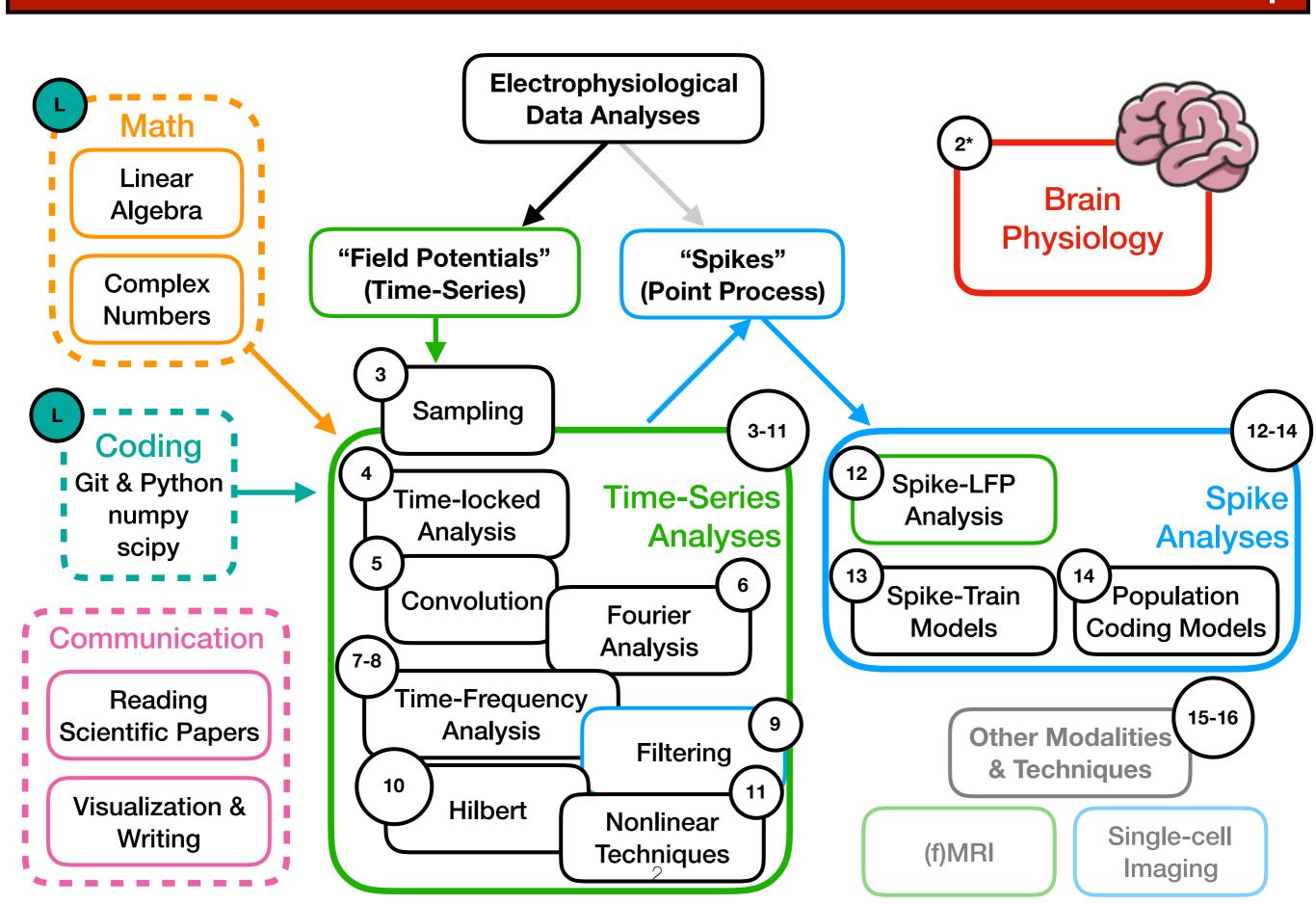
## COGS118C: Neural Signal Processing

# Filtering

Lecture 9 July 17, 2019



#### Course Outline: Road Map



## Goals for Today

- 1. Understand the concept of filtering and convolution
- 2. Evaluate filter parameter choices
- 3. scipy.signal.filtwin tutorial



## Why Filter?

**Digital filters act, well, like a filter**: it lets some frequencies through, and blocks out unwanted frequencies.

Much more intuitive to first think about in the frequency domain.

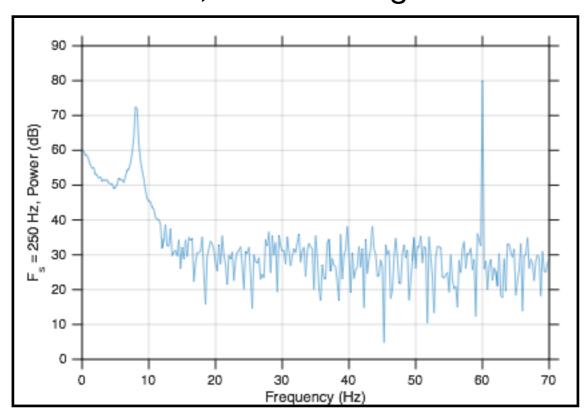
Come up with 3 examples of signals you can record, and which components you might want to filter out/keep from that signal.

Signal	Unwanted/Wanted Component	Frequencies
gopro audio during skydivina	hum + wind/ voice	
concert	audience/ music	
vocals/isolation	boys/girls	
bridges	resonant freqs	



## How to Filter?

Given this signal you recorded, and assuming everything 10Hz and below is the true signal, draw the PSD of the ideal, noiseless signal.



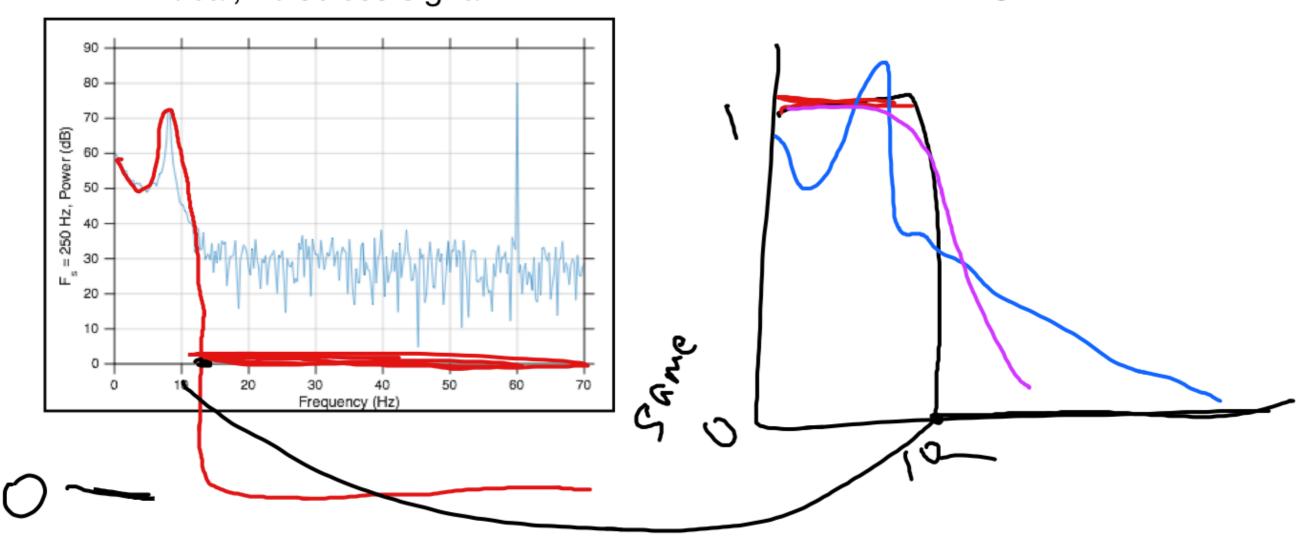
If the only operation you're allowed is element-wise multiplication, draw what you would apply to achieve the ideal PSD.



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## Frequency Response

$$X(f)H(f) = Y(f)$$

X(f): signal you record

Y(f): signal you want

H(f): filter frequency response

**Note:** this is multiplication of two vectors of complex numbers!

$$x(t) \circledast h(t) = y(t)$$
$$X(f)H(f) = Y(f)$$



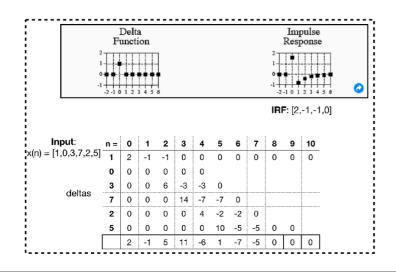
#### How to Filter

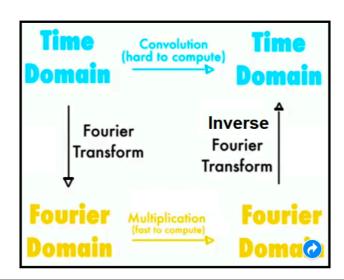
#### (Circular) Convolution Theorem

Convolution in time domain is equivalent to multiplication in frequency domain, and the converse is true as well (duality).

x: input h: system's IRF y: output

$$x(t) \circledast h(t) = y(t)$$
$$X(f)H(f) = Y(f)$$



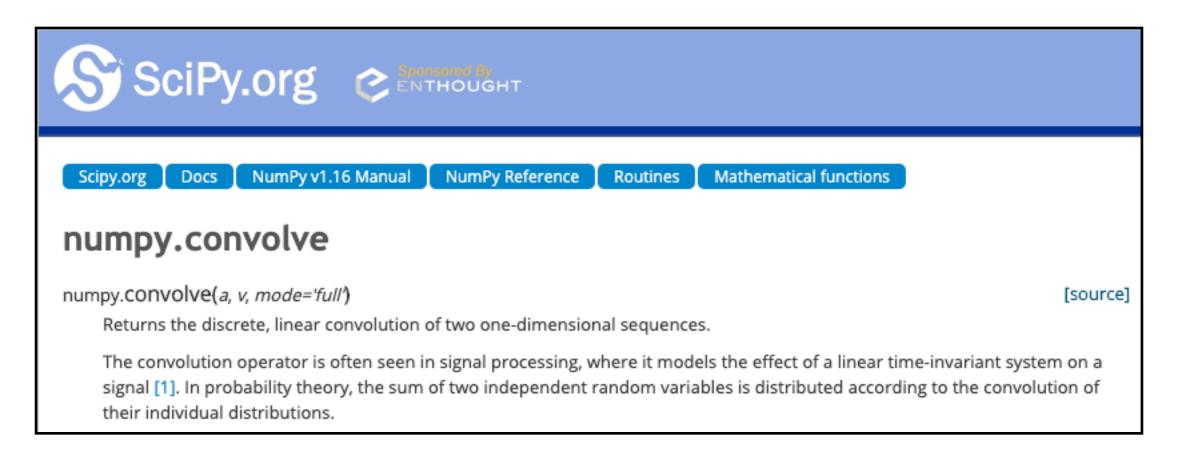


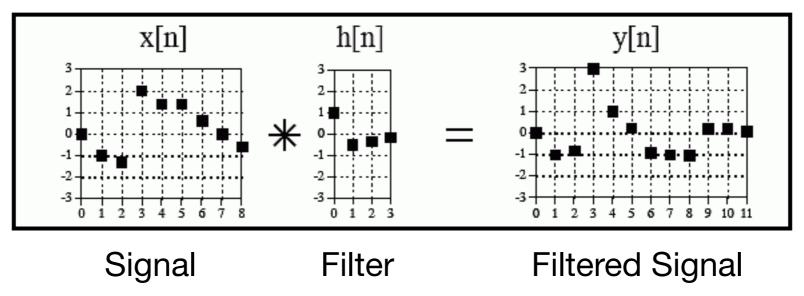
$$x(t) \circledast h(t) = y(t)$$
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In python, we'll call **np.convolve()**, but it essentially performs FFT-multiplication-iFFT.



#### How to Filter

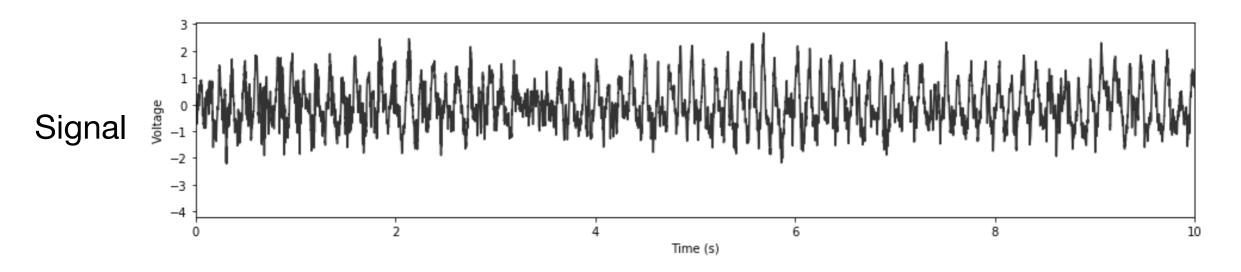




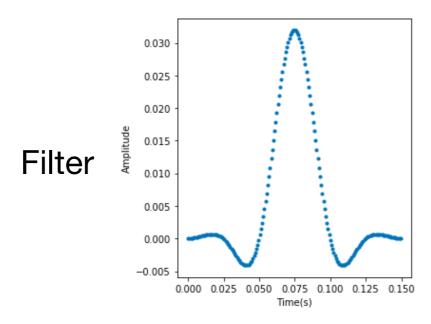
"Filter coefficients" is its Impulse Response Function



## Impulse Response Function



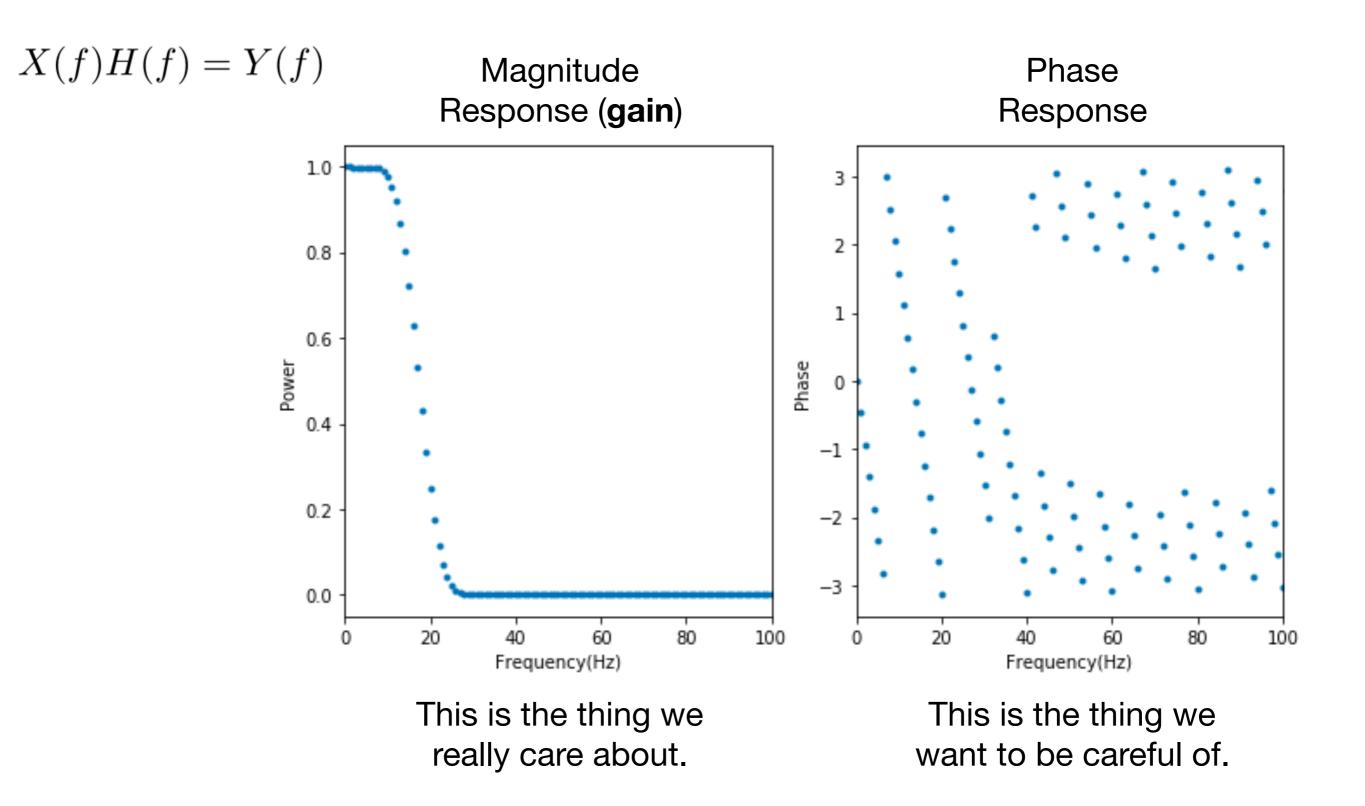
#### convolve



"Filter coefficients" is its Impulse Response Function



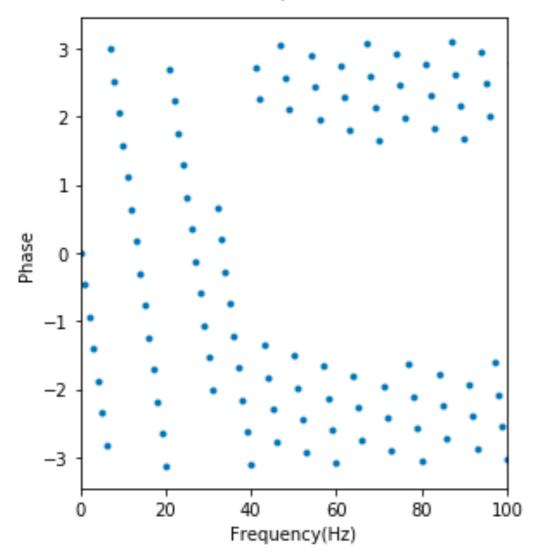
#### Magnitude & Phase Response





## Phase Response = Time Delay

#### Phase Response



This is the thing we want to be careful of.

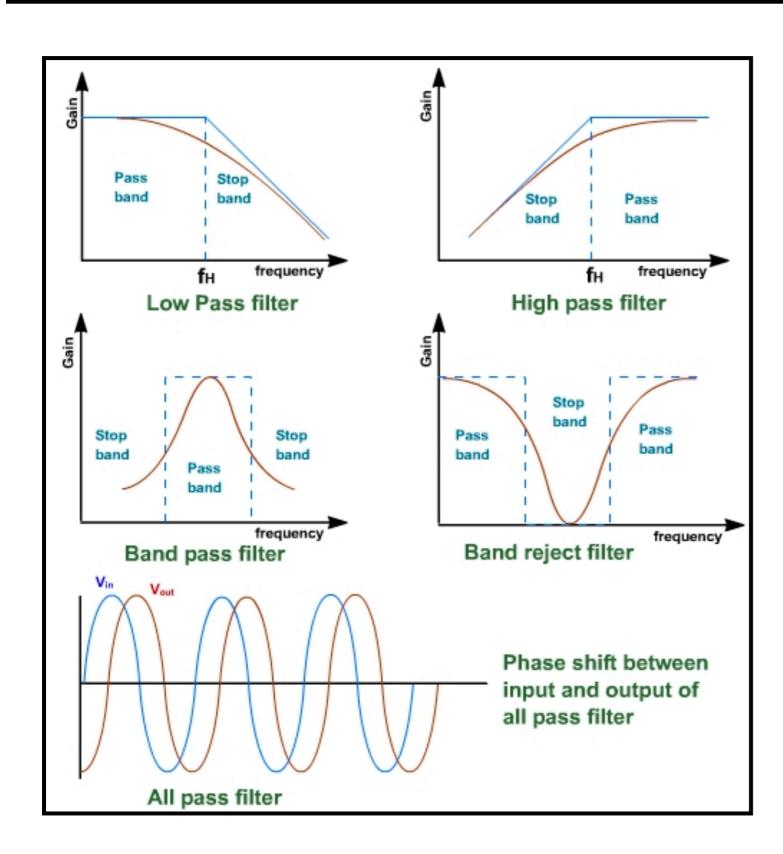
Non-zero phase response comes from time delay introduced by the causal filter.

(it's convolution, but shifted by a little bit)

Each data point, after filtering, is delayed by n points, where n is the length of the filter.



#### Magnitude Response - Types of Filter



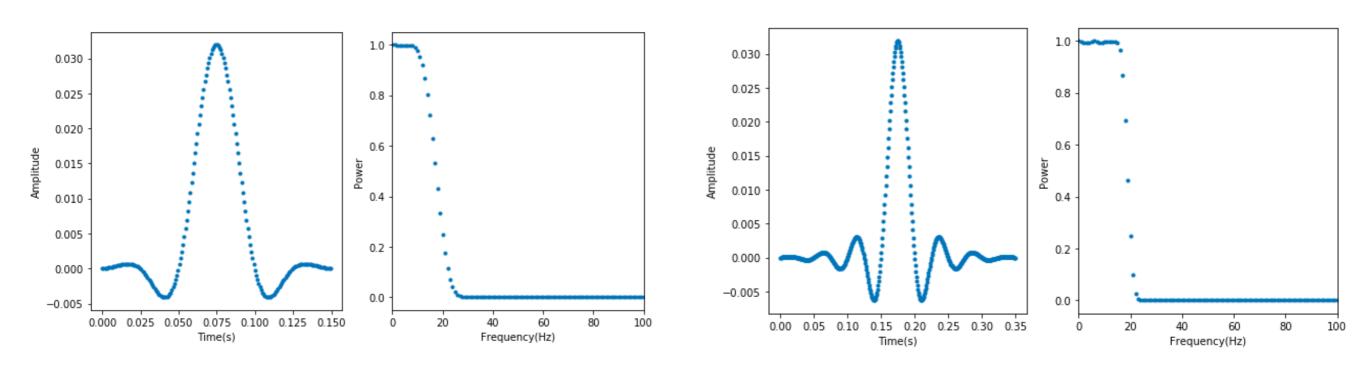
#### 3 min:

Come up with one example application for each type of filter.



## Time-Frequency Resolution Tradeoff II

Since we're interested in the frequency response of the filter, the same concept applies:



Longer filter = better frequency resolution, but worse time resolution

Filter roll-off or transition band



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https://tinyurl.com/cogs118c-att

