## PHYS 1200 EQUATION SHEET

Use only these equations on Preps

Units & prefixes

$$1 \text{ mile} = 1.609 \text{ km}$$

$$1 \text{ ft} = 0.3048 \text{ m}$$

1 inch = 
$$2.54 \text{ cm}$$

$$1 \text{ kg} = 2.20 \text{ lb}$$

$$1 \text{ km} = 1000 \text{ m (k} = 1000)$$

$$1 \text{ m} = 100 \text{ cm} \quad (c = 0.01)$$

$$1 \text{ m} = 1000 \text{ mm } (\text{m} = 0.001)$$

$$M = 10^6$$

Vectors  $\sin \theta = \frac{\text{opp}}{\text{hyp}}$   $\cos \theta = \frac{\text{adj}}{\text{hyp}}$   $\tan \theta = \frac{\text{opp}}{\text{adj}}$   $|\vec{C}| = C = \sqrt{C_x^2 + C_y^2}$ 

$$\cos \theta = \frac{\text{adj}}{\text{hyr}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$|\vec{C}| = C = \sqrt{C_x^2 + C_y^2}$$

Average speed, velocity, acceleration

$$\Delta \vec{x} = x_{\rm f} - x_{\rm i}$$

$$\Delta t = t_{\rm f} - t_{\rm i}$$

$$\Delta \vec{x} = x_f - x_i$$
  $\Delta t = t_f - t_i$   $\Delta \vec{v} = \vec{v}_f - \vec{v}_i$   $\bar{v} = \frac{d}{\Delta t}$   $\bar{\vec{v}} = \frac{\Delta \vec{x}}{\Delta t}$   $\bar{\vec{a}} = \frac{\Delta \vec{v}}{\Delta t}$ 

$$\bar{v} = \frac{d}{\Delta t}$$

$$\bar{\vec{v}} = \frac{\Delta \vec{x}}{\Delta t}$$

$$\bar{\vec{a}} = \frac{\Delta \vec{v}}{\Delta t}$$

Total distance, displacement, and time for *n* intervals

$$d_{1n} = d_1 + d_2 + \dots + d_n$$

$$d_{1n} = d_1 + d_2 + \ldots + d_n \qquad \qquad \Delta \vec{\mathbf{x}}_{1n} = \Delta \vec{\mathbf{x}}_1 + \Delta \vec{\mathbf{x}}_2 + \ldots + \Delta \vec{\mathbf{x}}_n \qquad \qquad \Delta t_{1n} = \Delta t_1 + \Delta t_2 + \ldots + \Delta t_n$$

$$\Delta t_{1n} = \Delta t_1 + \Delta t_2 + \ldots + \Delta t_n$$

**Kinematics: constant acceleration in 1D** 

$$\Delta \vec{x} = \frac{1}{2} \left( \vec{v}_i + \vec{v}_f \right) \Delta t$$

$$\Delta \vec{x} = \frac{1}{2} \left( \vec{v}_i + \vec{v}_f \right) \Delta t \qquad \Delta \vec{x} = \vec{v}_i \Delta t + \frac{1}{2} \vec{a} \Delta t^2 \qquad \vec{v}_f = \vec{v}_i + \vec{a} \Delta t \qquad v_f^2 = v_i^2 + 2 \vec{a} \Delta \vec{x} \qquad g = 9.81 \,\text{m/s}^2$$

$$\vec{v}_{\rm f} = \vec{v}_{\rm i} + \vec{a} \, \Delta t$$

$$v_{\rm f}^2 = v_{\rm i}^2 + 2\vec{a}\,\Delta\,\vec{x}$$

$$g = 9.81 \,\mathrm{m/s^2}$$

**Kinematics: constant acceleration in 2D** 

$$\Delta \vec{x} = \frac{1}{2} \left( \vec{v}_{ix} + \vec{v}_{fx} \right) \Delta \vec{x}$$

$$\Delta \vec{x} = \frac{1}{2} \left( \vec{v}_{ix} + \vec{v}_{fx} \right) \Delta t \qquad \Delta \vec{x} = \vec{v}_{ix} \Delta t + \frac{1}{2} \vec{a}_x \Delta t^2 \qquad \vec{v}_{fx} = \vec{v}_{ix} + \vec{a}_x \Delta t \qquad v_{fx}^2 = v_{ix}^2 + 2 \vec{a}_x \Delta \vec{x}$$

$$\vec{v}_{fx} = \vec{v}_{ix} + \vec{a}_{x} \Delta t$$

$$v_{\rm fy}^2 = v_{\rm iy}^2 + 2\vec{a}_{\rm x} \Delta \vec{b}$$

$$\Delta \vec{y} = \frac{1}{2} \left( \vec{v}_{iy} + \vec{v}_{fy} \right) \Delta t$$

$$\Delta \vec{y} = \vec{v}_{iy} \Delta t + \frac{1}{2} \vec{a}_{y} \Delta t^{2}$$

$$\Delta \vec{y} = \frac{1}{2} \left( \vec{v}_{\rm iy} + \vec{v}_{\rm fy} \right) \Delta t \qquad \Delta \vec{y} = \vec{v}_{\rm iy} \Delta t + \frac{1}{2} \vec{a}_{\rm y} \Delta t^2 \qquad \vec{v}_{\rm fy} = \vec{v}_{\rm iy} + \vec{a}_{\rm y} \Delta t \qquad v_{\rm fy}^2 = v_{\rm iy}^2 + 2 \vec{a}_{\rm y} \Delta \vec{y}$$

$$\vec{F}_{\text{net }x} = m \, \vec{a}_x$$

Forces & torques 
$$\vec{F}_{\text{net }x} = m \vec{a}_x$$
  $\vec{F}_{\text{net }y} = m \vec{a}_y$   $F_G = mg$   $F_K = \mu_K F_N$   $F_S \le \mu_S F_N$ 

$$F_{\rm K} = \mu_{\rm K} F_{\rm N}$$

$$F_{\rm S} \le \mu_{\rm S} F_{\rm N}$$

$$F_E = k \Delta x$$

$$\vec{\tau}_{\text{net}} = I \vec{\alpha}$$

$$\tau = F r \sin \theta$$

$$\vec{\tau}_{\text{net}} = I \vec{\alpha}$$
  $\tau = F r \sin \theta$   $I = I_{\text{cm}} + M d^2$ 

Work, energy, power  $K_{\rm T} = \frac{1}{2} m v^2$   $K_{\rm R} = \frac{1}{2} I \omega^2$   $U_{\rm G} = m g y$   $U_{\rm E} = \frac{1}{2} k x^2$  E = K + U

$$K_{\rm T} = \frac{1}{2}mv^2$$

$$K = \frac{1}{2}I\omega^2$$

$$U_{\rm G} = mgy$$

$$U_{\rm E} = \frac{1}{2} k x^2$$

$$E = K + U$$

$$W = F \Delta x \cos \theta$$

$$W_{\rm net} = K_{\rm f} - K_{\rm f}$$

$$W_{\rm NC,net} = E_{\rm f} - E_{\rm f}$$

$$W = F \Delta x \cos \theta$$
  $W_{\text{net}} = K_{\text{f}} - K_{\text{i}}$   $W_{\text{NC,net}} = E_{\text{f}} - E_{\text{i}}$   $P = \frac{W}{\Delta t} = \frac{E_{\text{used}}}{\Delta t}$ 

Conservation:  $E_i = E_f$ 

**Linear & Angular Momentum**  $\vec{p} = m\vec{v}$   $\vec{J} = \vec{F}_{\text{net}} \Delta t$   $\vec{J} = \Delta \vec{p}$   $\vec{L} = I \vec{\omega}$ 

$$\vec{p} = m\vec{v}$$

$$\vec{J} = \vec{F}_{\text{not}} \Delta t$$

$$\vec{J} = \Delta \vec{p}$$

$$\vec{I} = I\vec{a}$$

Conservation:  $\vec{p}_i = \vec{p}_f$   $\vec{L}_i = \vec{L}_f$ 

$$\vec{p}_{\rm i} = \vec{p}_{\rm f}$$

$$\vec{L}_{i} = \vec{L}_{i}$$

## **Rotational kinematics**

$$\Delta \vec{\theta} = \frac{1}{2} (\vec{\omega}_{i} + \vec{\omega}_{f}) \Delta t \qquad \Delta \vec{\theta} = \vec{\omega}_{i} \Delta t + \frac{1}{2} \vec{\alpha} \Delta t^{2} \qquad \vec{\omega}_{f} = \vec{\omega}_{i} + \vec{\alpha} \Delta t \qquad \omega_{f}^{2} = \omega_{i}^{2} + 2 \vec{\alpha} \Delta \vec{\theta}$$

$$1 \text{ rev} = 2\pi \text{ rad}$$

Circular motion, rolling 
$$s = r\Delta \theta$$
  $v = r \omega$  (radians only)  $a_c = \frac{v^2}{r}$ 

Oscillations 
$$T = 2\pi \sqrt{\frac{m}{k}}$$
  $T = 2\pi \sqrt{\frac{L}{g}}$   $f = \frac{1}{T}$   $T = \frac{1}{f}$ 

Waves & sound 
$$\lambda = \frac{v}{f}$$
  $v = \sqrt{\frac{F_T}{\mu}}$   $\mu = \frac{m}{L}$   $f_O = f_S\left(\frac{v \pm v_O}{v \pm v_S}\right)$  d

## **Standing waves**

both ends fixed/open: 
$$f_n = n \frac{v}{2L}$$
  $\lambda_n = \frac{2L}{n}$   $n = 1, 2, 3, ...$  one end free/open  $f_n = n \frac{v}{4L}$   $\lambda_n = \frac{4L}{n}$   $n = 1, 3, 5, ...$  both:  $f_n = n f_1$ 

## Interference

same frequency, constructive 
$$|r_2-r_1|=n\,\lambda$$
  $n=0,\,1,\,2,\,\ldots$  same frequency, destructive  $|r_2-r_1|=\left(n+\frac{1}{2}\right)\lambda$   $n=0,\,1,\,2,\,\ldots$  different frequencies: beat frequency  $f_b=|f_2-f_1|$