Introduction to scientific computing



Abstract

We teach basic software engineering, numerical methods, and computational engineering skills. They allow you to leverage tools from computational science and increase the transparency and extensibility of our implementations. In doing so, you expand the set of possible economic questions that you can address and improve the quality of your answers.

We organize the course around the two flagship codes of our group. We use them to explore selected issues in software engineering, numerical methods, and computational engineering.

• respy

We maintain a Python package for the simulation and estimation of a prototypical finite-horizon dynamic discrete choice model based on Keane and Wolpin (1997).

GitHub OpenSourceEconomics/respy

Docs respy.readthedocs.org

• estimagic

We maintain a Python package that helps to estimate (structural) econometric models. estimagic provides a consistent interface to a broad set of global and local optimizers. An interactive browser-based dashboard allows to monitor complicated optimizations.

GitHub OpenSourceEconomics/estimagic

Docs estimagic.readthedocs.org

 $^{{\}rm *Corresponding\ author:\ Philipp\ Eisenhauer,\ peisenha@uni-bonn.de.}$

Throughout the course, we will make heavy use of Python and its SciPy ecosystem and Jupyter Notebooks. Basic knowledge of this toolchain is a prerequisite. There exist numerous introductory resources, and we provide a curated list at ose-resources.readthedocs.io. We will use zulip for all course communications. Please be sure to join our workspace at ose.zulipchat.com.

• Introduction

We provide a general introduction to computational modeling in economics and our Open-SourceEconomics initiative. We outline opportunities for students to get involved.

- OpenSourceEconomics (2020b). OSE website. http://opensourceeconomics.github.io

• Testing

We discuss different types of automated tests and how we can apply them to scientific software projects. After presenting the basics, we show some examples in estimagic and respy.

- Okken, B. (2017). Python testing with pytest: Simple, rapid, effective, and scalable.
 Pragmatic Bookshelf, Raleigh, NC
- Arbuckle, D. (2010). Python testing: Beginner's guide. Packt Publishing, Birmingham, United Kindgom

• Collaboration

We introduce continuous integration features of GitHub and discuss workflows for different team sizes.

- Chacon, S. and Straub, B. (2014). *Pro git.* Apress, New York, NY
- Blischak, J. D., Davenport, E. R., and Wilson, G. (2016). A quick introduction to version control with git and github. *PLoS Computational Biology*, 12(1)

• Numerical optimization

After a brief theoretical introduction to local and global optimization, students will solve straightforward optimization problems with scipy. We then discuss the limitations of scipy.optimize in typical econometric workflows and introduce the students to the powerful optimization tools of the estimagic package.

- Locatelli, M. and Schoen, F. (2013). Global optimization. SIAM, Philadelphia, PA
- Nocedal, J. and Wright, S. J. (2006). Numerical optimization. Springer, New York,
 NY
- Gabler, J. (2019). estimagic: A Python tool for the estimation of (structural) econometric models

• Numerical derivatives

After a brief introduction to numerical differentiation, we show how to calculate gradients, Jacobian, and Hessian matrices using estimagic.

- Brodtkorb, P. A. and D'Errico, J. (2019). numdifftools
- Ridout, M. S. (2009). Statistical applications of the complex-step method of numerical differentiation. The American Statistician, 63(1):66-74
- Gabler, J. (2019). estimagic: A Python tool for the estimation of (structural) econometric models

• Numerical integration

We first introduce the participants to quadrature, Monte-Carlo, and Quasi-Monte-Carlo methods and provide them with (over)simplified guidelines to choose between the different techniques. We then show the convergence speed of different approaches in a discrete choice dynamic programming model.

- Davis, P. J. and Rabinowitz, P. (2007). Methods of numerical integration. Dover Books on Mathmatics, Cambridge, MA
- Heiss, F. and Winschel, V. (2008). Likelihood approximation by numerical integration on sparse grids. *Journal of Econometrics*, 144(1):62–80
- Judd, K. L. and Skrainka, B. S. (2011). High performance quadrature rules: How numerical integration affects a popular model of product differentiation. CEMMAP Working Paper (CWP03/11)

Discrete choice dynamic programming models

We first outline the underlying economic, mathematical, and computational model. We then provide an overview of its applications in economics. Finally, we use **respy** to showcase the application of earlier lessons for numerical integration, parallelization strategies, version control, software testing, and continuous integration.

- OpenSourceEconomics (2020a). Eckstein-Keane-Wolpin models: An invitation for transdisciplinary collaboration. Handout, http://bit.ly/ekw-handout
- Keane, M. P., Todd, P. E., and Wolpin, K. I. (2011). The structural estimation of behavioral models: Discrete choice dynamic programming methods and applications.
 In Ashenfelter, O. and Card, D., editors, *Handbook of Labor Economics*, volume 4A, pages 331–461. Elsevier Science, Amsterdam, Netherlands
- OpenSourceEconomics (2020). respy: An open-source package for the simulation and estimation of a canonical model of human capital investment

• Execution speed

Execution speed Python is often called a slow language. Nevertheless, it is one of the most widely used languages for high-performance computing. We teach students how to make their Python code fast with numpy and numba and how to parallelize it using multiprocessing and joblib. After the students solve simple examples, we look at some implementations is respy.

- Gorelick, M. and Ozsvald, I. (2014). High performance Python. O'Reilly Media, Sebastopol, CA
- Lanaro, G. (2017). Python high performance. Packt Publishing, Birmingham, United Kingdom