

# Algorithm WD

Compute matrices  $W$  and  $D$  of a synchronous circuit  $G$ .

1. Weight each edge  $u \xrightarrow{e} v \in E$  with  $(w(e), -d(u))$ .
2. Compute the weight of the shortest path joining each connected pair of vertices by solving an all-pairs shortest-paths algorithm — e.g., Floyd-Warshall algorithm.
3. For each shortest-path weight  $(x, y)$  between two vertices  $u$  and  $v$ , set

$$W(u, v) \leftarrow x$$

$$D(u, v) \leftarrow d(v) - y$$

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- The quantity  $W(u, v)$  is the minimum number of registers on any path from vertex  $u$  to vertex  $v$ .
  - We call a path  $u \xrightarrow{p} v$  such that  $w(p) = W(u, v)$  a *critical path* from  $u$  to  $v$ .
- The quantity  $D(u, v)$  is the maximum total propagation delay on any critical path from  $u$  to  $v$ .
- Both quantities are undefined if there is no path from  $u$  to  $v$ .