

- First step: Define the semantic domains
- Second Step: Define Big Step semantics

1 Semantic Domain - *Python*

Relação de Transição para Expressões:

$$s, b \vdash exp \Downarrow s', b', v'$$

Relação de Transição para Comandos:

$$b, s \vdash C \Downarrow b[C \mapsto b(C)], s'$$

Bindings:

$$(identifier \mapsto cell) \cup (identifier \mapsto closure).$$

Store:

$$cell \mapsto value$$

$$value = string_literal \cup num_literal \cup bool_literal \cup list$$

Regras de atribuição

Atribuição de Elemento não lista e que não exista nos bindings:

$$\frac{s, b \vdash \text{exp} \Downarrow s', b', v'}{b, s \vdash \text{identifier} = \text{exp} \Downarrow b'[\text{identifier} \mapsto v], s'} \text{ identifier} \notin \text{dom}(b), v \notin \text{list}$$

Atribuição de Elemento não lista e que exista nos bindings:

$$\frac{s, b \vdash \text{exp} \Downarrow s', b', v'}{b, s \vdash \text{identifier} = \text{exp} \Downarrow b'[b(\text{identifier}) \mapsto v], s'} \text{ identifier} \in \text{dom}(b), v \notin \text{list}$$

Atribuição de Elemento lista e que não exista nos bindings:

$$\frac{s, b \vdash \text{exp} \Downarrow s', b', v' \quad k := \text{alloc}(s', v)}{b, s \vdash \text{identifier} = \text{exp} \Downarrow b'[\text{identifier} \mapsto k], s'[k \mapsto v]} \text{ identifier} \notin \text{dom}(b), v \in \text{list}$$

Atribuição de Elemento lista e que exista nos bindings:

$$\frac{s, b \vdash \text{exp} \Downarrow s', b', v'}{b, s \vdash \text{identifier} = \text{exp} \Downarrow b', s'[b'(\text{identifier}) \mapsto v]} \text{ identifier} \in \text{dom}(b), v \in \text{list}$$

Atribuição em listas lista:

$$\frac{\begin{array}{l} s, b \vdash \text{exp} \Downarrow s', b', v' \quad s, b \vdash \text{exp} \Downarrow s', b', v'' \quad s, b \vdash \text{exp} \Downarrow s', b', v''' \\ (list-trib) \end{array} \quad v' \in \text{list}, v'' \in \text{num_literal}}{b, s \vdash \text{exp1}[\text{exp2}] = \text{exp3} \Downarrow b', s'[b'(\text{exp1}(\text{exp2})) \mapsto \text{exp3}]}$$

Regras de desvio condicional:

$$(Expression\ evaluated\ as\ True) \frac{s, b \vdash exp \Downarrow s', b', v'}{b, s \vdash if(exp) : C1 else : C2 \Downarrow b'[C1], s'[C1]} v = True$$

$$(Expression\ evaluated\ as\ False) \frac{s, b \vdash exp \Downarrow s', b', v'}{b, s \vdash if(exp) : C1 else : C2 \Downarrow b'[C2], s'[C2]} v = False$$

For loop

$$(For\ loop) \frac{s, b \vdash exp \Downarrow s', b', v'}{b, s \vdash for\ identifier\ in\ exp : command \Downarrow b'[command], s'[command]} exp \mapsto k, k \mapsto v, v \in list$$

$$(string-add) \frac{E1 \Downarrow string_literal1 \quad E2 \Downarrow string_literal2}{E1 + E2 \Downarrow string_literal3} string_literal3 = string_literal1.string_literal2$$

$$(num-add) \frac{E1 \Downarrow num_literal1 \quad E2 \Downarrow num_literal2}{E1 + E2 \Downarrow num_literal3} num_literal3 = num_literal1 + num_literal2$$

$$(num-sub) \frac{E1 \Downarrow num_literal1 \quad E2 \Downarrow num_literal2}{E1 - E2 \Downarrow num_literal3} num_literal3 = num_literal1 - num_literal2$$

$$(num-mult) \frac{E1 \Downarrow num_literal1 \quad E2 \Downarrow num_literal2}{E1 * E2 \Downarrow num_literal3} num_literal3 = num_literal1 * num_literal2$$

$$(num-div) \frac{E1 \Downarrow num_literal1 \quad E2 \Downarrow num_literal2}{E1 / E2 \Downarrow num_literal3} num_literal3 = num_literal1 / num_literal2$$

$$(variable-set) \frac{s}{identifier = value} (s[identifier] = cell, s[cell] = value, s', b')$$

$$(if-clause-true) \frac{if(exp) : command1 else : command2 \quad exp \Downarrow True}{command1} (s', b')$$

$$(if-clause-false) \frac{if(exp) : command1 else : command2 \quad exp \Downarrow False}{command2} (s', b')$$

$$(access-list) \frac{s[list_identifier \mapsto cell] \quad cell \mapsto value \quad exp \Downarrow num_literal}{list_identifier[exp]} (value, s, b)$$

Esquema da mquina:

$$\langle G, \rho, I, O, M, T_E, N_{MT} \rangle \triangleright \langle G', \rho', I', O', M', T'_E, N'_{MT} \rangle$$

Operation Call:

$$\frac{\begin{array}{l} indegree(w) = 0 \quad \bar{a} = Eval_{\rho}(\overline{E}) \quad A'_c = A_c - \{w \mapsto v \mid v \in V\} \quad A'_d = A_d - \{w \mapsto v \mid v \in V\} \\ G = \langle V[w : S!\overline{E}, w' : S?\overline{X}], A_c[w \mapsto w'], A_d \rangle \quad G' = \langle V[w' : S?\overline{X}], A'_c, A'_d \rangle \end{array}}{\langle G, \rho, I, O, M, T_E, N_{MT} \rangle \triangleright \langle G', \rho, I, O[\langle S, w', \bar{a} \rangle], M[\langle w : S!\overline{E}, w', now(), N_{MT} \rangle], T_E, N_{MT} \rangle}$$