# Bitcoin is dead: Long live Bitcoin?

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#### Abstract

### 1 Introduction

## 2 Data

I gathered transaction-level data on Bitcoin, Ether, Ripple, and Litecoin from the European coin exchange Bitstamp. The raw data includes information about each transaction in the history of the exchange, including the unix-timestamp<sup>1</sup>, trade price, and trade quantity. Several points to consider:

- The different coins were offered at different points in time. For example, Bitcoin was the first coin offered on the exchange, while Ether was the most recent addition. Thus, for consistency of the analysis I used the earliest date such that trade information exists for each coin.
- Each transaction is marked to the second. In order to use a smooth time series without missing or repeated observations, I found the smallest period of time such that at least one transaction took place for each series. In this case, Litecoin was the limiting factor in calculating the time periods there was a maximum gap of 5525 seconds between subsequent transactions. Thus, I made a dataset using this as the period length as well as a second dataset that used one-hour as the period length². Ultimately, for the analysis I used the hourly dataset.

The final series consisted of hourly periods ranging from Thursday, August 17, 2017 2:00:03 pm to Tuesday, April 24, 2018 4:00:03 am GMT. Figure 1 show the raw series, and table 1 shows the descriptive statistics.

 $<sup>^1\</sup>mathrm{The}$  unix-timestamp is given by the number of seconds that have passed since January 1, 1970 at 12:00:00 am GMT

<sup>&</sup>lt;sup>2</sup>Using one hour as the period length created a single missing observation in the Litecoin series.

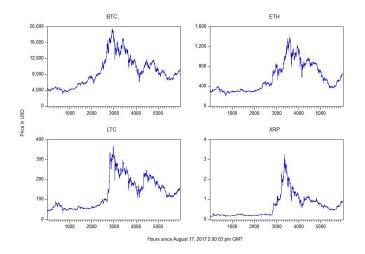


Figure 1: Time series of each coin in dataset.

	Bitcoin	Ethereum	Ripple	Litecoin
Maximum	\$19537.83	\$1405.34	\$3.25	\$370.28
Minimum	\$3009.53	\$204.85	\$0.15	\$36.17
Mean	\$8648.10	\$566.08	\$0.65	\$133.05
St. Dev	\$3749.17	\$284.70	\$0.57	\$76.66
Observations	5991	5990	5991	5991

Table 1: Descriptive statistics. Prices in USD.

Interestingly, the price for each coin are on different orders of magnitude and include an order of magnitude variation from the minimum to maximum. As the descriptive statistics show in table 1, Bitcoin has a maximum price of \$19,537.83 per BTC and minimum price of \$3009.53 per BTC. On the other end of the spectrum, Ripple has a maximum price of \$3.25 per XRP, and a minimum price of \$0.15 per XRP. Ethereum and Litecoin have similar relative variation. In order to better understand how the series moved in relative terms, I created a normalized series,  $\{s^n\}$ , by dividing the price at a given point in time by the series mean,  $\mu_s$ . Mathematically this is to say:

$$s_t^n = \frac{s_t}{\mu_s} \tag{1}$$

Since this helps to normalize the series deviations, we can view this graphically below:

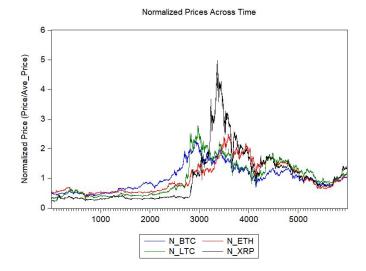


Figure 2: Overlay of each normalized series in dataset.

While the graph is a bit cluttered, what stands out is that Ripple experienced the largest percent increase at its peak, while Litcoin, Ether, and Bitcoin are all very similar. To get a clearer idea of how the series respond to each other, I restrict the graph to only Bitcoin and Ether:

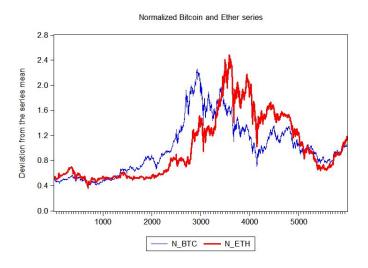


Figure 3: Overlay of Bitcoin and Ether's normalized series.

Here we see that, in normalized terms, Bitcoin's largest surge and drop seems to occur about a month (i.e. approximately 750 hours) before

Ether. Interesting, however, the last month or so in the dataset show much tighter price movements.

# 3 Analysis and Results

Since the series levels are clearly not stationary, I calculated the series of first differences ( $\Delta s_t = s_t - s_{t-1}$ ) and performed the Augmented Dicky-Fuller test for unit roots. In each differenced series, I am able to reject the null hypothesis that a unit root exists and accept that the level series are all integrated of degree one (i.e. I(1)). Visually we can see these differenced series below:

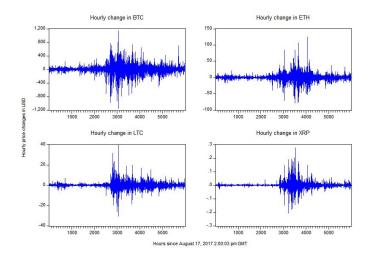


Figure 4: Time series of each differenced coin series in dataset.

## 3.1 Individual Analysis

While the differenced series do seem to have a time constant mean, the variance is definitely not. With that in mind, I tested various specifications using ARCH and GARCH errors to see how the data moves. For each series, the ACF and PACF suggest significant autocorrelation for two-periods (i.e. two hours). However, after finding the best-fit ARCH and GARCH, the series of squared residuals still indicates significant autocorrelation and partial autocorrelation. Thus, I finally settled on an AR(2) model with TGARCH errors, suggesting that traders are effected by whether the prices are rising or falling. The results for Bitcoin, Ether, and Ripple are presented below.

### 3.1.1 Bitcoin

The best fitting model for the Bitcoin data is an AR(3) with TGARCH error terms. After fitting I find the following model<sup>3</sup>:

$$\Delta BTC_t = 0.20 \Delta BTC_{t-1} - 0.12 \Delta BTC_{t-2} + 0.03 \Delta BTC_{t-3} + \epsilon_t$$
(15.34) (-8.25) (2.36)

With an error process given by:

$$E_{t-1}(\epsilon_t^2) = 23.25 + 0.068\epsilon_{t-1}^2 + 0.02D_{t-1}\epsilon_{t-1}^2 + 0.926h_{t-1}$$

$$(14.23) \quad (23.13) \quad (3.82) \quad (530.00)$$
(3)

Correlogram of Standardized Residuals

Next we look at the ACF and PACF of the residual and squared residual series from this estimation. We find that they mirror a white noise process.

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob
•	1 •	1	0.011	0.011	0.7479	
•		2	0.010	0.010	1.4037	
	•	3	-0.005	-0.006	1.5704	
i	1 1	4		0.003	1.6170	0.20
P	ļ <b>ķ</b>	5		-0.021	Participants of the Control of the C	0.12
	1 1	6		0.010		9000
	1	7	0.001	0.002		0.30
	"	8	0.007	0.007	5.1241	0.40
•	•	V 100 TO		-0.006		
	1 1	10.00		0.012	THE THE PARTY NAMED IN	0.50
•	1	3.3		-0.004		
1	1	12		0.018		0.48
1	"	13		0.005		
	1	14	0.031	0.030	14.363	0.21
1	1 1	15	0.006	E STATE OF THE STA	200 0 C TYPU TYPU	0.26
1	1	16		0.041		
1	"	17	0.024	T-00 T-00 T-00 T-00 T-00 T-00 T-00 T-00		0.01
	1	18	F12.717.73	T100717070		
	"	19		0.008		
	1 1	20	0.016	- TO TAKE THE	36.795	0.00
<u>"</u>	<u>"</u>	21	0.010	75.700	37.379	0.00
•		2000		-0.004		
1	<u>"</u>	100	0.011			0.00
		24	-0.005	-0.007	38.300	0.01

<sup>\*</sup>Probabilities may not be valid for this equation specification.

Figure 5: ACF and PACF of the residuals from the above AR(2) model with TGARCH errors on the differenced Bitcoin series.

 $<sup>^3</sup>$ Z-statistics in parentheses.

#### Correlogram of Standardized Residuals Squared

Date: 04/30/18 Time: 18:35 Sample: 1 5991

Included observations: 5987

Autocorrelation Partial Correlation AC PAC Q-Stat Prob\* 0.020 0.020 2.3194 0.128 -0.007 -0.007 2.5956 0.273 3 -0.003 -0.003 2.6666 0.446 4 -0.004 -0.004 2.7745 0.596 5 0.022 0.023 5.7744 0.329 6 -0.010 -0.011 6.3935 0.381 -0.010 -0.010 7.0496 0.424 8 -0.008 -0.008 7.4547 0.488 -0.005 -0.005 7.5967 0.575 10 0 000 -0 000 7 5969 0.668 -0.007 -0.007 7.8774 0.724 12 0.007 0.007 8.1515 0.773 13 -0.008 -0.008 8 5430 0.807 14 -0.003 -0.002 8.5877 0.857 15 -0.004 -0.004 8.6808 0.894 16 -0.002 -0.001 8.6974 0.925 17 -0.007 -0.008 8.9957 0.940 18 -0.004 -0.003 9.0766 0.958 19 -0.004 -0.004 9.1892 0.970 20 -0 005 -0 005 9 3353 0.979 21 -0.006 -0.006 9.5572 0.984 0.013 0.013 10.517 0.981 23 -0.008 -0.008 10.879 0.984 24 -0.006 -0.006 11.112 0.988

Figure 6: ACF and PACF of the squared residuals from AR(2) model with TGARCH errors on the differenced Bitcoin series.

#### 3.1.2 Ether

The best fitting model for the Ether data is an AR(2) with TGARCH error terms. After fitting I find the following model<sup>4</sup>:

$$\Delta ETH_t = 0.15\Delta ETH_{t-1} - 0.10\Delta ETH_{t-2} + \epsilon_t$$
(12.02) (-6.71) (4)

With an error process given by:

$$E_{t-1}(\epsilon_t^2) = 0.12 + 0.11\epsilon_{t-1}^2 + 0.02D_{t-1}\epsilon_{t-1}^2 + 0.89h_{t-1}$$

$$(12.72) (21.36) (2.84) (270.10)$$
(5)

We again look at the ACF and PACF of the residual and squared residual series from this estimation and confirm that they mirror a white noise process.

<sup>\*</sup>Probabilities may not be valid for this equation specification.

<sup>&</sup>lt;sup>4</sup>Z-statistics in parentheses.

Date: 05/01/18 Time: 10:03 Sample: 1 5991 Included observations: 5988 Q-statistic probabilities adjusted for 2 ARMA terms

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob*
ıļ .	1	1	0.038	0.038	8.7696	
l)	l ij	2	0.021	0.020	11.537	
•	8	3	-0.000	-0.002	11.537	0.001
ij	1 1	4	0.022	0.021	14.369	0.001
•		5	-0.016	-0.018	15.898	0.001
ı	l h	6	0.012	0.013	16.811	0.002
1	1 1	7	0.014	0.014	18.055	0.003
•		8	-0.004	-0.006	18.137	0.006
•		9	-0.002	-0.002	18.166	0.011
i)	l i	10	0.023	0.022	21.253	0.007
ų.	l i	11	0.011	0.010	22.024	0.009
	l p	12	0.007	0.006	22.303	0.014
ı ı	ļ Ņ	13	0.009	0.008	22.775	0.019
ı)	1	14	0.032	0.030	28.964	0.004
ı ı	l ii	15	0.014	0.012	30.221	0.004
ij	1 1	16	0.034	0.032	37.226	0.001
ij	1 1	17	0.027	0.024	41.743	0.000
1	i i	18	0.015	0.011	43.178	0.000
l)		19	0.015	0.014	44.616	0.000
ıj	1	20	0.048	0.045	58.514	0.000
li li	į į	21	0.015	0.010	59.846	0.000
•		22	-0.006	-0.010	60.098	0.000
•		23	-0.001	-0.002	60.104	0.000
ф	]	24	-0.029	-0.032	64.999	0.000

<sup>\*</sup>Probabilities may not be valid for this equation specification.

Figure 7: ACF and PACF of the residuals from the above AR(2) model with  $\operatorname{TGARCH}$  errors on the differenced Ether series.

Date: 05/01/18 Time: 10:03

Sample: 1 5991

Included observations: 5988

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob*
Autocorrelation	Partial Correlation	3 4 5 6 7 8 9	0.040 -0.009 -0.014 -0.021 0.005 -0.012 -0.014 -0.003 -0.010 -0.002	0.040 -0.010 -0.013 -0.020 0.006 -0.013 -0.002 -0.010 -0.002	9.5561 10.009 11.128 13.828 13.960 14.756 15.882 15.938 16.536 16.569	0.002 0.007 0.011 0.008 0.016 0.022 0.026 0.043 0.057 0.084
		14 15 16 17 18 19 20 21 22	0.001 0.003 -0.019 0.002 0.005 0.004 -0.017 -0.014 0.012 -0.009 0.004 -0.003 -0.000 0.001	0.004 0.003 -0.018 -0.013 0.013 -0.011 0.004 -0.004	16.571 16.632 18.836 19.025 19.102 20.788 22.039 22.947 23.453 23.558 23.630 23.631 23.641	0.121 0.164 0.128 0.170 0.213 0.263 0.236 0.230 0.240 0.267 0.315 0.367 0.424 0.482

<sup>\*</sup>Probabilities may not be valid for this equation specification.

Figure 8: ACF and PACF of the squared residuals from AR(2) model with TGARCH errors on the differenced Ether series.

### **3.1.3** Ripple

The best fitting model for the Ether data is an AR(2) with TGARCH error terms. After fitting I find the following model<sup>5</sup>:

$$\Delta XRP_t = 0.13\Delta XRP_{t-1} - 0.10\Delta XRP_{t-2} + \epsilon_t$$
(9.67) (-6.68)

With an error process given by:

$$E_{t-1}(\epsilon_t^2) = 0.000000312 + 0.14\epsilon_{t-1}^2 + 0.014D_{t-1}\epsilon_{t-1}^2 + 0.87h_{t-1}$$
(35.14) (26.60) (1.97) (261.57)

We again look at the ACF and PACF of the residual and squared residual series from this estimation and confirm that they mirror a white noise process.

 $<sup>^5\</sup>mathrm{Z}\text{-statistics}$  in parentheses.

Date: 05/01/18 Time: 10:10

Sample: 1 5991

Included observations: 5988
Q-statistic probabilities adjusted for 2 ARMA terms

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob*
ij	1 1	1	0.026	0.026	4.1606	
ıl I	l l	2	0.026	0.025	8.2374	
ų.		3	0.009	0.008	8.7675	0.003
ų.	1	4	0.015	0.014	10.143	0.006
•		5	-0.001	-0.002	10.149	0.017
1		6	0.017	0.016	11.906	0.018
ų.	1	7	0.013	0.012	12.887	0.024
•		8	-0.011	-0.013	13.671	0.034
I)	1	9	0.020	0.020	16.104	0.024
1	1	10	0.019	0.018	18.292	0.019
•		11	-0.006	-0.008	18.496	0.030
•		12	-0.002	-0.003	18.519	0.047
ı)	l l	13	0.017	0.017	20.349	0.041
ф	1	14	0.046	0.046	33.197	0.001
ı <b>j</b>	l l	15	0.022	0.019	36.002	0.001
ф	j j	16	0.036	0.031	43.774	0.000
ij	1	17	0.028	0.024	48.405	0.000
ıl I		18	0.025	0.021	52.226	0.000
ų.	1	19	0.015	0.010	53.558	0.000
ıjı	i i	20	0.035	0.030	60.754	0.000
1	1	21	0.009	0.005	61.238	0.000
1	1	22	0.023	0.020	64.503	0.000
1	į į	23	0.027	0.022	68.859	0.000
d	l ø	2.755	-0.027	-0.032	73.179	0.000

<sup>\*</sup>Probabilities may not be valid for this equation specification.

Figure 9: ACF and PACF of the residuals from the above AR(2) model with TGARCH errors on the differenced Ripple series.

Date: 05/01/18 Time: 10:10

Sample: 1 5991 Included observations: 5988

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob*
1		1	0.001	0.001	0.0042 0.0281	0.948 0.986
I	I	100		-0.002	0.0201	0.998
I		-		-0.005	0.1760	0.996
•		1900		-0.004	0.2817	0.998
•		6	-0.005	-0.005	0.4317	0.999
•		7	-0.002	-0.002	0.4503	1.000
•		8	-0.003	-0.003	0.5028	1.000
		9	-0.001	-0.001	0.5115	1.000
•		27.5		-0.002	0.5301	1.000
•		55.55		-0.002	0.5627	1.000
1	1	12	0.001	0.001	0.5687	1.000
· ·	1	13	0.001	0.001	0.5708	1.000
•	1	500		-0.002	0.5872	1.000
1	1	100		-0.002	0.6007	1.000
1	1	3 Table 1		-0.001	0.6073	1.000
Ī	1	2012		-0.002	0.6356	1.000
Ī	1	200		-0.002	0.6697	1.000
Ī	1	659-55		-0.003	0.7376	1.000
1			NEW TOTAL	-0.001	0.7433	1.000
1		21	0.001	0.000	0.7452	1.000
1		22	0.004	0.004	0.8374	1.000
Ī	i	76.4		-0.001	0.8489	1.000
	I •	24 -	-0.002	-0.002	0.8826	1.000

<sup>\*</sup>Probabilities may not be valid for this equation specification.

Figure 10: ACF and PACF of the squared residuals from AR(2) model with TGARCH errors on the differenced Ripple series.

#### Cointegrated Analysis 3.2

#### Conclusion 4