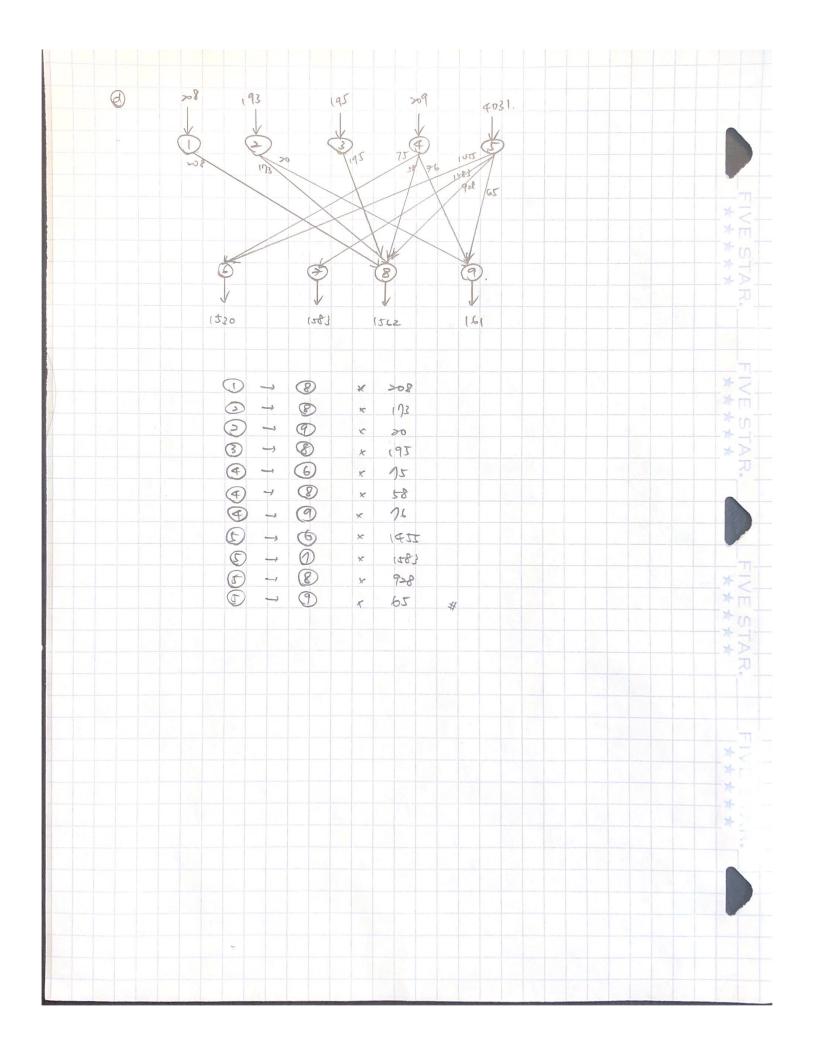
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$-(X_{16} + X_{26} + X_{36} + X_{46} + X_{46}) = -1530$ $-(X_{19} + X_{29} + X_{39} + X_{49} + X_{49}) = -1563$ $-(X_{19} + X_{24} = X_{38} + X_{68} + X_{69}) = -1563$ $-(X_{19} + X_{29} + X_{29} + X_{29} + X_{69}) = -161$ $X_{16} = 7400$ $X_{17} = 35766$ $X_{18} = 5707$ $X_{19} = (732)$ $X_{19} = (732)$ $X_{19} = (732)$ $X_{29} = 90$	$-(X_{16} + X_{36} + X_{36} + X_{46} + X_{46} + X_{46}) = -(130)$ $-(X_{19} + X_{39} + X_{39} + X_{49} + X_{49}) = -(163)$ $-(X_{19} + X_{39} + X_{29} + X_{49} + X_{49}) = -(161)$ $-(X_{19} + X_{39} + X_{29} + X_{49} + X_{49}) = -(161)$ $-(X_{19} + X_{39} + X_{29} + X_{49} + X_{49}) = -(161)$ $-(X_{19} + X_{39} + X_{29} + X_{49} + X_{49}) = -(161)$ $-(X_{19} + X_{39} + X_{29} + X_{49} + X_{49}) = -(161)$ $-(X_{19} + X_{39} + X_{29} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{29} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{29} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{29} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{49} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{49} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{49} + X_{49}) = -(162)$ $-(X_{19} + X_{39} + X_{49}) = -(162)$ $-(X_{19} + X_{39}) = -(162)$ $-(X_{19} + X_{39} + X_{49}) = -(162)$ $-(X_{19} + X_{49}) = -(162)$ $-(X_{19} + X_{29} + X_{49}) = -(162)$ $-(X_{19} + X_{29}) = -(162)$ $-(X_{19} + X_{29} + X_{29}) = -(162)$ $-(X_{19} + X_{29}) = -(161)$	$-(X_{16} + X_{26} + X_{36} + X_{46} + X_{46}) = -(130)$ $-(X_{19} + X_{29} + X_{39} + X_{49} + X_{49}) = -(169)$ $-(X_{19} + X_{24} = X_{36} + X_{49} + X_{49}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49}) = -(6)$ $-(X_{19} + X_{29} + X_{29} + X_{49}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{49}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29} + X_{29}) = -(16)$ $-(X_{19} + X_{29} + X_{29}) = -(16)$			Xab	4	Xay	+	Xes	4	-X49	1	209				
-(X/2 + X-2) + X3 + X4	$-(X_{1}7 + X_{2}7 + X_{3}7 + X_{4}7 + X_{4}7) = -(x_{3}8)$ $-(X_{1}8 + X_{2}8 + X_{3}8 + X_{4}8) = -(x_{3}8)$ $-(X_{1}8 + X_{2}8 + X_{3}8 + X_{4}8) = -(x_{3}8)$ $-(X_{1}9 + X_{2}9 + X_{3}9 + X_{4}9) = -(x_{3}$	$-(X_{1}7 + X_{2}7 + X_{3}7 + X_{4}7 + X_{4}7) = -(18)$ $-(X_{1}8 + X_{2}4 + X_{3}8 + X_{4}8) = -(18)$ $-(X_{1}9 + X_{2}4 + X_{3}8 + X_{4}8) = -(18)$ $-(X_{1}9 + X_{2}4 + X_{3}7 + X_{4}9 + X_{4}7) = -(6)$ $X_{1}6 = (740)$ $X_{1}7 = (740)$ $X_{1}8 = (740)$ $X_{1}9 = (740)$ $X_{1}9 = (740)$ $X_{1}9 = (740)$ $X_{2}9 = (740)$ $X_{3}9 = (740)$ $X_{4}9 = (740)$ $X_{$			X56	of	X59	-4	×58	4	X59	2	4031				
- (X ₁ 0 + X ₂ 0 + X ₂ 0 + X ₂ 0 + X ₃ 0) = -1563 - (X ₁ 0 + X ₂ 0 + X ₂ 0 + X ₃ 0 + X ₄ 0) = -16[X ₁ 0 = 7407 X ₁ 1 = 5566 X ₁ 1 = 4072 X ₁ 1 = 65 X ₂ 1 = 7407 X ₃ 1 = 4072 X ₄ 2 = 4073 X ₄ 3 = 4073 X ₄ 4 = 4073 X ₄ 5 = 103 X ₄ 5 = 103 X ₄ 6 = 5047 X ₄ 7 = 208 X ₄ 7 = 20	$-(X_{1} + X_{2} + X_{3} + X_{2} + X_{4} + X_{4}) = -1563$ $-(X_{1} + X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4} + X_{4}) = -16(1$ $X_{1} + X_{2} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X_{4}) = -16(1$ $X_{2} + X_{3} + X_{4} + X$	$-(X_{1} + X_{2} + X_{3} + X_{1} + X_{4} + X_{5}) = -156$ $-(X_{1} + X_{2} + X_{3} + X_{1} + X_{4} + X_{5}) = -161$ $X_{1} + X_{2} + X_{3} + X_{4} + X_{5} + X_{5} = -161$ $X_{1} + X_{2} + X_{4} + X_{5} + X_{4} + X_{5} = -161$ $X_{1} + X_{2} + X_{5} + X_{5} = -161$ $X_{1} + X_{2} + X_{5} + X_{5} = -161$ $X_{1} + X_{2} + X_{5} + X_{5} = -161$ $X_{1} + X_{2} + X_{5} + X_{5} = -161$ $X_{1} + X_{2} + X_{5} + X_{5} = -161$ $X_{2} + X_{3} + X_{5} = -161$ $X_{3} + X_{4} = -161$ $X_{4} + X_{5} + X_{5} = -161$ $X_{5} + X_{5} + X_{5} = -173$ $X_{5} + X_{5} + X_{$			- (X16	+	Xxb	4	X36	4	X46	4	X58)	= -1530			
$-(X, 9 + X_29 + X_27 + X_49 + X_59) = -161$ $X (6 = 740)$ $X (7 = 1740)$ $X (8 = 1740)$ $X (9 = 1732)$ $X (19 = 1732)$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		-	- (X1)	+	Xzy	4	×37	+	X 47	4	X++):	=-1583			
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$\times 59 = 65$	$\times 59 = 65$	$\times 59 = 65$												X56	= 1955		
X 39 £ 65 X79 = 65	X 39 £ 65 X79 = 65	X 39 £ 65 X79 = 65			X 58	4	7	3	+ 877	-				(ZX	= 1583		
X-9=65	X+9=65	X+9=65			X 59		6	5									
xij ≥0 ∀i, ∀j	xij ≥0 ∀i, ∀j	xij ≥0 ∀i, ∀j															
					Xii	> ,	, 1	1:	+/:					oth	arvive	=0	M.
					9		1	1	V								47



Problem 1

December 3, 2019

0.1 name: Yi Ping Tseng

0.2 uni: yt2690

0.3 email: yt2690@columbia.edu

0.4 github: https://github.com/r50206v/Optimization-Homework/tree/master/homework5

```
[]:
```

[]:

0.4.1 a.

Gurobi .lp file

```
[]: Minimize
     + 541.0 \times 1,6 + 386.0 \times 1,7 + 25.0 \times 1,8 + 1512.0 \times 1,9 + 234.0 \times 2,6
     + 899.0 x_2,7 + 103.0 x_2,8 + 1256.0 x_2,9 + 543.0 x_3,6 + 257.0 x_3,7
     + 1653.0 x_3,8 + 1085.0 x_3,9 + 1785.0 x_4,6 + 227.0 x_4,7 + 1670.0 x_4,8
     +823.0 \times 4.9 + 490.0 \times 5.6 + 1233.0 \times 5.7 + 1242.0 \times 5.8 + 1841.0 \times 5.9
     Subject To
     balance_1: + x_1,6 + x_1,7 + x_1,8 + x_1,9 = 208.0
     balance_2: + x_2,6 + x_2,7 + x_2,8 + x_2,9 = 193.0
     balance_3: + x_3,6 + x_3,7 + x_3,8 + x_3,9 = 195.0
     balance_4: + x_4,6 + x_4,7 + x_4,8 + x_4,9 = 209.0
     balance_5: + x_5,6 + x_5,7 + x_5,8 + x_5,9 = 4031.0
     balance_6: -x_1,6-x_2,6-x_3,6-x_4,6-x_5,6
     = -1530.0
     balance_7: -x_1,7 - x_2,7 - x_3,7 - x_4,7 - x_5,7
     = -1583.0
     balance_8: - x_1,8 - x_2,8 - x_3,8 - x_4,8 - x_5,8
     = -1562.0
     balance_9: -x_1,9-x_2,9-x_3,9-x_4,9-x_5,9
     = -161.0
     Bounds
```

```
x_1,6 \le 7407.0
x_1,7 \le 3546.0
x_1,8 \le 5072.0
x_1,9 \le 1932.0
x_2,6 \le 81.0
x_2,7 \le 90.0
x_2,8 \le 29.0
x_2,9 \le 902.0
x_3,6 \le 13.0
x 3,7 \le 8413.0
x 3,8 \le 8719.0
x_3,9 \le 7439.0
x_4,6 \le 5047.0
x_4,7 \le 83.0
x_4,8 \le 58.0
x_4,9 <= 76.0
x_5,6 \le 83.0
x_5,7 <= 7904.0
x_5,8 <= 73.0
x_5,9 \le 65.0
END
```

output in terminal

[]:

```
[]: Academic license - for non-commercial use only
     Gurobi Optimizer version 8.1.1 build v8.1.1rc0 (mac64)
     Copyright (c) 2019, Gurobi Optimization, LLC
     Read LP format model from file prob1-a.lp
     Reading time = 0.01 seconds
     : 9 rows, 20 columns, 40 nonzeros
     Optimize a model with 9 rows, 20 columns and 40 nonzeros
     Coefficient statistics:
      Matrix range
                       [1e+00, 1e+00]
      Objective range [2e+01, 2e+03]
      Bounds range
                      [1e+01, 9e+03]
      RHS range
                        [2e+02, 4e+03]
     Presolve time: 0.00s
     Solved in 0 iterations and 0.00 seconds
     Infeasible model
```

```
[]:
```

0.4.2 b.

```
[]: from gurobipy import *
     # create a model
     m = Model()
     # create variables
     x16 = m.addVar(vtype=GRB.CONTINUOUS, name="x16", lb=0)
     x17 = m.addVar(vtype=GRB.CONTINUOUS, name="x17", lb=0)
     x18 = m.addVar(vtype=GRB.CONTINUOUS, name="x18", lb=0)
     x19 = m.addVar(vtype=GRB.CONTINUOUS, name="x19", lb=0)
     x26 = m.addVar(vtype=GRB.CONTINUOUS, name="x26", 1b=0)
     x27 = m.addVar(vtype=GRB.CONTINUOUS, name="x27", 1b=0)
     x28 = m.addVar(vtype=GRB.CONTINUOUS, name="x28", 1b=0)
     x29 = m.addVar(vtype=GRB.CONTINUOUS, name="x29", 1b=0)
     x36 = m.addVar(vtype=GRB.CONTINUOUS, name="x36", lb=0)
     x37 = m.addVar(vtype=GRB.CONTINUOUS, name="x37", 1b=0)
     x38 = m.addVar(vtype=GRB.CONTINUOUS, name="x38", 1b=0)
     x39 = m.addVar(vtype=GRB.CONTINUOUS, name="x39", 1b=0)
     x46 = m.addVar(vtype=GRB.CONTINUOUS, name="x46", lb=0)
     x47 = m.addVar(vtype=GRB.CONTINUOUS, name="x47", lb=0)
     x48 = m.addVar(vtype=GRB.CONTINUOUS, name="x48", 1b=0)
     x49 = m.addVar(vtype=GRB.CONTINUOUS, name="x49", 1b=0)
     x56 = m.addVar(vtype=GRB.CONTINUOUS, name="x56", 1b=0)
     x57 = m.addVar(vtype=GRB.CONTINUOUS, name="x57", 1b=0)
     x58 = m.addVar(vtype=GRB.CONTINUOUS, name="x58", 1b=0)
     x59 = m.addVar(vtype=GRB.CONTINUOUS, name="x59", lb=0)
     theta_x16 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x16", lb=0)
     theta x17 = m.addVar(vtype=GRB.CONTINUOUS, name="theta x17", lb=0)
     theta_x18 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x18", lb=0)
     theta x19 = m.addVar(vtype=GRB.CONTINUOUS, name="theta x19", lb=0)
     theta_x26 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x26", 1b=0)
     theta_x27 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x27", 1b=0)
     theta_x28 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x28", 1b=0)
     theta_x29 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x29", 1b=0)
     theta x36 = m.addVar(vtype=GRB.CONTINUOUS, name="theta x36", 1b=0)
     theta_x37 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x37", 1b=0)
     theta_x38 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x38", lb=0)
     theta_x39 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x39", 1b=0)
     theta_x46 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x46", lb=0)
     theta_x47 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x47", lb=0)
     theta_x48 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x48", lb=0)
     theta_x49 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x49", lb=0)
     theta x56 = m.addVar(vtype=GRB.CONTINUOUS, name="theta x56", 1b=0)
     theta_x57 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x57", 1b=0)
```

```
theta_x58 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x58", lb=0)
theta_x59 = m.addVar(vtype=GRB.CONTINUOUS, name="theta_x59", 1b=0)
# integrate new variables
m.update()
# set objective
m.setObjective(
    541.0*theta_x16 + 386.0*theta_x17 + 25.0*theta_x18 + 1512.0*theta_x19 + 234.
 \rightarrow0*theta_x26 + 899.0*theta_x27 + 103.0*theta_x28 + 1256.0*theta_x29 + 543.
 \rightarrow0*theta_x36 + 257.0*theta_x37 + 1653.0*theta_x38 + 1085.0*theta_x39 + 1785.
 \rightarrow0*theta_x46 + 227.0*theta_x47 + 1670.0*theta_x48 + 823.0*theta_x49 + 490.
 -0*theta_x56 + 1233.0*theta_x57 + 1242.0*theta_x58 + 1841.0*theta_x59,
    GRB.MINIMIZE
# add constraints
m.addConstr(x16 + x17 + x18 + x19 == 208.0)
m.addConstr(x26 + x27 + x28 + x29 == 193.0)
m.addConstr(x36 + x37 + x38 + x39 == 195.0)
m.addConstr(x46 + x47 + x48 + x49 == 209.0)
m.addConstr(x56 + x57 + x58 + x59 == 4031.0)
m.addConstr(-1*(x16 + x26 + x36 + x46 + x56) == -1530.0)
m.addConstr(-1*(x17 + x27 + x37 + x47 + x57) == -1583.0)
m.addConstr(-1*(x18 + x28 + x38 + x48 + x58) == -1562.0)
m.addConstr(-1*(x19 + x29 + x39 + x49 + x59) == -161.0)
m.addConstr(x16 \le 7407.0 + theta_x16)
m.addConstr(x17 \le 3546.0 + theta_x17)
m.addConstr(x18 \le 5072.0 + theta x18)
m.addConstr(x19 \le 1932.0 + theta_x19)
m.addConstr(x26 \le 81.0 + theta x26)
m.addConstr(x27 <= 90.0 + theta_x27)
m.addConstr(x28 \le 29.0 + theta x28)
m.addConstr(x29 \le 902.0 + theta x29)
m.addConstr(x36 <= 13.0 + theta_x36)
m.addConstr(x37 \le 8413.0 + theta x37)
m.addConstr(x38 \le 8719.0 + theta_x38)
m.addConstr(x39 \le 7439.0 + theta_x39)
m.addConstr(x46 \le 5047.0 + theta_x46)
m.addConstr(x47 \le 83.0 + theta_x47)
m.addConstr(x48 <= 58.0 + theta_x48)
m.addConstr(x49 \le 76.0 + theta_x49)
m.addConstr(x56 \le 83.0 + theta_x56)
m.addConstr(x57 \le 7904.0 + theta x57)
m.addConstr(x58 \le 73.0 + theta_x58)
m.addConstr(x59 \le 65.0 + theta x59)
```

```
# optimize
     m.optimize()
     print("Model status: ", m.status)
     # print out decision variables
     for v in m.getVars():
         print(v.varName, v.x, "\n")
     print("-"*15)
     print("Obj Value: ", m.objVal)
[]: x16 0.0
    x17 0.0
    x18 208.0
     x19 0.0
     x26 0.0
     x27 0.0
    x28 173.0
     x29 20.0
     x36 0.0
     x37 0.0
     x38 195.0
     x39 0.0
     x46 75.0
     x47 0.0
     x48 58.0
     x49 76.0
     x56 1455.0
     x57 1583.0
     x58 928.0
     x59 65.0
     theta_x16 0.0
     theta_x17 0.0
     theta_x18 0.0
     theta_x19 0.0
     theta_x26 0.0
     theta_x27 0.0
     theta_x28 144.0
     theta_x29 0.0
     theta_x36 0.0
     theta_x37 0.0
     theta_x38 0.0
     theta_x39 0.0
     theta_x46 0.0
     theta_x47 0.0
```

theta_x48 0.0

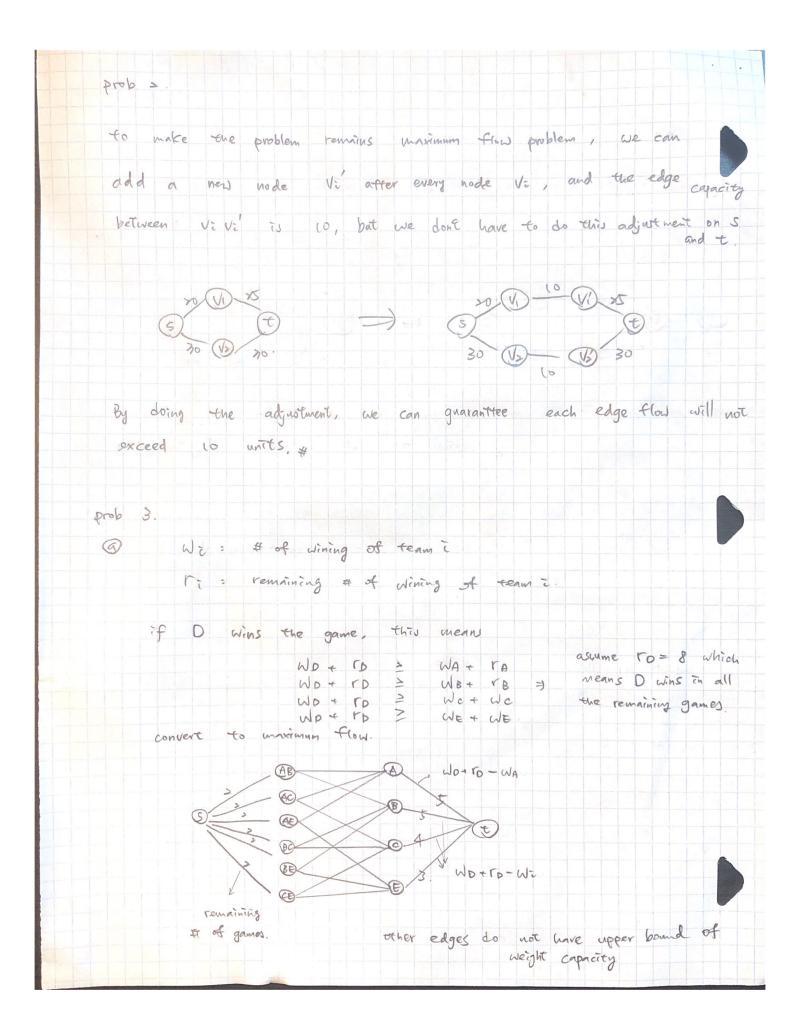
[]:

0.4.3 c.

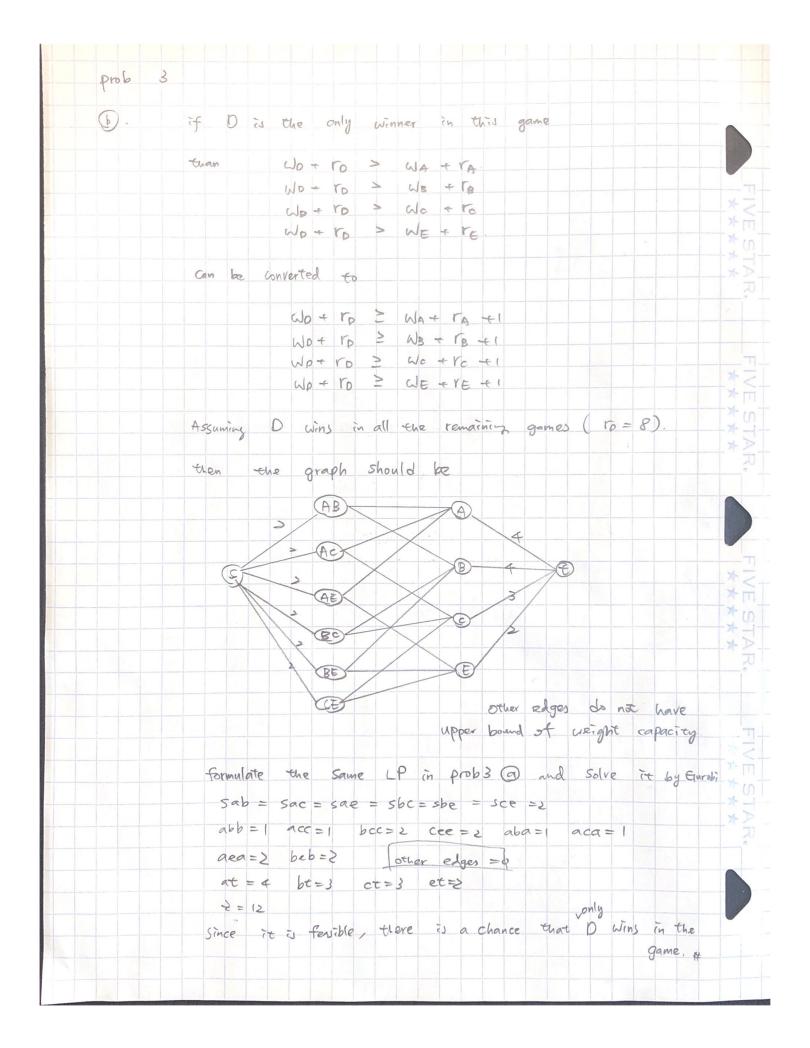
```
[]: from gurobipy import *
     # create a model
     m = Model()
     # create variables
     x16 = m.addVar(vtype=GRB.CONTINUOUS, name="x16", lb=0)
     x17 = m.addVar(vtype=GRB.CONTINUOUS, name="x17", lb=0)
     x18 = m.addVar(vtype=GRB.CONTINUOUS, name="x18", lb=0)
     x19 = m.addVar(vtype=GRB.CONTINUOUS, name="x19", lb=0)
     x26 = m.addVar(vtype=GRB.CONTINUOUS, name="x26", 1b=0)
     x27 = m.addVar(vtype=GRB.CONTINUOUS, name="x27", 1b=0)
     x28 = m.addVar(vtype=GRB.CONTINUOUS, name="x28", 1b=0)
     x29 = m.addVar(vtype=GRB.CONTINUOUS, name="x29", lb=0)
     x36 = m.addVar(vtype=GRB.CONTINUOUS, name="x36", lb=0)
     x37 = m.addVar(vtype=GRB.CONTINUOUS, name="x37", 1b=0)
     x38 = m.addVar(vtype=GRB.CONTINUOUS, name="x38", 1b=0)
     x39 = m.addVar(vtype=GRB.CONTINUOUS, name="x39", 1b=0)
     x46 = m.addVar(vtype=GRB.CONTINUOUS, name="x46", 1b=0)
     x47 = m.addVar(vtype=GRB.CONTINUOUS, name="x47", 1b=0)
     x48 = m.addVar(vtype=GRB.CONTINUOUS, name="x48", lb=0)
     x49 = m.addVar(vtype=GRB.CONTINUOUS, name="x49", lb=0)
     x56 = m.addVar(vtype=GRB.CONTINUOUS, name="x56", lb=0)
     x57 = m.addVar(vtype=GRB.CONTINUOUS, name="x57", lb=0)
     x58 = m.addVar(vtype=GRB.CONTINUOUS, name="x58", 1b=0)
     x59 = m.addVar(vtype=GRB.CONTINUOUS, name="x59", 1b=0)
     # integrate new variables
     m.update()
     # set objective
     m.setObjective(
```

```
541.0*x16 + 386.0*x17 + 25.0*x18 + 1512.0*x19 + 234.0*x26 + 899.0*x27 + 103.
 \rightarrow0*x28 + 1256.0*x29 + 543.0*x36 + 257.0*x37 + 1653.0*x38 + 1085.0*x39 + 1785.
 \Rightarrow0*x46 + 227.0*x47 + 1670.0*x48 + 823.0*x49 + 490.0*x56 + 1233.0*x57 + 1242.
 \rightarrow 0*x58 + 1841.0*x59
    GRB.MINIMIZE
)
# add constraints
m.addConstr(x16 + x17 + x18 + x19 == 208.0)
m.addConstr(x26 + x27 + x28 + x29 == 193.0)
m.addConstr(x36 + x37 + x38 + x39 == 195.0)
m.addConstr(x46 + x47 + x48 + x49 == 209.0)
m.addConstr(x56 + x57 + x58 + x59 == 4031.0)
m.addConstr(-1*(x16 + x26 + x36 + x46 + x56) == -1530.0)
m.addConstr(-1*(x17 + x27 + x37 + x47 + x57) == -1583.0)
m.addConstr(-1*(x18 + x28 + x38 + x48 + x58) == -1562.0)
m.addConstr(-1*(x19 + x29 + x39 + x49 + x59) == -161.0)
m.addConstr(x16 \le 7407.0 + 0.0)
m.addConstr(x17 \le 3546.0 + 0.0)
m.addConstr(x18 \le 5072.0 + 0.0)
m.addConstr(x19 \le 1932.0 + 0.0)
m.addConstr(x26 \le 81.0 + 0.0)
m.addConstr(x27 \le 90.0 + 0.0)
m.addConstr(x28 \le 29.0 + 144.0)
m.addConstr(x29 \le 902.0 + 0.0)
m.addConstr(x36 \le 13.0 + 0.0)
m.addConstr(x37 \le 8413.0 + 0.0)
m.addConstr(x38 \le 8719.0 + 0.0)
m.addConstr(x39 \le 7439.0 + 0.0)
m.addConstr(x46 \le 5047.0 + 0.0)
m.addConstr(x47 \le 83.0 + 0.0)
m.addConstr(x48 \le 58.0 + 0.0)
m.addConstr(x49 \le 76.0 + 0.0)
m.addConstr(x56 \le 83.0 + 1372.0)
m.addConstr(x57 \le 7904.0 + 0.0)
m.addConstr(x58 \le 73.0 + 855.0)
m.addConstr(x59 \le 65.0 + 0.0)
# optimize
m.optimize()
print("Model status: ", m.status)
# print out decision variables
for v in m.getVars():
    print(v.varName, v.x, "\n")
print("-"*15)
```

```
print("Obj Value: ", m.objVal)
[]: x16 0.0
     x17 0.0
     x18 208.0
     x19 0.0
     x26 0.0
     x27 0.0
     x28 173.0
     x29 20.0
     x36 0.0
     x37 0.0
     x38 195.0
     x39 0.0
     x46 75.0
     x47 0.0
     x48 58.0
     x49 76.0
     x56 1455.0
     x57 1583.0
     x58 928.0
     x59 65.0
     Obj Value: 4600787.0
[]:
```



```
prob 3 (continue)
        if we can find a solution in this maximum flow
     S > t , then this means D can still win in the game
     we can find if there is any feasible solution by applying
     linear programming on maximum flow problem.
          wax 2
               (sab + sac + sar + sbc + sbe + sce) x-1 = -2
           S.E.
                at + bt + ct + et
                 sab = aba + abb
                 Sac = aca + acc
                 Sac = aga + age
                 Sbc = bcb + bcc
                 sbe = beb + bee.
                 Sce = cec + cee
                 at = aba + aca + aea
                  bt = abb + bcb + beb
                 ct = acc + bcc + cec
                  et = aee + bee + cee.
                  5ab < 1
                          at 5 5
                  sac & > be & 5
                  sae = 2 ct = 4
                            et = 3.
                  56c = >
                  S 6 = 2
                  Sce 52
                  all variables = 0.
         Solved by gurobi
          Sac = sac = sae = sbc = sbe = sce = 2
          abb = 1 are = 2 aba=1 aca = 2
          bcb=2 beb=2 cec=2 lother edges =0
          at=3 bt=5 ct=2 et=2
          2=12 > since it is fersible, then there is possibility that D wins.
```



Problem 3

December 3, 2019

```
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```

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 $0.4 \hspace{0.2cm} github: \hspace{0.2cm} https://github.com/r50206v/Optimization-Homework/tree/master/homework5$

```
[]:
```

0.4.1 a.

```
[]: from gurobipy import *
     # create a model
     m = Model()
     # create variables
     sab = m.addVar(vtype=GRB.CONTINUOUS, name="sab", lb=0)
     sac = m.addVar(vtype=GRB.CONTINUOUS, name="sac", 1b=0)
     sae = m.addVar(vtype=GRB.CONTINUOUS, name="sae", 1b=0)
     sbc = m.addVar(vtype=GRB.CONTINUOUS, name="sbc", 1b=0)
     sbe = m.addVar(vtype=GRB.CONTINUOUS, name="sbe", 1b=0)
     sce = m.addVar(vtype=GRB.CONTINUOUS, name="sce", lb=0)
     abb = m.addVar(vtype=GRB.CONTINUOUS, name="abb", 1b=0)
     acc = m.addVar(vtype=GRB.CONTINUOUS, name="acc", 1b=0)
     aee = m.addVar(vtype=GRB.CONTINUOUS, name="aee", 1b=0)
     bcc = m.addVar(vtype=GRB.CONTINUOUS, name="bcc", 1b=0)
     bee = m.addVar(vtype=GRB.CONTINUOUS, name="bee", lb=0)
     cee = m.addVar(vtype=GRB.CONTINUOUS, name="cee", lb=0)
     aba = m.addVar(vtype=GRB.CONTINUOUS, name="aba", 1b=0)
     aca = m.addVar(vtype=GRB.CONTINUOUS, name="aca", lb=0)
```

```
aea = m.addVar(vtype=GRB.CONTINUOUS, name="aea", lb=0)
bcb = m.addVar(vtype=GRB.CONTINUOUS, name="bcb", 1b=0)
beb = m.addVar(vtype=GRB.CONTINUOUS, name="beb", 1b=0)
cec = m.addVar(vtype=GRB.CONTINUOUS, name="cec", lb=0)
at = m.addVar(vtype=GRB.CONTINUOUS, name="at", 1b=0)
bt = m.addVar(vtype=GRB.CONTINUOUS, name="bt", 1b=0)
ct = m.addVar(vtype=GRB.CONTINUOUS, name="ct", 1b=0)
et = m.addVar(vtype=GRB.CONTINUOUS, name="et", 1b=0)
z = m.addVar(vtype=GRB.CONTINUOUS, name="z", 1b=0)
# integrate new variables
m.update()
# set objective
# sum of outflow of s
m.setObjective(
    z,
    GRB.MAXIMIZE
# add constraints
# input/output constraints
m.addConstr(-1*(sab + sac + sae + sbc + sbe + sce) == -z)
m.addConstr(at + bt + ct + et == z)
# capacity constraints
m.addConstr(sab <= 2)</pre>
m.addConstr(sac <= 2)</pre>
m.addConstr(sae <= 2)</pre>
m.addConstr(sbc <= 2)</pre>
m.addConstr(sbe <= 2)</pre>
m.addConstr(sce <= 2)</pre>
m.addConstr(at <= 5)</pre>
m.addConstr(bt <= 5)</pre>
m.addConstr(ct <= 4)
m.addConstr(et <= 3)</pre>
# inflow equals to outflow constraints
m.addConstr(sab == aba + abb)
m.addConstr(sac == aca + acc)
m.addConstr(sae == aea + aee)
m.addConstr(sbc == bcb + bcc)
m.addConstr(sbe == beb + bee)
m.addConstr(sce == cec + cee)
m.addConstr(at == aba + aca + aea)
m.addConstr(bt == abb + bcb + beb)
m.addConstr(ct == acc + bcc + cec)
m.addConstr(et == aee + bee + cee)
```

```
# optimize
     m.optimize()
     print("Model status: ", m.status)
     # print out decision variables
     for v in m.getVars():
         print(v.varName, v.x, "\n")
     print("-"*15)
     print("Obj Value: ", m.objVal)
[]: sab 2.0
     sac 2.0
     sae 2.0
     sbc 2.0
     sbe 2.0
     sce 2.0
     abb 1.0
     acc 0.0
     aee 2.0
     bcc 0.0
     bee 0.0
     cee 0.0
     aba 1.0
     aca 2.0
     aea 0.0
     bcb 2.0
     beb 2.0
     cec 2.0
     at 3.0
     bt 5.0
     ct 2.0
     et 2.0
     z 12.0
     Obj Value: 12.0
[]:
[]:
```

0.4.2 b.

```
[]: from gurobipy import *
     # create a model
     m = Model()
     # create variables
     sab = m.addVar(vtype=GRB.CONTINUOUS, name="sab", lb=0)
     sac = m.addVar(vtype=GRB.CONTINUOUS, name="sac", lb=0)
     sae = m.addVar(vtype=GRB.CONTINUOUS, name="sae", lb=0)
     sbc = m.addVar(vtype=GRB.CONTINUOUS, name="sbc", 1b=0)
     sbe = m.addVar(vtype=GRB.CONTINUOUS, name="sbe", lb=0)
     sce = m.addVar(vtype=GRB.CONTINUOUS, name="sce", lb=0)
     abb = m.addVar(vtype=GRB.CONTINUOUS, name="abb", 1b=0)
     acc = m.addVar(vtype=GRB.CONTINUOUS, name="acc", 1b=0)
     aee = m.addVar(vtype=GRB.CONTINUOUS, name="aee", 1b=0)
     bcc = m.addVar(vtype=GRB.CONTINUOUS, name="bcc", 1b=0)
     bee = m.addVar(vtype=GRB.CONTINUOUS, name="bee", lb=0)
     cee = m.addVar(vtype=GRB.CONTINUOUS, name="cee", 1b=0)
     aba = m.addVar(vtype=GRB.CONTINUOUS, name="aba", 1b=0)
     aca = m.addVar(vtype=GRB.CONTINUOUS, name="aca", 1b=0)
     aea = m.addVar(vtype=GRB.CONTINUOUS, name="aea", 1b=0)
     bcb = m.addVar(vtype=GRB.CONTINUOUS, name="bcb", 1b=0)
     beb = m.addVar(vtype=GRB.CONTINUOUS, name="beb", 1b=0)
     cec = m.addVar(vtype=GRB.CONTINUOUS, name="cec", 1b=0)
     at = m.addVar(vtype=GRB.CONTINUOUS, name="at", 1b=0)
     bt = m.addVar(vtype=GRB.CONTINUOUS, name="bt", lb=0)
     ct = m.addVar(vtype=GRB.CONTINUOUS, name="ct", lb=0)
     et = m.addVar(vtype=GRB.CONTINUOUS, name="et", 1b=0)
     z = m.addVar(vtype=GRB.CONTINUOUS, name="z", 1b=0)
     # integrate new variables
     m.update()
     # set objective
     # sum of outflow of s
     m.setObjective(
         GRB. MAXIMIZE
     )
     # add constraints
     # input/output constraints
     m.addConstr(-1*(sab + sac + sae + sbc + sbe + sce) == -z)
```

```
# capacity constraints
     m.addConstr(sab <= 2)</pre>
     m.addConstr(sac <= 2)</pre>
     m.addConstr(sae <= 2)</pre>
     m.addConstr(sbc <= 2)</pre>
     m.addConstr(sbe <= 2)</pre>
     m.addConstr(sce <= 2)</pre>
     m.addConstr(at <= 4)</pre>
     m.addConstr(bt <= 4)</pre>
     m.addConstr(ct <= 3)</pre>
     m.addConstr(et <= 2)</pre>
     # inflow equals to outflow constraints
     m.addConstr(sab == aba + abb)
     m.addConstr(sac == aca + acc)
     m.addConstr(sae == aea + aee)
     m.addConstr(sbc == bcb + bcc)
     m.addConstr(sbe == beb + bee)
     m.addConstr(sce == cec + cee)
     m.addConstr(at == aba + aca + aea)
     m.addConstr(bt == abb + bcb + beb)
     m.addConstr(ct == acc + bcc + cec)
     m.addConstr(et == aee + bee + cee)
     # optimize
     m.optimize()
     print("Model status: ", m.status)
     # print out decision variables
     for v in m.getVars():
         print(v.varName, v.x, "\n")
     print("-"*15)
     print("Obj Value: ", m.objVal)
[]: sab 2.0
     sac 2.0
     sae 2.0
     sbc 2.0
     sbe 2.0
     sce 2.0
     abb 1.0
     acc 1.0
     aee 0.0
     bcc 2.0
     bee 0.0
```

m.addConstr(at + bt + ct + et == z)

```
cee 2.0
aba 1.0
aca 1.0
aea 2.0
bcb 0.0
beb 2.0
cec 0.0
at 4.0
bt 3.0
ct 3.0
et 2.0
z 12.0
------
Obj Value: 12.0
```

[]:

	problem 4:
	Q
	$f_{i}(j) = f_{i}(j-1) + f_{i-1}(j)$
	if either i or $j=0$, $f_{\bar{z}}(j)=1$. the i, j Start from 0.
1 134	
	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	1 3 6 (0 15 >1 >8
	1 4 1= 20 35 56 84
	7 4 7 2 2 2 2
	$f_{i}(j) = \max(f_{i}(j-1), f_{i-1}(j)) + I(i, j)$ i, j start from (
	I(i,j) = i if there is a coin at (i,j)
	0,0.2
	6090011
	0012223
	path should be this
	0 1 2 3 4 4 4