#### Notebook

March 26, 2021

```
[1]: dataset_name = 'all_em'
[2]: %reload_ext autoreload
     %autoreload 2
     default_figsize=(14,12)
[3]: import datasets
     import numpy as np
     import pandas as pd
     import seaborn as sn
     import matplotlib.pyplot as plt
     import matplotlib
     matplotlib.rcParams['figure.figsize'] = (14, 12)
     dataset_module = datasets.datasets_by_name_all[dataset_name]
     x,y,metadata = dataset_module.load(dropna=True,verbose=True)
     y = datasets.map_y_em(y,dataset_name)
     \# generate dataframe with both x and y
     xy = pd.concat([x,y],axis=1)
     xy.describe()
    Warning loading data from Mohr-Smith_2017.csv:
    Dropped 38 rows with missing values.
    Rows (original):
                       5915
    Rows (after drop): 5877
    Warning loading data from McSwain2005-2009_VPHAS-2MASS.csv:
    Dropped 2313 rows with missing values.
    Rows (original):
                      5455
    Rows (after drop): 3142
    Warning loading data from Hou2016_VPHAS-SDSS-IPHAS-2MASS.csv:
    Dropped 27 rows with missing values.
    Rows (original):
                       1034
    Rows (after drop): 1007
```

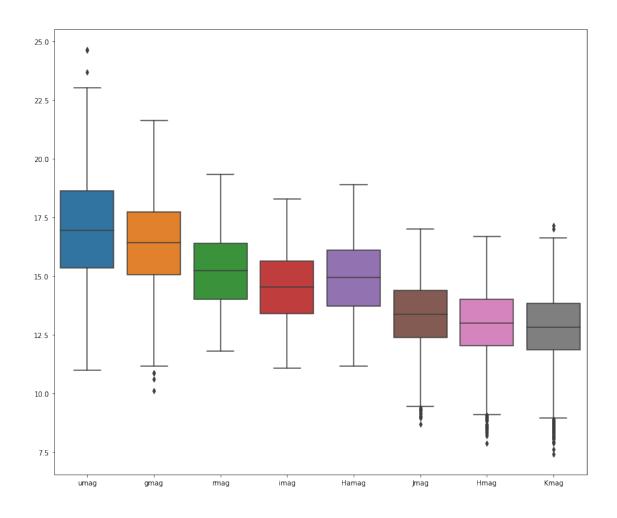
```
[3]:
                                                                  imag
                                                                                Hamag
                     umag
                                    gmag
                                                   rmag
                                          10307.000000
                                                         10307.000000
                                                                         10307.000000
     count
            10307.000000
                           10307.000000
                                              15.257591
                                                             14.554945
                                                                            14.953842
     mean
                16.952936
                               16.452857
     std
                                               1.548815
                                                              1.438887
                                                                             1.522385
                 2.135863
                                1.835733
     min
                10.980000
                               10.130000
                                              11.820000
                                                             11.081000
                                                                            11.160000
     25%
                15.340000
                               15.050000
                                              14.020000
                                                             13.400000
                                                                            13.730000
     50%
                16.940000
                               16.420000
                                              15.240000
                                                             14.534000
                                                                            14.940000
     75%
                18.625000
                               17.730000
                                              16.404500
                                                             15.633000
                                                                            16.100000
                24.651000
                               21.633000
                                              19.330000
                                                             18.290000
                                                                            18.890000
     max
                     Jmag
                                    Hmag
                                                   Kmag
                                                                    em
            10307.000000
                           10307.000000
                                          10307.000000
                                                         10307.000000
     count
                13.386535
                               12.990008
                                              12.802591
                                                              0.139129
     mean
                                                              0.346098
     std
                 1.354593
                                1.371860
                                               1.394660
     min
                 8.693000
                                7.870000
                                               7.414000
                                                              0.000000
     25%
                12.396000
                               12.040000
                                              11.868000
                                                              0.000000
     50%
                13.374000
                               13.010000
                                              12.833000
                                                              0.000000
     75%
                               14.003000
                                              13.831500
                                                              0.000000
                14.386000
                17.013000
                               16.700000
                                              17.150000
                                                              1.000000
     max
```

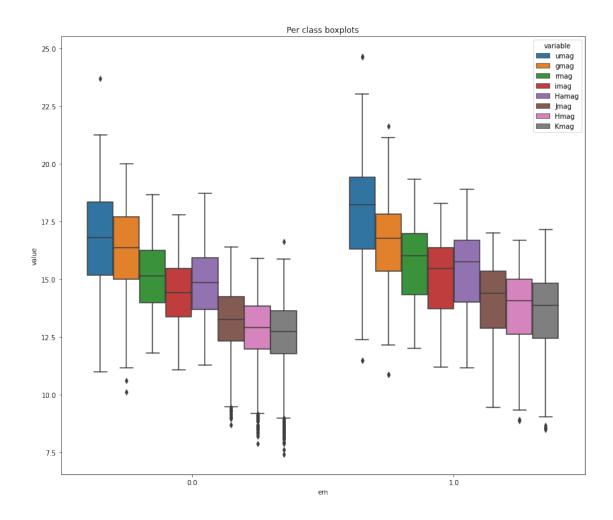
#### 1 Variable visualization

```
[4]: sn.boxplot(data=x)

plt.figure()
xy_long = pd.melt(xy, id_vars='em')
sn.boxplot(x='em', y='value', hue='variable', data=xy_long)
plt.title("Per class boxplots")
```

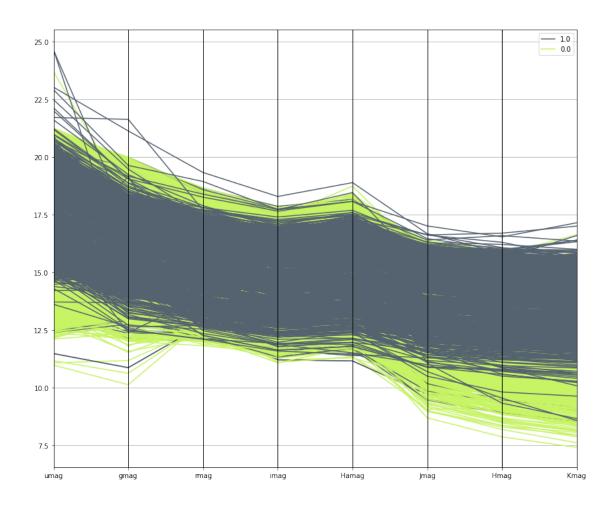
[4]: Text(0.5, 1.0, 'Per class boxplots')

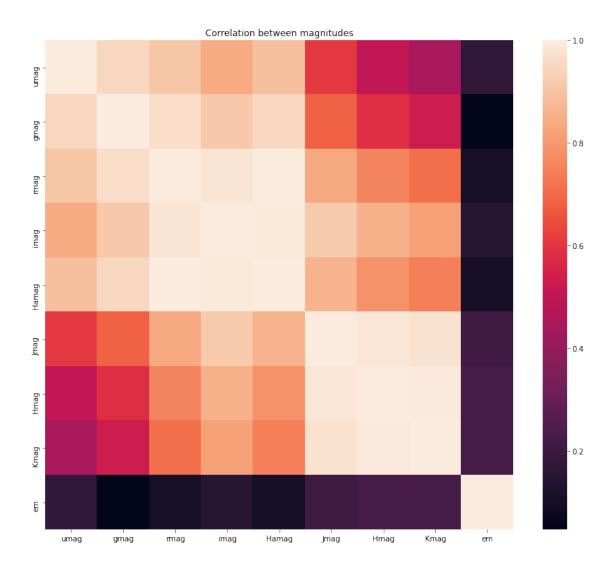




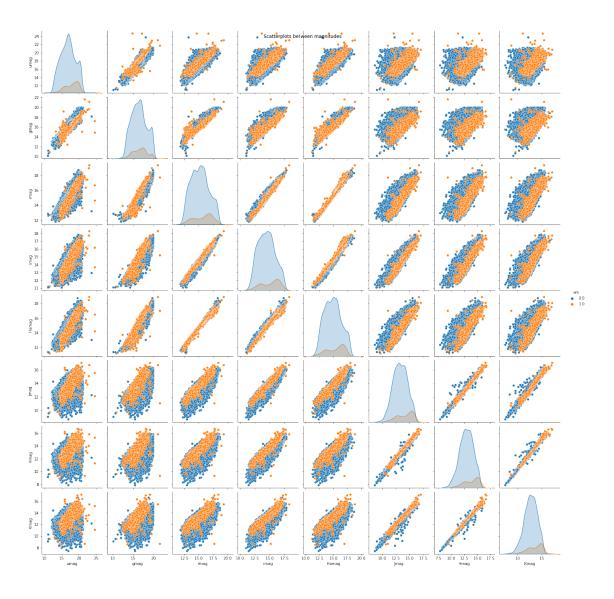
```
[5]: pd.plotting.parallel_coordinates(xy,"em",color=('#556270','#C7F464'))
```

[5]: <AxesSubplot:>





[6]: Text(0.5, 0.98, 'Scatterplots between magnitudes')



### 2 Outlier detection via confidence interval

```
[7]: from scipy import stats
    m = len(x.columns) # number of columns = number of hypothesis
    confidence= 0.99
    adjusted_confidence = 1- (1-confidence)/m # bonferroni-adjusted confidence
    max_zscore = stats.norm.ppf(adjusted_confidence)
    print(f"Confidence (desired): {confidence}")
    print(f"Confidence (adjusted): {adjusted_confidence}")
    print(f"Z-score (adjusted): {max_zscore}")

indices = (np.abs(stats.zscore(x-x.mean())) > max_zscore).any(axis=1)
    outliers_x = x[indices]
```

```
if dataset_name != "all_em":
   outliers_metadata = metadata[indices]
   outliers_x = pd.concat([outliers_x,outliers_metadata],axis=1)
outliers_x
```

Confidence (desired): 0.99 Confidence (adjusted): 0.99875

Z-score (adjusted): 3.023341439739154

[7]:		umag	gmag	rmag	imag	Hamag	Jmag	Hmag	Kmag
	40	23.710	18.130	13.210	12.940	13.010	12.250	12.170	12.180
	76	10.980	10.130	12.870	11.100	11.350	9.060	9.160	9.080
	89	11.480	10.870	12.730	11.210	11.160	9.710	9.610	9.520
	90	11.480	10.870	12.730	11.210	11.160	9.710	9.610	9.520
	144	11.170	10.630	12.740	11.110	11.320	9.570	9.560	9.490
	264	19.450	17.230	14.220	12.360	13.630	9.650	8.910	8.510
	314	17.230	15.975	13.523	12.100	13.031	9.670	8.930	8.536
	321	17.566	15.969	13.405	11.925	12.928	9.317	8.560	8.115
	327	17.929	16.214	13.487	11.917	12.970	9.144	8.367	7.875
	379	16.304	15.184	12.878	11.698	12.404	9.383	8.702	8.270
	412	16.936	15.480	12.953	11.486	12.341	8.693	7.870	7.414
	433	20.597	18.508	15.374	13.514	14.826	10.056	9.057	8.424
	466	16.588	15.619	13.410	12.131	12.934	9.722	9.025	8.567
	522	17.558	16.161	13.570	12.095	13.049	9.327	8.474	7.953
	582	14.975	14.257	12.236	11.081	11.762	8.968	8.297	7.940
	718	19.141	17.146	14.245	12.551	13.746	9.479	8.656	8.113
	736	15.700	14.928	12.883	11.681	12.432	9.315	8.620	8.200
	830	14.600	14.320	12.575	11.566	12.225	9.273	8.673	8.371
	839	14.593	14.293	12.563	11.542	12.169	9.450	8.950	8.520
	1401	14.979	14.243	12.437	11.366	11.680	9.488	8.925	8.498
	1994	15.168	14.395	12.444	11.318	11.885	9.005	8.365	8.059
	2064	14.353	13.961	12.394	11.538	11.903	9.465	8.881	8.555
	2218	17.744	16.371	13.813	12.309	13.302	9.674	8.837	8.406
	2526	16.736	16.161	13.962	12.592	13.489	9.756	8.880	8.334
	5034	16.710	15.442	13.140	11.778	12.642	9.577	8.856	8.469
	5640	16.351	15.423	13.115	11.700	12.603	9.018	8.190	7.617
	5844	14.949	14.260	12.473	11.405	12.035	9.485	8.892	8.531
	5886	15.297	14.487	12.594	11.352	12.067	9.205	8.511	8.126
	6003	20.484	18.317	15.149	13.372	14.604	9.970	9.007	8.402
	7620	19.190	15.990	13.720	12.080	13.140	9.836	8.866	8.505
	8321	20.270	16.750	14.240	12.350	13.660	9.725	8.603	8.161
	8641	14.210	13.950	13.340	12.930	13.150		9.971	8.329
	8876	20.660	16.880	14.000	12.590	13.460	9.700	8.521	8.118
	9186	20.140	16.660	14.010	12.480	13.430	9.984	8.943	8.580
	9432	24.635	17.203	16.660	16.170	16.480	15.515	15.300	15.175
	9854	20.728	19.168	18.390	17.730	18.080	17.013	16.539	17.150
	9929	24.651	14.845	14.630	13.680	14.190	12.102	11.286	11.082

## 3 Outlier detection via IQR

```
[8]: iqr_factor=1.5
    q25,q75=x.quantile(0.25),x.quantile(0.75)
    iqr=q75-q25
    min_values = q25-iqr_factor*iqr
    max_values = q75+iqr_factor*iqr
# ou
    indices = (np.logical_or(x<min_values,x>max_values)).any(axis=1)
    outliers_x = x[indices]
    if dataset_name != "all_em":
        outliers_metadata = metadata[indices]
        outliers_x = pd.concat([outliers_x,outliers_metadata],axis=1)
    outliers_x
```

```
[8]:
                                     imag
                                            Hamag
                                                     Jmag
                                                             Hmag
                                                                     Kmag
            umag
                     gmag
                             rmag
                          13.210
                                   12.940
                                           13.010 12.250
     40
          23.710
                  18.130
                                                           12.170
                                                                   12.180
     76
                          12.870
                                   11.100
                                           11.350
           10.980
                   10.130
                                                    9.060
                                                            9.160
                                                                    9.080
           11.480
                  10.870
                          12.730
                                   11.210
                                           11.160
                                                    9.710
                                                            9.610
                                                                    9.520
     90
           11.480
                  10.870
                          12.730
                                   11.210
                                           11.160
                                                    9.710
                                                            9.610
                                                                    9.520
     144
          11.170
                  10.630 12.740
                                  11.110
                                           11.320
                                                    9.570
                                                            9.560
                                                                    9.490
                                  12.360
     264
                  17.230 14.220
                                                    9.650
           19.450
                                           13.630
                                                            8.910
                                                                    8.510
     275
           17.560
                  16.460 13.810
                                  12.200
                                           13.270
                                                    9.780
                                                            9.140
                                                                    8.750
     299
                                  12.248
                                                    9.942
          17.129
                  15.965
                          13.610
                                           13.113
                                                            9.267
                                                                    8.845
     314
           17.230
                  15.975 13.523
                                  12.100
                                           13.031
                                                    9.670
                                                            8.930
                                                                    8.536
     321
           17.566
                  15.969
                          13.405
                                   11.925
                                           12.928
                                                    9.317
                                                            8.560
                                                                    8.115
     327
                                   11.917
          17.929
                  16.214
                          13.487
                                           12.970
                                                    9.144
                                                            8.367
                                                                    7.875
     338
          17.728
                  16.367
                          13.978
                                  12.543
                                           13.478 10.023
                                                            9.224
                                                                    8.802
     379
           16.304 15.184 12.878 11.698
                                           12.404
                                                    9.383
                                                            8.702
                                                                    8.270
     412
          16.936 15.480 12.953 11.486
                                           12.341
                                                    8.693
                                                            7.870
                                                                    7.414
     433
          20.597
                  18.508 15.374
                                  13.514
                                           14.826 10.056
                                                            9.057
                                                                    8.424
     466
           16.588
                  15.619 13.410 12.131
                                           12.934
                                                    9.722
                                                            9.025
                                                                    8.567
     522
                                  12.095
                                                                    7.953
           17.558
                  16.161
                          13.570
                                           13.049
                                                    9.327
                                                            8.474
     582
                                   11.081
           14.975
                  14.257
                          12.236
                                           11.762
                                                    8.968
                                                            8.297
                                                                    7.940
     587
          14.794
                  14.270 12.475
                                   11.404
                                           12.034
                                                    9.516
                                                            8.969
                                                                    8.667
     718
           19.141
                  17.146 14.245
                                   12.551
                                           13.746
                                                    9.479
                                                            8.656
                                                                    8.113
     736
          15.700
                  14.928 12.883
                                  11.681
                                           12.432
                                                    9.315
                                                            8.620
                                                                    8.200
     750
          17.844
                  16.488 14.034
                                   12.574
                                           13.513
                                                    9.870
                                                            9.100
                                                                    8.600
     830
          14.600
                  14.320 12.575
                                   11.566
                                           12.225
                                                    9.273
                                                            8.673
                                                                    8.371
     839
           14.593
                  14.293 12.563
                                   11.542
                                           12.169
                                                    9.450
                                                            8.950
                                                                    8.520
     1401 14.979
                  14.243
                          12.437
                                   11.366
                                           11.680
                                                    9.488
                                                            8.925
                                                                    8.498
     1994 15.168
                  14.395
                          12.444
                                   11.318
                                           11.885
                                                    9.005
                                                            8.365
                                                                    8.059
     2064
          14.353
                  13.961
                          12.394
                                   11.538
                                           11.903
                                                    9.465
                                                            8.881
                                                                    8.555
     2218 17.744
                  16.371
                          13.813
                                  12.309
                                           13.302
                                                    9.674
                                                            8.837
                                                                    8.406
```

```
2526
     16.736
              16.161
                      13.962
                              12.592
                                      13.489
                                               9.756
                                                       8.880
                                                                8.334
                                                                8.725
2642
     15.297
              14.605
                      12.680
                              11.556
                                      12.232
                                               9.689
                                                       9.120
4675
     16.992
              15.882
                      13.628
                              12.295
                                      13.172
                                              10.076
                                                       9.316
                                                                8.894
5034
     16.710
              15.442
                      13.140
                              11.778
                                      12.642
                                               9.577
                                                       8.856
                                                                8.469
5085
     14.948
              14.293
                      12.512
                              11.497
                                               9.699
                                                       9.197
                                                                8.898
                                      12.127
5451
     16.262
              15.748
                      13.700
                              12.411
                                      13.154
                                               9.975
                                                       9.167
                                                                8.738
5640 16.351
              15.423
                     13.115
                              11.700
                                      12.603
                                               9.018
                                                       8.190
                                                                7.617
5844 14.949
              14.260
                     12.473
                              11.405
                                      12.035
                                               9.485
                                                       8.892
                                                                8.531
5886 15.297
              14.487
                      12.594
                              11.352
                                      12.067
                                               9.205
                                                       8.511
                                                                8.126
6003
     20.484
                      15.149
                              13.372
                                      14.604
                                               9.970
                                                       9.007
              18.317
                                                                8.402
7430 16.870
              14.440
                      12.510
                              11.620
                                      12.130
                                               9.924
                                                       9.015
                                                                8.747
7620 19.190
              15.990
                      13.720
                              12.080
                                      13.140
                                               9.836
                                                       8.866
                                                                8.505
                              12.090
8152 18.690
              15.600
                      13.520
                                      13.010
                                              10.053
                                                       9.082
                                                                8.692
              16.750
                                                       8.603
8321
     20.270
                     14.240
                              12.350
                                      13.660
                                               9.725
                                                                8.161
8641 14.210
              13.950
                     13.340
                              12.930
                                      13.150
                                              12.348
                                                       9.971
                                                                8.329
8841 18.880
              15.780
                     13.350
                              12.230
                                      12.900
                                               9.957
                                                       8.990
                                                                8.636
8876 20.660
              16.880
                     14.000
                              12.590
                                      13.460
                                               9.700
                                                       8.521
                                                                8.118
9173 20.290
                              12.640
                                              10.106
                                                       9.070
              16.890
                     14.100
                                      13.600
                                                                8.703
9186 20.140
              16.660
                     14.010
                              12.480
                                      13.430
                                               9.984
                                                       8.943
                                                                8.580
9432 24.635
                      16.660
                              16.170
                                      16.480
                                              15.515
                                                      15.300
              17.203
                                                               15.175
9610 19.594
              18.110 17.700
                              17.240
                                      17.510
                                              16.625
                                                      16.700
                                                               17.006
9854 20.728
                      18.390
                              17.730
                                      18.080
                                              17.013
              19.168
                                                       16.539
                                                               17.150
9929 24.651
              14.845
                      14.630
                              13.680
                                      14.190
                                              12.102
                                                      11.286
                                                               11.082
9962 14.853
              13.601
                      12.860
                              12.310
                                      12.370
                                              10.700
                                                       9.547
                                                                8.578
9983
     21.713 21.633
                     17.700
                              15.200
                                      17.000
                                              11.054
                                                       9.331
                                                                8.658
```

## 4 Analysis of q-features $(q_3)$ (all magnitudes)

```
[9]: x_np=x.to_numpy()
import qfeatures
coefficients = dataset_module.coefficients
systems = dataset_module.systems
coefficients_np = np.array([coefficients[k] for k in x.columns])
systems = [systems[k] for k in x.columns]
q=qfeatures.calculate(x_np,coefficients_np,x.columns,systems,combination_size=3)
m = q.magnitudes

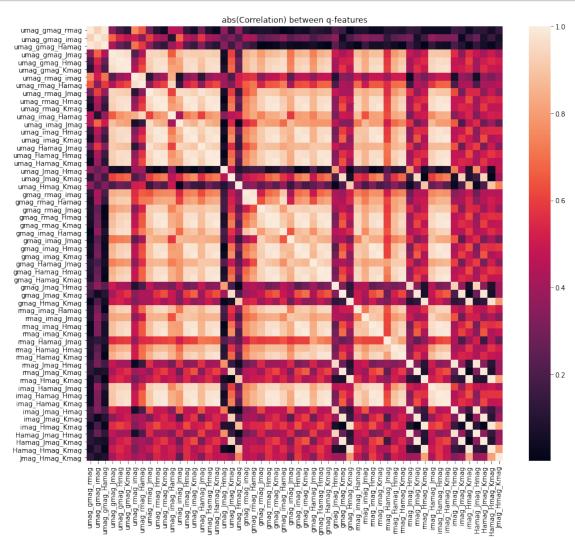
q_df = pd.DataFrame(m, columns = q.column_names)
q_df.describe()
```

```
[9]:
            umag_gmag_rmag
                             umag_gmag_imag
                                             umag_gmag_Hamag umag_gmag_Jmag
     count
              10307.000000
                               10307.000000
                                                 10307.000000
                                                                  10307.000000
                                  -0.709701
     mean
                 -0.063921
                                                    -0.263438
                                                                     -4.141992
     std
                  0.658024
                                   0.703104
                                                     0.668365
                                                                      1.920013
                                                                   -15.935431
     min
                 -6.198398
                                  -7.366959
                                                    -6.524593
                 -0.483868
     25%
                                  -1.148602
                                                    -0.695596
                                                                     -5.547403
```

50%	-0.202892	-1.020696	-0.427495	-4.001958	
75%	0.079946	-0.450000	-0.102033	-2.759167	
max	9.704550	9.063398	9.472379	5.653403	
	umag_gmag_Hmag	umag_gmag_Kmag u	umag_rmag_imag un	nag_rmag_Hamag \	
count	10307.000000	10307.000000	10307.000000	10307.000000	
mean	-7.705369	-12.502502	0.840664	1.400112	
std	3.425802	5.545913	0.771068	0.943564	
min	-29.070391	-46.138137	-4.042982	-3.367383	
25%	-10.231500	-16.576010	0.330058	0.764346	
50%	-7.360348	-11.786373	0.722339	1.295589	
75%	-5.125587	-8.249484	1.310099	1.996963	
max	4.414391	4.119078	10.171579	10.305607	
	umag_rmag_Jmag	umag_rmag_Hmag	imag_Hamag_Jmag	g imag_Hamag_Hmag	\
count	10307.000000	10307.000000			
mean	-3.709929	-8.558077	. 0.537134	1.436861	
std	1.897399	3.997383	0.273023	0.694547	
min	-15.186556	-33.829435	0.156500	-0.411696	
25%	-5.096611	-11.436261	0.314993	0.895750	
50%	-3.488778	-8.058565	0.497042	1.315304	
75%	-2.278667	-5.460239	0.729924	1.944413	
max	7.726667	5.797391	1.753681	5.368848	
	imag_Hamag_Kmag	imag_Jmag_Hmag	imag_Jmag_Kmag i	.mag_Hmag_Kmag \	
count	10307.000000	10307.000000	10307.000000	10307.000000	
mean	2.624102	0.315014	-0.720819	0.799348	
std	1.275666	0.375150	0.627362	0.622198	
min	-0.772131	-6.482065	-13.751588	-11.218902	
25%	1.635833	0.089261	-0.989706	0.460582	
50%	2.406157	0.310435	-0.644588	0.783667	
75%	3.540333	0.544804	-0.366000	1.161458	
max	9.922418	4.936783	4.142765	7.507065	
	Hamag_Jmag_Hmag	Hamag_Jmag_Kmag	Hamag_Hmag_Kmag	Jmag_Hmag_Kmag	
count	10307.000000	10307.000000	10307.000000	10307.000000	
mean	0.343245	-1.142496	0.934883	0.237285	
std	0.506861	0.925879	0.801468	0.194781	
min	-9.400609	-19.827601	-15.024588	-2.622131	
25%	0.064652	-1.545882	0.516039	0.126850	
50%	0.348696	-1.020052	0.925157	0.223863	
75%	0.641043	-0.602605	1.386402	0.336935	
max	6.374304	5.383026	9.521608	2.715843	
		<del></del>			

[8 rows x 56 columns]

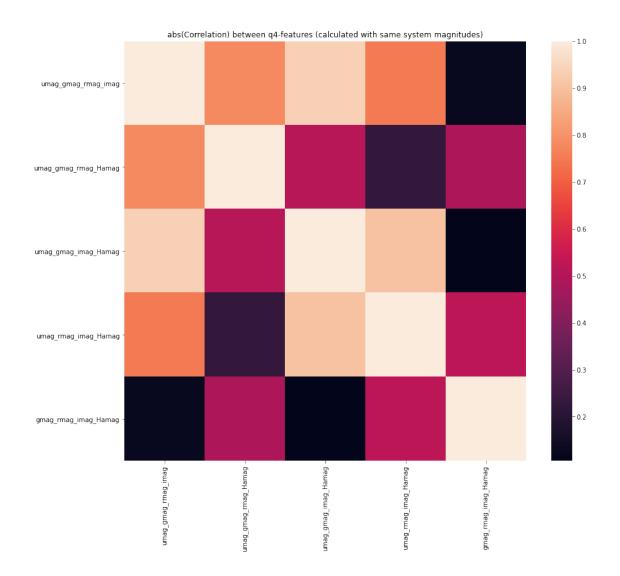
```
[10]: sn.heatmap(q_df.corr().abs())
    plt.title("abs(Correlation) between q-features")
    plt.show()
```



# 5 Analysis of q-features $(q_4)$ (calculated by system to avoid combinatory explosion)

```
[11]: x_np=x.to_numpy()
  import qfeatures
  coefficients = dataset_module.coefficients
  systems = dataset_module.systems
  coefficients_np = np.array([coefficients[k] for k in x.columns])
  systems = [systems[k] for k in x.columns]
```

```
q= qfeatures.calculate(x_np,coefficients_np,x.
      ⇒columns, systems, combination_size=4, by_system=True)
     m = q.magnitudes
      q_df = pd.DataFrame(m, columns = q.column_names)
      q_df.describe()
Γ11]:
             umag_gmag_rmag_imag
                                  umag_gmag_rmag_Hamag
                                                         umag_gmag_imag_Hamag
                    10307.000000
                                           10307.000000
                                                                  10307.000000
     mean
                       -0.776395
                                              -1.447490
                                                                     -0.511079
                        0.688391
                                                                     0.696245
     std
                                              1.001902
     min
                       -4.461667
                                              -9.456471
                                                                     -4.482791
     25%
                       -1.231108
                                              -1.919324
                                                                     -0.981256
     50%
                                              -1.639059
                                                                     -0.771860
                       -1.074867
     75%
                       -0.460083
                                              -0.995000
                                                                     -0.204186
                        8.080167
                                               6.984824
                                                                     8.513209
     max
             umag_rmag_imag_Hamag gmag_rmag_imag_Hamag
                     10307.000000
                                            10307.000000
      count
                        -0.234204
                                                0.276875
     mean
     std
                         0.811310
                                                0.349037
     min
                        -5.258953
                                               -3.315581
     25%
                        -0.752488
                                                0.131767
     50%
                        -0.521070
                                                0.248372
     75%
                         0.157907
                                                0.349721
     max
                        10.161395
                                                5.026581
[12]: sn.heatmap(q_df.corr().abs())
      _=plt.title("abs(Correlation) between q4-features (calculated with same system ∪
       →magnitudes)")
```



```
[13]: q_dfy=pd.concat([q_df,y],axis=1)
sn.pairplot(q_dfy,hue="em")
_=plt.suptitle("Scatter plots between q4-features (calculated with same system
→magnitudes)")
```

