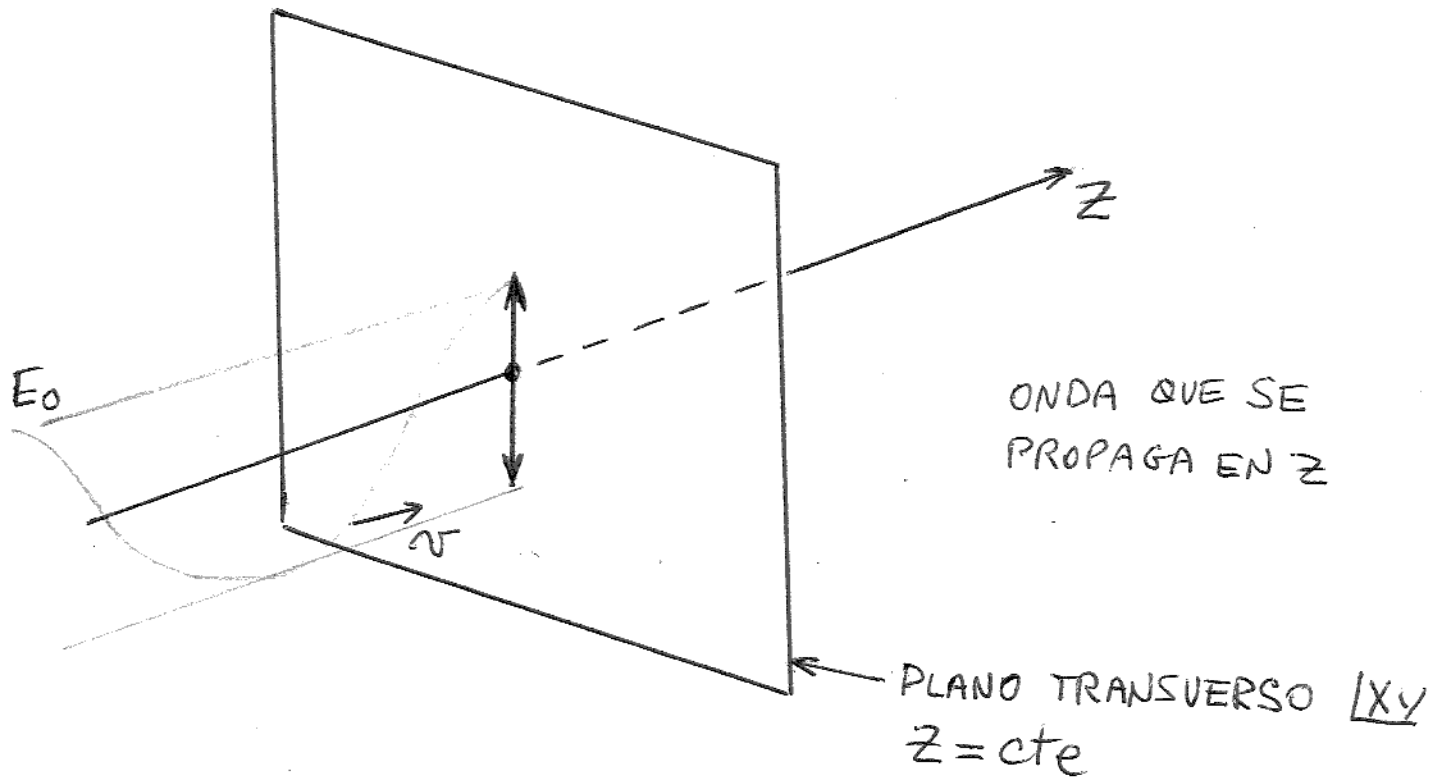


POLARIZACION:

LA POLARIZACION ES LA DIRECCION DEL VECTOR CAMPO ELECTRICO \vec{E} DE UNA ONDA QUE SE PROPAGA EN EL ESPACIO.



$$\vec{E} = \hat{a}_x E_x$$

$$\vec{E} = \hat{a}_x E_{01} \cos(\omega t - \beta z)$$

POLARIZACION HORIZONTAL

$$\vec{E} = \hat{a}_y E_y$$

$$\vec{E} = \hat{a}_y E_{02} \cos(\omega t - \beta z)$$

POLARIZACION VERTICAL.

$$\text{EN } z=0$$

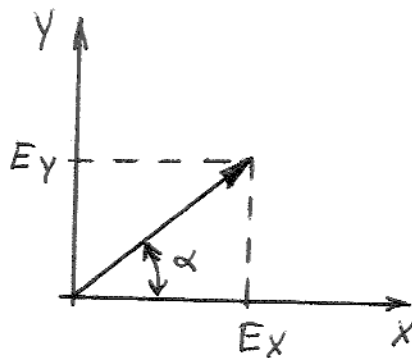
$$\vec{E} = \hat{i} E_{01} \cos \omega t \quad \text{POL. HOR}$$

$$\vec{E} = \hat{j} E_{02} \cos \omega t \quad \text{POL. VERT.}$$

POLARIZACION OBLICUA

$$\vec{E} = \hat{i} E_x + \hat{j} E_y$$

$$\vec{E} = \hat{i} E_{01} \cos \omega t + \hat{j} E_{02} \cos(\omega t + \delta)$$



α : ANGULO DE POLARIZACION LINEAL

$$\underline{\delta = 0}$$

$$\vec{E} = \hat{i} E_{01} \cos \omega t + \hat{j} E_{02} \cos \omega t$$

$$\alpha = \arctan \frac{E_y}{E_x} = \arctan \frac{E_{02}}{E_{01}}$$

$$0 \leq \alpha \leq \pi/2$$

$$\underline{\delta = \pi}$$

$$\vec{E} = \hat{i} E_{01} \cos \omega t + \hat{j} E_{02} (\cos \omega t + \pi)$$

$$\vec{E} = \hat{i} E_{01} \cos \omega t - \hat{j} E_{02} \cos \omega t$$

$$0 \leq \alpha \leq \pi/2$$

POLARIZACION ELÍPTICA

Si $\delta \neq 0$ LA ONDA ESTARA ELIPTICAMENTE POLARIZADA

$$\vec{E} = \hat{n} E_{01} \cos(\omega t - \beta z) + \hat{j} E_{02} \cos(\omega t - \beta z + \delta)$$

$$\underline{z=0}$$

$$E_x = E_{01} \cos \omega t$$

$$E_y = E_{02} \cos(\omega t + \delta) = E_{02} (\cos \omega t \cos \delta - \sin \omega t \sin \delta)$$

$$\text{como } \cos \omega t = \frac{E_x}{E_{01}}$$

$$E_y = E_{02} \left(\frac{E_x}{E_{01}} \cos \delta - \sin \omega t \sin \delta \right)$$

$$\sin \omega t \sin \delta = \frac{E_x}{E_{01}} \cos \delta - \frac{E_y}{E_{02}}$$

ELEVANDO AL CUADRADO SE OBTIENE

$$\sin^2 \omega t \sin^2 \delta = \left(\frac{E_x}{E_{01}} \right)^2 \cos^2 \delta - 2 \frac{E_x \cos \delta}{E_{01}} + \left(\frac{E_y}{E_{02}} \right)^2$$

como :

$$\sin^2 \omega t = 1 - \cos^2 \omega t = 1 - \left(\frac{E_x}{E_{01}} \right)^2$$

$$\left(1 - \left(\frac{E_x}{E_{01}} \right)^2 \right) \cdot \sin^2 \delta = \left(\frac{E_x}{E_{01}} \right)^2 \cos^2 \delta - 2 \frac{E_x \cos \delta}{E_{01}} + \left(\frac{E_y}{E_{02}} \right)^2$$

$$\sin^2 \delta = \left(\frac{E_x}{E_{01}} \right)^2 \underbrace{(\cos^2 \delta + \sin^2 \delta)}_{=1} - \frac{2E_x}{E_{01}} \cos \delta + \left(\frac{E_y}{E_{02}} \right)^2$$

$$\boxed{\sin^2 \delta = \left(\frac{E_x}{E_{01}} \right)^2 - 2 \left(\frac{E_x}{E_{01}} \right) \cos \delta + \left(\frac{E_y}{E_{02}} \right)^2}$$

ESTA ES LA EC. DE UNA ELIPSE

ECUACION GRAL DE UNA ELIPSE

$$A \cdot X^2 - BXY + CY^2 = 1$$

Ejemplo

$$E_{02} = \frac{E_{01}}{2} \quad \delta = \frac{\pi}{2}$$

$$E_x = E_{01} \cos \omega t$$

$$E_y = E_{02} \cos\left(\omega t + \frac{\pi}{2}\right) = \frac{E_{01}}{2} \cdot \cos\left(\omega t + \frac{\pi}{2}\right)$$

$$\vec{E} = \hat{i} E_{01} \cos \omega t + \hat{j} \frac{E_{01}}{2} \cos\left(\omega t + \frac{\pi}{2}\right)$$

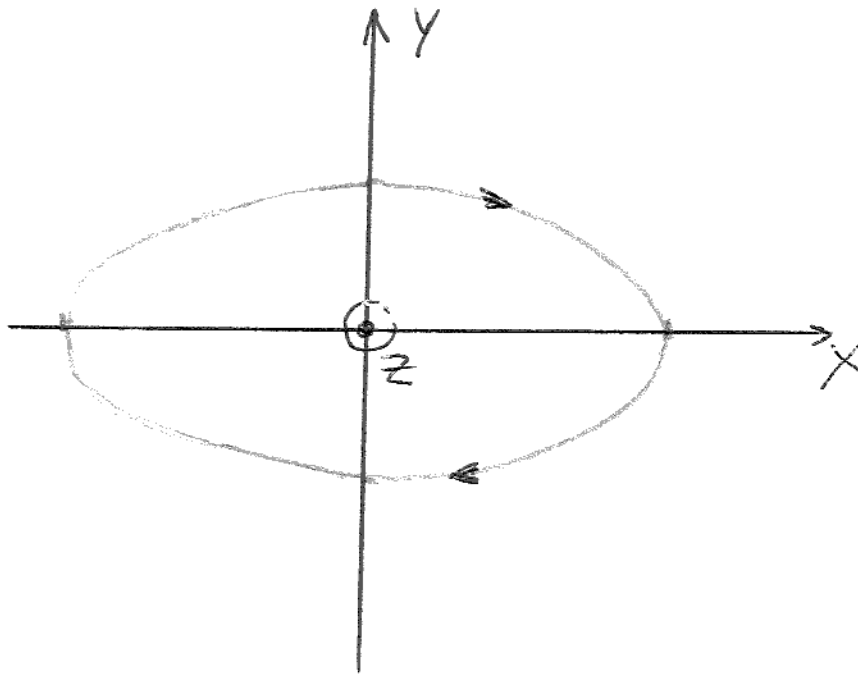
$$\vec{E} = \hat{i} E_{01} \cos \omega t + \hat{j} \frac{E_{01}}{2} (-\sin \omega t)$$

$$\frac{|\vec{E}|}{E_{01}} = \sqrt{\cos^2 \omega t + \frac{1}{4} \sin^2 \omega t}$$

ADEMAS :

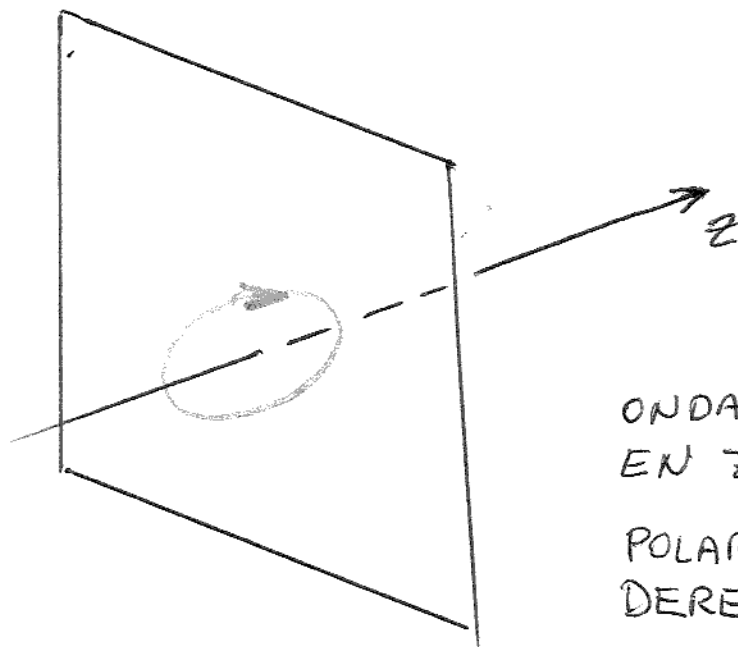
$$1 = \left(\frac{E_x}{E_{01}} \right)^2 + \left(\frac{E_y}{E_{02}} \right)^2$$

$$1 = \frac{E_x^2}{E_{01}^2} + \frac{E_y^2}{\left(\frac{E_{01}}{2} \right)^2}$$



NORMA IEEE


OBSERVADOR



ONDA QUE SE PROPAGA
EN Z

POLARIZACION
DERECHA

POLARIZACION CIRCULAR

$$E_{01} = E_{02}$$

$$\delta = \pm \frac{\pi}{2}$$

LA ECUACION DE LA ELIPSE QUEDA

$$\cos \delta = 0$$

$$\sin \delta = \pm 1$$

$$1 = \left(\frac{E_x}{E_{01}} \right)^2 + \left(\frac{E_y}{E_{01}} \right)^2$$

$$\boxed{E_{01}^2 = E_x^2 + E_y^2}$$

ES LA EC. DE UNA CIRCUNFERENCIA

$$\text{Si } \delta = +\frac{\pi}{2}$$

POLARIZACION CIRCULAR
IZQUIERDA

$$\delta = -\frac{\pi}{2}$$

POLARIZACION CIRCULAR
DERECHA.

SE HA VISTO QUE

$$\vec{E} = \hat{i} E_x + \hat{j} E_y$$

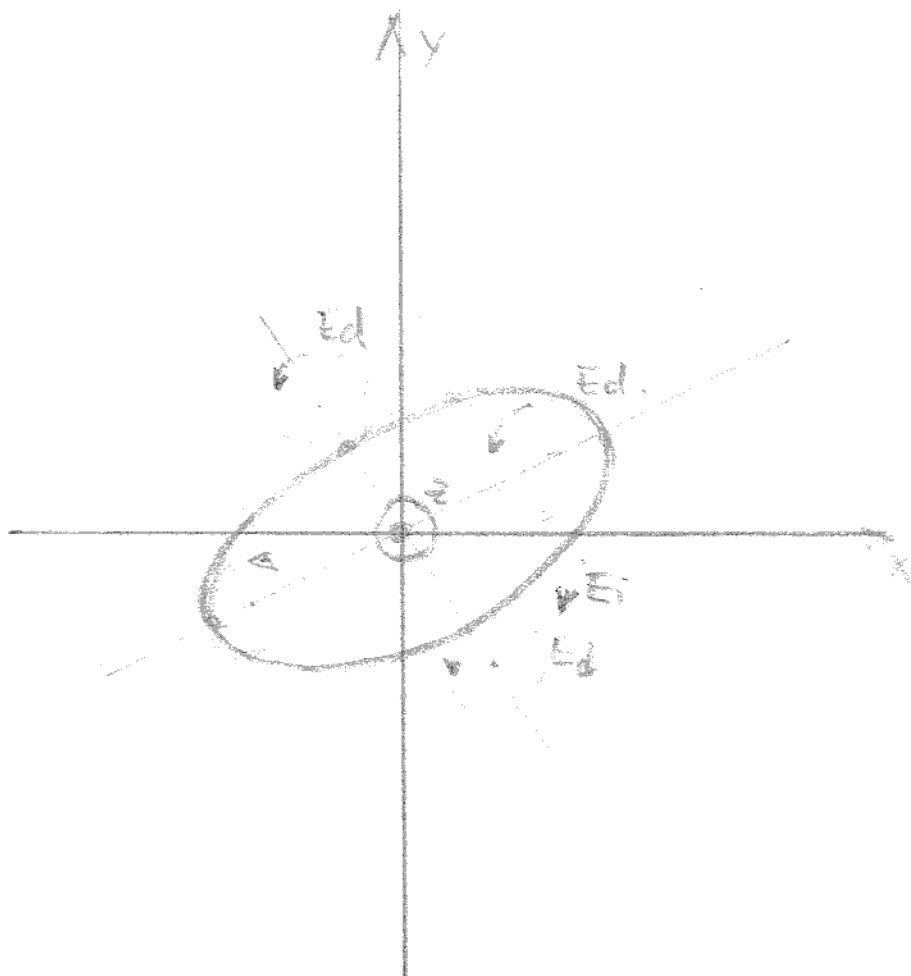
TAMBIEN SE PUEDE EXPRESAR

$$\vec{E} = \vec{E}_i(t) + \vec{E}_d(t)$$

$$\vec{E} = E_{oi} \left[\hat{i} \cos(\omega t + \psi) - \hat{j} \sin(\omega t + \psi) \right] + E_{od} \left[\hat{i} \cos(\omega t + \psi + \delta') + \hat{j} \sin(\omega t + \psi + \delta') \right]$$

$$|E_{MAX}| = |E_{oi} + E_{od}|$$

$$|E_{MIN}| = |E_{oi} - E_{od}|$$



RELACION AXIAL (R.A.)

$$R = \frac{E_{oi} + E_{od}}{E_{od} - E_{oi}}$$

$$R = \pm \frac{\text{LONGITUD EJE MAYOR}}{\text{LONGITUD EJE MENOR}}$$

$$R(\text{dB}) = 20 \log |R|$$

$$R \begin{cases} \rightarrow + \text{ POL. DER.} \\ \rightarrow - \text{ POL. NEG.} \end{cases}$$

$$1 \leq |R| < \infty$$

RELACION DE POLARIZACION CIRCULAR

$$\rho_c = \frac{E_{od}}{E_{oi}}$$

$$0 < \rho_c < \infty$$

$$\rho_c(\text{dB}) = 20 \log \frac{E_d}{E_i}$$

$$R = \frac{E_{oi} + E_{od}}{E_{od} - E_{oi}} = \frac{1 + \frac{E_{od}}{E_{oi}}}{\frac{E_{od}}{E_{oi}} - 1} = \frac{1 + S_c}{S_c - 1}.$$

RELACION ENTRE R Y S_c .

RELACION DE POLARIZACION LINEAL.

$$S_L = \frac{E_{o2}}{E_{o1}}$$