#### Notebook

#### March 26, 2021

```
[1]:
     dataset_name = 'liu'
[2]: %reload_ext autoreload
     %autoreload 2
     default_figsize=(14,12)
[3]: import datasets
     import numpy as np
     import pandas as pd
     import seaborn as sn
     import matplotlib.pyplot as plt
     import matplotlib
     matplotlib.rcParams['figure.figsize'] = (14, 12)
     dataset_module = datasets.datasets_by_name_all[dataset_name]
     x,y,metadata = dataset_module.load(dropna=True,verbose=True)
     y = datasets.map_y_em(y,dataset_name)
     \# generate dataframe with both x and y
     xy = pd.concat([x,y],axis=1)
     xy.describe()
[3]:
                                                        imag
                                                                   Hamag
                                                                                 Jmag
                  umag
                               gmag
                                           rmag
                                                                          281.000000
     count
            281.000000
                        281.000000
                                     281.000000
                                                 281.000000
                                                              281.000000
     mean
             15.111851
                          14.504733
                                      13.592100
                                                   12.929715
                                                               13.175018
                                                                            12.020854
     std
              1.816931
                           1.652762
                                       1.077114
                                                   1.025982
                                                                1.155292
                                                                             1.105942
    min
             10.980000
                          10.130000
                                      11.820000
                                                   11.100000
                                                               11.160000
                                                                             9.060000
     25%
             13.840000
                          13.140000
                                      12.650000
                                                   12.070000
                                                               12.100000
                                                                            11.350000
     50%
             14.630000
                         14.560000
                                      13.580000
                                                   12.820000
                                                               13.140000
                                                                            11.810000
     75%
             16.180000
                          15.880000
                                      14.400000
                                                   13.660000
                                                               14.010000
                                                                            12.730000
             23.710000
                          18.130000
                                      16.470000
                                                   16.310000
                                                               16.300000
                                                                            16.310000
     max
                  Hmag
                               Kmag
                                             em
                        281.000000
     count
            281.000000
                                     281.000000
             11.785267
                          11.635587
                                       0.341637
     mean
     std
              1.167985
                           1.205151
                                       0.475105
```

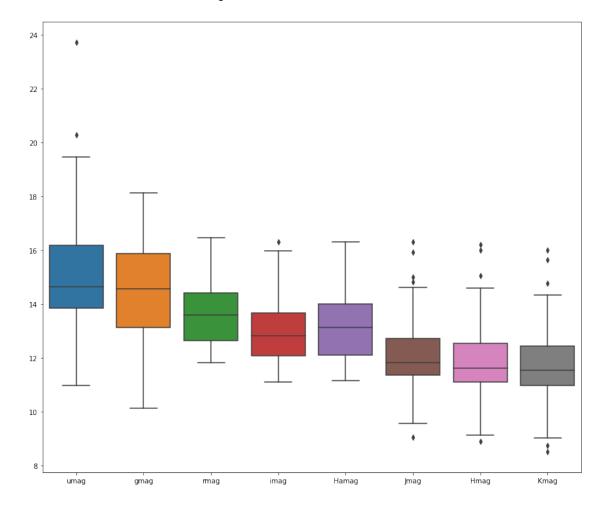
```
0.000000
         8.910000
                      8.510000
min
25%
        11.100000
                     10.970000
                                  0.000000
50%
        11.620000
                     11.550000
                                  0.000000
75%
        12.550000
                                  1.000000
                     12.430000
max
        16.210000
                     16.000000
                                  1.000000
```

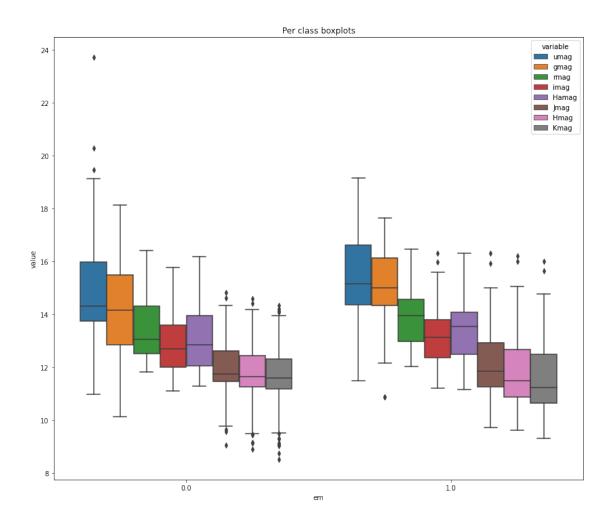
## 1 Variable visualization

```
[4]: sn.boxplot(data=x)

plt.figure()
xy_long = pd.melt(xy, id_vars='em')
sn.boxplot(x='em', y='value', hue='variable', data=xy_long)
plt.title("Per class boxplots")
```

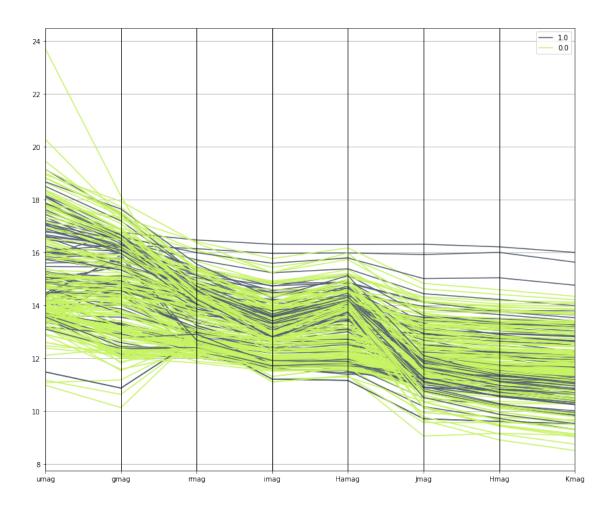
[4]: Text(0.5, 1.0, 'Per class boxplots')

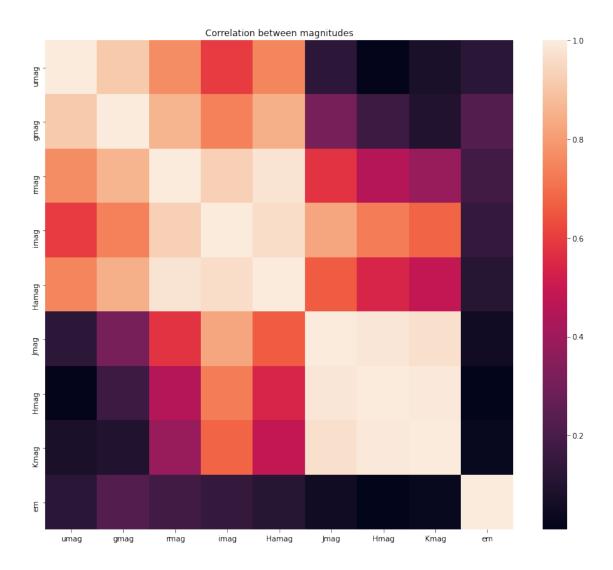




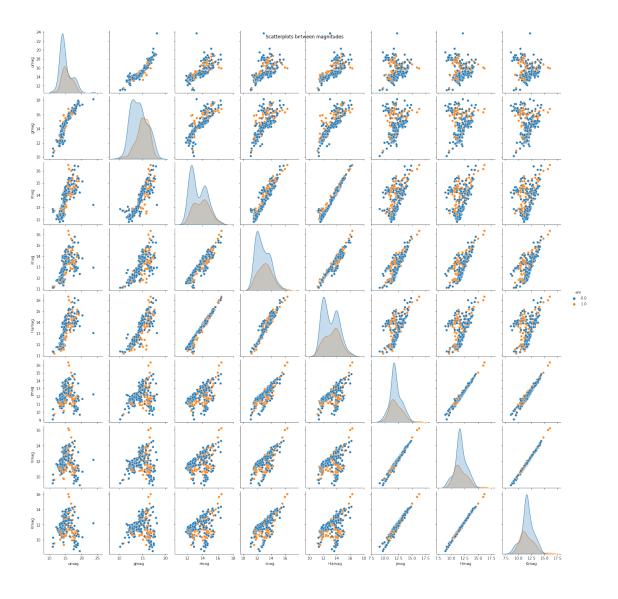
```
[5]: pd.plotting.parallel_coordinates(xy,"em",color=('#556270','#C7F464'))
```

[5]: <AxesSubplot:>





[6]: Text(0.5, 0.98, 'Scatterplots between magnitudes')



### 2 Outlier detection via confidence interval

```
[7]: from scipy import stats
    m = len(x.columns) # number of columns = number of hypothesis
    confidence= 0.99
    adjusted_confidence = 1- (1-confidence)/m # bonferroni-adjusted confidence
    max_zscore = stats.norm.ppf(adjusted_confidence)
    print(f"Confidence (desired): {confidence}")
    print(f"Confidence (adjusted): {adjusted_confidence}")
    print(f"Z-score (adjusted): {max_zscore}")

indices = (np.abs(stats.zscore(x-x.mean())) > max_zscore).any(axis=1)
    outliers_x = x[indices]
```

```
if dataset_name != "all_em":
         outliers_metadata = metadata[indices]
         outliers_x = pd.concat([outliers_x,outliers_metadata],axis=1)
     outliers_x
    Confidence (desired): 0.99
    Confidence (adjusted): 0.99875
               (adjusted): 3.023341439739154
    Z-score
[7]:
                                imag Hamag
                                                     Hmag
                                                            Kmag
                                                                  RAJ2000 1 \
          umag
                 gmag
                         rmag
                                              Jmag
     40
          23.71
                18.13
                       13.21
                               12.94
                                     13.01 12.25
                                                    12.17
                                                           12.18
                                                                   93.283401
          15.87 16.76
                       16.47
                               16.31
                                     16.30 16.31
                                                    16.21
                                                           16.00
     88
                                                                   94.851449
     227
         16.06 16.28 16.14 15.96 15.98 15.92
                                                   16.00 15.63
                                                                 104.223190
          model_prob _DEJ2000_1 original_index col1 LAMOST_sep Unnamed: 0
     40
                0.38
                       23.857319
                                         632.00
                                                  632
                                                              2.0
                                                                          634
                                                              2.0
                0.16
                       23.777745
                                          78.00
                                                   78
                                                                           78
     88
     227
                0.00
                                          27.00
                                                   27
                                                                           27
                        6.304176
                                                              2.0
```

## 3 Outlier detection via IQR

```
[8]: iqr_factor=1.5
    q25,q75=x.quantile(0.25),x.quantile(0.75)
    iqr=q75-q25
    min_values = q25-iqr_factor*iqr
    max_values = q75+iqr_factor*iqr
# ou
    indices = (np.logical_or(x<min_values,x>max_values)).any(axis=1)
    outliers_x = x[indices]
    if dataset_name != "all_em":
        outliers_metadata = metadata[indices]
        outliers_x = pd.concat([outliers_x,outliers_metadata],axis=1)
    outliers_x
```

```
[8]:
                                                             _RAJ2000_1 \
          umag
                gmag
                       rmag
                             imag
                                   Hamag
                                          Jmag
                                                 Hmag
                                                       Kmag
    40
         23.71 18.13
                     13.21 12.94
                                  13.01 12.25
                                                12.17
                                                      12.18
                                                              93.283401
    76
         10.98 10.13
                     12.87 11.10 11.35
                                          9.06
                                                 9.16
                                                       9.08
                                                              59.076031
         15.87 16.76 16.47 16.31 16.30 16.31
                                                16.21 16.00
                                                              94.851449
    129 20.28 17.36 15.13 13.79 14.61 11.66
                                                10.64 10.33
                                                             100.553070
    227 16.06 16.28 16.14 15.96 15.98 15.92
                                               16.00 15.63
                                                             104.223190
    244 17.85 17.33 16.41 15.77 16.17 14.83
                                                14.59 14.34
                                                              83.374873
    255 16.77 16.58 15.99 15.59 15.79 15.01
                                               15.04 14.76
                                                              88.270422
    264 19.45 17.23 14.22 12.36 13.63
                                          9.65
                                                 8.91
                                                       8.51
                                                             308.255134
    275 17.56 16.46 13.81 12.20 13.27
                                          9.78
                                                 9.14
                                                       8.75
                                                             308.147236
```

model\_prob \_DEJ2000\_1 original\_index col1 LAMOST\_sep Unnamed: 0

| 40  | 0.38 | 23.857319 | 632.00   | 632  | 2.0 | 634  |
|-----|------|-----------|----------|------|-----|------|
| 76  | 0.18 | 51.133020 | 937.00   | 937  | 2.0 | 939  |
| 88  | 0.16 | 23.777745 | 78.00    | 78   | 2.0 | 78   |
| 129 | 0.09 | 9.502543  | 74.00    | 74   | 2.0 | 74   |
| 227 | 0.00 | 6.304176  | 27.00    | 27   | 2.0 | 27   |
| 244 | 0.00 | 29.005993 | 1.032.00 | 1032 | 2.0 | 1034 |
| 255 | 0.00 | 22.163427 | 880.00   | 880  | 2.0 | 882  |
| 264 | 0.00 | 40.542745 | 402.00   | 402  | 2.0 | 403  |
| 275 | 0.00 | 41.245939 | 401.00   | 401  | 2.0 | 402  |

## 4 Analysis of q-features $(q_3)$ (all magnitudes)

```
[9]: x_np=x.to_numpy()
import qfeatures
coefficients = dataset_module.coefficients
systems = dataset_module.systems
coefficients_np = np.array([coefficients[k] for k in x.columns])
systems = [systems[k] for k in x.columns]
q=qfeatures.calculate(x_np,coefficients_np,x.columns,systems,combination_size=3)
m = q.magnitudes

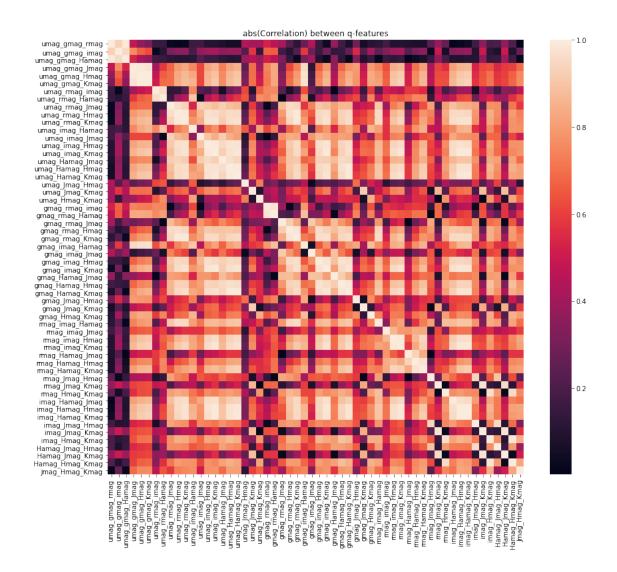
q_df = pd.DataFrame(m, columns = q.column_names)
q_df.describe()
```

| [9]: |                | umag_gmag_rmag           | umag_gmag_imag           | umag_gmag_Hamag          | umag_gmag_Jmag    | \    |
|------|----------------|--------------------------|--------------------------|--------------------------|-------------------|------|
|      | count          | 281.000000               | 281.000000               | 281.000000               | 281.000000        |      |
|      | mean           | 0.176481                 | -0.396841                | -0.070167                | -3.153199         |      |
|      | std            | 0.828204                 | 0.931151                 | 0.837281                 | 2.455464          |      |
|      | min            | -3.024675                | -4.052690                | -3.552477                | -9.888333         |      |
|      | 25%            | -0.241861                | -0.820643                | -0.437056                | -4.580278         |      |
|      | 50%            | 0.085887                 | -0.539825                | -0.112897                | -2.613333         |      |
|      | 75%            | 0.524026                 | 0.015439                 | 0.255280                 | -1.504306         |      |
|      | max            | 3.258442                 | 2.916433                 | 2.972150                 | 2.814444          |      |
|      |                |                          |                          |                          |                   |      |
|      |                | ${\tt umag\_gmag\_Hmag}$ | ${\tt umag\_gmag\_Kmag}$ | ${\tt umag\_rmag\_imag}$ | umag_rmag_Hamag   | \    |
|      | count          | 281.000000               | 281.000000               | 281.000000               | 281.000000        |      |
|      | mean           | -5.836835                | -9.613043                | 0.714044                 | 1.114363          |      |
|      | std            | 4.269958                 | 6.795943                 | 1.040089                 | 1.248407          |      |
|      | min            | -17.494783               | -28.841438               | -4.042982                | -3.367383         |      |
|      | 25%            | -8.132826                | -13.151503               | 0.263977                 | 0.471121          |      |
|      | 50%            | -4.710435                | -7.815948                | 0.656433                 | 0.916729          |      |
|      | 75%            | -2.732826                | -4.600065                | 1.151287                 | 1.446168          |      |
|      | max            | 2.990652                 | 3.563529                 | 10.171579                | 10.305607         |      |
|      |                |                          |                          |                          |                   |      |
|      | umag_rmag_Jmag |                          | ${\tt umag\_rmag\_Hmag}$ | imag_Hamag_Jm            | nag imag_Hamag_Hm | ag \ |
|      | count          | 281.000000               | 281.000000               | 281.0000                 | 281.0000          | 00   |

```
-3.019403
                              -6.650275
                                                    0.443990
                                                                       1.053812
mean
                               4.640293
std
              2.347558
                                                    0.271688
                                                                       0.745449
min
            -12.896667
                             -18.780435
                                                    0.004028
                                                                      -0.038696
25%
             -4.200000
                              -9.076957
                                                    0.239583
                                                                       0.489565
50%
             -2.366667
                              -5.164348
                                                    0.365556
                                                                      0.825000
75%
             -1.32222
                              -3.123478
                                                    0.615278
                                                                       1.424348
              7.726667
                               5.797391
                                                    1.117639
                                                                       3.142174
max
       imag Hamag Kmag
                         imag_Jmag_Hmag
                                          imag_Jmag_Kmag
                                                            imag Hmag Kmag
             281.000000
                              281.000000
                                               281.000000
                                                                281.000000
count
               1.917950
                                                -0.337591
mean
                                0.401837
                                                                  0.533012
std
               1.392776
                                0.320037
                                                 0.486605
                                                                  0.524202
min
               0.146471
                               -0.215217
                                                -2.172941
                                                                 -1.551438
25%
               0.849346
                                0.219783
                                                -0.645294
                                                                  0.213007
50%
               1.470065
                                0.310217
                                                -0.250000
                                                                  0.389804
75%
                                0.515435
               2.493137
                                                -0.038235
                                                                  0.848301
               5.924771
                                2.255217
                                                 2.104706
                                                                  1.883660
max
       Hamag_Jmag_Hmag
                         Hamag_Jmag_Kmag
                                            Hamag_Hmag_Kmag
                                                              Jmag_Hmag_Kmag
count
             281.000000
                               281.000000
                                                 281.000000
                                                                  281.000000
mean
               0.426916
                                -0.633676
                                                   0.567980
                                                                    0.108408
std
               0.473221
                                 0.710417
                                                   0.746762
                                                                    0.133023
min
              -0.554348
                                -3.221895
                                                  -2.051373
                                                                   -0.394379
25%
               0.156522
                                -1.002876
                                                   0.135490
                                                                    0.024052
50%
               0.291739
                                -0.444510
                                                                    0.073529
                                                   0.401569
75%
               0.648261
                                -0.143268
                                                   0.976667
                                                                    0.178039
                                 2.382810
                                                   2.523922
max
               2.598696
                                                                    0.756601
```

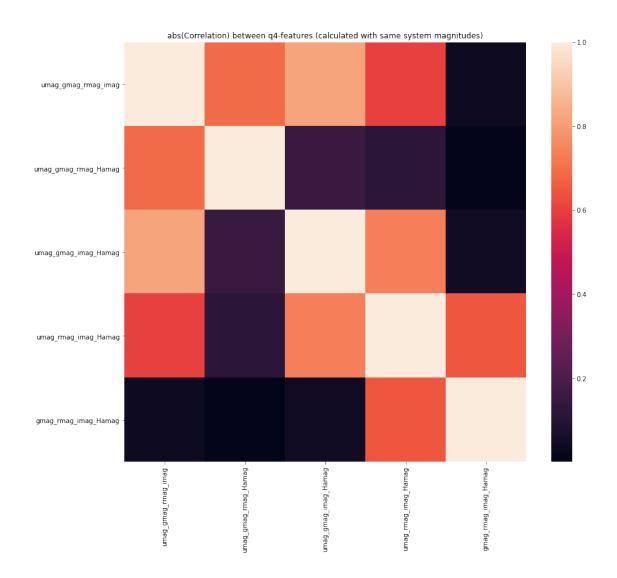
[8 rows x 56 columns]

```
[10]: sn.heatmap(q_df.corr().abs())
  plt.title("abs(Correlation) between q-features")
  plt.show()
```



# 5 Analysis of q-features $(q_4)$ (calculated by system to avoid combinatory explosion)

```
q_df = pd.DataFrame(m, columns = q.column_names)
      q_df.describe()
[11]:
                                   umag_gmag_rmag_Hamag
                                                         umag_gmag_imag_Hamag
             umag_gmag_rmag_imag
                      281.000000
                                             281.000000
                                                                    281.000000
      count
                       -0.596214
                                              -2.067113
                                                                     -0.014696
     mean
     std
                        0.821523
                                               1.676793
                                                                      0.840963
                                                                     -1.711163
     min
                       -3.788333
                                              -9.456471
     25%
                       -0.965500
                                              -2.481176
                                                                     -0.603023
     50%
                       -0.625167
                                              -1.647647
                                                                     -0.114186
                                              -1.179412
     75%
                       -0.220333
                                                                      0.420930
     max
                        5.089500
                                               4.297647
                                                                      5.402558
             umag_rmag_imag_Hamag
                                   gmag_rmag_imag_Hamag
                       281.000000
                                              281.000000
     count
     mean
                         0.333171
                                                0.347867
     std
                         1.100247
                                                0.747807
     min
                        -3.099302
                                               -3.315581
     25%
                        -0.465581
                                                0.062558
     50%
                         0.400000
                                                0.254651
     75%
                         0.859767
                                                0.551860
     max
                        10.161395
                                                4.758837
[12]: sn.heatmap(q_df.corr().abs())
      _=plt.title("abs(Correlation) between q4-features (calculated with same system_
       →magnitudes)")
```



```
[13]: q_dfy=pd.concat([q_df,y],axis=1)
sn.pairplot(q_dfy,hue="em")
_=plt.suptitle("Scatter plots between q4-features (calculated with same system
→magnitudes)")
```

