

## LÍNEA DE TRANSMISIÓN SIN PÉRDIDAS

$$\alpha = 0 \Rightarrow \gamma = j\beta.$$

$$V(z) = V^+ (e^{j\beta z} + \Gamma_L e^{-j\beta z})$$

$$I(z) = \frac{V^+}{Z_0} (e^{j\beta z} - \Gamma_L e^{-j\beta z})$$

$$Z(z) = Z_0 \frac{Z_L + Z_0 \tanh \gamma z}{Z_L \tanh \gamma z + Z_0}$$

$$\text{Como } \tanh j\beta z = j \tan \beta z$$

$$Z(z) = Z_0 \frac{Z_L + j Z_0 \tan \beta z}{j Z_L \tan \beta z + Z_0}$$

$$\Gamma(z) = \underbrace{|\Gamma_L| e^{j\theta}}_{\Gamma_L} e^{-2j\beta z}$$

LAS TENSIONES Y CORRIENTES SE PUEDEN ESCRIBIR:

$$V(z) = V^+ (e^{j\beta z} + \Gamma_L e^{-j\beta z}) = V^+ e^{j\beta z} (1 + \underbrace{\Gamma_L e^{-2j\beta z}}_{\Gamma(z)})$$

$$I(z) = \frac{V^+}{Z_0} (e^{j\beta z} - \Gamma_L e^{-j\beta z}) = \frac{V^+}{Z_0} e^{j\beta z} (1 - \underbrace{\Gamma_L e^{-2j\beta z}}_{\Gamma(z)})$$

COMO LA VARIACIÓN DE  $\Gamma(z)$  SE ENCUENTRA  $-|\Gamma(z)|$  Y  $|\Gamma(z)|$ , LA MAGNITUD DE  $V(z)$  ( $|V(z)|$ )

$$V_{\max} = |V^+| (1 + |\Gamma(z)|)$$

$$V_{\min} = |V^+| (1 - |\Gamma(z)|)$$

$$I_{\max} = \left| \frac{V^+}{Z_0} \right| (1 + |\Gamma(z)|)$$

$$I_{\min} = \left| \frac{V^+}{Z_0} \right| (1 - |\Gamma(z)|)$$

$$ROE = \frac{V_{\max}}{V_{\min}} = \frac{I_{\max}}{I_{\min}}$$

$$ROE = \frac{1 + |\Gamma(z)|}{1 - |\Gamma(z)|}$$

OTRA FORMA DE EXPRESAR  $|\Gamma(z)|$  ES:

$$ROE \cdot (1 - |\Gamma(z)|) = 1 + |\Gamma(z)|$$

$$ROE - ROE |\Gamma(z)| = 1 + |\Gamma(z)|$$

$$ROE - 1 = ROE |\Gamma(z)| + |\Gamma(z)|$$

$$ROE - 1 = |\Gamma(z)| (ROE + 1)$$

$$\boxed{|\Gamma(z)| = \frac{ROE - 1}{ROE + 1}}$$

SE HA VISTO

$$V(z) = V^+ (e^{\gamma z} + \Gamma_L e^{-\gamma z})$$

$$I(z) = \frac{V^+}{Z_0} (e^{\gamma z} - \Gamma_L e^{-\gamma z})$$

COMO EN UNA LÍNEA SIN PERDIDAS SE TIENE

$$\alpha = 0 \text{ y } \gamma = j\beta \text{ y } \Gamma_L = |\Gamma_L| e^{j\theta}$$

$$V(z) = V^+ e^{j\beta z} (1 + |\Gamma_L| e^{j\theta} e^{-2j\beta z})$$

$$I(z) = \frac{V^+}{Z_0} e^{j\beta z} (1 - |\Gamma_L| e^{j\theta} e^{-2j\beta z})$$

EN LA CARGA:  $z=0$ .

$$V_L = V^+ e^{j\beta z} (1 + |\Gamma_L| e^{j\theta} e^{-2j\beta z}) = V^+ (1 + |\Gamma_L| e^{j\theta})$$

$$I_L = \frac{V^+}{Z_0} (1 - |\Gamma_L|)$$

Si  $Z_L = Z_0$  CARGA ADAPTADA.

$$Z(z) = Z_0 \cdot \frac{\overbrace{Z_L}^{Z_0} + j Z_0 \tan \beta z}{\underbrace{j Z_L \tan \beta z}_{Z_0} + Z_0} = Z_0.$$

$$\Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = 0$$

$$V(z) = V^+ e^{j\beta z}$$

$$I(z) = \frac{V^+}{Z_0} e^{j\beta z}$$

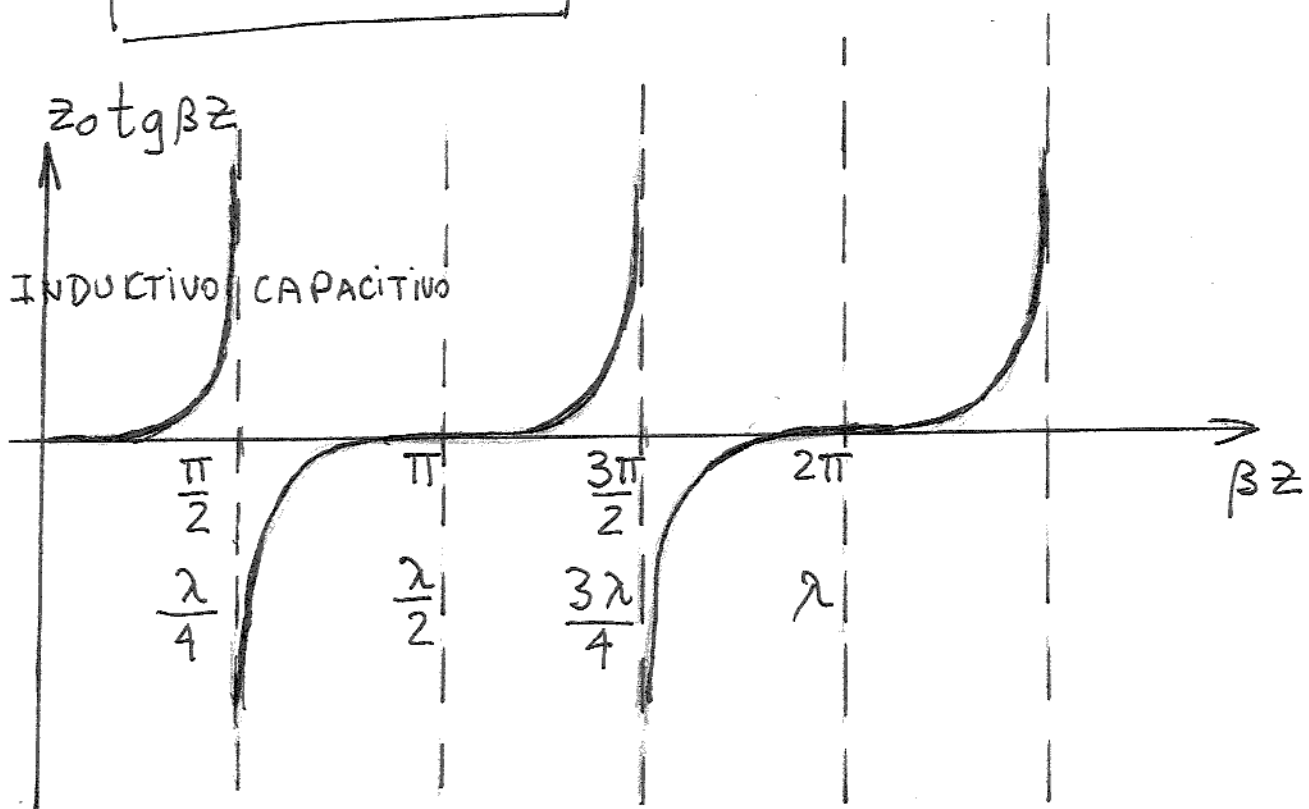
SOLO QUEDA LA ONDA QUE  
SE PROPAGA EN LAS  $+z$

"NO HAY ONDAS REFLEJADAS  
EN LA CARGA."

Si  $Z_L = 0$  CARGA EN CORTO CIRCUITO

$$Z(z) = Z_0 \cdot \frac{Z_L + j Z_0 \tan \beta z}{j Z_L \tan \beta z + Z_0} = Z_0 \frac{j \cancel{Z_0} \tan \beta z}{Z_0}$$

$$Z(z) = j Z_0 \tan \beta z$$



$$\Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = -1$$

$$ROE = \infty$$

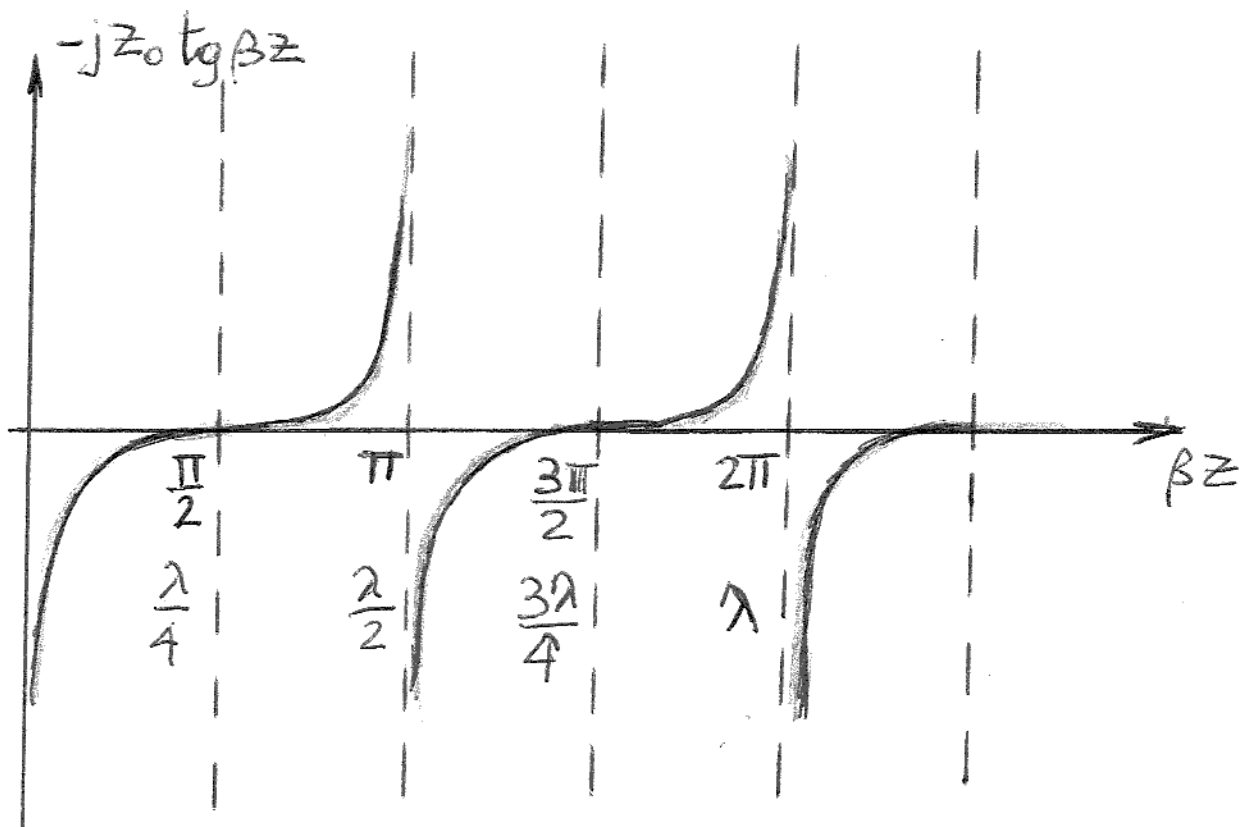
$$V(z) = V^+ e^{j\beta z} (1 - e^{-2j\beta z})$$

$$I(z) = \frac{V^+ e^{j\beta z}}{Z_0} (1 + e^{-2j\beta z})$$

Si  $Z_L \rightarrow \infty$  CARGA EN CIRC. ABIERTO.

$$Z(z) = Z_0 \frac{Z_L + jZ_0 \tan \beta z}{jZ_0 \tan \beta z + Z_0} = Z_0 \frac{Z_L/Z_0 + j \tan \beta z}{j Z_L/Z_0 \tan \beta z + 1}$$

$$Z(z) \Big|_{Z_L \rightarrow \infty} = \frac{Z_0}{j \tan \beta z} = -j Z_0 \cot \beta z$$



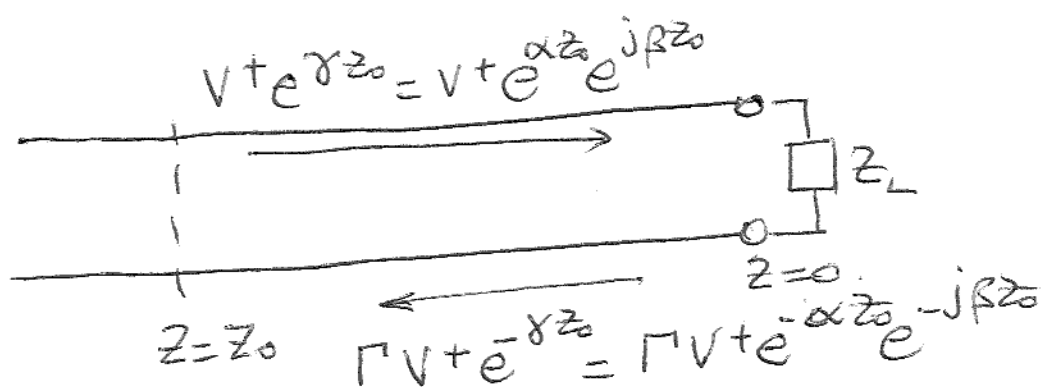
$$\Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = 1$$

$$ROE = \infty$$

$$V(z) = V^+ e^{j\beta z} \cdot (1 + e^{-2j\beta z})$$

$$I(z) = \frac{V^+}{Z_0} e^{j\beta z} \cdot (1 - e^{-2j\beta z})$$

## RELACIONES DE POTENCIA EN UNA LÍNEA DE TRANSMISIÓN



SE DESEA OBTENER LA POTENCIA EN  $Z_0$

$$V(z_0) = V^+ (e^{j\beta z_0} + \Gamma_L e^{-j\beta z_0})$$

$$I(z_0) = \frac{V^+}{Z_0} (e^{j\beta z_0} - \Gamma_L e^{-j\beta z_0})$$

$Z_0$ :  $Z$  CARACTERÍSTICA.

$$P_i = \frac{1}{2} \operatorname{Re}(V_{z_0} I_{z_0}^*) = \frac{1}{2} \operatorname{Re} \left[ V^+ (e^{j\beta z_0} + \Gamma_L e^{-j\beta z_0}) \left[ \frac{V^+}{Z_0} (e^{j\beta z_0} - \Gamma_L e^{-j\beta z_0}) \right]^* \right]$$

$$= \frac{|V^+|^2}{2} \operatorname{Re} \left\{ e^{j\beta z_0} \frac{e^{-j\beta z_0}}{Z_0^*} - \frac{e^{j\beta z_0} e^{-j\beta z_0} \Gamma_L^*}{Z_0^*} + \frac{\Gamma_L e^{-j\beta z_0} e^{j\beta z_0}}{Z_0^*} - \frac{|\Gamma_L|^2 e^{-j\beta z_0} e^{j\beta z_0}}{Z_0^*} \right\}$$

$$= \frac{|V^+|^2}{2} \operatorname{Re} \left\{ \frac{e^{2j\beta z_0} - e^{-2j\beta z_0} |\Gamma_L|^2}{Z_0^*} + \frac{e^{j\beta z_0} \Gamma_L^* - e^{-j\beta z_0} \Gamma_L}{Z_0^*} \right\}$$

$$\text{Si } Z_0 = |Z_0| e^{j\theta_{Z_0}}$$

$$= \frac{|V+|^2}{2|Z_0|} \cdot \operatorname{Re} \left\{ \left( e^{2\alpha z_0} + 2j|\Gamma_L| \sin(\theta_T - 2\beta z_0) - |\Gamma_L|^2 e^{2\alpha z_0} \right) e^{-j\theta_{Z_0}} \right\}$$

$$= \frac{|V+|^2}{2|Z_0|} \cdot \left( e^{2\alpha z_0} \cos \theta_{Z_0} - |\Gamma_L|^2 e^{-2\alpha z_0} \cos \theta_{Z_0} \right)$$

$$P_i = \frac{|V+|^2}{2|Z_0|} \cdot \left( e^{2\alpha z_0} - |\Gamma_L|^2 e^{-2\alpha z_0} \right) \cos \theta_{Z_0} \quad [W]$$

LA PRIMER COMPONENTE SE PROPAGA HACIA LA CARGA.  
LA SEGUNDA COMPONENTE SE PROPAGA HACIA EL GENERADOR.

Si  $z_0 = 0$  ES LA POTENCIA EN LA CARGA.

$$P_{\text{LOAD}} = \frac{|V+|^2}{2|Z_0|} (1 - |\Gamma_L|^2) \cos \theta_{Z_0}$$

Si  $\alpha = 0$  LÍNEA SIN PÉRDIDAS y  $Z_0 = \text{Real}$

$$P_i = \frac{|V+|^2}{2Z_0} (1 - |\Gamma_L|^2)$$

ES LA POTENCIA EN CUALQUIER PUNTO DE LA LÍNEA  
PARA LA LÍNEA SIN PÉRDIDAS.

SI LA CARGA ESTÁ ADAPTADA  $Z_L = Z_0 \Rightarrow \Gamma_L = 0$

$P_i = \frac{|V+|^2}{2Z_0}$  TODA LA POTENCIA LLEGA A LA CARGA.