

2-3 Correctness of Horner's rule

a. In terms of Θ -notation, what is the running time of this code fragment for Horner's rule?

Answer

$\Theta(n)$

b. Write pseudocode to implement the naive polynomial-evaluation algorithm that computes each term of the polynomial from scratch. What is the running time of this algorithm? How does it compare to Horner's rule?

Answer

NAIVE-POLINOMIAL-EVALUATION(A, x)

```
1   $sum = 0$ 
2  for  $j = 1$  to  $A.length - 1$ 
3       $y = A[j]$ 
4      for  $i = 1$  to  $j$ 
5           $y = y \cdot x$ 
6       $sum = sum + y$ 
```

This naive implementation has $T(n) = n(n-1)(n-2)\dots(n-k) = n!$. So, the worst-case running time is $\Theta(n!)$. As we seen on **prob1-1** the $n!$ is pretty bad compared to the linear complexity of Horner's rule.

c.

Answer

d.

Answer