Genetic Algorithms and Function Minimization

University of Geneva

Metahuristique pour l'Optimisation November 29 2021

(UNIGE) Genetic Algorithm 2021 1/10

Evolutionary Algorithms and Genetic Algorithm

Evolutionary Algorithms:

- Family based on Darwin's "survival of the fittest" evolution
- Organisms adapt to more complex tasks
- Computer Model: Best individuals evolve through reproduction and mutation

Genetic Algorithms:

- Population Metaheuristics
- Individual = genome/chromosome
- Fitness = quality of individual
- Problem evolves by generations (iterations)
 - Selection of best individuals
 - Crossover + Mutation



(UNIGE) Genetic Algorithm 2021 2 / 10

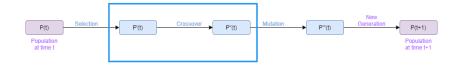


Selection

ullet Randomly draw N individuals from P(t) according to fitness values, to increase the good individuals in each generation

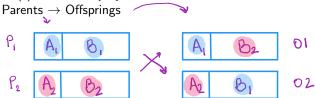
4□ ▶ 4回 ▶ 4 亘 ▶ 4 亘 ・ りへ@

(UNIGE) Genetic Algorithm 2021 3/10



Crossover

• P"(t) is formed by hybridization:



(UNIGE) Genetic Algorithm 2021 3/10





Mutation

- Individuals in P"(t) undergo mutation with small $p_{mutation}$
- Errors in genome allow the emergence of new individuals/solutions
- P"'(t) becomes P(t+1)

- 4日 > 4個 > 4 種 > 4種 > 種 > 種 の Q (C)

(UNIGE) Genetic Algorithm 2021 3 / 10

The three GA operations: Selection, Crossover, and Mutation do <u>not</u> guarantee that the best individual/selection is present in the next generation/iteration.

We can perform Elitism:

• Best individual at Generation P(t) replaces worst individual at P(t+1) if fitness of best individual at P(t) is better than that of the best individual at P(t+1)

End Condition

- Max number of generations/iterations
- Fitness Stagnation



(UNIGE) Genetic Algorithm 2021 4 / 10

Genetic Algorithms and Function Minimization

TP Objective:

Minimize the function:

$$f(x,y) = -\left|\frac{1}{2}x\sin\left(\sqrt{|x|}\right)\right| - \left|y\sin\left(30\sqrt{\left|\frac{x}{y}\right|}\right)\right|$$

where $x, y \in [10, 1000] \cap \mathbb{N}$.

(UNIGE) Genetic Algorithm 2021 5/10

Individuals and Fitness

Each individual, a solution of the optimization problem, should be represented as a binary sequence made up of two halves, representing the x and y coordinates of the individual.

Each coordinate will be made up of m=10 bits.

In order to compute the fitness, the use of a mapping function is needed:

$$map: x \mapsto \frac{x}{2^m}(b-a)+a$$

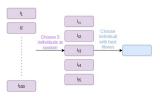
to ensure that $map(x) \in [a, b] \cap \mathbb{R}$.

Starting from the above formula, propose a mapping function to minimize f(x,y), i.e., for $x,y\in[10,1000]\cap\mathbb{N}$.

(UNIGE) Genetic Algorithm 2021 6 / 10

Selection

5 Tournament



Repeat N times

Crossover

 One Point with Mid-Break



- $p_c = 0.6$
- Repeat $\frac{N}{2}$ times

Mutation

- $p_m = 0.01$
- $p_m = 0.1$

Powents

X_{t}	¥.
X2	Yz
offsprings	
V	M

ı

Set Population Size N to 100

(UNIGE) Genetic Algorithm 2021 7 / 10

GA Pseudo Code

```
1: generation = 0
2: Randomly initialize population N = 100
3: while not stop condition do
        generation ++
4.
        Compute Individuals' Fitnesses .
5:
6.
        Selection: 5 Tournament -
        Crossover: One Point Mid-Break -
7:
        Mutation -
8:
        if no new best then
9:
             insert best, remove worst
10:
11:
        end if
12: end while
13: output best
```

(UNIGE) Genetic Algorithm 2021 8 / 10

Work To Do

Function Visualization

Visualize the function to minimize in a 3D space to get an idea on how difficult is to find its global minimum, and localize its global minimum.

Tests

You should experiment the following:

- Selection 5 Tournament, One Point Mid-Break Crossover with p_c , Mutation with p_m =0.01
- Selection 5 Tournament, One Point Mid-Break Crossover with p_c , Mutation with p_m =0.1
- Selection 5 Tournament, no Crossover, Mutation with p_m =0.01
- Selection 5 Tournament, no Crossover, Mutation with p_m =0.1

(UNIGE) Genetic Algorithm 2021 9 / 10

Work To Do

Evaluations

Measure and present:

- The cumulative empirical probability to reach the following solution qualities (optimum, relative distance to optimum = 1.0%, relative distance to optimum = 2.5%) over the number of evaluations.
- Report the best, average and standard deviation of fitness among the populations for 10^3 , 10^4 , and 10^5 fitness evaluations. $\xrightarrow{\times -0.8 \text{ is}}$ The number of fitness evaluations can be estimated by the product of the population size with the number of generations. These statistics should be computed over several runs of the genetic

algorithm (e.g., 10 runs).

2021

10 / 10