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Assignment 1 – Programming Question

a)

Pseudo Code:

ExponentialTetranacci(n):

INPUT: Integer n

OUTPUT: The n'th tetranacci number

START:

if n = 0 then return 0

if n = 1 then return 0

if n = 2 then return 0

if n = 3 then return 1

return ExponentialTetranacci(n-1) + ExponentialTetranacci(n-2) +
ExponentialTetranacci(n-3) + ExponentialTetranacci(n-4)
END

b)

Pseudo Code:

TRTetranacci(n, base0, base1, base2, base3):

INPUT: Integer n and the previous 4 calculations, starting with the base cases

OUTPUT: The n'th tetranacci number

BEGIN:

if n = 0 then return base0

if n = 1 then return base1

if n = 2 then return base2

if n = 3 then return base3

TRTetranacci(n - 1, base1, base2, base3, base0 + base1 + base2 + base3)
END

c)

c)

level	tree	nodes → Nb of recursive calls at it's level
0	n	1 $\Rightarrow 1^0$
1	 n-1	1 $\Rightarrow 1^1$
2	 n-2	1 $\Rightarrow 1^2$
3	 n-3	1 $\Rightarrow 1^3$
...
d	 3	1

Nb of total recursive calls

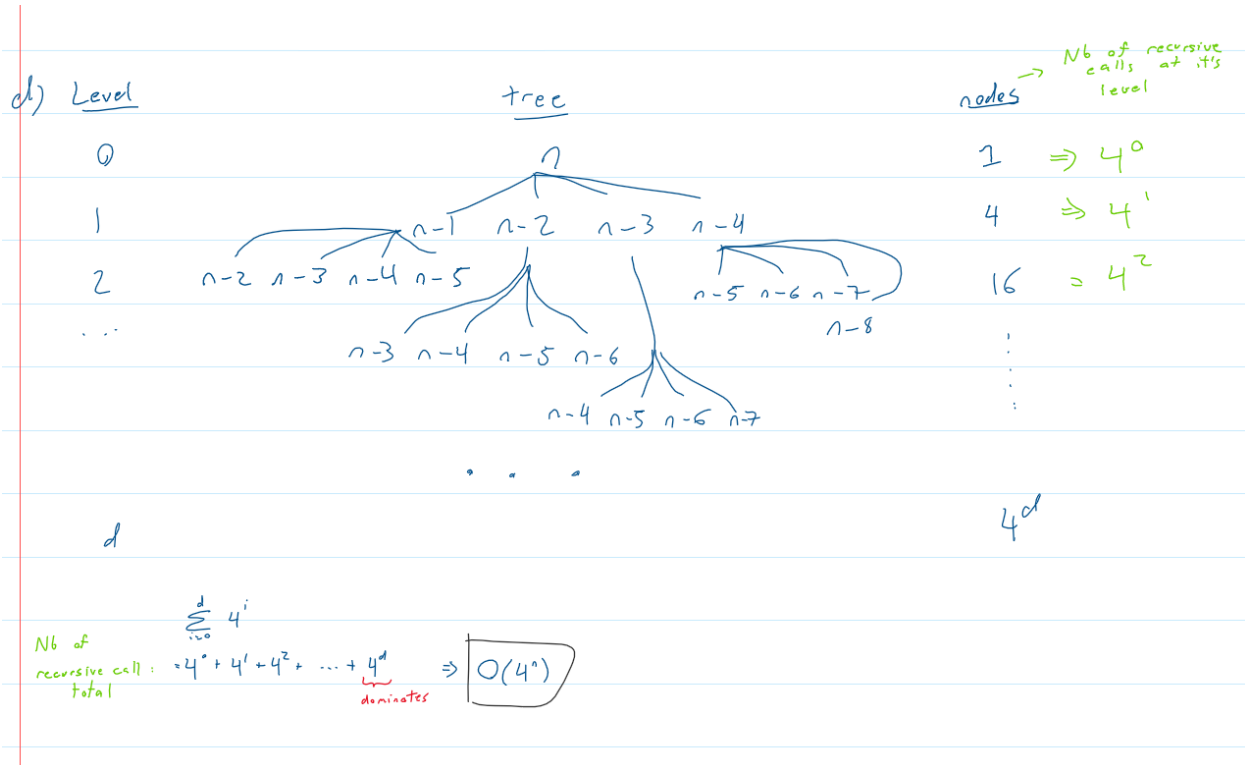
$$\sum_{i=0}^d 1^i$$

$$= \sum_{i=0}^d 1 = d - \cancel{0} + 1$$

$- \underbrace{d+1}_{\text{dominates}} \Rightarrow \boxed{O(n)}$

The Tail Recursive Tetranacci calculation is Linear since there is only 1 recursive call to itself at any point.

d)



Exponential Tetranacci has an Exponential time complexity because each time you calculate the value of an n'th number, you have to recalculate all the 4 values before it, each recursive call will call itself 4 times.