

# The Variability of the Belgian Business Survey Indicator and its Predictive Power

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Thanks my family and friends the National Bank of Belgium Laurent, ... KULeuven
"Statistics are the heart of democracy."
- Simeon Strunsky

#### **Abstract**

This Master Thesis explores the Variance of the Belgian Business Survey. Several finding concerning the nature and properties of the Variance are found as the bounds and relation with the mean.

In a second part, the predictive power of the variance is examined and it's found that

It's also the first time that à Markov Switching model is used in this context. It was showed that  $\dots$ 

# Keywords

Business Surveys - Business Barometer - Survey Variance - Markov Switching -

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#### Introduction

?

Business Survey Indicator / Business Barometer / Business Confidence Indicator A widespread method to predict the evolution of National Economies is the survey-based Business indicator. Belgium have been collecting this indicator for more than 60 years. This long evolution

- Talk about tradition of improving BSB

This Thesis is included in the continuity of a long tradition of papers proposing improvement and ways to add value to the Business Barometer (......) will propose ways to add information to the Belgian Business Barometer, that could also be applied to others Since 1968, the National Bank of Belgium publishes each month the national

## The Business Survey Indicator

This first chapter is a more general description of the Belgian Business Survey Indicator, that we will also call the Business Barometer. We will present it different calculations, the weighting that are applied and

explain the two types of weightings

#### 2.1 History

In 1954 started the Business Survey of the National Bank of Belgium.

At the European level, in 1961, is launched the launched by the Commission decision of 15 November 1961. The first survey was the harmonised business survey in the manufacturing industry conducted in 1962. Since then, the sector coverage of the programme has widened considerably. The BCS programme was extended to the construction sector and to investment plans in the manufacturing sector in 1966, to consumers in 1972, to the retail trade in 1984, and to the services sector in 1996. More info see (?)

Almost 20 years later, in 1972, results where first synthesised in an indicator. It has since then been well known for been a very informative and useful indicator. For example in 1999 an article was published in the Wall Street Journal titled "Euroland Discovers A Surprise Indicator: Belgian Confidence" (?) that noted the accuracy and of it predictions.

Today Now-casting is a well studied subject and very important for public and private organisation to have an as clear as possible view of the state of the economy.

With the study of business cycles, that will be looked at more in details in part ...., nowcasting are two important objectives that will be looked at in this work.

Due to the structure of Belgian economy and ... it was also shown as been a good predictor for the European economy ?

changes in 2009 see later (section 2.3)

#### 2.2 Sampling Method

. . .

### 2.3 Objective and Methodology

A large improvement of the indicator happened in 2009 which was explained in a working paper untitled "The National Bank of Belgium's new business survey indicator" (?)

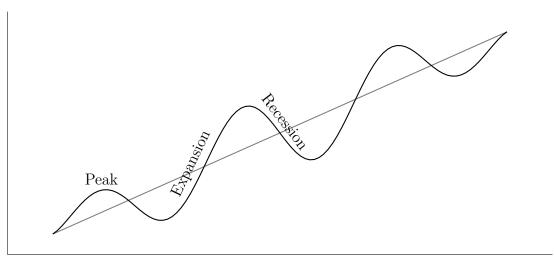
Objectives:

Using specific questions to identify the business cycles and turning points

It can be included in what's now called nowcasting, which is now and short time forecasting of the evolution of the economy.

- only take a limited amount of questions into account, the most relevant ones (3-4 questions)
- inclusion of the services in the global indicator
- lighten smoothing method

#### A Business Cycles theory



#### **Quality Criterion**

- high correlation with Economical Indicators
- fluctuation that's mostly explained by the conjuncture
- predictive power for the future months more information can be found in ? ...

## 2.4 Questionnaire

.... questionnaire can be found in appendix Questions taken into account for RS975: .... originally question Q18, 27, 32 and 33, for simplicity numbered here as 1, 2, 3 and 4.

#### 2.5 Calculation of the Indicator

This section presents the method for calculating the indicator. The calculation in itself is standard, but the different ways to write it are important for interpretation and to better understand the following chapters.

#### 2.5.1 Unweighted Indicator

The calculation of the unweighted indicator for a specific question at a specific time can be written as follow;

$$E(X) = \frac{\sum_{i=1}^{n} x_i}{n}$$
 (2.1)

where

 $x_i$  is the answer of the respondent i and can each take value -1, 0 and 1 n is the total of respondents

Since x can only take three different values, we can decompose it into

$$E(X) = \frac{\sum_{i=1}^{n} x_{+i} + \sum_{i=1}^{n} x_{Ni} + \sum_{i=1}^{n} x_{-i}}{n}$$
 (2.2)

where

 $x_{+i}$ ,  $x_{Ni}$  and  $x_{-i}$  are the positive(+), neutral (N) and negative (-) answers of the respondent i

n is the total of respondents

We know that  $\sum_{i=1}^{n} x_{Ni} = 0$  so we can write

$$E(X) = \frac{\sum_{i=1}^{n} x_{+i}}{n} + \frac{\sum_{i=1}^{n} x_{-i}}{n}$$
 (2.3)

 $\sum_{i=1}^{n} x_{+i}/n$  is the proportion of positive answers and  $\sum_{i=1}^{n} x_{-i}/n$  is the negative proportion of negative answer so for simplicity we write it

$$E(X) = \pi_{+} - \pi_{-} \tag{2.4}$$

where  $\pi_+$  and  $\pi_-$  are the proportion of respondents answering positive and negative.  $\pi$  is use here also in the probabilistic way as it can also be seen as the probability that a respondent answers positive, negative or neutral  $(\pi_0)$  with  $\pi_+ + \pi_0 + \pi_- = 1$ .

#### 2.5.2 Weighted Indicator

Globalisation procedure

Weighting procedure

Calculation

$$E(X) = \frac{\sum_{i=1}^{n} (\omega_i p_i x_i)}{\sum_{i=1}^{n} \omega_i p_i}$$
 (2.5)

where

 $x_i$  is the answer of the respondent i and can each take value -1, 0 and 1

 $p_i$  is the weight of the globalisation of the company i  $\omega_i$  is the weight of the company i

$$E(X) = \frac{\sum_{i=1}^{n} \omega_{+i} p_{+i} x_{+i} + \sum_{i=1}^{n} \omega_{Ni} p_{Ni} x_{Ni} + \sum_{i=1}^{n} \omega_{-i} p_{-i} x_{-i}}{n}$$
(2.6)

$$E(X) = \frac{\sum_{i=1}^{n} \omega_{+i} p_{+i} x_{+i}}{n} + \frac{\sum_{i=1}^{n} \omega_{-i} p_{-i} x_{-i}}{n}$$
 (2.7)

$$E(X) = \pi_{+} - \pi_{-} \tag{2.8}$$

where  $\pi_+$  and  $\pi_-$  are the **weighted** proportion of respondents answering positive and negative.  $\pi$  is use here also in the probabilistic way as it can also be seen as the probability that a respondent answers positive, negative or neutral  $(\pi_0)$  with  $\pi_+ + \pi_0 + \pi_- = 1$ .

#### 2.5.3 Properties

E(X) has -1 as lower bound and 1 as upper bound

#### 2.5.4 Take different questions into account

The previous calculations where specific to each question. The published indicators are usually taking different survey questions into account. For example the Industry indicator that we will be interested in is composed of four questions that have all the same weight:

Industry Business Indicator = 
$$\frac{E(X_{Q1}) + E(X_{Q2}) + E(X_{Q3}) + E(X_{Q4})}{4}$$
 (2.9)

where  $E(X_{Q1})$ ,  $E(X_{Q2})$ ,  $E(X_{Q3})$  and  $E(X_{Q4})$  are the different averages for question 18, 27, 32 and 33 (can be weighted or unweighted)

#### Variance of the Indicator

The variance is, with the mean, one of the first tool for Statisticians to study a certain variable.

In the context of the Business Survey, the variance haven't been used much.

#### difference sampling error and variance

here variance is a measure of the "dispersion" of the answers.

#### difference between nominal and continuous variable variance

As done for the Indicator, two different variances will be take into account here, the weighted and the unweighted variance of the indicator.

#### 3.0.1 Variance of the Unweighted Indicator

The main variance cite

$$Var(X) = E\left[(X - E(X))^{2}\right]$$

$$= E\left(X^{2}\right) - E\left(X\right)^{2}$$

$$= \left(\frac{\sum_{i=1}^{n} x_{+i}^{2}}{n}\right) + \left(\frac{\sum_{i=1}^{n} x_{Ni}^{2}}{n}\right) + \left(\frac{\sum_{i=1}^{n} x_{-i}^{2}}{n}\right) - E(X)^{2}$$

$$= \pi_{+} + \pi_{-} - (\pi_{+} - \pi_{-})^{2}$$

$$= \pi_{+} + \pi_{-} = x_{+i}, x_{-i}^{2} = x_{-i} \text{ and } E(X) = \pi_{+} - \pi_{-}$$
(3.1)

We then have several different ways to write the previous equation;

$$Var(X) = \pi_{+} + \pi_{-} - (\pi_{+} - \pi_{-})^{2}$$

$$= \pi_{+} + \pi_{-} - E(X)^{2}$$

$$= 1 - \pi_{n} - E(X)^{2}$$
(3.2)

Equation 3.1 is interesting

Equation 3.2

Equation 3.3

# 3.0.2 Generalization for Weighted Indicators / Variance of the Weighted Indicator

$$Var(X) = \frac{1}{\sum \omega_i p_i} \sum_{i=1}^{N} \omega_i p_i (X_i - \bar{X})^2$$
(3.4)

$$Var(X) = \pi_{+} + \pi_{-} - (\pi_{+} - \pi_{-})^{2}$$
(3.5)

$$= \pi_{+} + \pi_{-} - E(X)^{2} \tag{3.6}$$

$$= 1 - \pi_0 - E(X)^2 \tag{3.7}$$

#### 3.0.3 Properties

Property 1: The variance of X is bounded between -1 and 1

Property 2: The variance = A5 and E(X)

Property 3: .....

## 3.1 Take different questions into account

### 3.2 Discussion regarding the 'true variance'

There is another way to calculate the variance that have been ignored for, that is calculating the variance for each lowest group of globalisation, and then combine those calculated variances.

Interestingly, it have been calculated for several Questions of the business barometer, and it is approximately 10 times smaller than the variance based on all the answer a ones.

The reasons why it will not be used here - losing information - weight of globalisation taken into account in the weighted variance

# Indicator of the Evolution of Individual Responses

#### Why this new indicator

Also Called Z indicator

Can be better understood as the indicator of the Changes in individual answers between t-1 and t

An issue for this indicator was to find an optimal name for it so that it would be easily understand by the largest number.

#### Explain the new indicator

$$t - 1 \begin{vmatrix} t & & t \\ - & 0 & + \\ 0 & \pi_{--} & \pi_{-0} & \pi_{-+} \\ 0 & \pi_{0-} & \pi_{00} & \pi_{0+} \\ + & \pi_{+-} & \pi_{+0} & \pi_{++} \end{vmatrix}$$

The Indicator of the evolution of the individual responses can be obtained by

$$E(Z) = \pi_{0+} + \pi_{-0} - \pi_{+0} - \pi_{0-} + 2\pi_{-+} - 2\pi_{+-}$$

$$\tag{4.1}$$

where

 $\pi$  is the proportion/probability of respondent answering (-,0,+) at t-1 and (-,0,+) at time t

$$E(Z) = \begin{array}{c|cccc} & - & \mathbf{0} & + \\ \hline - & 0 & +1 & +2 \\ \mathbf{0} & -1 & 0 & +1 \\ + & -2 & -1 & 0 \end{array}$$
 (4.2)

#### The Indicator of the Evolution of Individual Responses

$$\pi_{++} + \pi_{+0} + \pi_{+-} + \pi_{0+} + \pi_{00} + \pi_{0-} + \pi_{-+} + \pi_{-0} + \pi_{--} = 1$$
 (4.3)

# Variance of the Evolution of Individual Responses / Volatility of Responses

That we will also call the **volatility of the indicator**, in the sens that the variance of the evolution of the indicator account for the dispersion of the difference in answers over a two times period.

In this case, the highers variance of Z, will be obtained when half of the companies went from a negative answer to a positive answer and the other half did the opposite and changed from a positive answer at t-1 to a negative answer at t.

waza see Chapter 5

The idea is that this variance of Z is complementary to the estimation of Z since they have two very interesting but different interpretations. Further interpretation will be

#### 5.1 Presentation

$$\pi_{++} + \pi_{+0} + \pi_{+-} + \pi_{0+} + \pi_{00} + \pi_{0-} + \pi_{-+} + \pi_{-0} + \pi_{--} = 1 \tag{5.1}$$

$$Var(Z) = \pi_{0+} + \pi_{-0} + \pi_{+0} + \pi_{0-} + 4\pi_{-+} + 4\pi_{+-}$$

$$-(\pi_{0+} + \pi_{-0} - \pi_{+0} - \pi_{0-} + 2\pi_{-+} - 2\pi_{+-})^{2}$$

$$= \pi_{0+} + \pi_{-0} + \pi_{+0} + \pi_{0-} + 4\pi_{-+} + 4\pi_{+-} - E(Z)^{2}$$

$$= 1 - \pi_{++} - \pi_{00} - \pi_{--} + 3\pi_{+-} + 3\pi_{-+} - E(Z)^{2}$$
(5.2)

$$Var(Z) = \begin{pmatrix} - & 0 & + \\ - & 0 & +1 & +4 \\ 0 & +1 & 0 & +1 \\ + & +4 & +1 & 0 \end{pmatrix} - \begin{pmatrix} - & 0 & + \\ - & 0 & +1 & +2 \\ 0 & -1 & 0 & +1 \\ + & -2 & -1 & 0 \end{pmatrix}^{2}$$

$$= \begin{pmatrix} - & 0 & + \\ - & 0 & +1 & +4 \\ 0 & +1 & 0 & +1 \\ + & +4 & +1 & 0 \end{pmatrix} - (E(Z))^{2}$$

$$= 1 + \begin{pmatrix} - & 0 & + \\ - & -1 & 0 & +3 \\ 0 & 0 & -1 & 0 \\ + & +3 & 0 & -1 \end{pmatrix} - (E(Z))^{2}$$

#### 5.1.1 Properties

Property 1: the variance of Z is bounded between -1 and 1

Property 2:

#### Seasonal Effects

The National Bank, before publishing the Business Survey Indicator, applies a X11 seasonal correction

The literature about seasonal effects is very rich and variate

- NBB developed JDemetra+ and has since been recommended by the ECB and Eurostat for all NSI in Europe.
- at the same time the department of Business Survey uses as a X11 adapted method to correct for seasonality because don't want to correct for previous publications.

Methodology

- test for seasonality
- run the analysis without corrections
- apply corrections and see if more accurate

#### 6.1 JDemetra+

- 6.2 X11
- 6.2.1 Seasonal correction of the Indicator
- 6.2.2 Seasonal correction of the Variance
- 6.2.3 Seasonal correction of the Indicator of the Evolution
- 6.2.4 Seasonal correction of the Variance of Z
- 6.2.5 Seasonal correction of the Proportions

#### 6.3 Limitations

explain the issue of seasonal correction on "future data"

# Non-Response, Dropout and Attrition

Aside of Seasonal effect, there are three main biases that could arise in the context of the BSI; non-reponse, dropout and attrition

- cor(time, var) = 0.5Add period!

Table 7.1: Correlation Matrix

	E_3	Var_3	$Z_{-3}$	Var_Z_3	GDP	GDP_year
$E_{-}3$	1	-0.555	0.231	-0.487	0.473	0.703
$Var_3$	-0.555	1	-0.078	0.847	-0.196	-0.167
$Z_{-}3$	0.231	-0.078	1	-0.053	0.160	0.011
$Var_{-}Z_{-}3$	-0.487	0.847	-0.053	1	-0.031	-0.056
GDP	0.473	-0.196	0.160	-0.031	1	0.628
$GDP\_year$	0.703	-0.167	0.011	-0.056	0.628	1

# 7.1 Non-Response

## 7.2 Dropout

Non parametric test?

#### 7.3 Attrition

Attrition / Panel Conditioning Master Thesis done about the Belgian Labor Force Survey, where attrition was studied ?

Non parametric test?

limitation: only some periods of

# **Exploratory Analysis**

- 8.1 Data At hand
- 8.2 Small vs Large
- 8.3 By Sector
- 8.4 Correlations

There are three different correlations that need to be looked at

# 8.5 Correlation between questions

Table 8.1: Correlation Matrix

	$E_{-}1$	E_2	E_3	E_4
$E_{-1}$	1	0.262	0.412	0.416
$E_{-}2$	0.262	1	0.939	0.876
$E_{-3}$	0.412	0.939	1	0.938
$E_4$	0.416	0.876	0.938	1

# 8.6 Auto-Correlation

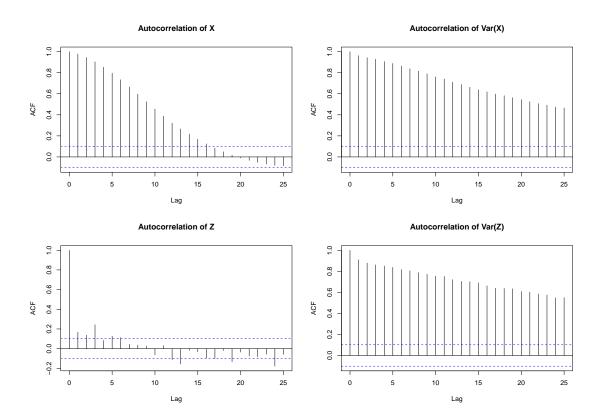


Figure 8.1: Plot

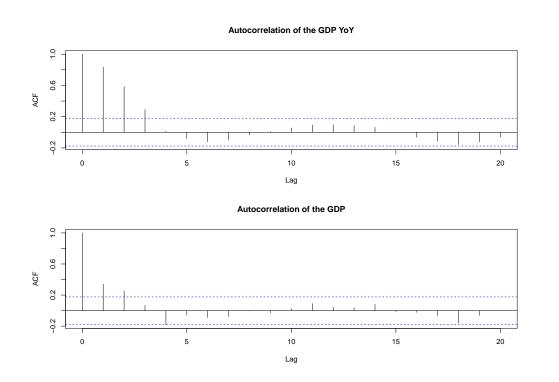


Figure 8.2: Plot

#### 8.7 Correlation with GDP

Belgian industry claims 25% of the labour force in Belgium and have been shown as been the best indicator to predict the year to year GDP citeAlain Quartier and Isabelle

#### GDP vs GDP YoY

Table 8.2: Correlation Matrix

	GDP	GDP_year	E_I	$E_{-}1$	E_2	E_3	$E_{-4}$
GDP	1	0.628	0.502	0.222	0.439	0.473	0.556
$GDP\_year$	0.628	1	0.707	0.092	0.729	0.703	0.717
$\mathrm{E}_{-}\mathrm{I}$	0.502	0.707	1	0.483	0.952	0.982	0.963
$\mathrm{E}_{-}1$	0.222	0.092	0.483	1	0.266	0.414	0.406
$\mathrm{E}_{ ext{-}2}$	0.439	0.729	0.952	0.266	1	0.942	0.886
$E_{-}3$	0.473	0.703	0.982	0.414	0.942	1	0.938
$\mathrm{E}_{ extsf{-}4}$	0.556	0.717	0.963	0.406	0.886	0.938	1

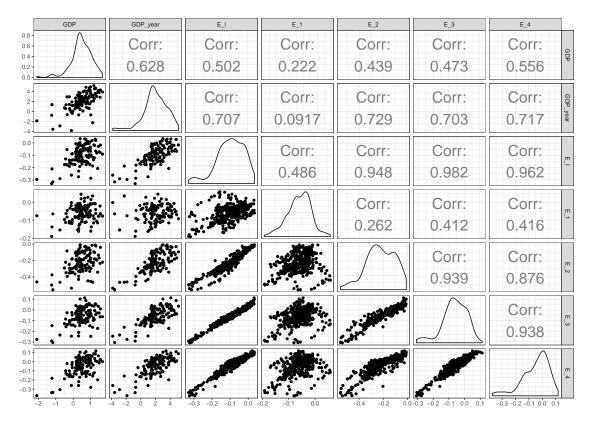


Figure 8.3: Plot

# 8.8 GDP vs Explanatory Indicators

Table 8.3: Correlation Matrix

	GDP	GDP_year	$\mathrm{E}_{-}\mathrm{I}$	Var_I	$\mathrm{Z}_{-}\mathrm{I}$	Var_Z_I
GDP	1	0.628	0.502	-0.074	0.151	0.021
$GDP\_year$	0.628	1	0.707	-0.101	-0.058	0.011
$E\_I$	0.502	0.707	1	-0.615	0.166	-0.484
$Var_{-}I$	-0.074	-0.101	-0.615	1	-0.045	0.887
$Z\_I$	0.151	-0.058	0.166	-0.045	1	-0.072
$Var_{-}Z_{-}I$	0.021	0.011	-0.484	0.887	-0.072	1

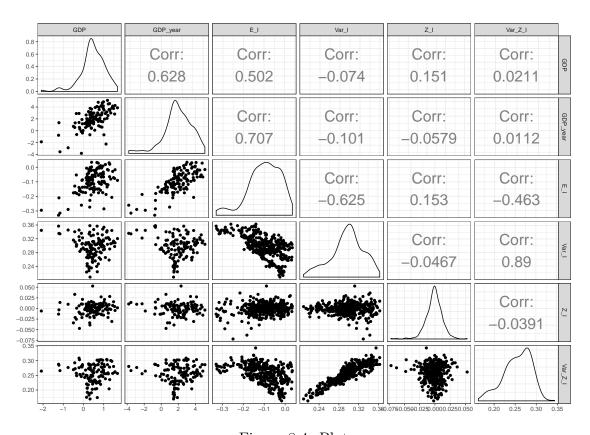


Figure 8.4: Plot

**GDP** vs Indicator

GDP vs Var

GDP vs Z

GDP vs Var Z

# 8.9 Specificity of question 3 and 4, are peoples predictions correct?

Table 8.4: Correlation Matrix

	GDP	GDP_year	E_3	E_3_lag1	E_3_lag2	E_3_lag3	E_3_lag4
GDP	1	0.628	0.477	0.520	0.545	0.546	0.531
$\mathrm{GDP}$ _year	0.628	1	0.707	0.679	0.673	0.628	0.560
$E_{-3}$	0.477	0.707	1	0.969	0.948	0.906	0.846
$E_3$ lag1	0.520	0.679	0.969	1	0.975	0.940	0.892
$E_3$ lag2	0.545	0.673	0.948	0.975	1	0.974	0.933
$E_3$ lag3	0.546	0.628	0.906	0.940	0.974	1	0.969
$E_3$ lag4	0.531	0.560	0.846	0.892	0.933	0.969	1

Table 8.5: Correlation Matrix

	GDP	GDP_year	E_4	E_4_lag1	E_4_lag2	E_4_lag3	E_4_lag4
GDP	1	0.628	0.558	0.555	0.591	0.566	0.536
$GDP\_year$	0.628	1	0.719	0.650	0.647	0.593	0.501
$\mathrm{E}_{ extsf{-}4}$	0.558	0.719	1	0.959	0.941	0.890	0.804
$E_4_{lag1}$	0.555	0.650	0.959	1	0.970	0.928	0.863
$E_4_{lag2}$	0.591	0.647	0.941	0.970	1	0.970	0.917
$E_4_{lag3}$	0.566	0.593	0.890	0.928	0.970	1	0.959
$E_4_{1}$	0.536	0.501	0.804	0.863	0.917	0.959	1

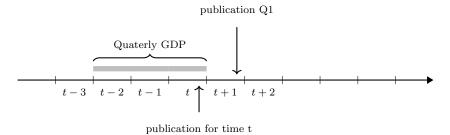
# Linear (Auto-Regressive) Models

#### 9.1 Method

#### 9.1.1 Month vs Quarterly data

Error to aggregate everything to quarterly - lost of information

#### 9.1.2 Timing of the Data



The quaterly GDP and the Quaterly YoY GDP is set at t. This is the common way to go..

publication GDP Q1

Quaterly GDP

Jan Feb Man Apr May Jun Jul Aug Sep

publication BSI of March

# 9.2 Linear Model

$$GDP_{t} = \mu + \sum_{i=1}^{n} \sum_{j=0}^{q} \beta_{1,j} X_{i,t-j} + \epsilon_{t}$$
(9.1)

Auto-Regressive model

$$GDP_{t} = \mu + \sum_{j=1}^{p} \phi_{j}GDP_{t-j} + \sum_{i=1}^{n} \sum_{j=0}^{q} \beta_{1,j}X_{i,t-j} + \epsilon_{t}$$
(9.2)

where

 $GDP_t$  GDP growth over the last semester

 $X_{i,t}$  monthly predictors

 $\mu$  constant

 $\phi_j$  auto-regressive coefficients

 $\beta_{i,j}$  regression coefficients

## 9.3 Model

		Linear Re	egression			
	Year on Year GDP (in %)					
	(1)	(2)	(3)	(4)		
Constant	3.434*** (0.170)	1.114*** (0.255)	$-1.829^{**}$ (0.867)	$-4.052^{***}$ (0.922)		
3 months lag of YoY GDP		0.690*** (0.066)	0.525*** (0.078)			
BSI	15.053*** (1.364)	4.957*** (1.387)	10.621*** (2.079)	22.080*** (1.392)		
Variance			12.831*** (3.628)	27.506*** (3.349)		
Observations $R^2$	124 0.499	123 0.743	123 0.767	124 0.679		
Adjusted R <sup>2</sup> Residual Std. Error F Statistic	0.495 $1.172$ $121.753***$	0.738 0.847 173.266***	0.761 0.809 130.755***	0.673 0.943 127.781***		

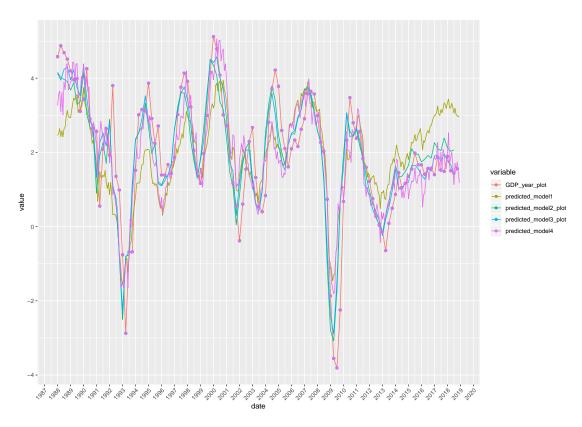


Figure 9.1: Plot

 ${\rm GDP\_year}$ 

	(1)	(2)	(3)	(4)
Constant	3.364***	$-4.052^{***}$	-3.993***	-0.985
	(0.173)	(0.922)	(0.917)	(0.797)
E_I	14.491***	22.080***	21.579***	5.629***
	(1.390)	(1.392)	(1.421)	(2.091)
$\mathrm{E_{I_diff}}$	11.538*		8.181	24.063***
	(6.560)		(5.309)	(4.488)
Var_I		27.506***	27.105***	7.179**
		(3.349)	(3.340)	(3.433)
GDP_year_lag1				0.687***
·				(0.076)
${\mathrm{R}^{2}}$	0.512	0.679	0.685	0.813
Adjusted $R^2$	0.504	0.673	0.677	0.806
Residual Std. Error	1.162	0.943	0.938	0.729
F Statistic	63.468***	127.781***	86.947***	128.113***

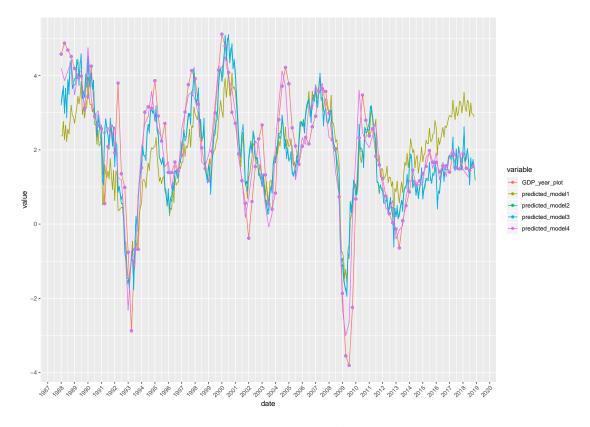


Figure 9.2: Plot

	(1)	(2)
$\mathrm{E}_{-}\mathrm{I}$	22.783***	23.088***
	(1.340)	(1.319)
Var_I	22.151***	28.508***
	(6.050)	(3.133)
$Z_{-}I$	$-24.279^{***}$	-25.008***
	(5.765)	(5.746)
Var_Z_I	6.609	
	(5.383)	
Constant	-4.090***	$-4.265^{***}$
	(0.871)	(0.861)
${\mathrm{R}^{2}}$	0.726	0.722
Adjusted $R^2$	0.717	0.716
Residual Std. Error	0.878 (df = 119)	0.880 (df = 120)
F Statistic	$78.806^{***} (df = 4; 119)$	$104.133^{***} (df = 3; 120)$

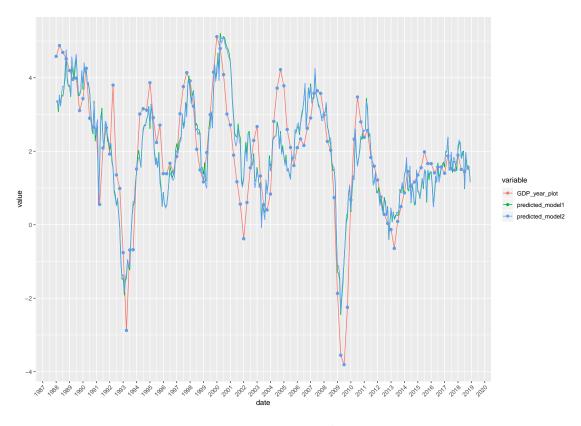


Figure 9.3: Plot

- 9.4 Evaluation
- 9.4.1 R-square
- 9.4.2 AIC and BIC
- 9.4.3 Mean Square Prediction Error
- 9.4.4 Diebold-Mariano Test
- 9.4.5 Out-of-Sample performances
- $9.5 \log(GDP)$
- 9.6 Variance(X) VS Variance(Z)
- 9.7 Take Question 1 out of the calculation of the Indicator

# Markov Switching Models

#### Small Introduction + why are we using it

Since the pioneer work by ?, Markov Switching models have been largely used to model business cycles.

Markov Switching models have been very popular since? to model business cycles and predict Turning points (see?, ...).

Able to predict the 2008 financial crisis if used MS-VAR model?

## 10.1 Model(s) Specification

#### **10.1.1** Notation

 $\begin{array}{lll} S_t = \{0,1\} & \text{states} \\ N=2 & \text{number of states (2)} \\ T=372 & \text{number of observations} \\ x_{t=1\dots T} & \text{(hidden) state at time t} \\ y_{t=1\dots T} & \text{Change of the Industrial production indices at time t} \\ p_{i=1\dots n,j=1\dots n} & \text{probability of transition from state $i$ to state $j$} \\ F(y|\theta) & \text{probability distribution of an observation, parametrized on $\theta$} \end{array}$ 

#### 10.1.2 Model

#### Model

$$y_{t} = \begin{cases} \mu_{0} + \sum_{j=1}^{p} \phi_{j} GDP_{t-j} + \epsilon_{t} & \text{if } S_{t} = 0\\ \mu_{1} + \sum_{j=1}^{p} \phi_{j} GDP_{t-j} + \epsilon_{t} & \text{if } S_{t} = 1 \end{cases}$$
(10.1)

where  $\epsilon$  is  $N(0, \sigma_s)$   $\mu_s = \beta_0 = c_s = \alpha_s \quad \text{regime-specific mean}$   $\beta_s = \phi_s \quad \text{regime-specific auto-regressive parameter}$   $\sigma_s \quad \text{regime-specific variance}$ 

#### Transition equation/probability

$$P = P(S_t = s_t \mid S_{t-1} = s_{t-1}) = \begin{bmatrix} 1 - p_t & p_t \\ q_t & 1 - q_t \end{bmatrix}$$
 (10.2)

We have then,

$$P(S_t = 1 \mid S_{t-1} = 1) = p_t$$

$$P(S_t = 0 \mid S_{t-1} = 1) = 1 - p_t$$

$$P(S_t = 0 \mid S_{t-1} = 0) = q_t$$

$$P(S_t = 1 \mid S_{t-1} = 0) = 1 - q_t$$

$$P(S_t = 0 \mid S_{t-1} = 1) = 1 - p$$

$$P(S_t = 0 \mid S_{t-1} = 0) = q_t$$

$$P(S_t = 1 \mid S_{t-1} = 0) = 1 - q_t$$

or

$$P = P(S_t = s_t \mid S_{t-1} = s_{t-1}) = \begin{bmatrix} 1 - p_t & p_t \dots \\ q_t \dots & 1 - q_t \end{bmatrix}$$
 (10.3)

# Conclusion

A large

It was seen that

Discussion

#### Recruitment procedure and panel data

not real sampling theory

#### Z that takes more periods into account

#### Limitations

Variance influence by drop-out, attrition, ...

# Improve the Business Survey

Change participants

Mo

From a statisticians point of view, a more sampling theory Including SRS or else would be more optimal

#### Further Research

More complex Nowcasting model with Space space models / MIDAS .... Combine mixed models and Markov Chain for Panel Data (?) State Space Model Bayesian estimation?

# List of Abbreviations

BSI Business Survey Indicator GDP

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Appendix

# Further Explanation of the Evolution of the responses ...

Notation	$x_{t-1}$	$ x_t $	$ z_t $
$\pi_{}$	-1	-1	0
$\pi_{-0}$	-1	0	1
$\pi_{-+}$	-1	1	2
$\pi_{0-}$	0	-1	-1
$\pi_{00}$	0	0	0
$\pi_{0+}$	0	1	1
$\pi_{+-}$	1	-1	-2
$\pi_{+0}$	1	0	-1
$\pi_{++}$	1	1	0

Further Explanation of the Markov Switching model ...

#### CONJUNCTUURONDERZOEKINGEN - NIJVERHEID

TEL. + 32 (0)2 221 49 97

Product:

E-mail: nationalbanksurveys@nbb.be

Kruis per vraag, het vakje aan dat overeenstemt met uw antwoord en stuur per product uw antwoorden binnen de 10 dagen terug. U kunt gebruik maken van ons gratis faxnummer 0800 95 969 (enkel geldig binnen België) of van het faxnummer + 32 (0)2 221 31 07 (vanuit het buitenland).

**OKTOBER 2018** 

Gelieve enkel voor het hierboven vermelde product te antwoorden. Vermeld alle schommelingen, zelfs indien ze van geringe omvang zijn. Antwoord elke maand op alle vragen. Indien u in de beschouwde maand het product niet heeft geproduceerd (of geen bestellingen heeft ontvangen), vermeldt u "verminderd". Antwoord "onveranderd" gedurende de maand(en) dat deze toestand voortduurt totdat de productie herneemt. Uw antwoorden worden strikt vertrouwelijk behandeld. Verloop en beoordeling Uw <u>huidige</u> gezamenlijke orderpositie voor dit product Uw productietempo voor dit product is in september 2018 t.o.v. augustus 2018: beschouwt u als: 27 1 hoger dan 5 normaal 9 lager dan 5 onveranderd 9 vertraagd Hou geen rekening met schommelingen als gevolg van het maandelijks veranderlijke aantal werkdagen of betaald verlof. Indina un onderneming uitsluitend uit voorraad levert, dient u "orderpositie" op te vatten als "het peil van de vraag" naar dit vragenlijst voorbehouden Tijdens de afgelopen 3 maanden was de trend van uw productie voor dit product: Indien u het <u>huidige</u> fabricatietempo voor dit product handhaaft, is uw activiteit nog verzekerd voor ongeveer: 16 1 stiigend 5 onveranderd 9 dalend Hou evenwel geen rekening met louter seizoengebonden maand(en) en/of schommelingen. gedeelten van een maand. g Uw verkoopprijzen voor dit product zijn in september 2018 Te ramen op basis van uw orderpositie of, bij gebrek hieraan, op t.o.v. augustus 2018: basis van uw productieplannen. gebruik van 5 onveranderd 9 gedaald 17 1 gestegen Uw huidige positie inzake bestellingen uit het buitenland Geef de tendens van uw prijzen aan op basis van uw contracten of voor dit product beschouwt u als: ğ 31 1 hoger dan 9 lager dan Alle rechten Uw huidige voorraad van dit product beschouwt u, voor het Indien uw onderneming uitsluitend uit voorraad levert, dient u uw buitenlandse orderpositie op te vatten als "het peil van de 5 normaal 18 1 hoger dan 9 lager dan normaal (voldoende) buitenlandse vraag" naar dit product. - 2008 -(te hoog) (te laag) Kruis "niet van toepassing" aan indien u dit niet van product nooit uitvoert. Kruis "niet van toepassing" aan niet van indien u nooit voorraad hebt van dit product. Bank van België Vooruitzichten voor de volgende drie maanden Bij het beantwoorden van de volgende twee vragen (22 en 26), mag u geen melding maken van de zuivere seizoenschommelingen die het verloop van de bestellingen gedurende de maand <u>september 2018</u> kunnen hebben beïnvloed. De werkelijke tendens van de bestellingen moet dus tot uiting komen. Het personeel (arbeiders en technici) tewerkgesteld voor de fabricatie van dit product zal volgens u: 32 \_\_\_ 1 worden 5 onveranderd 9 worden verminderd uitgebreid blijven Uw ontvangen bestellingen voor dit product vanwege de Het invoeren van gedeeltelijke werkloosheid dient als een vermindering van het personeel te worden beschouwd. binnenlandse markt zijn in september 2018 t.o.v. augustus 2018: 22 1 vermeerderd 5 onveranderd 9 verminderd De vraag van uw klanten naar dit product zal volgens u: Hou eveneens rekening met de van andere afdelingen van uw firma 33 1 belangrijker 9 minder 5 even ontvangen bestellingen en met loonwerk. belangrijk zijn dan gewoonlijk tijdens die periode van het jaar. Kruis "niet van toepassing" aan indien u dit product nooit op de binnenlandse markt levert. Geef enkel de tendens van de vraag van de klanten weer en laat toepassing derhalve de zuivere seizoenschommelingen buiten beschouwing. Uw ontvangen bestellingen voor dit product vanwege de Uw productie zal voor dit product volgens u: buitenlandse markt zijn in september 2018 t.o.v. augustus 2018: 36 1 toenemen 5 gelijk blijven 9 afnemen 26 1 vermeerderd 5 onveranderd 9 verminderd Uw verkoopprijzen van dit product zullen volgens u: Hou eveneens rekening met loonwerk. 34 1 stijgen 5 onveranderd 9 dalen Kruis "niet van toepassing" aan indien u dit niet van bliiven product nooit op de buitenlandse markt levert. 4100N REFERENTIE: Enquête:

Figure 1: The Business Survey Questionnaire in Dutch for the Industrial Sector

Code

R code for Seasonal Adjustment

R code for Creating Lags

R code for Linear (Auto-Regressive) Models

R code for Markov Switching Models

