Heurísticas com Paralelismo através do Problema do Caixeiro Viajante

Fabio Galuppo, M.Sc.

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Microsoft MVP Visual Studio and Development Technologies https://mvp.microsoft.com/en-us/PublicProfile/9529

TODO: Address



Award Categories
Visual Studio and Development
Technologies

First year awarded: 2002

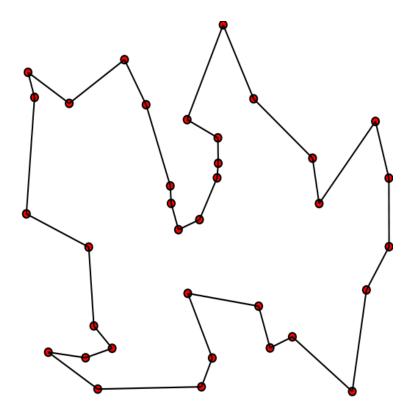
Number of MVP Awards:

Fabio Razzo Galuppo, M.Sc.

Novembro 1973

- Mestrado em Engenharia Elétrica (Universidade Presbiteriana Mackenzie)
 - Ciência da Computação Inteligência Artificial
- Por mais de 10 anos premiado com Microsoft MVP em Visual C++
- Engenheiro de Software (Programador)
- Matemática Aplicada
- Linguagens de programação prediletas:
 - C++
 - F#
 - Haskell
- Rock'n'Roll
 - E boa música em geral
- http://fabiogaluppo.com
- https://twitter.com/FabioGaluppo
- https://github.com/fabiogaluppo
- http://simplycpp.com

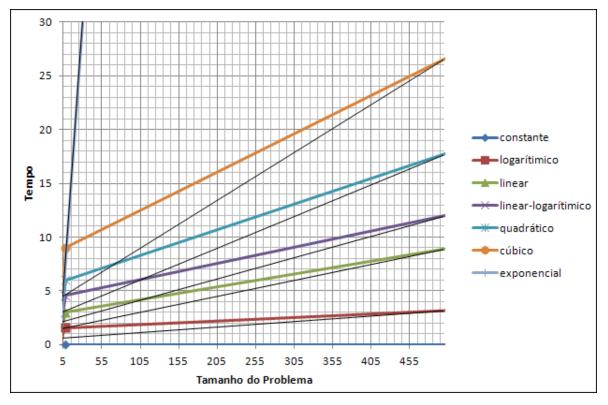




UMA VIAGEM AOS PROBLEMAS INTRATÁVEIS VIA HEURÍSTICAS COM PARALELISMO

Problemas Intratáveis

 Um problema é considerado intratável quando não existe um algoritmo conhecido que o resolva deterministicamente em tempo polinomial.



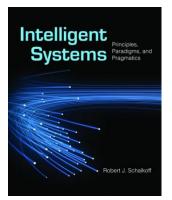
- Este tipo de problema é denominado NP.
 - Aquele que possui tempo polinomial não determinístico.

Problemas Intratáveis

Complexidade Computacional

	n(Size)							
Growth	1	20	50	100	1000	10,000	100,000	1,000,000
n n ²	1 × 10 ⁻⁶ sec	$\begin{array}{c} 20\times10^{-6}\\ \text{sec} \end{array}$	$\begin{array}{c} 50\times10^{-6}\\ \text{sec} \end{array}$	$\begin{array}{c} 1\times 10^{-4}\\ \text{sec} \end{array}$	$^{1\times10^{-3}}_{\rm sec}$	$^{1\times10^{-2}}_{\rm sec}$	0.1 sec	1 sec
n^2	1 × 10 ⁻⁶ sec	4×10^{-4} sec	$\begin{array}{c} 2.5\times 10^{-2}\\ \text{sec} \end{array}$	$\begin{array}{c} 1\times 10^{-2}\\ \text{sec} \end{array}$	1.0 sec	1.67 min	2.78 hours	11.6 days
n ³ 2 ⁿ	1 × 10 ⁻⁶ sec	8×10^{-3} sec	$\begin{array}{c} 2.5\times 10^{-3}\\ \text{sec} \end{array}$	$\begin{array}{c} 1.25\times10^{-1}\\ \text{sec} \end{array}$	16.8 min	11.6 days	3.17 × 10 ⁵ CENT	-
2"	2 × 10 ⁻⁶ sec	1.05 sec	35.7 years	sec 1 × 10 ⁻² sec 1.25 × 10 ⁻¹ sec 4.02 × 10 ¹⁴ CENT	-	-	-	-
exp (n)	2.7 × 10 ⁻⁶ sec	8.10 min	$\begin{array}{c} 1.65\times10^6 \\ \text{CENT} \end{array}$	-	-	-	-	-

Figure 3.5 Sample Growth of Problem Complexity (one step = 10^{-6} sec.)



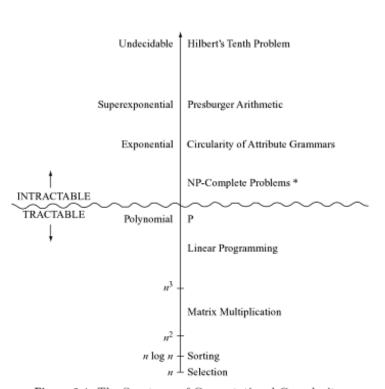


Figure 3.4 The Spectrum of Computational Complexity

P = NP?

http://www.claymath.org/millennium-problems/p-vs-np-problem



P=NP?
50 3D 4E 50 3F
ASCII encoding in hexadecimal

a conjecture encoded in binary form — P=NP?

Donald Knuth, qual é a sua opinião sobre P vs. NP?

17. Andrew Binstock, Dr. Dobb's: At the ACM Turing Centennial in 2012, you stated that you were becoming convinced that P = NP. Would you be kind enough to explain your current thinking on this question, how you came to it, and whether this growing conviction came as a surprise to you?

Don Knuth: As you say, I've come to believe that P = NP, namely that there does exist an integer M and an algorithm \mathcal{A} that will solve every n-bit problem belonging to the class NP in n^M elementary steps.

Some of my reasoning is admittedly naïve: It's hard to believe that $P \neq NP$ and that so many brilliant people have failed to discover why. On the other hand if you imagine a number M that's finite but incredibly large—like say the number 10 $\uparrow\uparrow\uparrow\uparrow\uparrow$ 3 discussed in my paper on "coping with finiteness"—then there's a humongous number of possible algorithms that do n^M bitwise or addition or shift operations on n given bits, and it's really hard to believe that all of those algorithms fail.

My main point, however, is that I don't believe that the equality P = NP will turn out to be helpful even if it is proved, because such a proof will almost surely be nonconstructive. Although I think M probably exists, I also think human beings will never know such a value. I even suspect that nobody will even know an upper bound on M.

Mathematics is full of examples where something is proved to exist, yet the proof tells us nothing about how to find it. Knowledge of the mere existence of an algorithm is completely different from the knowledge of an actual algorithm.

For example, RSA cryptography relies on the fact that one party knows the factors of a number, but the other party knows only that factors exist. Another example is that the game of $N \times N$ Hex has a winning strategy for the first player, for all N. John Nash found a beautiful and extremely simple proof of this theorem in 1952. But Wikipedia tells me that such a strategy is still unknown when N = 9, despite many attempts. I can't believe anyone will ever know it when N is 100.

More to the point, Robertson and Seymour have proved a famous theorem in graph theory: Any class $\mathcal C$ of graphs that is closed under taking minors has a finite number of minor-minimal graphs. (A minor of a graph is any graph obtainable by deleting vertices, deleting edges, or shrinking edges to a point. A minor-minimal graph H for $\mathcal C$ is a graph whose smaller minors all belong to $\mathcal C$ although H itself doesn't.) Therefore there exists a polynomial-time algorithm to decide whether or not a given graph belongs to $\mathcal C$: The algorithm checks that G doesn't contain any of $\mathcal C$'s minor-minimal graphs as a minor.

But we don't know what that algorithm is, except for a few special classes \mathcal{C} , because the set of minor-minimal graphs is often unknown. The algorithm exists, but it's not known to be discoverable in finite time.

This consequence of Robertson and Seymour's theorem definitely surprised me, when I learned about it while reading a paper by Lovász. And it tipped the balance, in my mind, toward the hypothesis that P = NP.

The moral is that people should distinguish between known (or knowable) polynomial-time algorithms and arbitrary polynomial-time algorithms. People might never be able to implement a polynomial-time-worst-case algorithm for satisfiability, even though *P* happens to equal *N P*.

O Problema do Caixeiro Viajante (PCV)

- Problema de Minimização
 - Encontrar o menor ciclo para um conjunto de cidades a serem visitadas obrigatoriamente e retornando a origem
 - Uma de suas instâncias considera a função objetivo como a distância euclidiana entre as cidades
 - Problema NP, inerentemente intratável
- Intratabilidade
 - Simétrica = $\frac{\Gamma(N)}{2}$
 - Assimétrica = $\Gamma(N)$

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Out[19]:= 12 413 915 592 536 072 670 862 289 047 373 375 038 521 486 354 677 760 000 000 000
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Origens do PCV Ciclo Euleriano Ciclo Hamiltoniano

 No ano de 1930, o problema se caracterizou como PCV por Merrill Flood da Universidade de Princeton e da RAND Corporation.

O Problema do Caixeiro Viajante (PCV)

$$f_{objetivo} = minimizar \sum_{i=1}^{N} \sum_{j=1}^{N} c_{ij} x_{ij}$$

Onde:

 $c_{ij} \rightarrow custo$ ou distância da cidade i para cidade j $N \rightarrow quantidade$ de cidades a serem visitadas

$$i, j, N \in \mathbb{N}^+, i \neq j$$

 $x_{ij} = \begin{cases} 1, & vai \ da \ cidade \ i \ para \ cidade \ j \\ 0, & n\~ao \ vai \ da \ cidade \ i \ para \ cidade \ j \end{cases}$

 $x_{ij} \rightarrow variáveis binárias de decisão$

Solution of a large-scale traveling-salesman problem

1954

G Dantzig, R Fulkerson, S Johnson

http://citeseer.ist.psu.edu/viewdoc/summary?doi=10.1.1.134.9319

Restrições:

$$\sum_{i=1}^{N} x_{ij} = 1 \qquad \forall_{j} \in \mathbb{N}^{+}$$

$$\sum_{i=1}^{N} x_{ij} = 1 \qquad \forall_i \in \mathbb{N}^+$$

$$\sum_{i,j\in S} x_{ij} \le |S| - 1 \quad \forall_{S} \subset \mathbb{N}^{+}$$

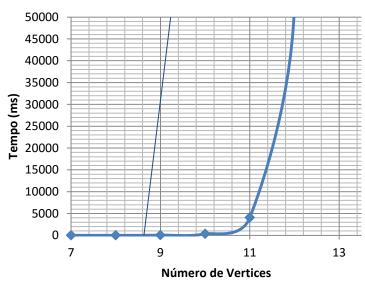
Modelagem Matemática programação binária

O Problema do Caixeiro Viajante (PCV)

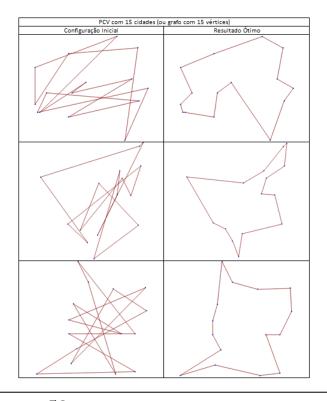
Complexidade

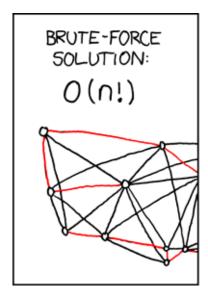
	Tempo (ms)
Número de Cidades	Força Bruta
13	743691
12	53093
11	4056
10	331
9	39
8	2
7	1

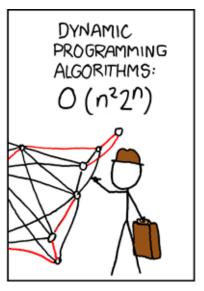
PCV com Força Bruta



PCV com 15 Cidades					
Força Bruta					
Solução Ótima	Tempo (ms)	Tempo (h)			
359,399	165340592	45,928			
317,232	165590540	45,997			
368,79	165517424	45,977			





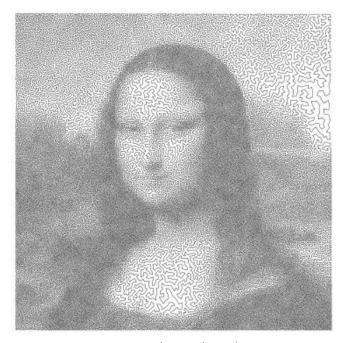




Travelling Salesman Problem XKCD http://xkcd.com/399/



George Dantzig (25K vértices) http://www.oberlin.edu/math/faculty/bosch/tspart-page.html



Mona Lisa (100K vértices) http://www.math.uwaterloo.ca/tsp/data/ml/monalisa.html

Travelling Salesman is a 2012 intellectual thriller film about four mathematicians solving the P versus NP problem, one of the most challenging mathematical problems in history.

http://en.wikipedia.org/wiki/Travelling Salesman (2012 film)

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JULIAN LETHBRIDGE

Traveling Salesman, 1995 Lithograph 43 3/4 x 42 in Edition 50

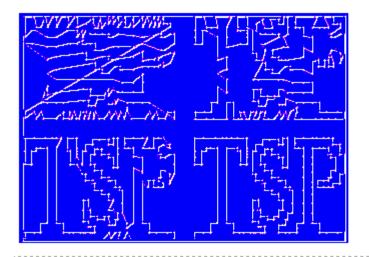


http://www.travellingsalesmanmovie.com/

http://www.larissagoldston.com/artists/julianlethbridge/index.aspx

TSPLIB

RUPRECHT-KARLS-UNIVERSITÄT HEIDELBERG



TSPLIB

TSPLIB is a library of sample instances for the TSP (and related problems) from various sources and of various types.

Note that it is not intended to add further problems instances (1.1.2013)

http://www.iwr.uni-heidelberg.de/groups/comopt/software/TSPLIB95/

Resolução exata do PCV com 24.978 cidades

Optimal Tour of Sweden



In May 2004, the traveling salesman problem of visiting all 24,978 cities in Sweden was solved: a tour of length 855,597 TSPLIB units (approximately 72,500 kilometers) was found and it was proven that no shorter tour exists. At the time of the computation, this was the largest solved TSP instance, surpassing the previous record of 15,112 cities through Germany set in April 2001. The current record an 85,900-city tour that arose in a chipdesign application.

- The 24,978 cities
- Pictures of the Sweden Tour
- How was the tour found?
- Details of the computation
- · Data sets for Sweden TSP and tour

Research Team

- David Applegate, AT&T Labs Research
- Robert Bixby, ILOG and Rice University
- Vašek Chvátal, Rutgers University
- · William Cook, University of Waterloo
- Keld Helsgaun, Roskilde University

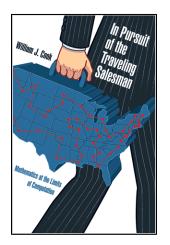
The cumulative CPU time used in the five branch-and-cut runs and in the cutting-plane procedures for the five root LPs was approximately 84.8 CPU years on a single Intel Xeon 2.8 GHz processor. Details of the computation times are given on the CPU Time page.

We began the initial cutting-plane procedure on the first LP in March 2003 and the final branch-andcut run finished in January 2004. After the run completed, we made a final check of the 14,827,429 cutting planes (besides subtour inequalities) that were generated and used during the process. This final checking was completed in May 2004.

http://www.math.uwaterloo.ca/tsp/sweden/index.html

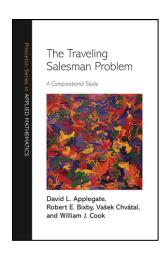
Quer saber mais sobre PCV?

http://www.math.uwaterloo.ca/tsp/



The Traveling Salesman Problem

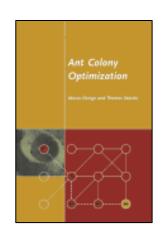
The Traveling Salesman Problem is one of the most intensively studied problems in computational mathematics. These pages are devoted to the history, applications, and current research of this challenge of finding the shortest route visiting each member of a collection of locations and returning to your starting point.



http://nbviewer.ipython.org/url/norvig.com/ipython/TSPv3.ipynb

In [74]: plot_tsp(repeated_altered_nn_tsp, USA_map)

- http://iridia.ulb.ac.be/~mdorigo/ACO/ACO.html
 - http://iridia.ulb.ac.be/~mdorigo/ACO/aco-code/public-software.html



Quer saber ainda mais sobre PCV?

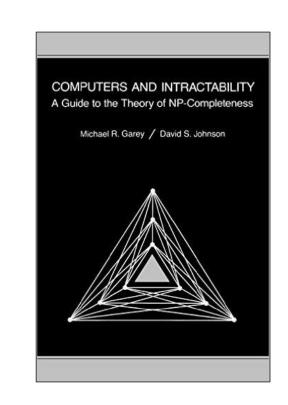
Recomendo fortemente!

http://davidsjohnson.net/TSPcourse.html

David S. Johnson - The TSP in Theory and Practice

Last Updated: 6 May 2014

- 1. Lecture 01, 21 January 2014 -- Course Introduction
- 2. Lecture 02, 28 January 2014 -- NP-Hardness
- 3. Lecture 03, 4 February 2014 -- Polynomial-Time Special Cases
- 4. Lecture 04, 11 February 2014 -- Polynomial-Time Special Cases Concluded, Pratical Heuristics Begun
- 5. Lecture 05, 18 February 2014 -- Tour Construction Heuristics
- 6. Lecture 06, 25 February 2014 -- Exploiting Geometry
- 7. Lecture 07, 4 March 2014 -- Local Optimization
- 8. Lecture 08, 11 March 2014 -- Lin-Kernighan and Beyond
- 9. Lecture 09, 25 March 2014 -- Optimization 101, or "How I spent my Spring Break"
- 10. Lecture 10, 1 April 2014 -- The Cutting Plane and Branch-and-Bound Approaches to TSP Optimization
- 11. Lecture 11, 8 April 2014 -- Branch & Cut & Concorde
- 12. Lecture 12, 15 April 2014 -- Optimal Tour Lengths for Random Euclidean Instances
- 13. Lecture 13, 22 April 2014 -- The Maximum TSP Problem
- 14. Lecture 14, 29 April 2014 -- More on Maximum TSP problems
- 15. Instructions for installing Concorde on a Mac (from Jeffrey Scholz)
- 16. <u>Lecture to Data Structures Course, 17 April 2014</u> -- The Traveling Salesman Problem



In Memoriam: David S. Johnson



exposition. The book is one of the most cited references in all of computer science, with over 55,000 citations. Johnson continued to write on NP-completeness throughout his career, maintaining a column on the subject from 1982 until 1992 in the Journal of Algorithms.

Born December 9, 1945, Johnson attended Amherst as an undergraduate studying mathematics and went on to MIT where he earned a PhD in mathematics in 1973 for his thesis Near-Optimal Bin Packing Algorithms. The same year, he started his long and productive career at Bell Labs (and later AT&T Research) that would last until 2014. During this time, he published continuously, including several books and well over 100 papers and articles, many of which concern the best ways to cope with computational intractability and his developing interest in the interplay between theoretical and experimental analysis in computer science.

Minha Abordagem ao Problema

Inteligência Artificial + Computação Paralela +
 Modelo Composicional (Teoria das Categorias e
 Programação Funcional) + Problema Complexo +
 Pesquisa Operacional

 $Computação Paralela \circ IA (problema) = Metaheurística Paralela$

$$f \circ g$$
 (problema)

$$M(TSP) \xrightarrow{TSP \to M(TSP^*)} M(TSP^*)$$

$$f \equiv SA \lor AG \lor ACO \lor OBL$$

$$M(TSP) \xrightarrow{TSP \xrightarrow{SA} M(TSP)} M(TSP) \xrightarrow{TSP \xrightarrow{2-Opt} M(TSP)} M(TSP^*)$$

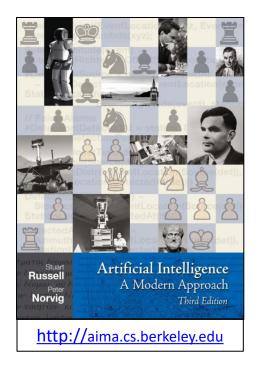
Resolução de Problemas através de Busca

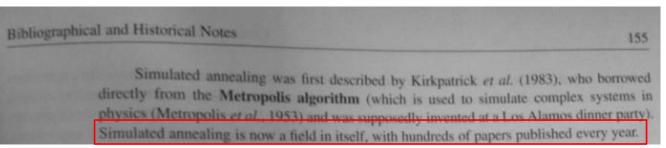
Simulated Annealing

```
void simulated annealing(const double initial temperature,
                         const double stopping criteria temperature,
                         const double decreasing_factor,
                         const int monte carlo steps,
                         tsp class& tsp instance,
                         tsp class::rand function rnd tsp,
                         std::function<double()> rnd probability)
    double temperature = initial temperature;
    while(temperature > stopping criteria temperature)
        double cycle_length = tsp_instance.do_cycle_length();
        tsp class temp tsp instance = tsp instance;
        int i = monte carlo steps;
        while(i-- > 0)
            temp tsp instance.do pertubation(rnd tsp, false);
            double temp_cycle_length = temp_tsp_instance.do_cycle_length();
            double dE = temp cycle length - cycle length;
            bool update = false;
            if(dE < 0.0)
                update = true;
            else
                //Inferior solution can be allowed to move from local optimal solution
                //using probability of acceptance based on Boltzmann's function
                auto boltzmannFunction = std::exp(-dE / temperature);
                auto acceptanceProbability = rnd probability();
                update = boltzmannFunction > acceptanceProbability;
            if(update)
                tsp instance = temp tsp instance;
                cycle_length = temp_cycle_length;
        temperature *= decreasing factor;
```

Resolução de Problemas através de Busca

Simulated Annealing





Optimization by simulated annealing

1983

S. Kirkpatrick, C. D. Gelatt, M. P. Vecchi

http://citeseer.ist.psu.edu/viewdoc/summary?doi=10.1.1.123.7607&rank=1

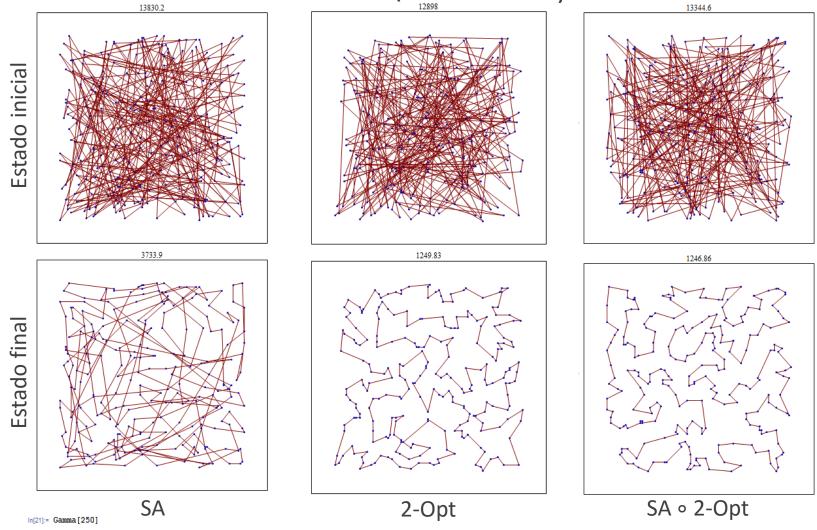


"The purpose of computing is insight, not numbers"

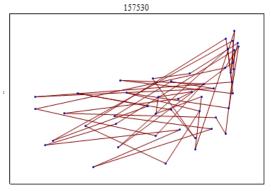
Numerical Methods for Scientists and Engineers
Richard Wesley Hamming
Turing Award 1968

Composição de soluções

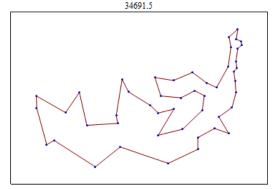
random250 (250 cidades)



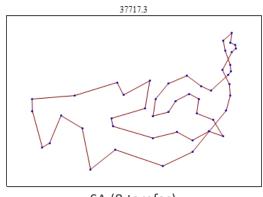
att48.tsp (48 cidades)



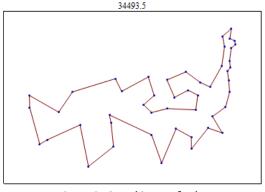
Estado Inicial



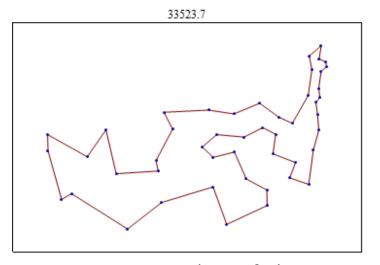
2-opt (8 tarefas)



SA (8 tarefas)



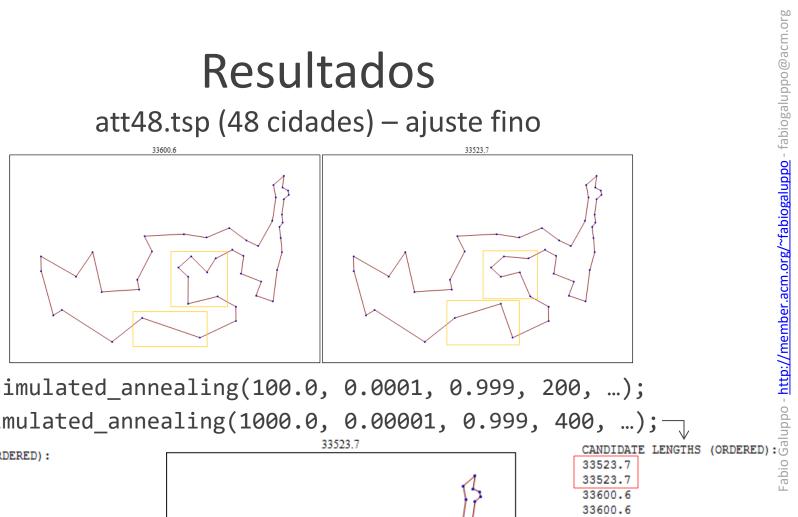
SA • 2-Opt (8 tarefas) 1 geração



SA • 2-Opt (8 tarefas) 10 gerações – resultado ótimo encontrado na geração 7

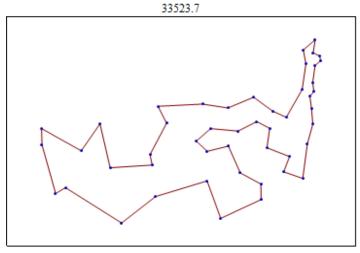
```
START SOLUTION:
[1](6734, 1453) : [8](7265, 1268) :
GraphPlot[{0 -> 1, 1 -> 2, 2 -> 3,}
[1](6734, 1453) : [16](6107, 669) :
[1](6734, 1453) : [8](7265, 1268) :
[1](6734, 1453): [40](6271, 2135)
[1](6734, 1453) : [16](6107, 669) :
[1] (6734, 1453) : [16] (6107, 669) : O. [1] (6734, 1453) : [16] (6107, 669) : O. [1] (6734, 1453) : [8] (7265, 1268) : O. [1] (6734, 1453) : [22] (6101, 1110)
[1] (6734, 1453) : [8] (7265, 1268) :
CANDIDATE LENGTHS:
34993.4
34344.2
34155.6
33831.7
34229.1
33600.6
34594
33523.7
CANDIDATE
33600.6
33831.7
34155.6
34229.1
34344.2
34594
34993.4
[1](6734, 1453) : [8](7265, 1268) :
GraphPlot[{0 -> 1, 1 -> 2, 2 -> 3,}
6051 ms
```

att48.tsp (48 cidades) – ajuste fino

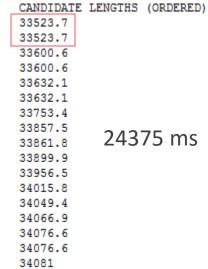


simulated_annealing(100.0, 0.0001, 0.999, 200, ...); simulated_annealing(1000.0, 0.00001, 0.999, 400, ...);

```
CANDIDATE LENGTHS (ORDERED):
33600.6
33600.6
33600.6
33600.6
33600.6
33600.6
33600.6
             18487 ms
33600.6
33600.6
33600.6
33600.6
33600.6
33600.6
33600.6
33600.6
33600.6
```



SA • 2-Opt



TSP Monad

```
//unit: value -> tsp_monad value
        [or tsp -> TSP tsp]
//bnd: tsp monad value -> (value -> tsp monad value) -> tsp monad value
        [or TSP tsp -> (t -> TSP tsp) -> TSP tsp]
struct tsp monad final
   typedef Maybe value type;
   typedef std::function<tsp_monad(value_type)> function_type;
   template <typename U>
   auto map(std::function<U(value_type)> f) const -> U
       return bnd(*this, f);
   auto map(function type f) const -> tsp monad
        return std::move(bnd<tsp monad>(*this, f));
   static auto unit(const value_type& value) -> tsp_monad
        tsp monad result;
        result.value = value;
        return std::move(result);
   static auto bnd(const tsp monad& t, function type f) -> tsp monad
        auto value = t.value;
       if (has_value(value))
            return std::move(f(value));
        return std::move(unit(nothing()));
   template <typename U>
   static auto bnd(const tsp monad& t, std::function<U(value type)> f) -> U
       if (has(t))
           return f(t.value);
        return U();
```

Monad

In functional programming, a monad is a structure that represents computations defined as sequences of steps. A type with a monad structure defines what it means to chain operations, or nest functions of that type together. This allows the programmer to build pipelines that process data in steps, in which each action is decorated with additional processing rules provided by the monad. [1] As such, monads have been described as "programmable semicolons"; a semicolon is the operator used to chain together individual statements in many imperative programming languages. [1] thus the expression implies that extra code will be executed between the statements in the pipeline. Monads have also been explained with a physical metaphor as assembly lines, where a conveyor belt transports data between functional units that transform it one step at a time. [2] They can also be seen as a functional design pattern to build generic types [3]

Purely functional programs can use monads to structure procedures that include sequenced operations like those found in structured programming. [4][5] Many common programming concepts can be described in terms of a monad structure, including side effects such as input/output, variable assignment, exception handling, parsing, nondeterminism, concurrency, and continuations. This allows these concepts to be defined in a purely functional manner, without major extensions to the language's semantics. Languages like Haskell provide monads in the standard core, allowing programmers to reuse large parts of their formal definition and apply in many different libraries the same interfaces for combining functions. [6]

Formally a monad consists of a type constructor M and two operations, bind and return (where return is often also called unit). The operations must fulfill several

Fonte: http://en.wikipedia.org/wiki/Monad (functional programming)

Left unit:

unit
$$a \times \lambda b$$
. $n = n[a/b]$

Right unit:

$$m \times \lambda a$$
. unit $a = m$

Associativity:

$$m \times (\lambda a. n \times \lambda b. o) = (m \times \lambda a. n) \times \lambda b. o$$

class Monad m where

return ::

 $m \times (\lambda a. n \times \lambda b. o) = (m \times \lambda a. n) \times \lambda b. o$

Figura 26: As leis da Monad (Adaptação da formalização de Wadler (WADLER, 1995)).

TSP Monad Leis

```
//Scala notation: unit(x) flatMap f == f(x)
{
    //Left Identity (1st Law)
    auto x = just(read_att48_tsp());

auto f = [](TSP::T t){ return ref(t).do_cycle_length(); };

double fun_result = bnd<double>(ret(x), f); //functional composition double oo_result = ret(x).map<double>(f); //object-oriented

bool fun_holds = fun_result == f(x);
bool oo_holds = oo_result == f(x);
```

1ª Lei

```
//Scala notation: m flatMap unit == m
{
    //Right Identity (2nd Law)
    auto m = make_TSP(read_att48_tsp());

auto fun_result = bnd(m, ret);
auto oo_result = m.map(ret);

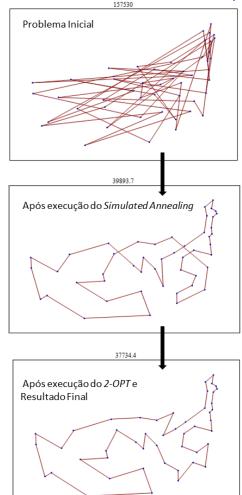
bool fun_holds = fun_result == m;
bool oo_holds = oo_result == m;
```

```
2ª Lei
```

```
//Scala notation: m flatMap f flatMap g == m flatMap (x => f(x) flatMap g)
    //Associativity (3rd Law)
    auto m = make TSP(read att48 tsp());
    auto f = [](TSP::T t) -> TSP
        auto u = ref(t);
        std::swap(u.cities[0], u.cities[1]);
        return make TSP(u);
   };
    auto g = [](TSP::T t) -> TSP
        auto u = ref(t);
        std::swap(u.cities[2], u.cities[3]);
        return make_TSP(u);
    };
    auto fun_result_1 = bnd(bnd(m, f), g);
   auto fun_result_2 = bnd(m, [&](TSP::T t) {
        return bnd(f(t), g);
   });
    auto oo result_1 = m.map(f).map(g);
   auto oo_result_2 = m.map([&](TSP::T t) {
        return f(t).map(g);
   });
    bool fun holds = fun result 1 == fun result 2;
   bool oo_holds = oo_result_1 == oo_result_2;
```

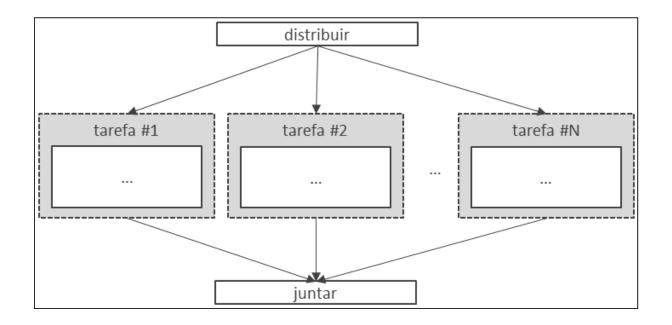
Pipeline com Simulated Annealing e 2-OPT TSP -> SA -> 2-OPT -> TSP'

```
//TSP -> SA -> 2-OPT -> TSP'
void Pipeline_Simple_SA_20PT(tsp_class& tsp_instance, unsigned int, unsigned int)
    auto a = Args<General args type>(make General args(1, 1));
    auto sa = Args<SA_args_type>(make_SA_args(1000.0, 0.00001, 0.999, 400));
    const char* pipeline description = "TSP -> SA -> 2-OPT -> TSP'";
   display args(pipeline description, a, sa, Args<ACO args type>(), Args<GA args type>());
    auto TSP = TSP(just(tsp instance));
    auto DisplayInput = Display("TSP INPUT", DisplayFlags::All);
    auto _SA = Measure(SA(sa[0].initial_temperature, sa[0].stopping_criteria_temperature,
                          sa[0].decreasing factor, sa[0].monte carlo steps),
                       Display("Simulated Annealing", DisplayFlags::EmitMathematicaGraphPlot));
    auto 20PT = Measure( 20PT(), Display("2-OPT", DisplayFlags::EmitMathematicaGraphPlot));
    auto DisplayOutput = Display("TSP OUTPUT", DisplayFlags::EmitMathematicaGraphPlot);
    //TSP -> SA -> 2-OPT -> TSP'
   auto result = TSP /* Instância do PCV */
                    .map( DisplayInput)
                    .map( SA /* Simulated Annealing functor */)
                    .map( 20PT /* 2-0PT functor */)
                    .map( DisplayOutput);
```



Onde entrou o Paralelismo?

Fork/Join pattern



Paralelismo e Composição

 $TSP \rightarrow NN \rightarrow Generations(g, ForkJoin(n, SA \rightarrow 2 - OPT)) \rightarrow TSP^*$

Considerações sobre o Modelo Composicional

 $TSP \rightarrow NN \rightarrow Generations(g, ForkJoin(n, Circular(ACO, SA \rightarrow 2 - OPT, GA)) \rightarrow k - OPT \rightarrow TSP^*$

 $f_1: TSP \to Generations(g', ForkJoin(n', GA)) \to TSP^*$ $f_2: TSP \to Generations(g'', ForkJoin(n'', SA)) \to TSP^*$

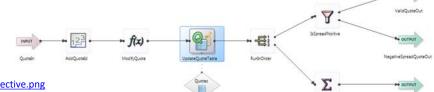
 $f_3: TSP \rightarrow Generations(g''', ForkJoin(n''', ACO)) \rightarrow TSP^*$

 $TSP \rightarrow NN \rightarrow Generations(g'''', ForkJoin(n'''', Circular(f_1, f_2, f_3)) \rightarrow 2 - OPT \rightarrow TSP^*$

 $TSP \rightarrow NN \rightarrow Generations(g, ForkJoin(n, Circular(ACO_{GPU}, GA_{GPU}, 3 - OPT_{GPU})) \rightarrow TSP^* \stackrel{\circ}{=}$

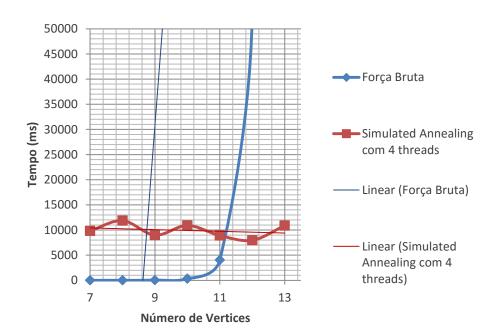
 $TSP \rightarrow NN \rightarrow Generations(g, ForkJoin(n, AdaptiveExecution(ACO_{GPU}, GA_{Cloud}, ...)) \rightarrow TSP^*$

Empresas investem em produtos que é baseado neste conceito de composição

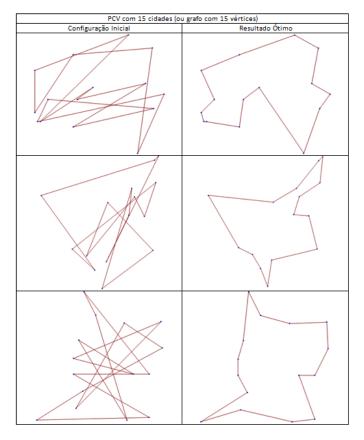


Revisitando a complexidade

	Tempo (ms)			
Número de Vertices	Força Bruta	Simulated Annealing com 4 threads		
13	743691	10885		
12	53093	7964		
11	4056	8901		
10	331	10908		
9	39	8979		
8	2	11852		
7	1	9843		



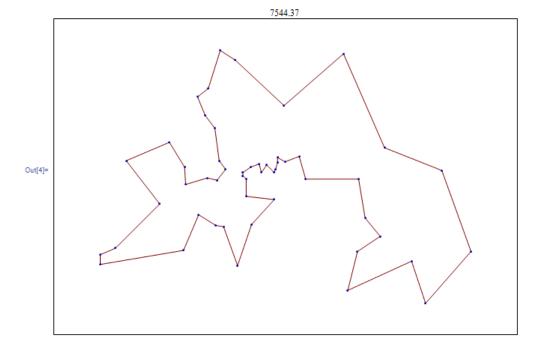
PCV com 15 Cidades					
SA					
Solução Ótima	Tempo (ms)	Tempo (s)			
359,399	9749	9,749			
317,232	13735	13,735			
368,79	13735	13,735			



Instância da TSPLIB berlin52.tsp com resultado ótimo

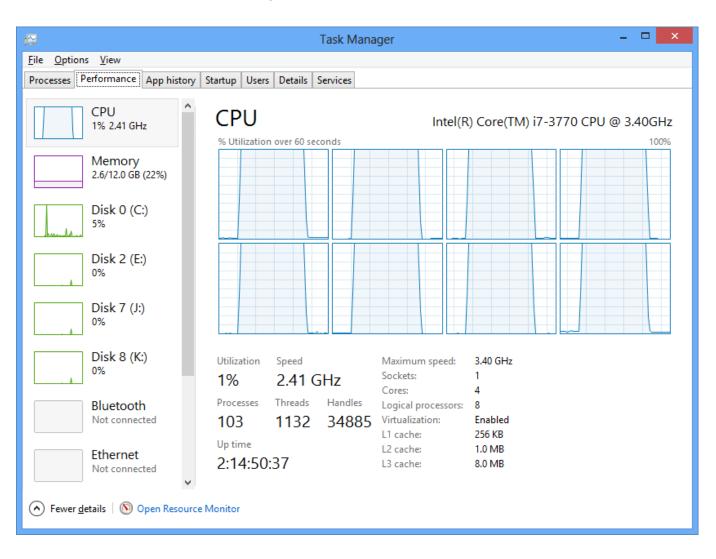
```
In[4]:= GraphPlot[{0 -> 1, 1 -> 2, 2 -> 3, 3 -> 4, 4 -> 5, 5 -> 6, 6 -> 7, 7 -> 8, 8 -> 9, 9 -> 10, 10 -> 11, 11 -> 12, 12 -> 13, 13 -> 14, 14 -> 15, 15 -> 16, 16 -> 17, 17 -> 18, 18 -> 19, 19 -> 20, 20 -> 21, 21 -> 22, 22 -> 23, 23 -> 24, 24 -> 25, 25 -> 26, 26 -> 27, 27 -> 28, 28 -> 29, 29 -> 30, 30 -> 31, 31 -> 32, 32 -> 33, 33 -> 34, 34 -> 35, 35 -> 36, 36 -> 37, 37 -> 38, 38 -> 39, 39 -> 40, 40 -> 41, 41 -> 42, 42 -> 43, 43 -> 44, 44 -> 45, 45 -> 46, 46 -> 47, 47 -> 48, 48 -> 49, 49 -> 50, 50 -> 51, 51 -> 0}, PlotLabel -> "7544.37", Frame -> True, VertexLabeling -> False,

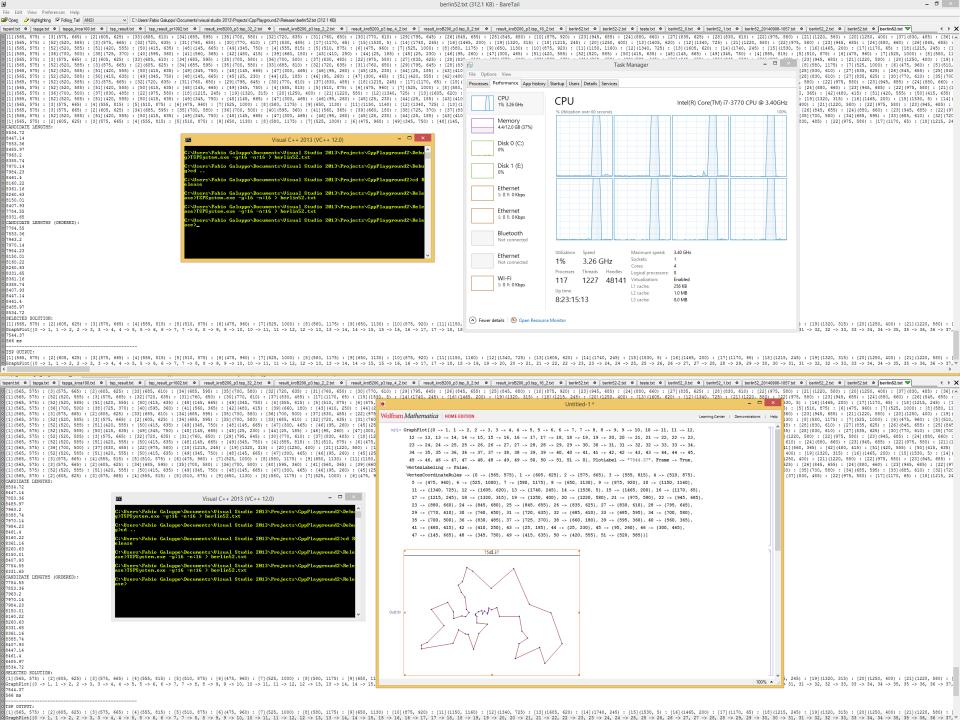
VertexCoordinateRules -> {0 -> {565, 575}, 1 -> {605, 625}, 2 -> {575, 665}, 3 -> {555, 815}, 4 -> {510, 875}, 5 -> {475, 960}, 6 -> {525, 1000}, 7 -> {580, 1175}, 8 -> {650, 1130}, 9 -> {875, 920}, 10 -> {1150, 1160}, 11 -> {1340, 725}, 12 -> {1605, 620}, 13 -> {1740, 245}, 14 -> {1530, 5}, 15 -> {1465, 200}, 16 -> {1170, 65}, 17 -> {1215, 245}, 18 -> {1320, 315}, 19 -> {1250, 400}, 20 -> {1220, 580}, 21 -> {975, 580}, 22 -> {945, 685}, 23 -> {880, 660}, 24 -> {845, 680}, 25 -> {845, 655}, 26 -> {835, 625}, 27 -> {830, 610}, 28 -> {795, 645}, 29 -> {770, 610}, 30 -> {760, 650}, 31 -> {720, 635}, 32 -> {685, 610}, 33 -> {685, 595}, 34 -> {700, 580}, 35 -> {700, 500}, 36 -> {830, 485}, 37 -> {725, 370}, 38 -> {660, 180}, 39 -> {595, 360}, 40 -> {560, 365}, 41 -> {480, 415}, 42 -> {410, 250}, 43 -> {25, 185}, 44 -> {25, 230}, 45 -> {95, 260}, 46 -> {300, 465}, 47 -> {145, 665}, 48 -> {345, 750}, 49 -> {415, 635}, 50 -> {420, 555}, 51 -> {520, 585}}]
```



```
SOLUTION ARGUMENTS:
TSP -> NN -> Generations ( g, ForkJoin ( n, SA -> 2-OPT ) ) -> TSP'
GENERAL ARGUMENTS:
Number of Iterations or Generations = 32
Number of Tasks in Parallel = 32
SIMULATED ANNEALING ARGUMENTS:
   Initial Temperature = 1200
   Stopping Criteria Temperature = 1e-007
   Decreasing Factor = 0.991
   Monte Carlo Steps = 120
TSP INPUT:
[1](565, 575) : [2](25, 185) : [3](345, 750) : [4](945, 685) : [5]
GraphPlot[{0 \rightarrow 1, 1 \rightarrow 2, 2 \rightarrow 3, 3 \rightarrow 4, 4 \rightarrow 5, 5 \rightarrow 6, 6 \rightarrow 7,}
GENERATION: 1
START SOLUTION:
[1](565, 575): [22](520, 585): [49](605, 625): [32](575, 665):
GraphPlot[{0 \rightarrow 1, 1 \rightarrow 2, 2 \rightarrow 3, 3 \rightarrow 4, 4 \rightarrow 5, 5 \rightarrow 6, 6 \rightarrow 7,}
8980.92
  ...
```

Desempenho e Paralelismo

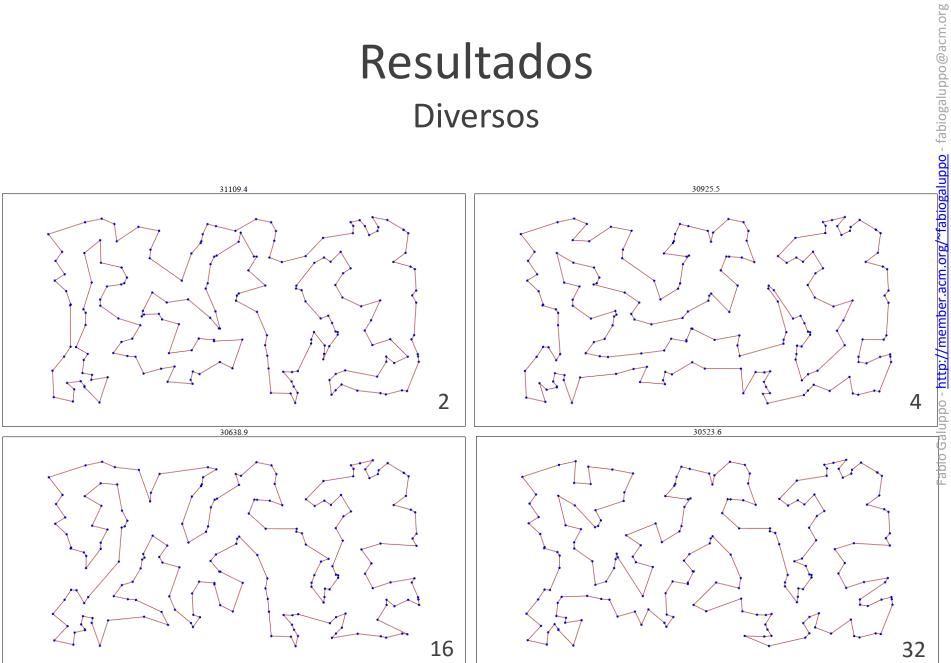




Resultados Diversos

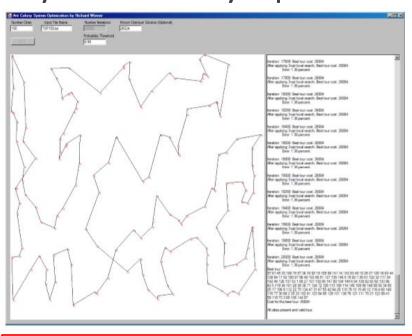
Instância	Número de	Distând	cia Euclidiana (Melhor Res	ultado com 32 ta	arefas)	
TSPLIB	Cidades	Obtido*	Literatura*	Diferença (%)	Iteração	
att48		33523.7		0.0000	14 1	
	48	33523.7	10628 (ATT) ou ~33523	0.0000	9 2	
		33523.7		0.0000	3 3	
kroA100		21285.4		0.0000	15 1	
	100	21285.4	21282	0.0000	26 2	
	100	21285.4		0.0000	8 3	
		21285.4		0.0000	8 4	
	100	22139.1		0.0000	3 1	
kroB100		22139.1	22141	0.0000	6 2	
KIODIOO		22139.1		0.0000	5 3	
		22139.1		0.0000	2 4	
	100	20750.8	0.0000	5 1		
kroC100		100	20750.8	20749	0.0000	29 2
KIOCIOO		20750.8	20743	0.0000	29 3	
		20750.8		0.0000	15 4	
	100	21294.3	0.0000	16 1		
kroD100		21294.3	21294	0.0000	10 2	
KIODIOO		21294.3		0.0000	13 3	
			21294.3		0.0000	27 4
	100	22068.8	22068	0.0000	8 1	
kroE100		22068.8		0.0000	12 2	
		22068.8		0.0000	6 3	
		22068.8		0.0000	23 4	

Diversos



Observação

Ant System Colony Optimization



The Ant Colony System produces results that are superior to those obtained by this author using either simulated annealing or genetic programming. What is particularly attractive is the small number of parameters that need to be tuned, especially compared to simulated annealing.

About the author



Richard Wiener is Chair of Computer Science at the University of Colorado at Colorado Springs. He is also the Editor-in-Chief of JOT and former Editor-in-Chief of the Journal of Object Oriented Programming. In addition to University work, Dr. Wiener has authored or co-authored 22 books and works actively as a consultant and software contractor whenever the possibility arises. His latest book, published by Thomson, Course Technology in April 2006, is entitled *Modern Software Development Using*

C#/.NET.

Publicação

Resoluções do problema do caixeiro viajante aplicando algoritmos de aproximação, randomização e heurísticas de inteligência artificial com computação paralela

Autor(a): Fabio Razzo Galuppo
Orientador: Prof. Dr. Nizam Omar

Defesa: 19/02/2014

Linha de Pesquisa: Computação e Sistemas Adaptativos

Resumo

Esta obra tem como essência a aplicação das técnicas denominadas coletivamente de metaheurística paralela no contexto do Problema do Caixeiro Viajante (PCV), um dos problemas de otimização combinatória mais importantes. A abordagem desta obra contém uma proposta composicional que permite a criação de pipelines para endereçar o problema. Estas técnicas extraídas da Computação Paralela associadas aos algoritmos de busca da Inteligência Artifi cial possibilitam grandes oportunidades para a exploração do espaço de estados do problema em questão. Usando as combinações propostas, boas soluções ou, até mesmo ótimas soluções, emergirão dentro de um tempo de processamento satisfatório, possibilitando suas aplicações na resolução de problemas reais semelhantes. É fundamental revisitar as soluções existentes e fornecer para a indústria as melhores opções para resolução do PCV utilizando as capacidades computacionais contemporâneas e as variedades de equipamentos disponíveis. Nesta obra, estão incluídos a implementação, a análise e a medição de algoritmos aplicados ao contexto referenciado.

Palavras-Chave: Computação paralela, computação concorrente, algoritmos, desempenho e otimização de algoritmos, metaheurística, metaheurística paralela, inteligência arti ficial, problema do caixeiro viajante e otimização combinatória.

Texto completo: PDF