從零開始的 關聯式學習

Pandas 與 Mlxtend

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Work Experience

- 2022/2~ Now Associate Professor National Taichung University of Science and Technology
- 2018/2 ~ Now
 Adjunct Assistant Professor
 National Cheng Kung University
- ➤ 2015/8 ~ 2017/11
 Project Manager & Data Scientist
 NEXCOM International Co., Ltd.

About Me

- [Since Jan. 2019] Young Professionals Chair, IET Taipei Local Network.
- [Since Dec. 2017] Consultant, NEXCOM Industry 4.0 Center.
- [Jan. 2017] Ph.D. degree, National Cheng Kung University.

Research Topics

- a) Natural Language Processing
 - ✓ Natural Language Understanding
 - ✓ Chatbot
 - ✓ Text Summarization / Classification
- o) Deep Learning
- c) Data Mining
- d) Internet of Things
 - ✓ Smart Speaker



關聯規則學習

Association Rule Learning

概念

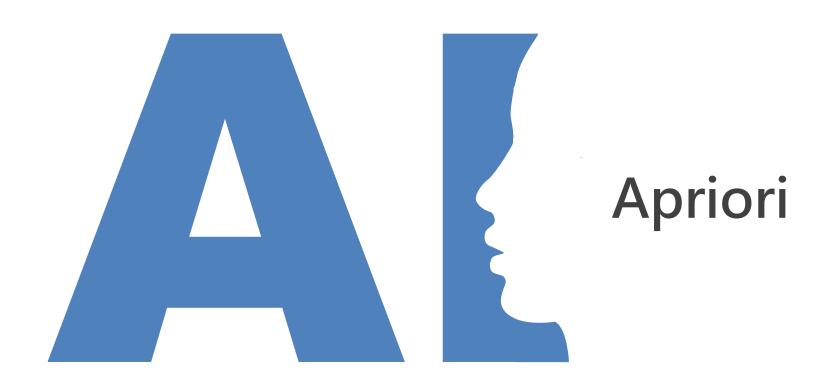
- 在大型資料庫中發現項目間關聯的方法。
 - {牛奶, 麵包}→{可樂}:代表某人同時買了牛奶和 麵包,就可能會買可樂。
- 該方法常使用於電子商務上,通常可為促銷、 產品推薦等行銷活動的決策依據。



定義

- 商品的項目集合(itemset) · / = { /₁, /₂ ..., /_m} · #Item
- 交易資料庫(Database), $D = \{t_1, t_2, ..., t_n\}$ 。 #Transaction
- 關聯規則(Association Rule), $X \rightarrow Y$



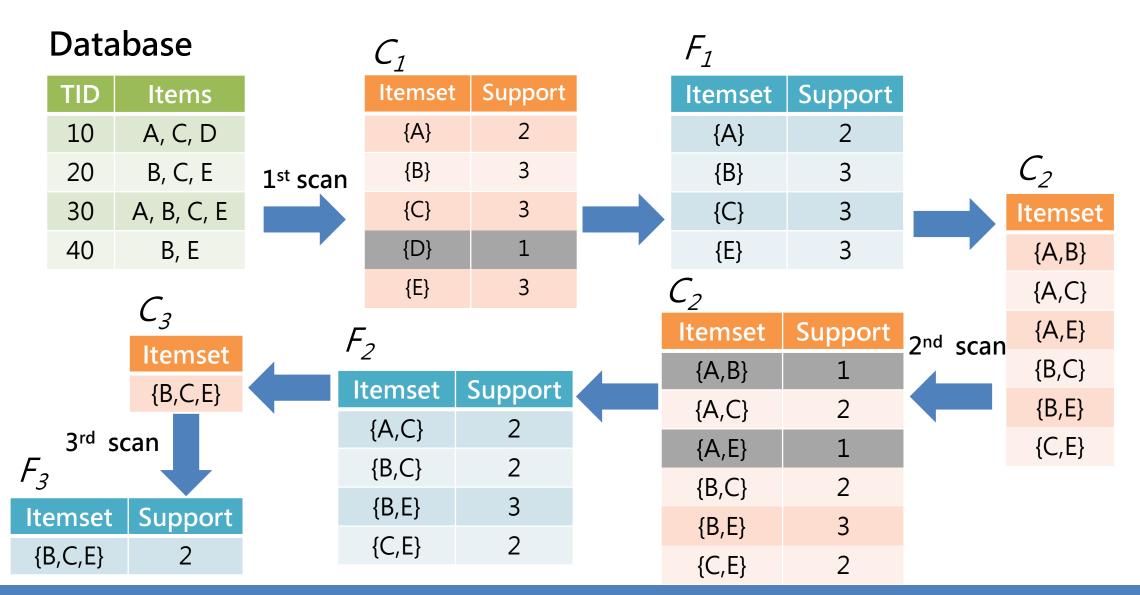


概念

- 逐層搜索的迭代方法。
- *k*-itemset 用於探索(*k* + 1) itemset。
 - 1. 找出 frequent 1-itemset $F_1 \circ F_1$ 用來找 frequent 2-itemset $F_2 \circ F_3$ 而 F_2 用來找到 F_3 。直到不能找到 k-itemset。
 - 2. 每找一個 F_k 需要掃描一次資料庫。為提高頻繁項集逐層產生的效率, Apriori 性質則可減少搜索。
- Apriori 性質: frequent itemset 的所有非空子集都必須是頻繁的。
 - 若某個 *k*-itemset 的 candidate 的 subsets 不在 (*k*-1)-itemset 時, 這個 candidate 就可以直接删除。



當最小支持度為 2 時的情況



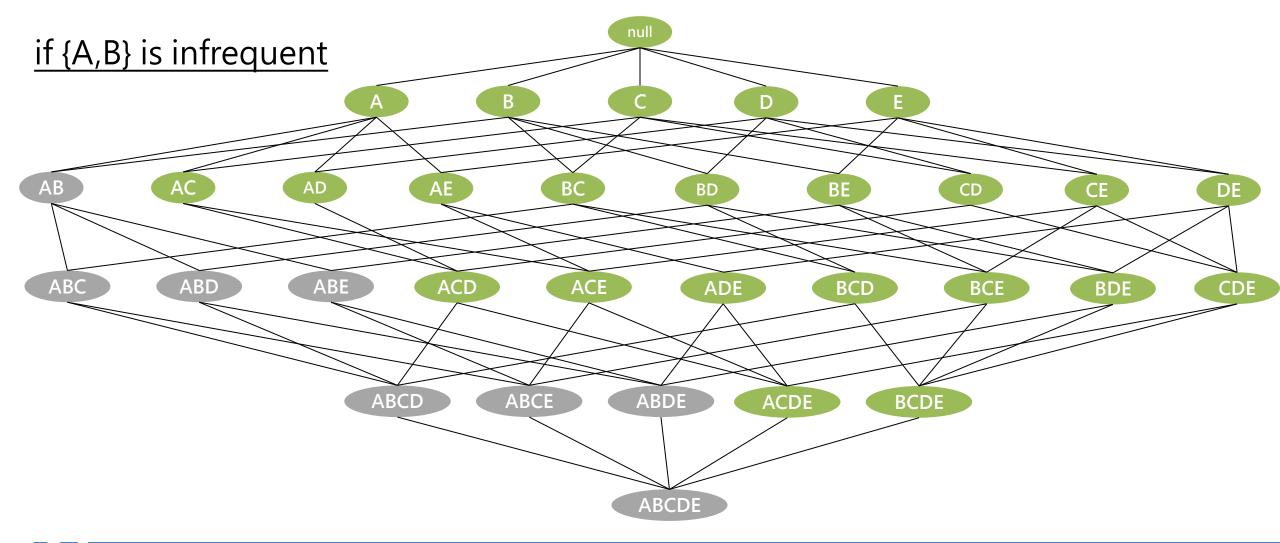


方法

- $1. C_3 = F_2$ 的組合
 - $F_2 = \{\{A, C\}, \{B, C\}, \{B, E\}, \{C, E\}\}\}$ $C_3 = \{\{A, B, C\}, \{A, C, E\}, \{B, C, E\}\}\}$
- 2. 使用 Apriori 性質剪枝:某個 frequent itemset 的所有 subsets 必須是頻繁的, 對 candidate itemset C_3 ,我們可以刪除其非頻繁的 subsets :
 - {A, B, C} 的 2-itemset 是 {A, B}, {A, C}, {B, C}, 其中 {A, B} 不是 F₂的元素,所以删除;
 - {A, C, E} 的 2-itemset 是 {A, C}, {A, E}, {C, E} · 其中 {A, E} 不是 F₂的元素 · 所以刪除;
 - {B, C, E} 的 2-itemset 是 {B, C}, {B, E}, {C, E}, 所有 2-itemset 都是 F₂的元素,因此保留。
- 3. 剪枝後得到 *C*₃ = {{B, C, E}}



剪枝





案例

TID	網球拍	網 球	運動鞋	羽毛球
1	1	1	1	0
2	1	1	0	0
3	1	0	0	0
4	1	0	1	0
5	0	1	1	1
6	1	1	0	0

- 顧客購買記錄的資料庫 D,包含 6 個 Transactions
- 項目集 / = {網球拍, 網球, 運動鞋, 羽毛球}

觀察關聯規則,網球拍 → 網球。

- 1. Transaction 1, 2, 3, 4, 6 包含網球拍。
- 2. Transaction 1, 2, 6 同時包含網球拍和網球。
- 3. 支持度 = 3/6 = 0.5,信心度 = 3/5 = 0.6。
- 若最小支持度為 0.5,最小信心度為 0.6。
- 關聯規則"網球拍→網球" 是存在強關聯的。

- 1-itemset (4): {網球拍}, {網球}, {運動鞋}, {羽毛球}
- 2-itemset (7): {網球拍, 網球}, {網球拍, 運動鞋}, {網球拍, 羽毛球}, {網球,運動鞋}, {網球,羽毛球}, {運動鞋,羽毛球}
- 3-itemset (4): {網球拍, 網球, 運動鞋}, {網球拍, 網球, 羽毛球}, {網球拍, 運動鞋, 羽毛球} {網球,運動鞋,羽毛球}





實作開始

Google Colab





Mlxtend

http://rasbt.github.io/mlxtend/api_subpackages/mlxtend.frequent_patterns/

```
min_support : float (default: 0.5)
```

✓ A float between 0 and 1 for minumum support of the itemsets returned.

transactions_where_item(s)_occur / total_transactions

$$\operatorname{support}(A \to C) = \operatorname{support}(A \cup C), \quad \operatorname{range:} [0,1]$$

$$\operatorname{confidence}(A o C) = \frac{\operatorname{support}(A o C)}{\operatorname{support}(A)}, \quad \operatorname{range:} [0,1]$$



Mlxtend

http://rasbt.github.io/mlxtend/user_guide/frequent_patterns/association_rules/

$$\operatorname{lift}(A \to C) = \frac{\operatorname{confidence}(A \to C)}{\operatorname{support}(C)}, \quad \operatorname{range:} [0, \infty] \quad = \quad \frac{\operatorname{Support}}{\operatorname{Supp}(X) \times \operatorname{Supp}(Y)}$$

$$\operatorname{levarage}(A \to C) = \operatorname{support}(A \to C) - \operatorname{support}(A) \times \operatorname{support}(C), \quad \operatorname{range:} [-1, 1]$$

$$\operatorname{conviction}(A \to C) = \frac{1 - \operatorname{support}(C)}{1 - \operatorname{confidence}(A \to C)}, \quad \operatorname{range:} [0, \infty] \quad = \quad \mathsf{P}(\mathsf{A})\mathsf{P}(\mathsf{B}')/\mathsf{P}(\mathsf{A} \cap \mathsf{B}')$$



UCI - Online Retail Data Set



https://archive.ics.uci.edu/ml/datasets/online+retail

Check out the beta version of the new UCI Machine Learning Repository we are currently testing! Contact us if you have any issues, questions, or concerns. Click here to try out the new site.

Online Retail Data Set

Download: Data Folder, Data Set Description

Abstract: This is a transnational data set which contains all the transactions occurring between 01/12/2010 and 09/12/2011 for a UK-based and registered non-store online retail.

Data	a Set Characteristics:	Multivariate, Sequential, Time-Series	Number of Instances:	541909	Area:	Business
Attr	ribute Characteristics:	Integer, Real	Number of Attributes:	8	Date Donated	2015-11-06
Ass	sociated Tasks:	Classification, Clustering	Missing Values?	N/A	Number of Web Hits:	764798

Source:

Dr Daging Chen, Director: Public Analytics group, chend '@' Isbu.ac.uk, School of Engineering, London South Bank University, London SE1 0AA, UK.

Data Set Information:

This is a transnational data set which contains all the transactions occurring between 01/12/2010 and 09/12/2011 for a UK-based and registered non-store online retail. The company mainly sells unique all-occasion gifts. Many customers of the company are wholesalers.

Attribute Information:

InvoiceNo: Invoice number. Nominal, a 6-digit integral number uniquely assigned to each transaction. If this code starts with letter 'c', it indicates a cancellation

StockCode: Product (item) code. Nominal, a 5-digit integral number uniquely assigned to each distinct product.

Description: Product (item) name. Nominal.

Quantity: The quantities of each product (item) per transaction. Numeric.

InvoiceDate: Invice Date and time. Numeric, the day and time when each transaction was generated.

UnitPrice: Unit price. Numeric, Product price per unit in sterling.

CustomerID: Customer number. Nominal, a 5-digit integral number uniquely assigned to each customer.

Country: Country name. Nominal, the name of the country where each customer resides.





