## Exploratory analysis

#### March 18, 2021

```
[91]: %reload_ext autoreload
      %autoreload 2
      default_figsize=(14,12)
[92]: import datasets
      import numpy as np
      import pandas as pd
      import seaborn as sn
      import matplotlib.pyplot as plt
      import matplotlib
      matplotlib.rcParams['figure.figsize'] = (14, 12)
      dataset_name = "mcswain"
      dataset_module = datasets.datasets_by_name_all[dataset_name]
      x,y,metadata = dataset_module.load(dropna=True,verbose=True)
      y = datasets.map_y_em(y,dataset_name)
      \# generate dataframe with both x and y
      xy = pd.concat([x,y],axis=1)
      xy.describe()
     Warning loading data from McSwain2005-2009_VPHAS-2MASS.csv:
     Dropped 2313 rows with missing values.
     Rows (original):
                         5455
     Rows (after drop): 3142
[92]:
                                                            imag
                                                                        Hamag \
                    umag
                                 gmag
                                               rmag
      count
             3142.000000
                          3142.000000
                                       3142.000000
                                                     3142.000000
                                                                  3142.000000
      mean
               16.304806
                            15.668695
                                          14.651512
                                                       14.076811
                                                                    14.398883
      std
                1.572447
                             1.225343
                                           1.047182
                                                        1.035455
                                                                     1.041201
      min
                            12.530000
                                          11.990000
                                                       11.450000
                                                                    11.690000
               12.260000
      25%
               15.150000
                            14.722500
                                         13.842500
                                                       13.260000
                                                                    13.580000
      50%
               16.445000
                            15.740000
                                         14.700000
                                                       14.100000
                                                                    14.435000
      75%
               17.337500
                            16.650000
                                          15.510000
                                                       14.900000
                                                                    15.250000
               20.840000
                            19.050000
                                          17.500000
      max
                                                       17.090000
                                                                    17.170000
                    Jmag
                                 Hmag
                                               Kmag
      count 3142.000000 3142.000000 3142.000000 3142.000000
```

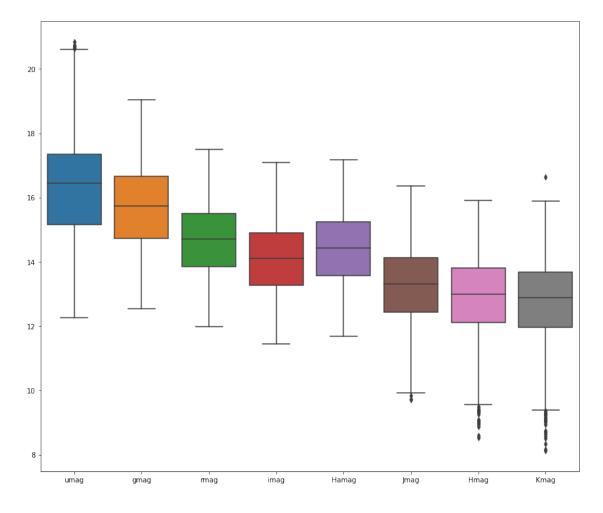
mean	13.248104	12.876838	12.739313	0.001591
std	1.128721	1.221364	1.259059	0.039866
min	9.700000	8.521000	8.118000	0.000000
25%	12.434000	12.101000	11.957000	0.000000
50%	13.306000	13.000000	12.876000	0.000000
75%	14.126750	13.801000	13.682000	0.000000
max	16.368000	15.912000	16.631000	1.000000

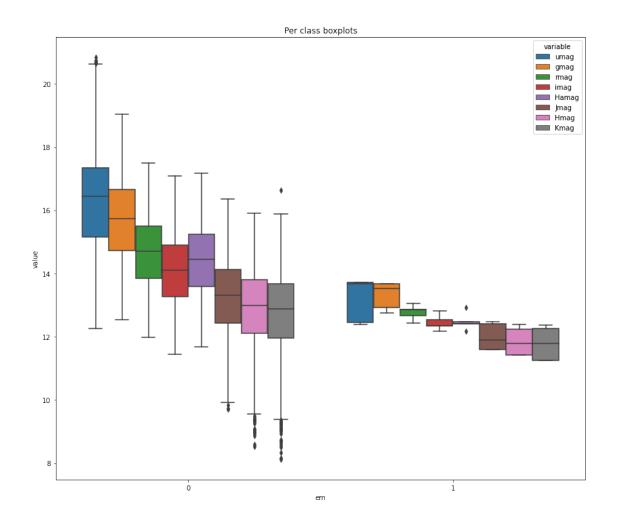
### 1 Variable visualization

```
[93]: sn.boxplot(data=x)

plt.figure()
xy_long = pd.melt(xy, id_vars='em')
sn.boxplot(x='em', y='value', hue='variable', data=xy_long)
plt.title("Per class boxplots")
```

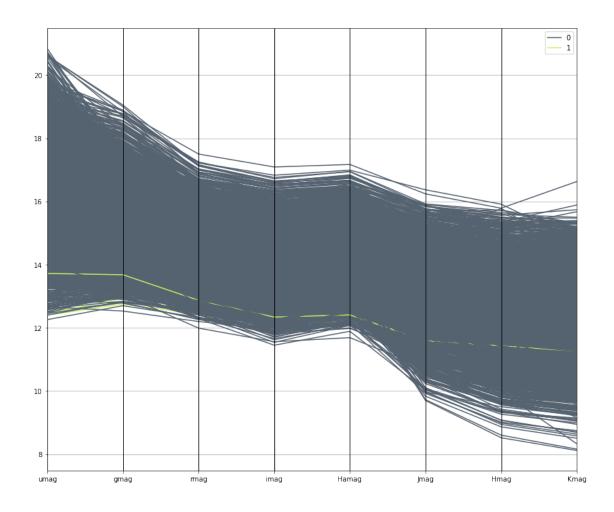
[93]: Text(0.5, 1.0, 'Per class boxplots')

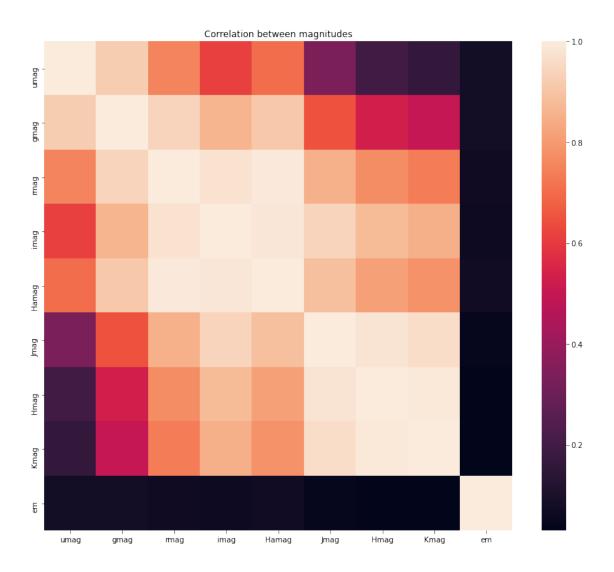




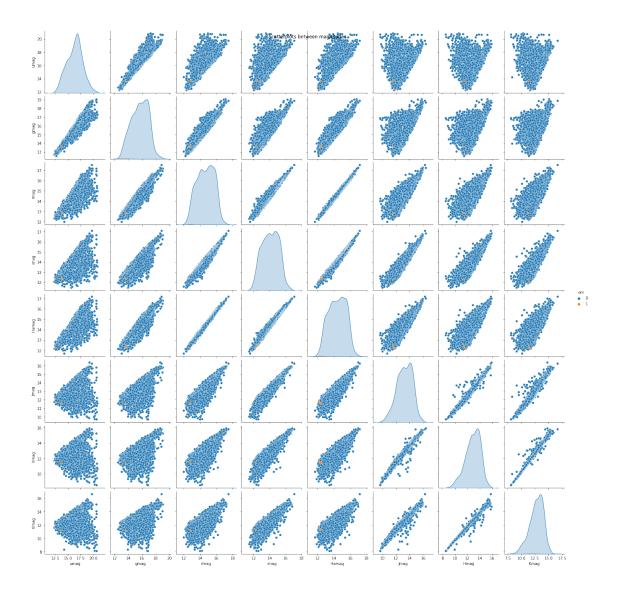
```
[94]: pd.plotting.parallel_coordinates(xy,"em",color=('#556270','#C7F464'))
```

[94]: <AxesSubplot:>





[95]: Text(0.5, 0.98, 'Scatterplots between magnitudes')



### 2 Outlier detection via confidence interval

```
[96]: from scipy import stats
    m = len(x.columns) # number of columns = number of hypothesis
    confidence = 0.98
    adjusted_confidence = 1- (1-confidence)/m # bonferroni-adjusted confidence
    max_zscore = stats.norm.ppf(adjusted_confidence)
    print(f"Confidence (desired): {confidence}")
    print(f"Confidence (adjusted): {adjusted_confidence}")
    print(f"Z-score (adjusted): {max_zscore}")

indices = (np.abs(stats.zscore(x-x.mean())) > max_zscore).any(axis=1)
    outliers_x = x[indices]
```

```
outliers_x = outliers_x.
       →merge(outliers_metadata,left_index=True,right_index=True)
      outliers x
     Confidence
                  (desired): 0.98
     Confidence (adjusted): 0.9975
                 (adjusted): 2.807033768343811
     Z-score
[96]:
                                                             Hmag
                                                                      Kmag
                                                                            Rad
             umag
                     gmag
                             rmag
                                    imag
                                          Hamag
                                                     Jmag
      240
             19.72
                    18.86
                           17.50
                                   17.09
                                           17.17
                                                  16.239
                                                          15.786
                                                                   16.631
                                                                            NaN
      1272
                    14.44
                                   11.62
            16.87
                           12.51
                                          12.13
                                                   9.924
                                                            9.015
                                                                    8.747
                                                                            NaN
      1345
            18.19
                    15.56
                           13.42
                                   12.18
                                          12.96
                                                  10.290
                                                            9.387
                                                                    9.042
                                                                            NaN
      1462
            19.19
                    15.99
                           13.72
                                   12.08
                                          13.14
                                                                     8.505
                                                                            NaN
                                                   9.836
                                                            8.866
                                   13.54
      1533
            20.84
                    17.27
                            14.97
                                           14.47
                                                  11.570
                                                           10.644
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                                                                            NaN
      1539
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      1570 16.64
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                                                            9.265
                                                                    8.993
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      1836
            20.73
                    17.62
                           15.27
                                   13.97
                                           14.77
                                                  11.809
                                                          10.792
                                                                   10.536
                                                                            NaN
      1967
            20.71
                    16.97
                           14.51
                                   12.96
                                          13.92
                                                  10.553
                                                            9.426
                                                                     9.080
                                                                            NaN
      1994
            18.69
                                   12.09
                    15.60
                           13.52
                                           13.01
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      2163
            20.27
                    16.75
                           14.24
                                   12.35
                                           13.66
                                                   9.725
                                                            8.603
                                                                     8.161
                                                                            NaN
      2415
                    13.97
                                   11.45
                                                            9.318
                                                                            NaN
            15.63
                            12.29
                                           11.89
                                                  10.025
                                                                     9.145
      2437
            17.55
                    14.91
                           12.91
                                   11.91
                                           12.47
                                                  10.235
                                                            9.362
                                                                     9.122
                                                                            NaN
      2463
           16.69
                    14.61
                           12.67
                                   11.70
                                          12.25
                                                  10.084
                                                            9.333
                                                                    9.075
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      2483
                    13.95
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            14.21
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                                          13.15
                                                  12.348
                                                            9.971
                                                                     8.329
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      2661
           18.26
                    15.52
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                                   12.22
                                          12.79
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      2678
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                                   11.84
           15.84
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                                           12.66
                                                   9.967
                                                            9.502
                                                                     9.238
                                                                            NaN
                                   12.23
      2683
            18.88
                    15.78
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                                          12.90
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                                                   9.957
      2699
            16.36
                    16.05
                            15.11
                                   14.53
                                           14.80
                                                  13.671
                                                           10.260
                                                                     9.155
                                                                            NaN
      2718
            20.66
                    16.88
                           14.00
                                   12.59
                                           13.46
                                                   9.700
                                                            8.521
                                                                     8.118
                                                                            NaN
      3015
            20.29
                                           13.60
                                                  10.106
                                                                     8.703
                    16.89
                            14.10
                                   12.64
                                                            9.070
                                                                            NaN
      3028
            20.14
                    16.66
                            14.01
                                   12.48
                                           13.43
                                                   9.984
                                                            8.943
                                                                     8.580
                                                                            NaN
      3102
            20.42
                    16.94
                           14.25
                                   12.54
                                           13.67
                                                  10.398
                                                            9.341
                                                                     8.945
                                                                            NaN
              DEJ2000
                                Cluster
                                         vsini
                                                 e_Hmag
                                                                  e_Rad
                                                                          e_y-Ha
                                                          e_rmag
      240 -25.483167
                             Haffner 16
                                            NaN
                                                            0.05
                                                                           0.115
                                                  0.126
                                                                     NaN
      1272 -57.660417
                                IC 2581
                                            NaN
                                                  0.022
                                                            0.00
                                                                     NaN
                                                                           0.073
      1345
            -5.765472
                                Basel 1
                                            NaN
                                                  0.022
                                                            0.00
                                                                     NaN
                                                                           0.064
      1462
            -5.966361
                                                  0.042
                                                            0.00
                                                                           0.065
                                Basel 1
                                            NaN
                                                                    NaN
                                                                           0.088
      1533
            -5.886528
                                Basel 1
                                            NaN
                                                  0.026
                                                            0.01
                                                                    NaN
      1539
            -5.854250
                                Basel 1
                                            NaN
                                                  0.023
                                                            0.01
                                                                           0.092
                                                                    NaN
      1570 -58.287500
                               NGC 3293
                                            NaN
                                                  0.023
                                                            0.00
                                                                    NaN
                                                                           0.064
      1836 -60.696194
                            Trumpler 20
                                                  0.021
                                                            0.00
                                                                           0.101
                                            NaN
                                                                     NaN
      1967 -60.611472
                            Trumpler 20
                                                  0.022
                                                            0.00
                                                                     NaN
                                                                           0.075
                                            {\tt NaN}
      1994 -60.631167
                            Trumpler 20
                                            NaN
                                                  0.025
                                                            0.01
                                                                     NaN
                                                                           0.067
      2163 -60.574639
                           Trumpler 20
                                            NaN
                                                  0.018
                                                            0.01
                                                                     NaN
                                                                           0.072
```

if dataset\_name != "all\_em":

outliers\_metadata = metadata[indices]

```
2415 -47.466806
                         NGC 6200
                                      NaN
                                             0.024
                                                       0.00
                                                                NaN
                                                                       0.050
                         NGC 6200
2437 -47.544444
                                             0.024
                                                       0.00
                                                                       0.061
                                      NaN
                                                                NaN
2463 -47.478972
                         NGC 6200
                                      NaN
                                             0.026
                                                       0.00
                                                                NaN
                                                                       0.058
2483 -46.933944
                         NGC 6204
                                      NaN
                                                NaN
                                                       0.01
                                                                NaN
                                                                       0.102
                         NGC 6249
                                             0.023
                                                       0.00
                                                                       0.057
2661 -44.725972
                                      NaN
                                                                NaN
2678 -33.431944
                      Trumpler 27
                                      NaN
                                             0.024
                                                       0.00
                                                                       0.092
                                                                NaN
                      Trumpler 28
                                                       0.00
                                                                       0.081
2683 -32.467667
                                      {\tt NaN}
                                             0.029
                                                                NaN
2699 -32.420083
                      Trumpler 28
                                      {\tt NaN}
                                               NaN
                                                       0.00
                                                                NaN
                                                                       0.091
                      Trumpler 28
2718 -32.443972
                                      {\tt NaN}
                                             0.034
                                                       0.00
                                                                NaN
                                                                       0.098
                      Trumpler 34
                                                       0.00
3015
      -8.509889
                                      {\tt NaN}
                                             0.023
                                                                NaN
                                                                       0.047
                      Trumpler 34
3028
      -8.389750
                                      NaN
                                             0.023
                                                       0.00
                                                                NaN
                                                                       0.078
3102 -5.930500
                          Basel 1
                                      NaN
                                             0.022
                                                       0.01
                                                                NaN
                                                                       0.084
      e_Kmag
                  _RAJ2000
                            SB?
                                  e_gmag
```

```
240
         {\tt NaN}
               117.481417
                             NaN
                                    0.01
1272
       0.021
               157.007667
                             NaN
                                    0.01
1345
       0.024
                                    0.00
               282.029125
                             NaN
       0.021
                                    0.00
1462
               282.104792
                             NaN
1533
       0.025
               282.153042
                            NaN
                                    0.01
1539
       0.023
               282.156125
                             NaN
                                    0.01
       0.019
1570
               158.856375
                            NaN
                                    0.00
       0.023
               189.831292
                                    0.02
1836
                            {\tt NaN}
1967
       0.020
               189.910875
                            {\tt NaN}
                                    0.01
       0.018
1994
               189.925042
                            NaN
                                    0.01
2163
       0.029
               190.020042
                             NaN
                                    0.01
2415
       0.025
               250.958125
                             NaN
                                    0.00
               251.046333
2437
       0.023
                             NaN
                                    0.00
2463
       0.023
               251.131750
                            {\tt NaN}
                                    0.01
2483
         NaN
               251.693333
                             NaN
                                    0.01
       0.020
2661
               254.576000
                             NaN
                                    0.00
       0.023
                                    0.00
2678
               264.084292
                             NaN
       0.026
2683
               264.121042
                             NaN
                                    0.00
2699
         NaN
               264.186458
                             NaN
                                    0.01
2718
       0.031
               264.235167
                             NaN
                                    0.01
3015
       0.020
               280.074042
                             NaN
                                    0.00
3028
       0.023
               280.084833
                             NaN
                                    0.01
3102
       0.021
               281.981750
                            {\tt NaN}
                                    0.01
```

[23 rows x 43 columns]

### 3 Outlier detection via IQR

```
[97]: iqr_factor=1.5
q25,q75=x.quantile(0.25),x.quantile(0.75)
iqr=q75-q25
min_values = q25-iqr_factor*iqr
```

```
max_values = q75+iqr_factor*iqr
# ou
indices = (np.logical_or(x<min_values,x>max_values)).any(axis=1)
outliers_x = x[indices]
if dataset_name != "all_em":
    outliers_metadata = metadata[indices]
    outliers_x = outliers_x.
    →merge(outliers_metadata,left_index=True,right_index=True)
outliers_x
```

```
[97]:
                                     imag
                                           Hamag
                                                      Jmag
                                                              Hmag
                                                                       Kmag
                                                                             Rad
                                                                                   \
              umag
                     gmag
                             rmag
      165
             19.95
                    16.73
                            14.29
                                    12.98
                                           13.77
                                                   10.709
                                                             9.637
                                                                      9.278
                                                                             NaN
      235
                    16.00
                                    12.54
                                           13.20
                                                   10.597
                                                                      9.236
             18.90
                            13.75
                                                             9.569
                                                                             NaN
      240
                                    17.09
             19.72
                    18.86
                            17.50
                                           17.17
                                                   16.239
                                                            15.786
                                                                     16.631
                                                                             NaN
      256
                    18.69
                                    15.72
                                                            13.883
                                                                             NaN
             20.66
                            16.47
                                           16.01
                                                   14.595
                                                                     13.670
      470
             20.62
                    19.00
                            16.91
                                    16.25
                                           16.49
                                                   15.197
                                                            14.309
                                                                     14.071
                                                                             NaN
      906
             20.11
                    16.77
                            14.16
                                   12.97
                                           13.82
                                                   10.665
                                                             9.660
                                                                      9.270
                                                                             NaN
      1272
             16.87
                    14.44
                            12.51
                                    11.62
                                           12.13
                                                    9.924
                                                             9.015
                                                                      8.747
                                                                             NaN
      1345
             18.19
                    15.56
                            13.42
                                   12.18
                                           12.96
                                                   10.290
                                                             9.387
                                                                      9.042
                                                                             NaN
      1395
             19.78
                    16.67
                            14.23
                                    12.84
                                           13.77
                                                   10.572
                                                             9.561
                                                                      9.217
                                                                             NaN
      1405
             19.27
                    16.12
                            13.86
                                    12.60
                                                   10.574
                                                             9.658
                                                                      9.369
                                                                             NaN
                                           13.40
      1462
             19.19
                    15.99
                            13.72
                                    12.08
                                           13.14
                                                    9.836
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                                                                      8.505
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      1533
                    17.27
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                                           14.47
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                                                                             NaN
      1539
             20.73
                    17.59
                            15.46
                                    14.16
                                           15.01
                                                   12.216
                                                            11.319
                                                                     11.070
                                                                             NaN
      1570
             16.64
                    14.45
                            12.64
                                    11.76
                                           12.22
                                                   10.061
                                                             9.265
                                                                      8.993
                                                                             NaN
                                    12.04
                                                                      9.301
      1577
             15.15
                    14.38
                            12.88
                                           12.51
                                                   10.323
                                                             9.570
                                                                             NaN
      1836
             20.73
                    17.62
                            15.27
                                    13.97
                                           14.77
                                                   11.809
                                                            10.792
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                                                             9.426
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      1994
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      2163
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      2437
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                                                             9.362
                                                                      9.122
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      2463
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             16.69
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      2483
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                                                             9.971
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      2661
             18.26
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                                    12.22
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                                                             9.340
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      2674
             16.20
                    14.57
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      2678
             15.84
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      2683
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      2699
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                                                            10.260
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      2713
            16.57
                    14.70
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                                                             9.581
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      2718
                    16.88
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            20.66
                            14.00
                                           13.46
                                                    9.700
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      2750
            18.60
                    15.82
                            13.67
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                                                             9.607
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      3015
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      3027
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                                                   11.284
                                                            10.356
                                                                     10.017
                                                                             NaN
      3028
             20.14
                    16.66
                            14.01
                                    12.48
                                           13.43
                                                    9.984
                                                             8.943
                                                                      8.580
                                                                             NaN
      3102
             20.42
                    16.94
                            14.25
                                   12.54
                                           13.67
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```

```
DEJ2000
                          Cluster
                                    vsini
                                                              e_Rad
                                                                     e_y-Ha \
                                            e_Hmag
                                                     e_rmag
                                                                      0.069
165
     -20.711139
                         NGC 2421
                                             0.022
                                                       0.00
                                                                NaN
                                      NaN
235
     -20.649944
                         NGC 2421
                                      NaN
                                             0.024
                                                       0.00
                                                                NaN
                                                                      0.064
     -25.483167
240
                       Haffner 16
                                      NaN
                                             0.126
                                                       0.05
                                                                NaN
                                                                      0.115
                                             0.022
                                                                      0.089
256
     -25.517722
                       Haffner 16
                                      NaN
                                                       0.01
                                                                NaN
470
                       Haffner 16
                                      NaN
                                               NaN
                                                       0.01
                                                                      0.099
     -25.544778
                                                                NaN
    -53.920361
                                             0.022
906
                      Ruprecht 79
                                      NaN
                                                       0.00
                                                                NaN
                                                                      0.077
1272 -57.660417
                          IC 2581
                                      NaN
                                             0.022
                                                       0.00
                                                                NaN
                                                                      0.073
1345
                          Basel 1
                                      NaN
                                             0.022
                                                       0.00
                                                                      0.064
      -5.765472
                                                                NaN
1395
                          Basel 1
      -5.913583
                                      NaN
                                             0.027
                                                       0.01
                                                                NaN
                                                                      0.073
                          Basel 1
1405
      -5.772222
                                      NaN
                                             0.021
                                                       0.00
                                                                NaN
                                                                      0.071
1462
      -5.966361
                          Basel 1
                                      NaN
                                             0.042
                                                       0.00
                                                                      0.065
                                                                NaN
1533
      -5.886528
                          Basel 1
                                      NaN
                                             0.026
                                                       0.01
                                                                NaN
                                                                      0.088
1539
      -5.854250
                          Basel 1
                                      NaN
                                             0.023
                                                       0.01
                                                                NaN
                                                                      0.092
1570 -58.287500
                         NGC 3293
                                             0.023
                                                       0.00
                                                                      0.064
                                      NaN
                                                                NaN
1577 -58.192194
                         NGC 3293
                                      NaN
                                             0.028
                                                       0.00
                                                                NaN
                                                                      0.057
1836 -60.696194
                      Trumpler 20
                                                       0.00
                                                                      0.101
                                      NaN
                                             0.021
                                                                NaN
                      Trumpler 20
1967 -60.611472
                                      NaN
                                             0.022
                                                       0.00
                                                                NaN
                                                                      0.075
1994 -60.631167
                      Trumpler 20
                                      NaN
                                             0.025
                                                       0.01
                                                                NaN
                                                                      0.067
                      Trumpler 20
                                                                      0.072
2163 -60.574639
                                      NaN
                                             0.018
                                                       0.01
                                                                NaN
2415 -47.466806
                         NGC 6200
                                      NaN
                                             0.024
                                                       0.00
                                                                NaN
                                                                      0.050
                         NGC 6200
                                                                      0.061
2437 -47.544444
                                      NaN
                                             0.024
                                                       0.00
                                                                NaN
                         NGC 6200
                                             0.026
                                                       0.00
                                                                      0.058
2463 -47.478972
                                      NaN
                                                                NaN
2483 -46.933944
                         NGC 6204
                                      NaN
                                               NaN
                                                       0.01
                                                                NaN
                                                                      0.102
                         NGC 6249
                                             0.023
                                                       0.00
                                                                      0.057
2661 -44.725972
                                      NaN
                                                                NaN
2674 -35.635611
                        Bochum 13
                                      NaN
                                             0.030
                                                       0.00
                                                                NaN
                                                                      0.093
2678 -33.431944
                      Trumpler 27
                                      NaN
                                             0.024
                                                       0.00
                                                                NaN
                                                                      0.092
                      Trumpler 28
                                                                      0.081
2683 -32.467667
                                      NaN
                                             0.029
                                                       0.00
                                                                NaN
2699 -32.420083
                      Trumpler 28
                                      NaN
                                               NaN
                                                       0.00
                                                                NaN
                                                                      0.091
2713 -32.481056
                      Trumpler 28
                                      NaN
                                             0.026
                                                       0.00
                                                                NaN
                                                                      0.060
                      Trumpler 28
2718 -32.443972
                                      NaN
                                             0.034
                                                       0.00
                                                                NaN
                                                                      0.098
2750 -32.552806
                      Trumpler 28
                                             0.025
                                                       0.00
                                                                      0.068
                                      NaN
                                                                NaN
                      Trumpler 34
3015
      -8.509889
                                      NaN
                                             0.023
                                                       0.00
                                                                NaN
                                                                      0.047
3027
      -8.526639
                      Trumpler 34
                                      NaN
                                             0.024
                                                       0.00
                                                                NaN
                                                                      0.065
3028
      -8.389750
                      Trumpler 34
                                             0.023
                                                       0.00
                                                                      0.078
                                      NaN
                                                                NaN
                  •••
3102
      -5.930500
                          Basel 1
                                      NaN
                                             0.022
                                                       0.01
                                                                NaN
                                                                      0.084
                  •••
                 _RAJ2000
                            SB?
      e_Kmag
                                  e_gmag
165
       0.021
               114.083458
                            NaN
                                    0.00
235
       0.019
               114.173500
                            NaN
                                    0.00
240
         NaN
               117.481417
                            NaN
                                    0.01
256
       0.043
               117.495292
                            NaN
                                    0.01
470
         NaN
                                    0.01
               117.722875
                            NaN
906
       0.023
               145.126708
                            NaN
                                    0.01
       0.021
1272
               157.007667
                            NaN
                                    0.01
       0.024
               282.029125
                                    0.00
1345
                            NaN
1395
       0.021
               282.059333
                            NaN
                                    0.01
```

```
0.019 282.067375 NaN
1405
                                0.00
                                0.00
1462
      0.021 282.104792 NaN
1533
      0.025 282.153042 NaN
                                0.01
1539
      0.023 282.156125 NaN
                                0.01
1570
      0.019 158.856375 NaN
                                0.00
      0.026
1577
            159.009542 NaN
                                0.00
1836
      0.023
            189.831292 NaN
                                0.02
      0.020 189.910875 NaN
1967
                                0.01
1994
      0.018 189.925042 NaN
                                0.01
2163
      0.029
             190.020042 NaN
                                0.01
2415
      0.025 250.958125 NaN
                                0.00
2437
      0.023 251.046333 NaN
                                0.00
2463
      0.023 251.131750 NaN
                                0.01
2483
        NaN 251.693333 NaN
                                0.01
2661
      0.020 254.576000 NaN
                                0.00
2674
      0.027
             259.347000 NaN
                                0.00
2678
      0.023
            264.084292 NaN
                                0.00
2683
      0.026
            264.121042 NaN
                                0.00
2699
        NaN 264.186458 NaN
                                0.01
2713
      0.023
            264.221958 NaN
                                0.00
2718
      0.031
             264.235167 NaN
                                0.01
2750
      0.023 264.319042 NaN
                                0.00
3015
      0.020 280.074042 NaN
                                0.00
3027
      0.023 280.084708 NaN
                                0.01
3028
      0.023 280.084833 NaN
                                0.01
3102
      0.021 281.981750 NaN
                                0.01
```

[35 rows x 43 columns]

# 4 Analysis of q-features $(q_3)$ (all magnitudes)

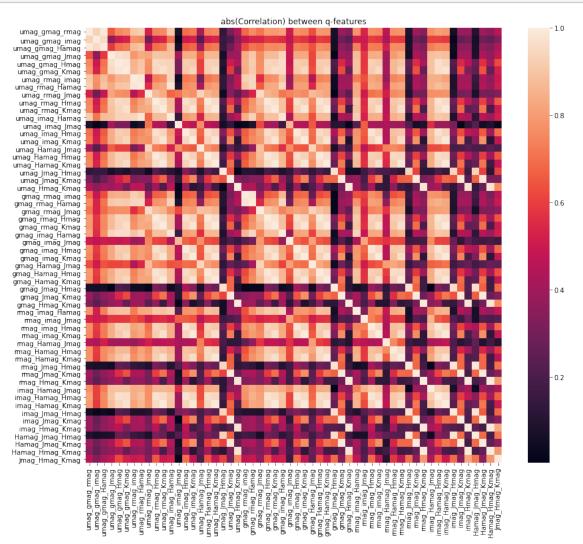
```
[98]: x_np=x.to_numpy()
import qfeatures
coefficients = dataset_module.coefficients
systems = dataset_module.systems
coefficients_np = np.array([coefficients[k] for k in x.columns])
systems = [systems[k] for k in x.columns]
q=qfeatures.calculate(x_np,coefficients_np,x.columns,systems,combination_size=3)
m = q.magnitudes

q_df = pd.DataFrame(m, columns = q.column_names)
q_df.describe()
```

```
[98]: umag_gmag_rmag umag_gmag_imag umag_gmag_Hamag umag_gmag_Jmag \
count 3142.000000 3142.000000 3142.000000
mean 0.156141 -0.378599 -0.010663 -3.028395
```

std	0.477268	0.333868	0.437317	0.940956	
min	-0.759654	-1.321813	-0.903692	-7.115069	
25%	-0.126526	-0.615351	-0.282897	-3.564993	
50%	0.016104	-0.469503	-0.131121	-2.951368	
75%	0.231807	-0.232851	0.094217	-2.415524	
max	2.579221	1.192398	2.186495	-0.466389	
	umag_gmag_Hmag	umag_gmag_Kmag	umag_rmag_imag u	mag_rmag_Hamag \	
count	3142.000000	3142.000000	3142.000000	3142.000000	
mean	-5.979377	-9.798617	0.954243	1.407748	
std	2.229224	3.864487	0.827491	0.977587	
min	-16.027196	-27.431046	-0.711111	-0.596636	
25%	-7.162250	-11.795907	0.425526	0.813995	
50%	-5.624293	-9.041667	0.664269	1.106449	
75%	-4.540071	-7.278962	1.343070	1.737780	
max	-0.952413	-1.686405	4.944912	6.135140	
	${\tt umag\_rmag\_Jmag}$	${\tt umag\_rmag\_Hmag}$	imag_Hamag_Jma	g imag_Hamag_Hmag $\setminus$	\
count	3142.000000	3142.000000	3142.00000	0 3142.000000	
mean	-2.400995	-6.371318	0.36519	9 1.100709	
std	0.870262	2.649514	0.18469	1 0.539457	
min	-7.689333	-21.841478	0.02890	3 0.046913	
25%	-2.914667	-7.681826	0.24143	1 0.755772	
50%	-2.415333	-5.949609	0.31988	9 0.973728	
75%	-1.835278	-4.581130	0.46309	4 1.322918	
max	0.383778	-0.032348	1.37555	6 4.200283	
	$imag\_Hamag\_Kmag$	${\tt imag\_Jmag\_Hmag}$		$imag\_Hmag\_Kmag$ \	
count	3142.000000	3142.000000	3142.000000	3142.000000	
mean	2.010004	0.029678	-0.817382	0.638187	
std	0.976299	0.406704	0.884542	0.772481	
min	0.031895	-6.482065	-13.751588	-11.218902	
25%	1.366315	-0.095897	-1.125529	0.350629	
50%	1.780310	0.037130	-0.677735	0.625464	
75%	2.436038	0.174163	-0.364721	0.986067	
max	7.662516	4.936783	4.142765	7.507065	
	Hamag_Jmag_Hmag	Hamag_Jmag_Kmag			
count	3142.000000	3142.000000			
mean	0.004697	-1.210278			
std	0.581073	1.279983			
min	-9.400609	-19.827601			
25%	-0.192011	-1.668518			
50%	0.027500	-0.991654			
75%	0.236761	-0.543185			
max	6.374304	5.383026	9.521608	2.715843	

```
[99]: sn.heatmap(q_df.corr().abs())
   plt.title("abs(Correlation) between q-features")
   plt.show()
```

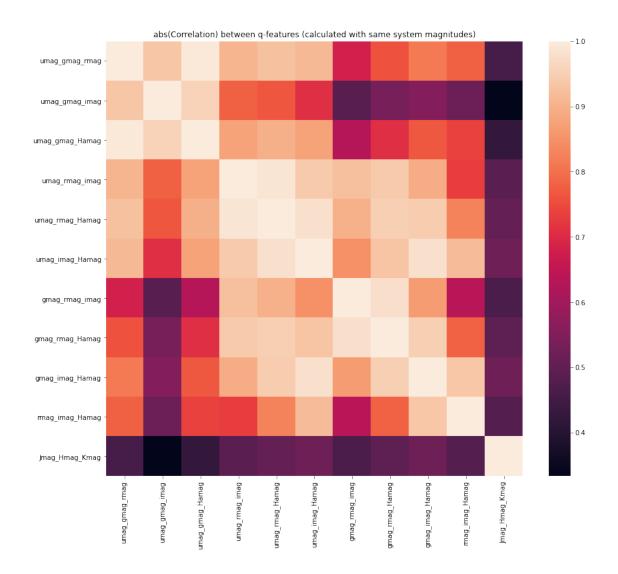


## 5 Analysis of q-features $(q_3)$ (calculated by system)

```
[100]: x_np=x.to_numpy()
    import qfeatures
    coefficients = dataset_module.coefficients
    systems = dataset_module.systems
    coefficients_np = np.array([coefficients[k] for k in x.columns])
    systems = [systems[k] for k in x.columns]
```

```
→columns,systems,combination_size=3,by_system=True)
       m = q.magnitudes
       q df = pd.DataFrame(m, columns = q.column names)
       q_df.describe()
「100]:
              umag_gmag_rmag
                               umag_gmag_imag
                                                umag_gmag_Hamag
                                                                 umag_rmag_imag
                  3142.000000
                                  3142.000000
                                                    3142.000000
                                                                     3142.000000
       count
       mean
                    0.156141
                                     -0.378599
                                                      -0.010663
                                                                        0.954243
       std
                    0.477268
                                     0.333868
                                                       0.437317
                                                                        0.827491
       min
                    -0.759654
                                    -1.321813
                                                      -0.903692
                                                                       -0.711111
       25%
                                                                         0.425526
                    -0.126526
                                    -0.615351
                                                      -0.282897
       50%
                                                                        0.664269
                    0.016104
                                    -0.469503
                                                      -0.131121
       75%
                    0.231807
                                    -0.232851
                                                       0.094217
                                                                         1.343070
                     2.579221
                                     1.192398
                                                        2.186495
                                                                        4.944912
       max
              umag_rmag_Hamag
                                umag_imag_Hamag
                                                  gmag_rmag_imag
                                                                   gmag_rmag_Hamag
                  3142.000000
                                    3142.000000
                                                     3142.000000
                                                                       3142.000000
       count
                      1.407748
                                        2.631337
                                                         0.684462
                                                                           0.900313
       mean
       std
                      0.977587
                                        1.403822
                                                         0.334951
                                                                           0.397890
       min
                     -0.596636
                                       -0.202336
                                                         0.068421
                                                                           0.117617
       25%
                      0.813995
                                        1.770654
                                                         0.461711
                                                                           0.643785
       50%
                                        2.298271
                                                         0.602632
                      1.106449
                                                                           0.812547
       75%
                      1.737780
                                        3.101028
                                                         0.885789
                                                                           1.145245
                      6.135140
                                        9.560561
                                                         2.063684
                                                                           2.630187
       max
                                                  Jmag_Hmag_Kmag
              gmag_imag_Hamag
                                rmag_imag_Hamag
                  3142.000000
                                    3142.000000
                                                     3142.000000
       count
                      1.831181
                                        0.665001
                                                         0.254415
       mean
       std
                      0.723852
                                        0.265588
                                                         0.264408
       min
                      0.310000
                                        0.073178
                                                        -2.622131
       25%
                      1.364100
                                        0.474112
                                                         0.119691
       50%
                                                         0.231033
                      1.712173
                                        0.636916
       75%
                      2.188703
                                        0.817757
                                                         0.380542
                      5.373318
                                        2.257290
                                                         2.715843
       max
[101]: sn.heatmap(q_df.corr().abs())
       plt.title("abs(Correlation) between q-features (calculated with same system ⊔
        →magnitudes)")
       plt.show()
       q_dfy=pd.concat([q_df,y],axis=1)
       sn.pairplot(q_dfy,hue="em")
       plt.suptitle("Scatter plots between q-features (calculated with same systemu
        →magnitudes)")
```

q= qfeatures.calculate(x\_np,coefficients\_np,x.



[101]: Text(0.5, 0.98, 'Scatter plots between q-features (calculated with same system magnitudes)')

