# Exploratory analysis

#### March 18, 2021

```
[80]: %reload ext autoreload
      %autoreload 2
      default_figsize=(14,12)
[81]: import datasets
      import numpy as np
      import pandas as pd
      import seaborn as sn
      import matplotlib.pyplot as plt
      import matplotlib
      matplotlib.rcParams['figure.figsize'] = (14, 12)
      dataset_name = "hou"
      dataset_module = datasets.datasets_by_name_all[dataset_name]
      x,y,metadata = dataset_module.load(dropna=True,verbose=True)
      y = datasets.map_y_em(y,dataset_name)
      \# generate dataframe with both x and y
      xy = pd.concat([x,y],axis=1)
      xy.describe()
     Warning loading data from Hou2016_VPHAS-SDSS-IPHAS-2MASS.csv:
     Dropped 27 rows with missing values.
     Rows (original):
                         1034
     Rows (after drop): 1007
[81]:
                                                            imag
                                                                         Hamag \
                    umag
                                  gmag
                                               rmag
      count
             1007.000000
                          1007.000000
                                       1007.000000
                                                     1007.000000
                                                                  1007.000000
      mean
               17.947877
                            16.366036
                                          15.557746
                                                       15.048451
                                                                     15.347805
      std
                1.660195
                             1.368795
                                           1.418495
                                                        1.370818
                                                                      1.440670
               13.616000
                            12.398000
      min
                                          12.100000
                                                       11.590000
                                                                     11.450000
      25%
               16.505000
                            15.296000
                                          14.365000
                                                       13.825000
                                                                     14.125000
      50%
               18.217000
                            16.618000
                                          15.950000
                                                       15.430000
                                                                     15.750000
      75%
               19.226000
                            17.470500
                                          16.755000
                                                       16.225000
                                                                     16.560000
               24.651000
      max
                            21.633000
                                          19.330000
                                                       18.290000
                                                                     18.890000
                    Jmag
                                  Hmag
                                               Kmag
                                                         em
      count
            1007.000000
                         1007.000000
                                       1007.000000 1007.0
```

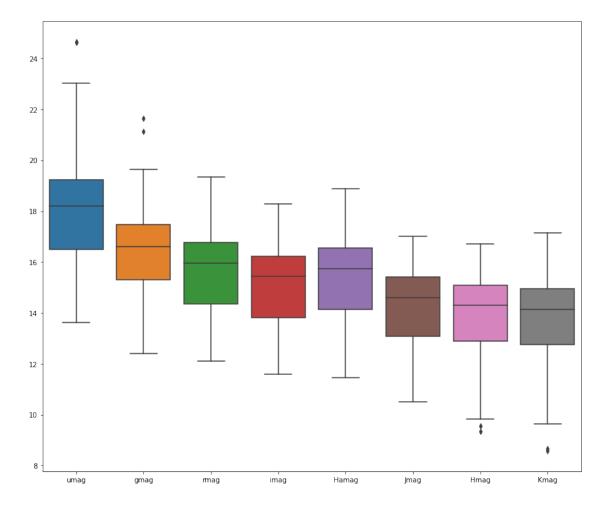
mean	14.248893	13.983537	13.843248	1.0
std	1.329480	1.331519	1.341729	0.0
min	10.501000	9.331000	8.578000	1.0
25%	13.083000	12.900500	12.767000	1.0
50%	14.586000	14.294000	14.133000	1.0
75%	15.405500	15.085000	14.954000	1.0
max	17.013000	16.700000	17.150000	1.0

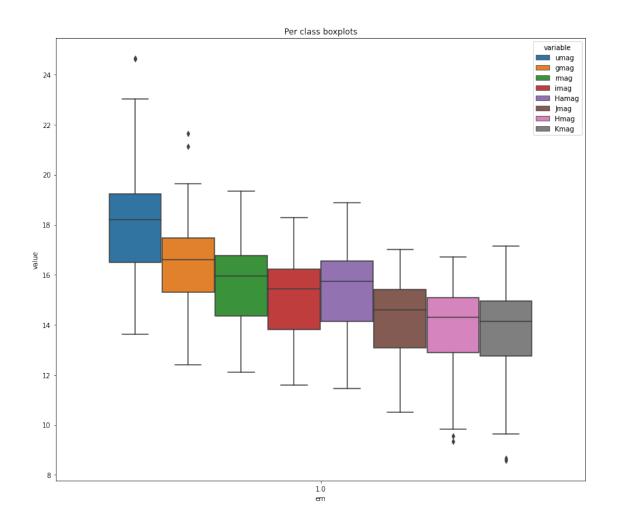
### 1 Variable visualization

```
[82]: sn.boxplot(data=x)

plt.figure()
  xy_long = pd.melt(xy, id_vars='em')
  sn.boxplot(x='em', y='value', hue='variable', data=xy_long)
  plt.title("Per class boxplots")
```

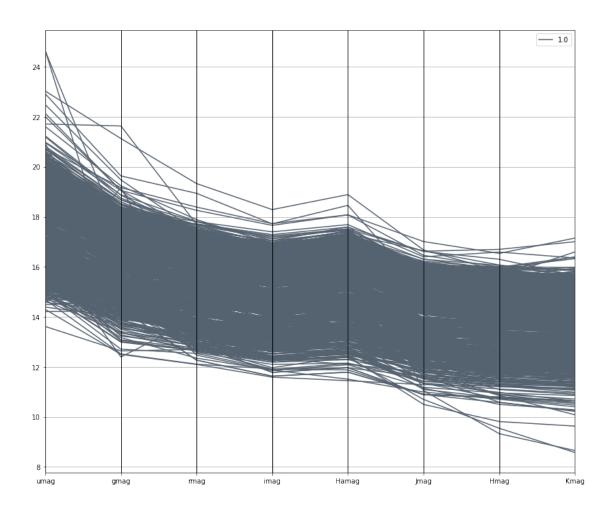
[82]: Text(0.5, 1.0, 'Per class boxplots')

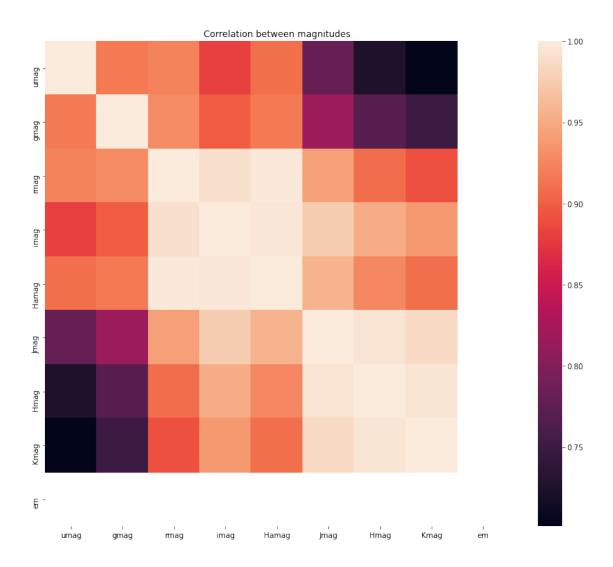




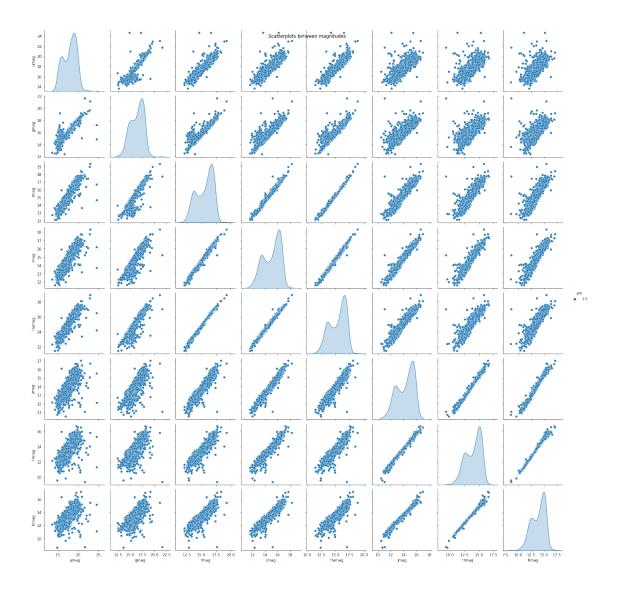
```
[83]: pd.plotting.parallel_coordinates(xy,"em",color=('#556270','#C7F464'))
```

[83]: <AxesSubplot:>





[84]: Text(0.5, 0.98, 'Scatterplots between magnitudes')



# 2 Outlier detection via confidence interval

```
[85]: from scipy import stats
    m = len(x.columns) # number of columns = number of hypothesis
    confidence = 0.98
    adjusted_confidence = 1- (1-confidence)/m # bonferroni-adjusted confidence
    max_zscore = stats.norm.ppf(adjusted_confidence)
    print(f"Confidence (desired): {confidence}")
    print(f"Confidence (adjusted): {adjusted_confidence}")
    print(f"Z-score (adjusted): {max_zscore}")

indices = (np.abs(stats.zscore(x-x.mean())) > max_zscore).any(axis=1)
    outliers_x = x[indices]
```

```
if dataset_name != "all_em":
          outliers_metadata = metadata[indices]
          outliers_x = outliers_x.
       →merge(outliers_metadata,left_index=True,right_index=True)
      outliers x
     Confidence (desired): 0.98
     Confidence (adjusted): 0.9975
     Z-score
                (adjusted): 2.807033768343811
[85]:
                            rmag
                                         Hamag
                                                   Jmag
                                                           Hmag
                                                                   Kmag Fe_type
             umag
                     gmag
                                   imag
      72
           22.918
                  19.636
                           18.94
                                  17.72
                                         18.46
                                                15.065
                                                        14.027
                                                                 13.628
                                                                            NaN
      94
           23.028
                   21.130
                           19.33
                                 18.29
                                                16.676
                                                        15.830
                                                                 15.471
                                                                            NaN
                                         18.89
      132 24.635
                   17.203
                           16.66
                                  16.17
                                         16.48
                                                15.515
                                                        15.300
                                                                 15.175
                                                                            NaN
      331
           14.300
                   12.500
                           12.10
                                  11.59
                                         11.45
                                                11.290
                                                        11.231
                                                                 11.149
                                                                            NaN
      622
          16.941
                           12.83
                                                          9.816
                   15.160
                                  11.97
                                         12.42
                                                10.501
                                                                  9.634
                                                                            NaN
      629
          24.651
                  14.845
                           14.63
                                  13.68
                                         14.19
                                                12.102
                                                        11.286
                                                                 11.082
                                                                            NaN
      662 14.853 13.601
                           12.86
                                  12.31
                                         12.37
                                                10.700
                                                          9.547
                                                                  8.578
                                                                            NaN
      683 21.713
                   21.633
                           17.70
                                  15.20
                                         17.00
                                                11.054
                                                          9.331
                                                                  8.658
                                                                            NaN
      691
          14.690 12.519
                           12.11
                                  11.92
                                         11.96
                                                11.622
                                                        11.604
                                                                            NaN
                                                                 11.546
      775
          16.656 12.398
                           13.93
                                  13.49
                                         13.71
                                                12.687
                                                        12.464
                                                                 12.359
                                                                            NaN
           h_err ...
                     Halpha_type
                                  w1_err
                                         e_Hmag
                                                  e_rmag
                                                            objtype_SIMBAD
      72
           0.092
                              ΙI
                                   0.027
                                           0.092
                                                    0.02
                                                                       NaN
      94
           0.120 ...
                              ΙI
                                   0.047
                                           0.120
                                                    0.04
                                                                       NaN
      132 0.105 ...
                                                    0.01
                              ΙI
                                   0.042
                                           0.105
                                                                       NaN
      331 0.022 ...
                              ΙI
                                   0.023
                                           0.022
                                                    0.00
                                                                      Star
      622 0.026 ...
                              VI
                                                    0.00
                                                                       NaN
                                   0.023
                                           0.026
      629 0.030 ...
                              VI
                                   0.062
                                           0.030
                                                    0.00
                                                                       NaN
      662 0.029
                               V
                                   0.031
                                           0.029
                                                    0.00
                                                                       NaN
      683 0.024
                                   0.023
                                                    0.01
                              ΙI
                                           0.024
                                                                       NaN
      691 0.025
                                   0.022
                              ΙI
                                           0.025
                                                    0.00 Star in Cluster
      775 0.024
                              ΙI
                                   0.023
                                           0.024
                                                    0.00
                                                                       NaN
              _RA2000 e_Kmag
                                    k e_gmag
                                                _DEC2000
      72
                        0.080
            87.994208
                              13.628 0.029
                                              22.254083
      94
            83.549950
                               15.471 0.033
                        0.146
                                              29.150907
      132
            81.378157
                        0.118
                               15.175
                                       0.005
                                              29.639252
      331
            92.968107
                        0.017
                               11.149
                                       0.001
                                              23.729066
      622
            97.414520
                        0.026
                                9.634
                                       0.005
                                               0.917894
      629
                        0.044 11.082 0.004
            88.095161
                                              20.697878
      662
            87.728220
                        0.020
                                8.578
                                      0.003
                                              20.246568
      683
           100.284660
                        0.023
                                8.658
                                       0.047
                                              10.402258
      691
           102.043940
                        0.024
                               11.546
                                       0.002
                                               9.644880
      775
            99.229276
                        0.024
                               12.359
                                       0.002
                                               9.463165
```

[10 rows x 28 columns]

### 3 Outlier detection via IQR

```
[86]: igr factor=1.5
     q25,q75=x.quantile(0.25),x.quantile(0.75)
     iqr=q75-q25
     min_values = q25-iqr_factor*iqr
     max values = q75+iqr factor*iqr
      # ou
     indices = (np.logical_or(x<min_values,x>max_values)).any(axis=1)
     outliers_x = x[indices]
     if dataset_name != "all_em":
         outliers_metadata = metadata[indices]
         outliers_x = outliers_x.
      →merge(outliers_metadata,left_index=True,right_index=True)
     outliers x
[86]:
                                                                Kmag Fe_type \
                                  imag Hamag
                                                Jmag
                                                        Hmag
            umag
                    gmag
                           rmag
     94
          23.028
                  21.130 19.33 18.29
                                       18.89 16.676
                                                      15.830
                                                              15.471
                                                                         NaN
     132 24.635 17.203 16.66 16.17
                                       16.48 15.515 15.300
                                                              15.175
                                                                         NaN
     629 24.651 14.845 14.63 13.68 14.19 12.102 11.286
                                                              11.082
                                                                         NaN
     662 14.853 13.601 12.86 12.31 12.37 10.700
                                                      9.547
                                                               8.578
                                                                         NaN
     683 21.713 21.633 17.70 15.20 17.00 11.054
                                                       9.331
                                                               8.658
                                                                         NaN
          h_err ... Halpha_type w1_err e_Hmag e_rmag objtype_SIMBAD \
     94
          0.120 ...
                             ΙI
                                  0.047
                                         0.120
                                                  0.04
                                                                   NaN
                                                  0.01
     132 0.105 ...
                             ΙI
                                  0.042
                                         0.105
                                                                   NaN
     629 0.030 ...
                                         0.030
                                                  0.00
                             VI
                                  0.062
                                                                   NaN
     662 0.029 ...
                             V
                                  0.031
                                         0.029
                                                  0.00
                                                                   NaN
     683 0.024 ...
                             ΙI
                                  0.023
                                         0.024
                                                  0.01
                                                                   NaN
             _RA2000 e_Kmag
                                   k e_gmag
                                              DEC2000
           83.549950
                     0.146 15.471 0.033 29.150907
     94
                       0.118 15.175 0.005 29.639252
     132
           81.378157
     629
                       0.044 11.082 0.004 20.697878
           88.095161
     662
           87.728220
                       0.020
                             8.578 0.003 20.246568
     683 100.284660
                       0.023
                               8.658 0.047 10.402258
     [5 rows x 28 columns]
```

## 4 Analysis of q-features $(q_3)$ (all magnitudes)

```
[87]: x_np=x.to_numpy()
import qfeatures
coefficients = dataset_module.coefficients
systems = dataset_module.systems
coefficients_np = np.array([coefficients[k] for k in x.columns])
```

```
systems = [systems[k] for k in x.columns]
      q=qfeatures.calculate(x_np,coefficients_np,x.columns,systems,combination_size=3)
      m = q.magnitudes
      q_df = pd.DataFrame(m, columns = q.column_names)
      q_df.describe()
[87]:
                              umag_gmag_imag
                                               umag_gmag_Hamag
                                                                  umag_gmag_Jmag
                                                                                   \
             umag_gmag_rmag
                 1007.000000
                                  1007.000000
                                                    1007.000000
                                                                     1007.000000
      count
                    1.200440
                                     0.741977
                                                       1.063210
                                                                       -1.623278
      mean
      std
                    0.823664
                                     0.872624
                                                       0.843513
                                                                        1.436653
                   -6.198398
                                    -7.366959
                                                      -6.524593
                                                                      -15.935431
      min
      25%
                    1.178662
                                     0.741553
                                                       1.024215
                                                                       -2.055917
      50%
                    1.369199
                                     0.963304
                                                       1.265187
                                                                       -1.360764
      75%
                    1.489747
                                     1.051404
                                                       1.369208
                                                                       -0.828021
      max
                    9.704550
                                     9.063398
                                                       9.472379
                                                                        5.653403
                                                umag_rmag_imag
                                                                 umag_rmag_Hamag
             umag_gmag_Hmag
                              umag_gmag_Kmag
                 1007.000000
                                  1007.000000
                                                   1007.000000
                                                                     1007.000000
      count
                   -4.063644
                                    -7.404559
                                                      1.770638
                                                                        2.186077
      mean
      std
                    2.257856
                                     3.456072
                                                      0.516441
                                                                        0.622566
                  -29.070391
                                   -46.138137
                                                     -0.026327
                                                                       -0.079757
      min
      25%
                   -4.958109
                                    -8.856859
                                                      1.531942
                                                                        1.868495
      50%
                   -3.670370
                                                      1.732561
                                    -6.819732
                                                                        2.143327
      75%
                   -2.723609
                                    -5.253641
                                                      1.956249
                                                                        2.447827
                    4.414391
                                     4.119078
                                                      8.865444
                                                                        9.593336
      max
             umag_rmag_Jmag
                              umag_rmag_Hmag
                                                   imag_Hamag_Jmag
                                                                     imag Hamag Hmag
                                  1007.000000
                                                       1007.000000
                                                                         1007.000000
      count
                 1007.000000
                   -1.391000
                                    -4.728029
                                                          0.356941
                                                                            0.975940
      mean
      std
                    1.015766
                                     2.267895
                                                          0.134663
                                                                            0.385626
                                   -33.829435
                                                                           -0.067130
      min
                  -15.186556
                                                         -0.094083
      25%
                   -1.894056
                                    -5.835587
                                                                            0.739326
                                                          0.273833
      50%
                   -1.311667
                                    -4.451217
                                                          0.339347
                                                                            0.922130
      75%
                   -0.854889
                                    -3.377304
                                                          0.421736
                                                                            1.161500
                    4.667222
                                     1.825435
                                                          1.751083
                                                                            5.368848
      max
             imag_Hamag_Kmag
                                imag_Jmag_Hmag
                                                 imag_Jmag_Kmag
                                                                  imag_Hmag_Kmag
                  1007.000000
                                   1007.000000
                                                    1007.000000
                                                                     1007.000000
      count
                     1.814892
                                      0.228467
                                                      -0.512821
                                                                        0.491838
      mean
      std
                     0.720126
                                      0.231544
                                                       0.514158
                                                                        0.610817
```

-5.255294

-0.738353

-0.444235

-0.242647

2.277294

-2.465464

0.206157

0.462778

0.749595

5.374222

-0.871457

0.099630

0.231152

0.353446

1.406913

min

25%

50%

75%

max

-0.639804

1.356389

1.719804

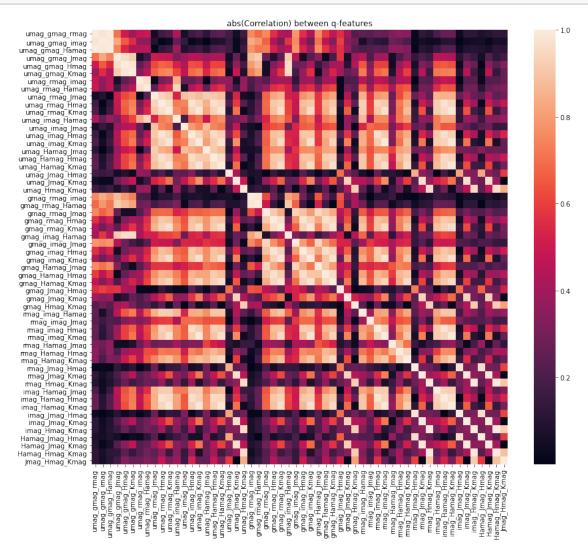
2.188350

9.922418

	${\tt Hamag\_Jmag\_Hmag}$	${\tt Hamag\_Jmag\_Kmag}$	${\tt Hamag\_Hmag\_Kmag}$	${\tt Jmag\_Hmag\_Kmag}$
count	1007.000000	1007.000000	1007.000000	1007.000000
mean	0.279772	-0.783490	0.594054	0.146156
std	0.341645	0.754679	0.813179	0.185327
min	-1.889261	-8.177190	-3.191216	-0.707641
25%	0.092609	-1.085876	0.228765	0.047830
50%	0.280348	-0.676980	0.558020	0.132556
75%	0.472978	-0.394304	0.937892	0.221882
max	1.874522	3.231967	7.073667	1.382222

[8 rows x 56 columns]

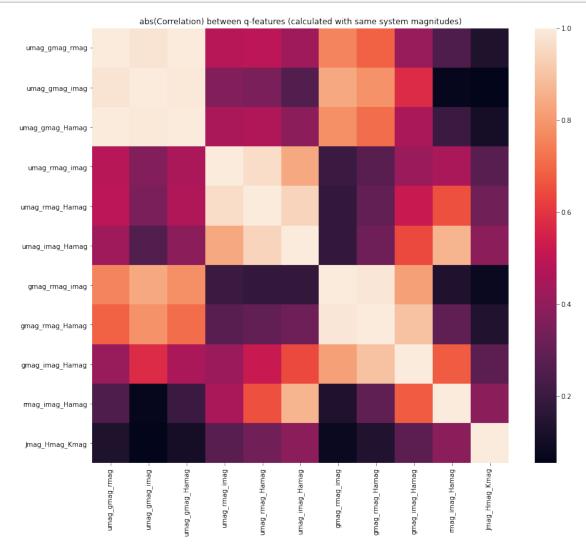
```
[88]: sn.heatmap(q_df.corr().abs())
plt.title("abs(Correlation) between q-features")
plt.show()
```



# 5 Analysis of q-features $(q_3)$ (calculated by system)

```
[89]: x np=x.to numpy()
      import qfeatures
      coefficients = dataset module.coefficients
      systems = dataset_module.systems
      coefficients_np = np.array([coefficients[k] for k in x.columns])
      systems = [systems[k] for k in x.columns]
      q= qfeatures.calculate(x_np,coefficients_np,x.
       →columns,systems,combination_size=3,by_system=True)
      m = q.magnitudes
      q_df = pd.DataFrame(m, columns = q.column_names)
      q df.describe()
[89]:
             umag_gmag_rmag
                              umag_gmag_imag
                                               umag_gmag_Hamag
                                                                 umag rmag imag
      count
                 1007.000000
                                 1007.000000
                                                    1007.000000
                                                                    1007.000000
                    1.200440
                                     0.741977
                                                       1.063210
                                                                        1.770638
      mean
      std
                   0.823664
                                     0.872624
                                                       0.843513
                                                                        0.516441
      min
                   -6.198398
                                    -7.366959
                                                      -6.524593
                                                                       -0.026327
      25%
                    1.178662
                                     0.741553
                                                       1.024215
                                                                        1.531942
      50%
                    1.369199
                                                                        1.732561
                                     0.963304
                                                       1.265187
      75%
                    1.489747
                                     1.051404
                                                       1.369208
                                                                        1.956249
                    9.704550
                                     9.063398
                                                       9.472379
                                                                        8.865444
      max
                               umag_imag_Hamag
                                                                  gmag_rmag_Hamag
             umag_rmag_Hamag
                                                 gmag_rmag_imag
                  1007.000000
                                    1007.000000
                                                    1007.000000
                                                                       1007.000000
      count
      mean
                     2.186077
                                       3.274319
                                                        0.513435
                                                                          0.711168
                     0.622566
                                       0.933284
                                                        0.502015
                                                                          0.513900
      std
      min
                    -0.079757
                                      -0.057140
                                                       -1.786737
                                                                         -1.633776
      25%
                     1.868495
                                       2.703061
                                                        0.264421
                                                                          0.430860
      50%
                     2.143327
                                       3.166897
                                                        0.384263
                                                                          0.595234
      75%
                     2.447827
                                       3.692626
                                                        0.550079
                                                                          0.796355
                     9.593336
                                      11.609692
                                                        5.197842
                                                                          5.329972
      max
             gmag_imag_Hamag
                               rmag_imag_Hamag
                                                 Jmag_Hmag_Kmag
                  1007.000000
                                    1007.000000
                                                    1007.000000
      count
      mean
                     1.540003
                                       0.593226
                                                        0.146156
      std
                     0.671485
                                       0.221377
                                                        0.185327
                    -0.928542
                                                       -0.707641
      min
                                       0.003178
      25%
                     1.103883
                                       0.454486
                                                        0.047830
      50%
                     1.399318
                                       0.556916
                                                        0.132556
      75%
                                       0.708364
                                                        0.221882
                     1.821056
                     7.770383
                                       3.004673
                                                        1.382222
      max
```

```
[90]: sn.heatmap(q_df.corr().abs())
plt.title("abs(Correlation) between q-features (calculated with same system
→magnitudes)")
plt.show()
q_dfy=pd.concat([q_df,y],axis=1)
sn.pairplot(q_dfy,hue="em")
plt.suptitle("Scatter plots between q-features (calculated with same system
→magnitudes)")
```



[90]: Text(0.5, 0.98, 'Scatter plots between q-features (calculated with same system magnitudes)')

