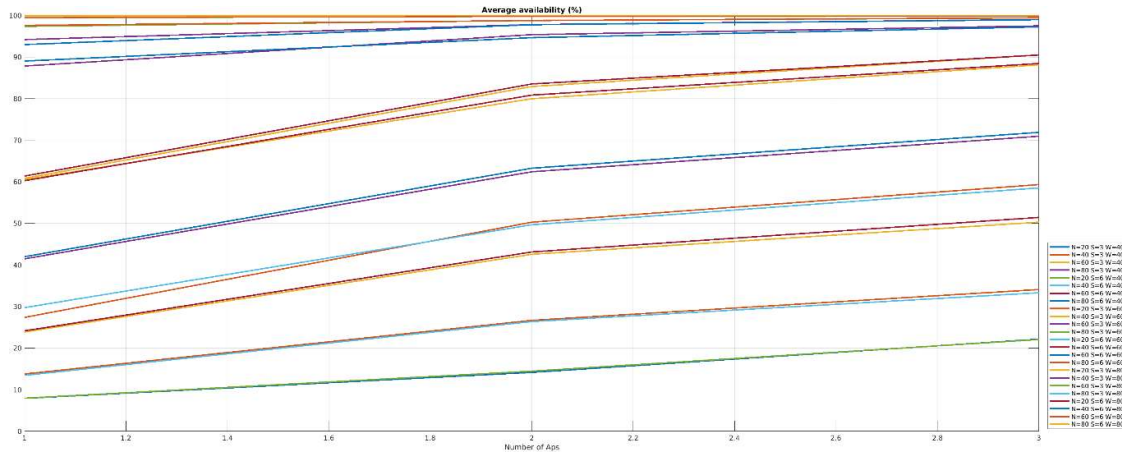


Figura 7- Disponibilidade média por número de APs.

$x = [1, 2, 3];$

```

Y1 = [0.0791, 0.1415, 0.2215].*100;
Y2 = [0.1377, 0.2666, 0.3408].*100;
Y3 = [0.2387, 0.4255, 0.5027].*100;
Y4 = [0.4145, 0.6239, 0.7094].*100;
Y5 = [0.0795, 0.1445, 0.2206].*100;
Y6 = [0.1344, 0.2637, 0.3330].*100;
Y7 = [0.2415, 0.4311, 0.5142].*100;
Y8 = [0.4197, 0.6325, 0.7187].*100;
Y9 = [0.2738, 0.5027, 0.5932].*100;
Y10 = [0.6052, 0.7996, 0.8811].*100;
Y11 = [0.8782, 0.9537, 0.9748].*100;
Y12 = [0.9736, 0.9877, 0.9940].*100;
Y13 = [0.2973, 0.4965, 0.5851].*100;
Y14 = [0.6025, 0.8083, 0.8844].*100;
Y15 = [0.8901, 0.9464, 0.9723].*100;
Y16 = [0.9759, 0.9877, 0.9942].*100;
Y17 = [0.6082, 0.8289, 0.9048].*100;
Y18 = [0.9418, 0.9778, 0.9900].*100;
Y19 = [0.9944, 0.9977, 0.9984].*100;
Y20 = [0.9995, 0.9997, 0.9998].*100;
Y21 = [0.6136, 0.8351, 0.9048].*100;
Y22 = [0.9298, 0.9776, 0.9897].*100;
Y23 = [0.9946, 0.9978, 0.9987].*100;
Y24 = [0.9995, 0.9997, 0.9998].*100;

```

```

figure('Name','Radio range')

l=plot(x,Y1,x,Y2,x,Y3,x,Y4,x,Y5,x,Y6,x,Y7,x,Y8,x,Y9,x,Y10,x,Y11,x,Y12,x,Y
13,x,Y14,x,Y15,x,Y16,x,Y17,x,Y18,x,Y19,x,Y20,x,Y21,x,Y22,x,Y23,x,Y24);
for k=1:24
    l(k).LineWidth = 2;
end
title('Average availability (%)')
xlabel('Number of Aps')
legend('N=20 S=3 W=40','N=40 S=3 W=40','N=60 S=3 W=40','N=80 S=3
W=40','N=20 S=6 W=40','N=40 S=6 W=40','N=60 S=6 W=40','N=80 S=6
W=40','N=20 S=3 W=60','N=40 S=3 W=60','N=60 S=3 W=60','N=80 S=3
W=60','N=20 S=6 W=60','N=40 S=6 W=60','N=60 S=6 W=60','N=80 S=6
W=60','N=20 S=3 W=80','N=40 S=3 W=80','N=60 S=3 W=80','N=80 S=3
W=80','N=20 S=6 W=80','N=40 S=6 W=80','N=60 S=6 W=80','N=80 S=6
W=80','location','southeast')
axis([1 3 0 100])
grid on

```

e) À medida que adicionamos mais nodes, usando um baixo range, verifica-se uma maior variação nos resultados (intrevalo de confiança aumenta). Por outro lado, se o range for mais elevado, esta tendencia inverte-se (intrevalo de confiança diminui).

f)

1 AP - Encontra-se numa das melhores localizações (centro).

Ex: (80,3,40)

[250,100] - A 41% M 19%

[260,100] - A 41% M 16%

[240,100] - A 39% M 12%

[250,150] - A 36% M 19%

[250,50] - A 40% M 20%

(20,3,80)

[250,100] - A 61% M 45%

[300,100] - A 60% M 40%

[200,100] - A 58% M 48%

[250,150] - A 57% M 41%

[250,50] - A 57% M 39%

Outras localizações possuem resultados inferiores ou que se encontram dentro da margem de erro de aproximadamente 2%.

2 AP - Deve ser feita uma translação do ponto onde existe mais uniformidade da distribuição das áreas sem cobertura para ranges baixos, para o que possui maior uniformidade para ranges elevados.

Ex: (20,3,80)

[150,100; 350,100] - A 83% M 67%

[125,100; 375,100] - A 88% M 77%

(20,3,40)

[150,100; 350,100] - A 14% M 3%

[125,100; 375,100] - A 14% M 2%

Ou seja, novas posições [125,100; 375,100].

3 AP - O AP central encontra-se bem localizado. Os outros 2 deviam ser deslocados um para a posição [80,100] e o outro para a posição [420,100] para permitir maximizar a área de cobertura dos AP. É melhor ter duas pequenas áreas no meio de 2 AP sem cobertura do que quatro metades das duas áreas, estando duas delas apenas na fronteira de 1 AP e as outras 2 no meio de 2 AP. Ou seja, é melhor [80,100] e [420,100] que [85,100] e [425,100].

Ex: (20,3,80)

[50,50; 250,100; 450,150] - A 90% M 82%

[80,100; 250,100; 420,100] - A 94% M 84%

(20,3,40)

[50,50; 250,100; 450,150] - A 22% M 7%

[80,100; 250,100; 420,100] - A 22% M 8%

Ou seja, novas posições [80,100; 250,100; 420,100].

g) O número mínimo encontrado de Aps foi 10, sendo eles os seguintes:
[50,50; 270,50; 375,50; 470,50; 235,150; 345,150; 450,150; 45,150;165,45;135,145].

Modelo usado para alcançar a um resultado base:

```
theta = linspace(0,2*pi);

x1 = 60*cos(theta) + 50;
y1 = 60*sin(theta) + 50;

x2 = 60*cos(theta) + 270;
y2 = 60*sin(theta) + 50;

x3 = 60*cos(theta) + 375;
y3 = 60*sin(theta) + 50;

x4 = 60*cos(theta) + 470;
y4 = 60*sin(theta) + 50;

x5 = 60*cos(theta) + 235;
y5 = 60*sin(theta) + 150;

x6 = 60*cos(theta) + 345;
y6 = 60*sin(theta) + 150;

x7 = 60*cos(theta) + 450;
y7 = 60*sin(theta) + 150;

x8 = 60*cos(theta) + 45;
y8 = 60*sin(theta) + 150;

x9 = 60*cos(theta) + 165;
y9 = 60*sin(theta) + 45;

x10 = 60*cos(theta) + 135;
y10 = 60*sin(theta) + 145;

plot (x1,y1,x2,y2,x3,y3,x4,y4,x5,y5,x6,y6,x7,y7,x8,y8,x9,y9,x10,y10)
axis([0 500 0 200])
```