

R Notebook

This is an R Markdown Notebook. When you execute code within the notebook, the results appear beneath the code.

What does Ljung box-statistic do; should they be significant or not? Should residuals look normal? Are the * in eacf mean its significant? What should ACF look like for stationarity?

```
library(TSA)
```

```
## Loading required package: leaps
## Loading required package: locfit
## locfit 1.5-9.1    2013-03-22
## Loading required package: mgcv
## Loading required package: nlme
## This is mgcv 1.8-22. For overview type 'help("mgcv-package")'.
## Loading required package: tseries
##
## Attaching package: 'TSA'
## The following objects are masked from 'package:stats':
##
##     acf, arima
## The following object is masked from 'package:utils':
##
##     tar
```

```
library(tseries)
library(astsa)
library(imputeTS)
```

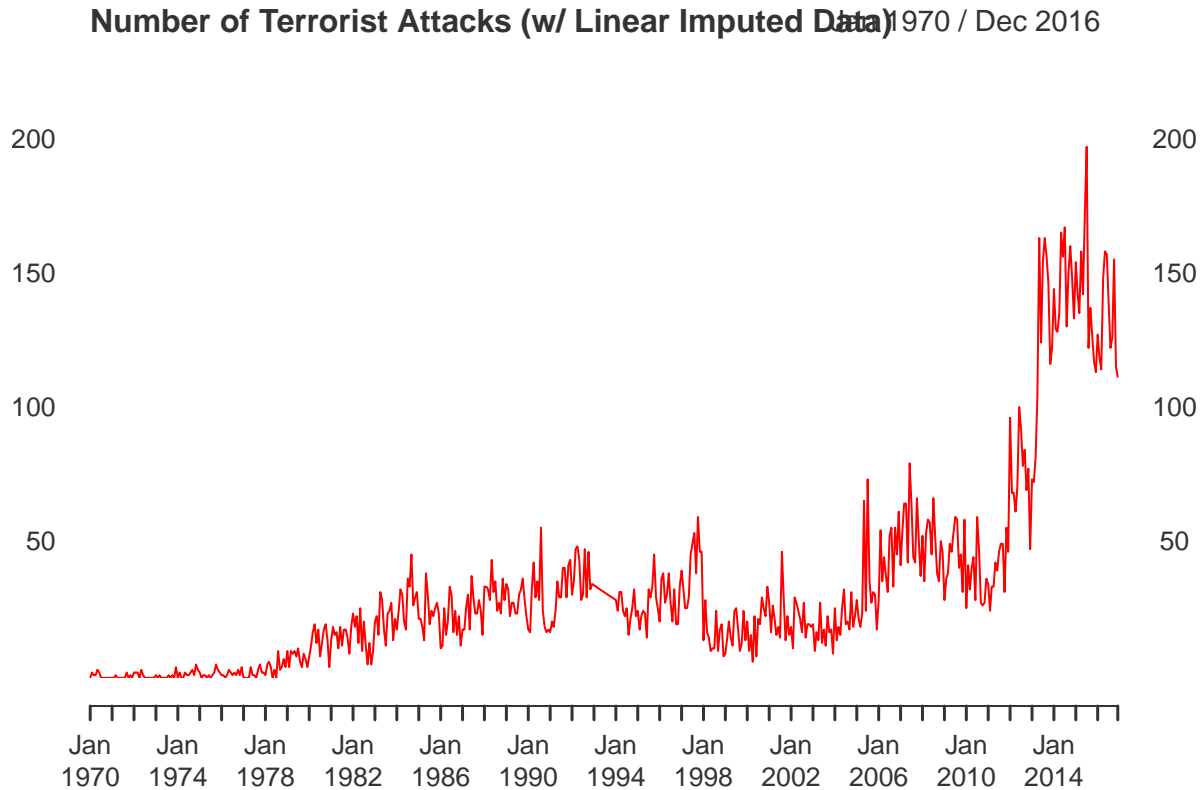
```
##
## Attaching package: 'imputeTS'
## The following object is masked from 'package:tseries':
##
##     na.remove
```

```
library(tsoutliers)
library(xts)
```

```
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following object is masked from 'package:imputeTS':
##
##     na.locf
## The following objects are masked from 'package:base':
##
##     as.Date, as.Date.numeric
```

Try executing this chunk by clicking the *Run* button within the chunk or by placing your cursor inside it and pressing *Cmd+Shift+Enter*.

```
terror2 <- read.csv("input/og_num_casualties_greater_than_10.csv")
terror3 <- na.interpolation(terror2$num.attacks.with.kill.thresh, option="linear")
plot(as.xts(ts(terror3, frequency = 12, start=1970)), main = "Number of Terrorist Attacks (w/ Linear Imputed Data) 1970 / Dec 2016")
```



```
pdf("image/og_ts.pdf")
lines(as.xts(ts(terror2$num.attacks.with.kill.thresh, frequency = 12, start=1970)), col="black")
dev.off()
```

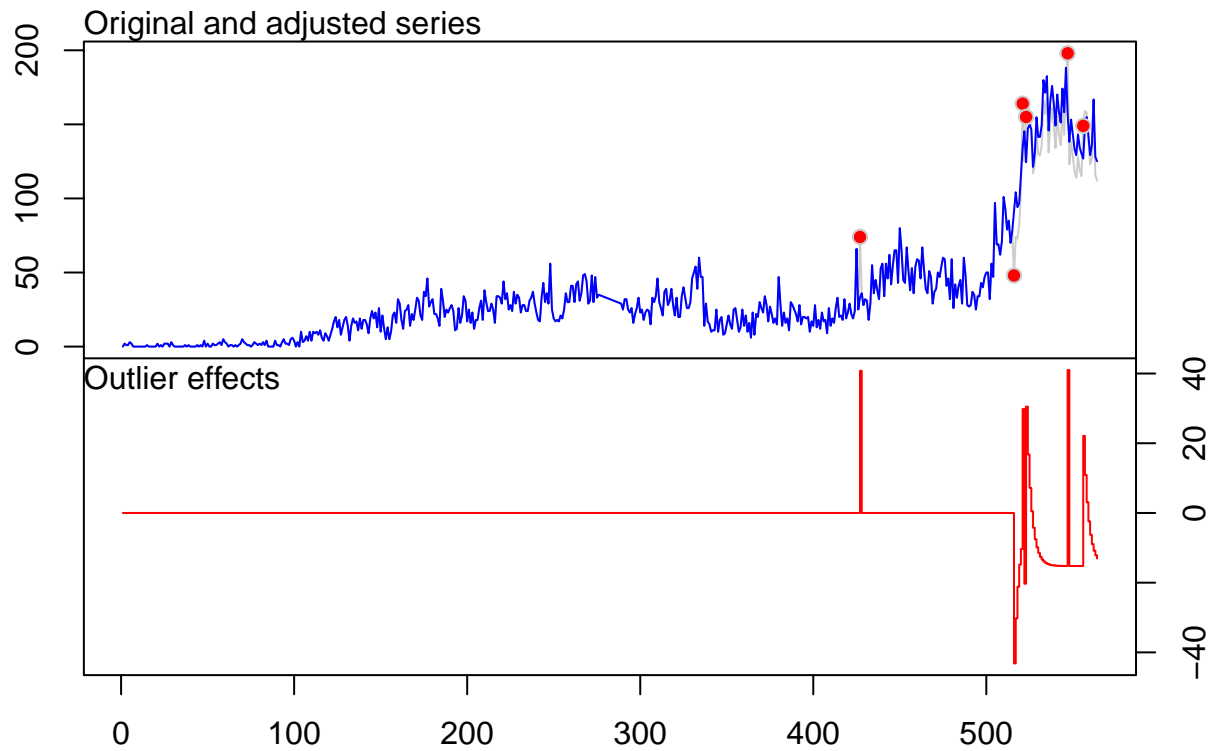
```
## pdf
## 2
```

```
#pdf("image/imputed_ts.pdf")
#plot(as.xts(ts(terror3, frequency = 12, start=1970)), main = "Number of Terrorist Attacks (w/ Linear Imputed Data) 1970 / Dec 2016")
#dev.off()
```

```
outlier_terror3 <- tso(ts(terror3), types = c("TC", "AO", "IO"))
```

```
## Warning in locate.outliers.oloop(y = y, fit = fit, types = types, cval =
## cval, : stopped when 'maxit.oloop = 4' was reached
```

```
plot(outlier_terror3)
```

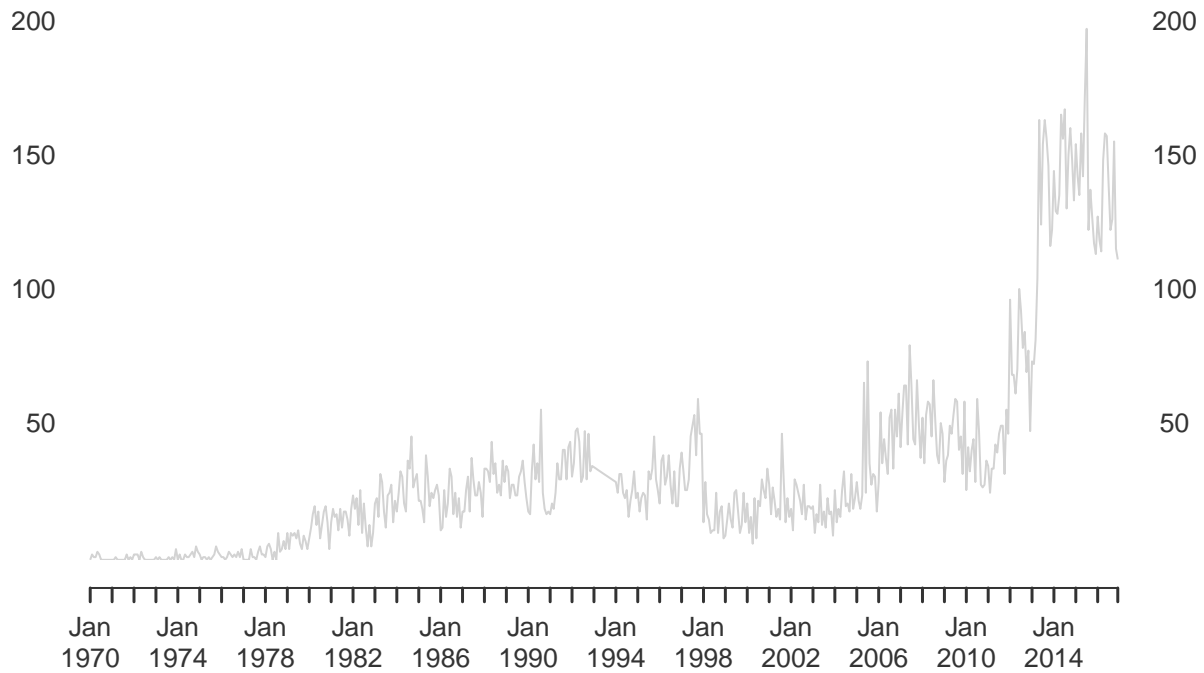


```
#plot outlier effects
pdf("image/outlier_effects.pdf")
plot(as.xts(ts(outlier_terror3$effects, frequency = 12, start=1970)), main = "Outlier Effects", major.f
dev.off()
```

```
## pdf
## 2
```

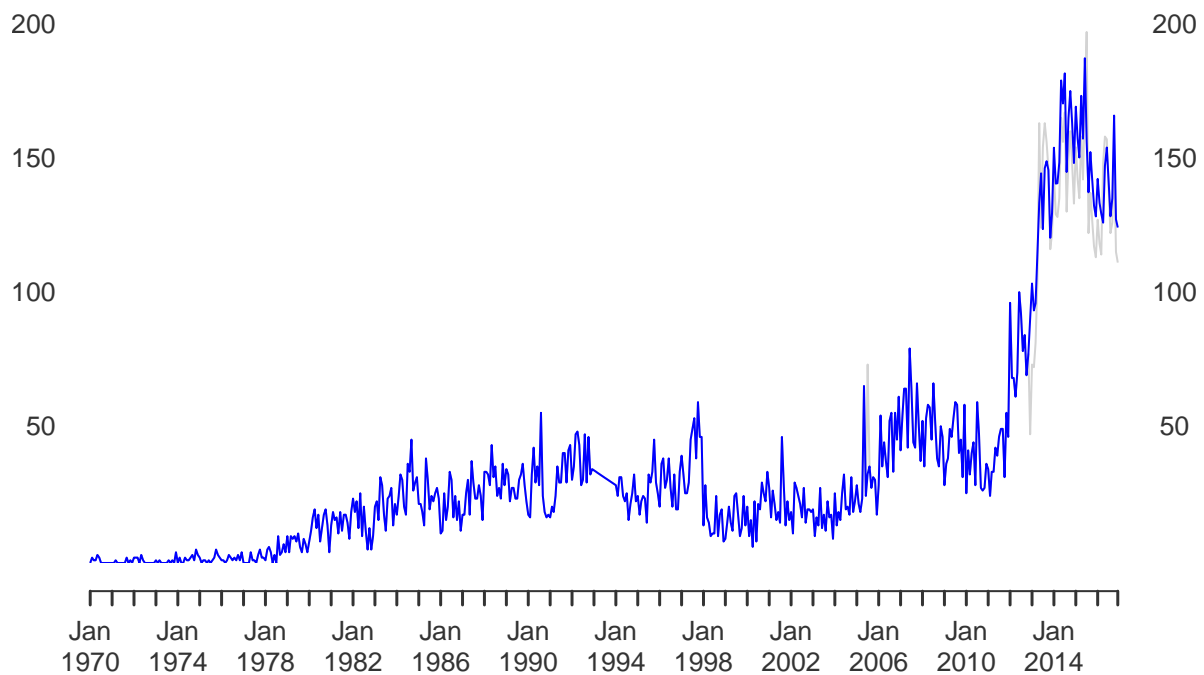
```
#Plot outlier time series
xts.terror3 <- as.xts(ts(terror3, frequency = 12, start=1970))
plot(as.xts(ts(terror3, frequency = 12, start=1970)), main = "Number of Terrorist Attacks (Outliers Rem
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



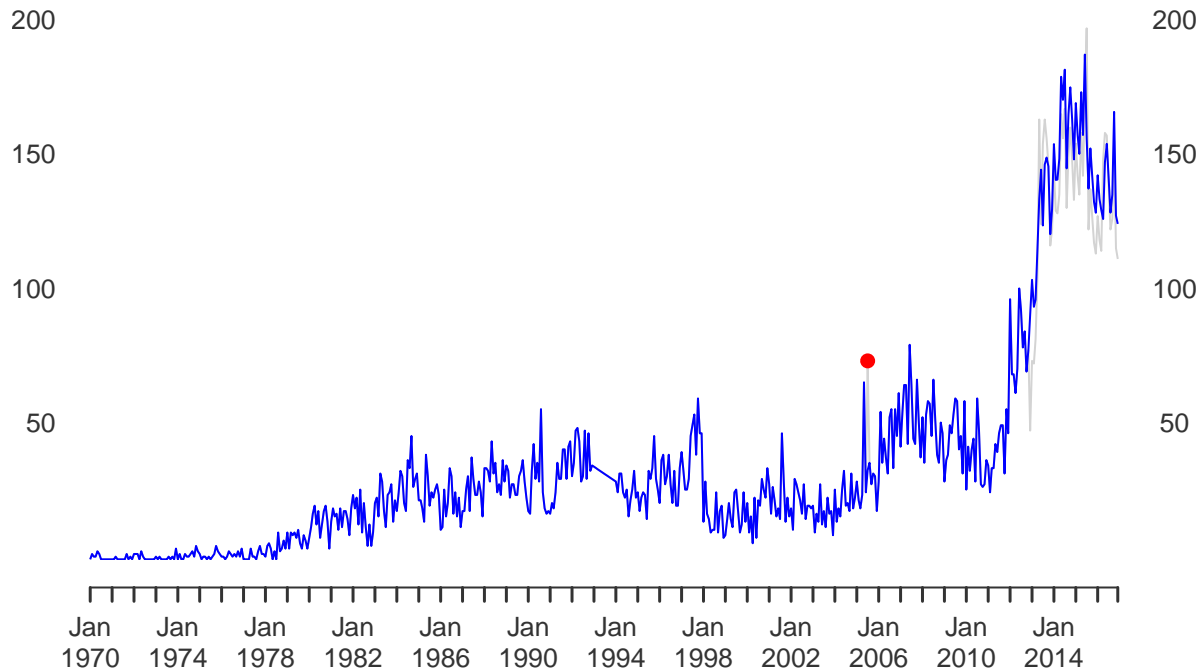
```
lines(as.xts(ts(outlier_terror3$yadj, frequency = 12, start=1970)), col="blue")
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



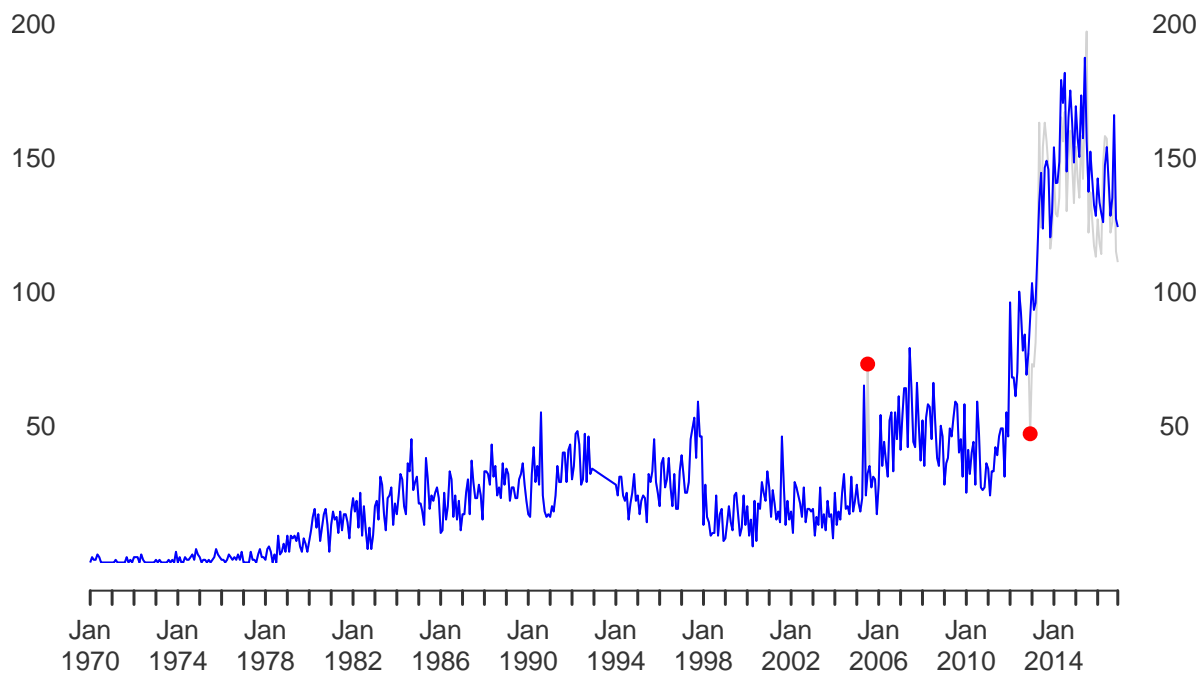
```
points(xts.terror3[427], col="red",pch=19, cex=1)
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



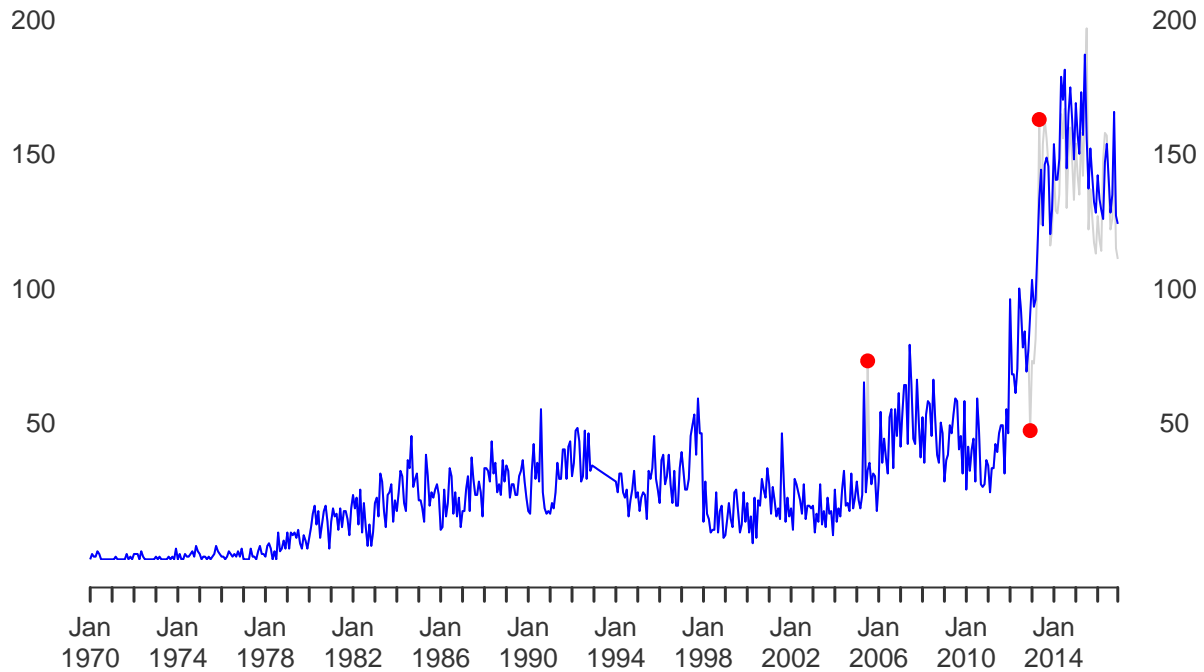
```
points(xts.terror3[516], col="red",pch=19, cex=1)
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



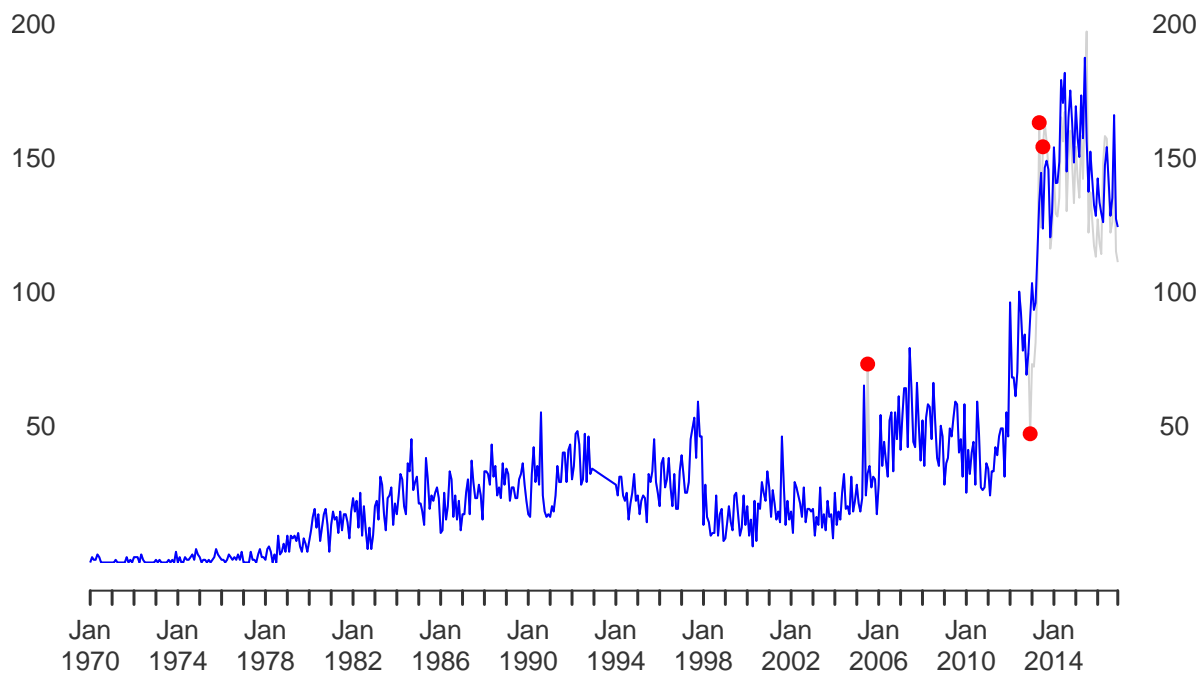
```
points(xts.terror3[521], col="red",pch=19, cex=1)
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



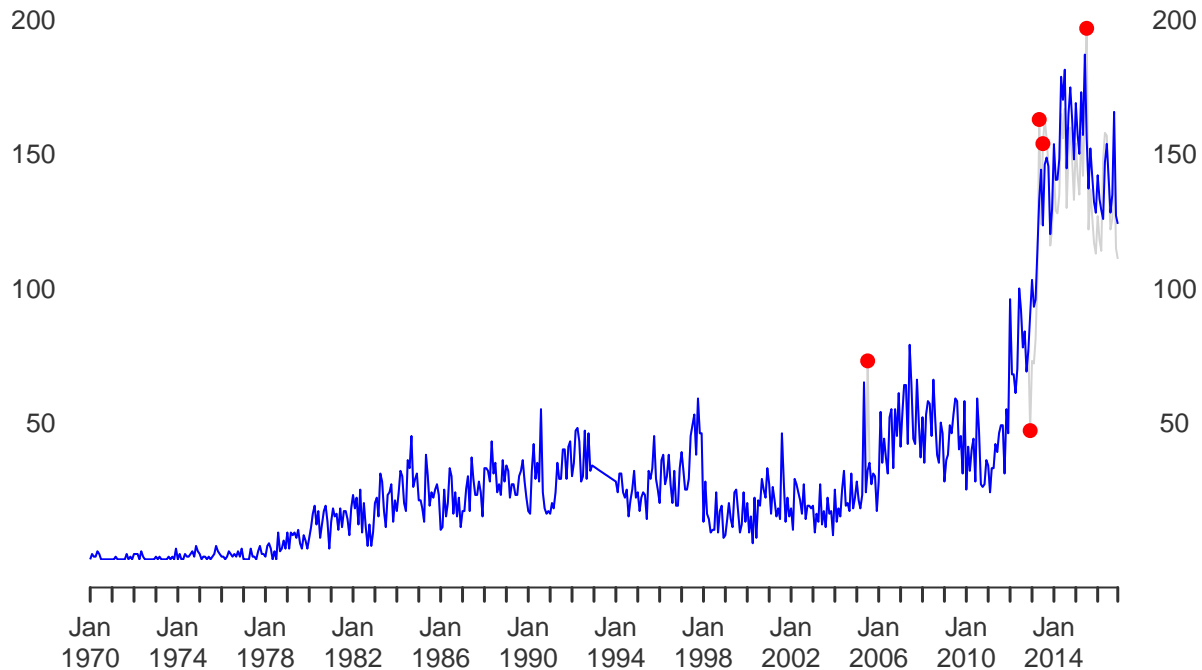
```
points(xts.terror3[523], col="red",pch=19, cex=1)
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



```
points(xts.terror3[547], col="red", pch=19, cex=1)
```

Number of Terrorist Attacks (Outliers Removed) Jan 1970 / Dec 2016



```
pdf("image/outlier_comparison.pdf")
points(xts.terror3[556], col="red", pch=19, cex=1)
dev.off()
```

```
## pdf
## 2
```

```
terror4 <- outlier_terror3$yadj
```

```
#terror3 <- na.kalman(terror2$num.attacks, model="auto.arima")
cutoff.index <- length(terror4) - 48 #floor(0.1 * length(terror3))
cutoff.index2 <- length(terror4) - 12
terror4.valid <- terror4[(cutoff.index+1) : cutoff.index2]
terror4.testing <- terror4[(cutoff.index2 + 1) : length(terror4)]
terror4 <- terror4[1: cutoff.index]
```

```
#plot(as.xts(ts(terror4, frequency = 12, start=1970)), main = "Number of Terrorist Attacks (Training Set)")
```

```
#plot(as.xts(ts(terror4.valid, frequency = 12, start=1970)), main = "Number of Terrorist Attacks (Valid Set)")
```

```
#log_terror4 <- log(outlier_terror3$yadj)
adf.test(terror4, k=1)
```

```
## Warning in adf.test(terror4, k = 1): p-value smaller than printed p-value
```

```
##
```

```
## Augmented Dickey-Fuller Test
```

```

##
## data:  terror4
## Dickey-Fuller = -5.8969, Lag order = 1, p-value = 0.01
## alternative hypothesis: stationary
adf.test(diff(terror4), k=1)

## Warning in adf.test(diff(terror4), k = 1): p-value smaller than printed p-
## value

##
## Augmented Dickey-Fuller Test
##
## data:  diff(terror4)
## Dickey-Fuller = -24.495, Lag order = 1, p-value = 0.01
## alternative hypothesis: stationary
adf.test(diff(diff(terror4)), k=1)

## Warning in adf.test(diff(diff(terror4)), k = 1): p-value smaller than
## printed p-value

##
## Augmented Dickey-Fuller Test
##
## data:  diff(diff(terror4))
## Dickey-Fuller = -32.125, Lag order = 1, p-value = 0.01
## alternative hypothesis: stationary
pdf("image/first_diff.pdf")
plot(as.xts(ts(diff(terror4), frequency = 12, start=1970)), main = "Number of Terrorist Attacks (First I
dev.off()

## pdf
## 2
pdf("image/second_diff.pdf")
plot(as.xts(ts(diff(diff(terror4)), frequency = 12, start=1970)), main = "Number of Terrorist Attacks (
dev.off()

## pdf
## 2
#ts.plot(diff(terror4))
#ts.plot(diff(diff(terror4)))

m = floor(sqrt(length(diff(terror4))))
pdf("image/raw_periodogram.pdf")
mvspec(diff(terror4), log="no", main="Raw Periodogram")
dev.off()

## pdf
## 2
pdf("image/smooth_tapered_periodogram.pdf")
mvspec(diff(terror4), kernel('daniell', m), log="no", taper=0.1, main="Smoothed and Tapered Periodogram
dev.off()

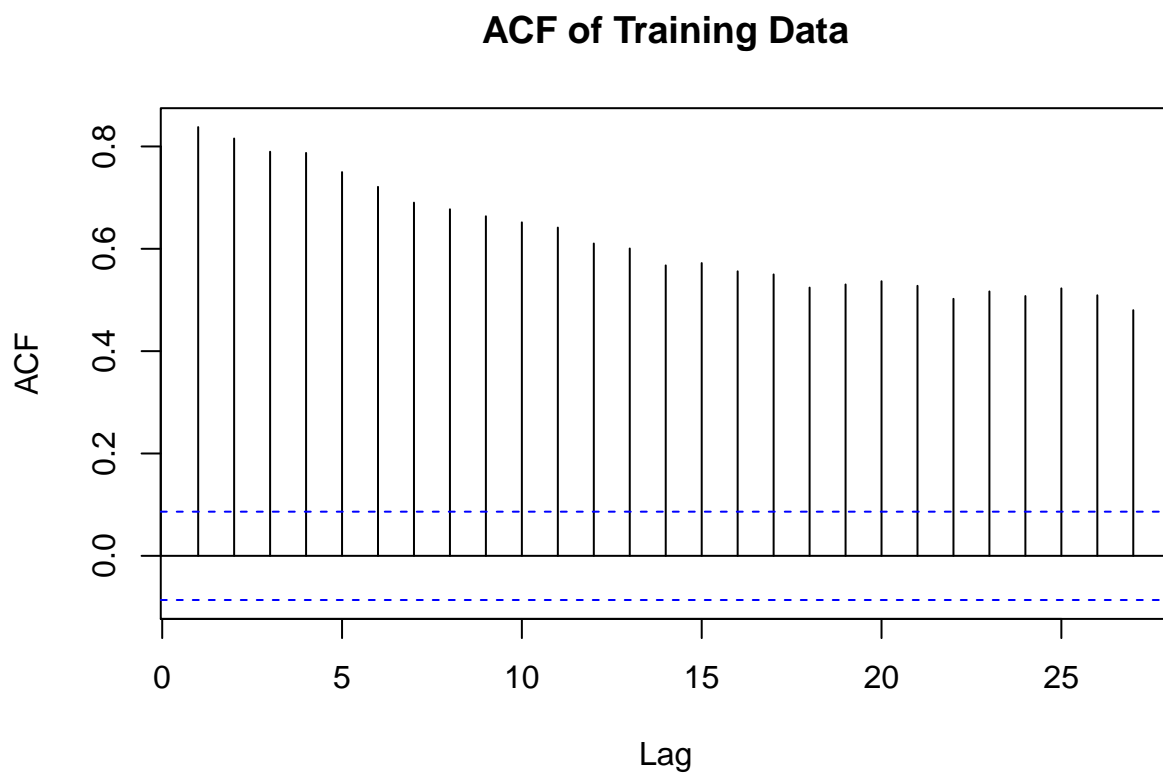
## pdf
## 2

```



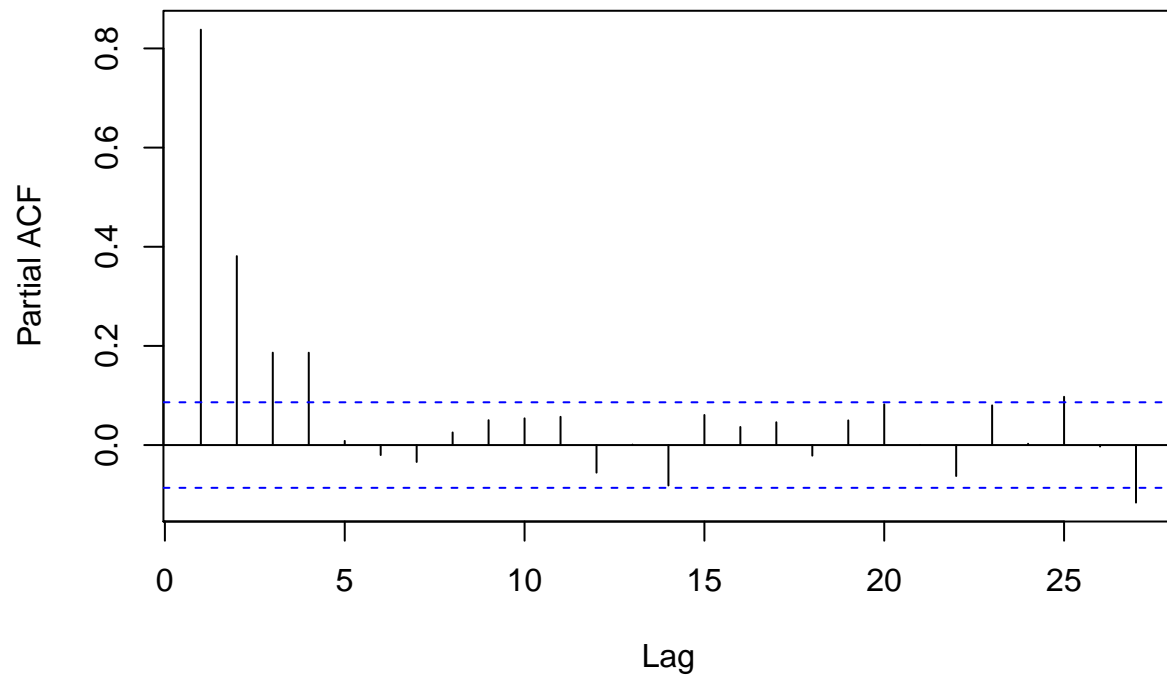
```
#mvspec(diff(log_terror4), kernel('daniell', m), log="no")
```

```
acf(terror4, main="ACF of Training Data")
```



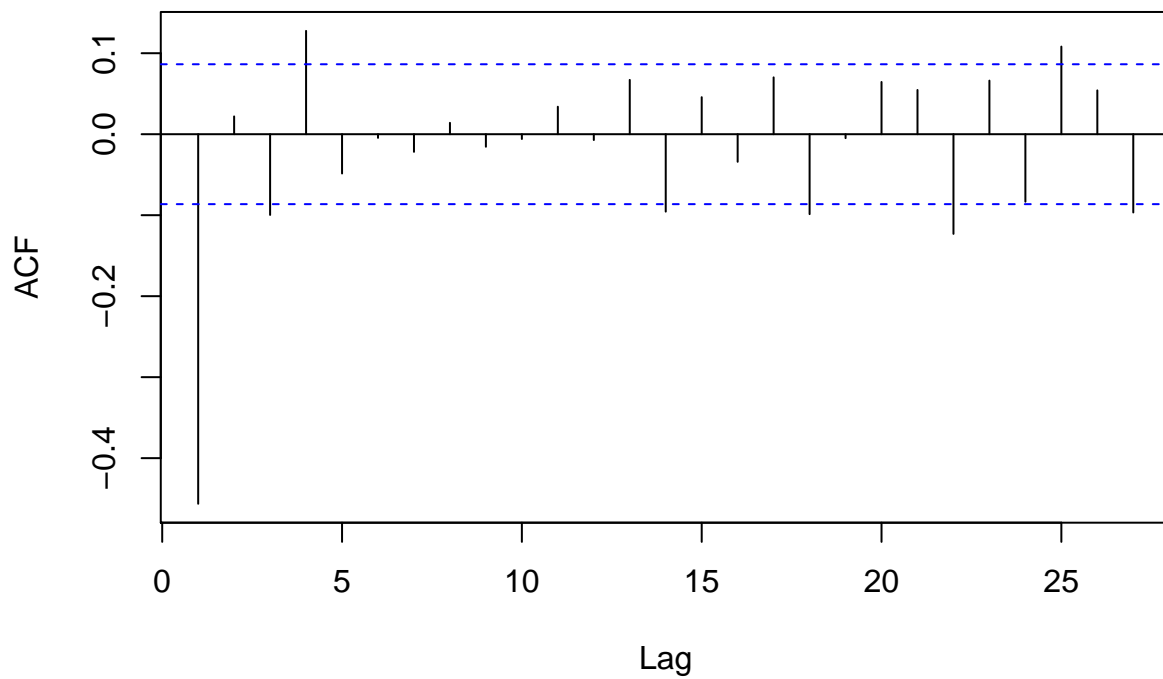
```
pacf(terror4, main="PACF of Training Data")
```

PACF of Training Data



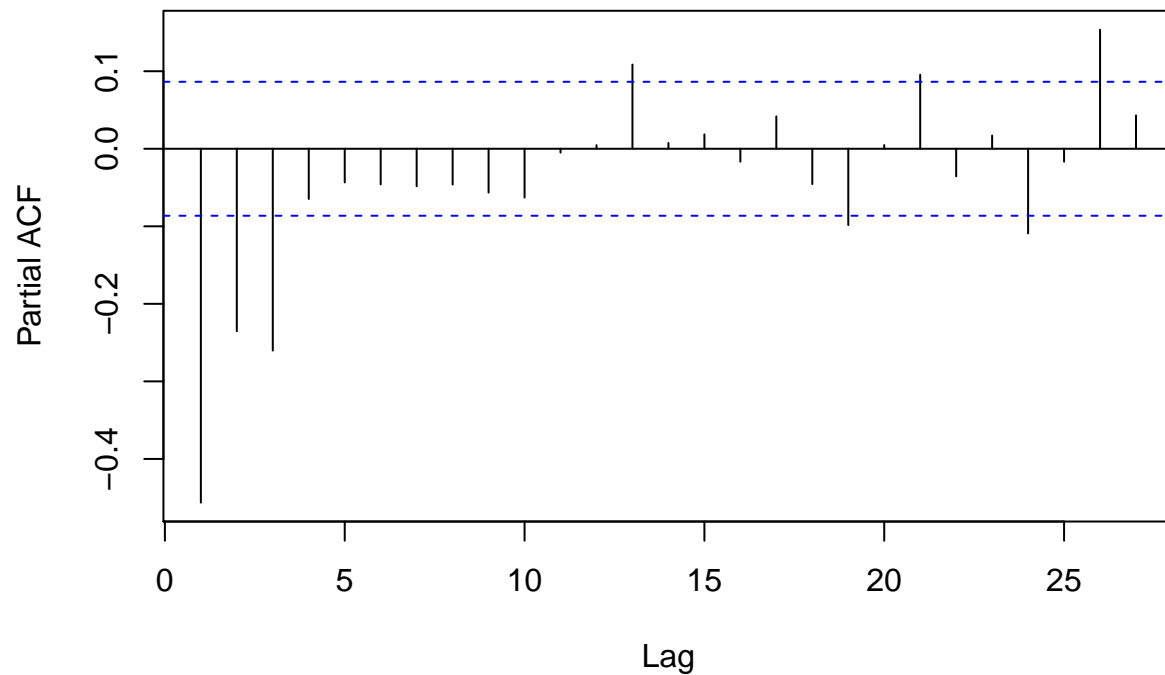
```
acf(diff(terror4), main="ACF of First Diff Training Data")
```

ACF of First Diff Training Data



```
pacf(diff(terror4), main="PACF of Second Diff Training Data")
```

PACF of Second Diff Training Data



```
eacf(diff(terror4))
```

```
## AR/MA
##   0 1 2 3 4 5 6 7 8 9 10 11 12 13
## 0 x o x x o o o o o o o o o x
## 1 x x o x o o o o o o o o o o
## 2 x x x x o o o o o o o o o o
## 3 x x x x o o o o o o o o o o
## 4 x o o o o o o o o o o o o o
## 5 x x o o o o o o o o o o o o
## 6 x x o o o o o o o o o o o o
## 7 x x o o o o o o o o o o o o
```

```
eacf(diff(diff(terror4)))
```

```
## AR/MA
##   0 1 2 3 4 5 6 7 8 9 10 11 12 13
## 0 x x x x o o o o o o o o o x
## 1 x x x x o o o o o o o o o o
## 2 x x x x o o o o o o o o o o
## 3 x o o o o o o o o o o o o o
## 4 x x o o o o o o o o o o o o
## 5 x x o o o o x o o o o o o o
## 6 x x x o o o o o o o o o o o
## 7 x x o o o o o o o o o o o o
```

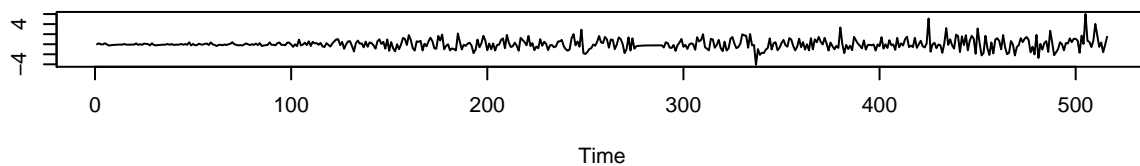
```
sarima(terror4, 0, 1, 1)
```

```
## initial value 2.302665
## iter 2 value 2.148680
## iter 3 value 2.132396
```

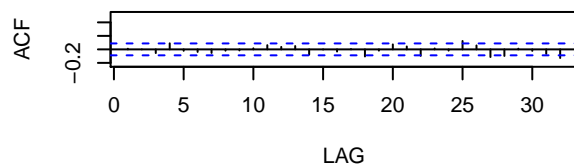
```
## iter 4 value 2.128997
## iter 5 value 2.121714
## iter 6 value 2.120506
## iter 7 value 2.120430
## iter 8 value 2.120364
## iter 9 value 2.120362
## iter 10 value 2.120362
## iter 10 value 2.120362
## iter 10 value 2.120362
## final value 2.120362
## converged
## initial value 2.120944
## iter 2 value 2.120943
## iter 3 value 2.120942
## iter 3 value 2.120942
## iter 3 value 2.120942
## final value 2.120942
## converged
```

Model: (0,1,1)

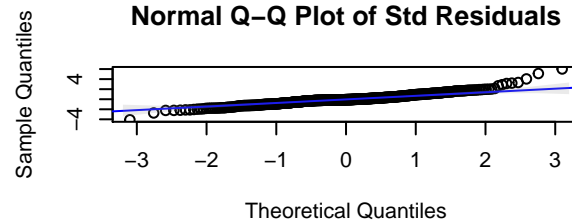
Standardized Residuals



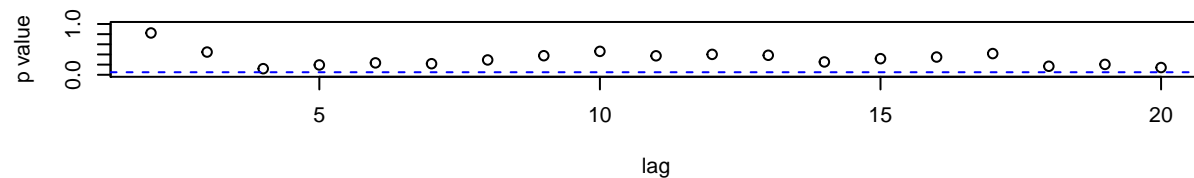
ACF of Residuals



Normal Q-Q Plot of Std Residuals



p values for Ljung-Box statistic



```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##     reltol = tol))
##
## Coefficients:
##          ma1  constant
##      -0.6746   0.1596
```

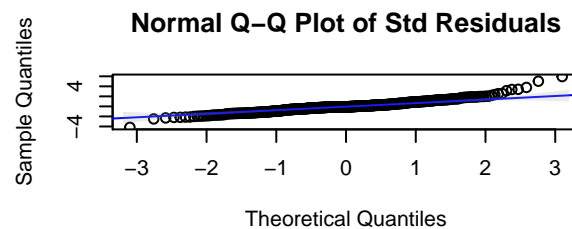
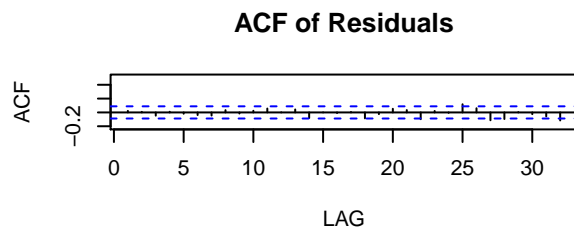
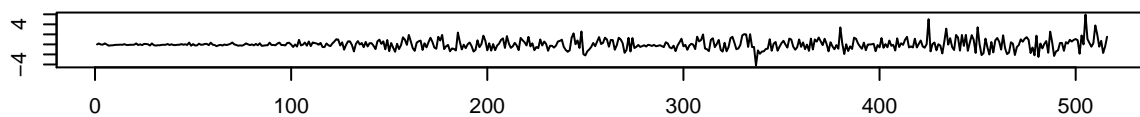
```
## s.e.    0.0336    0.1200
##
## sigma^2 estimated as 69.46:  log likelihood = -1823.04,  aic = 3652.08
##
## $degrees_of_freedom
## [1] 513
##
## $ttable
##          Estimate      SE  t.value p.value
## ma1         -0.6746 0.0336 -20.0780 0.0000
## constant     0.1596 0.1200   1.3306 0.1839
##
## $AIC
## [1] 5.248457
##
## $AICc
## [1] 5.252424
##
## $BIC
## [1] 4.264915
```

```
sarima(terror4, 0, 1, 1, 1, 0, 1, 4)
```

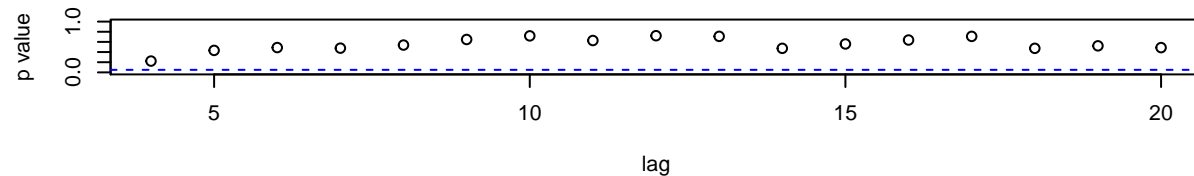
```
## initial  value 2.306485
## iter    2 value 2.160550
## iter    3 value 2.137688
## iter    4 value 2.128502
## iter    5 value 2.123569
## iter    6 value 2.120401
## iter    7 value 2.119951
## iter    8 value 2.119925
## iter    9 value 2.119914
## iter   10 value 2.119906
## iter   11 value 2.119902
## iter   12 value 2.119881
## iter   13 value 2.119531
## iter   14 value 2.119158
## iter   15 value 2.118895
## iter   16 value 2.118789
## iter   17 value 2.118773
## iter   18 value 2.118748
## iter   19 value 2.118211
## iter   20 value 2.116368
## iter   21 value 2.115097
## iter   22 value 2.114878
## iter   23 value 2.114721
## iter   24 value 2.114670
## iter   25 value 2.114631
## iter   26 value 2.114584
## iter   27 value 2.114555
## iter   28 value 2.114550
## iter   29 value 2.114550
## iter   29 value 2.114550
## final   value 2.114550
## converged
```

```
## initial value 2.111537
## iter 2 value 2.111531
## iter 3 value 2.111529
## iter 4 value 2.111529
## iter 5 value 2.111529
## iter 6 value 2.111529
## iter 7 value 2.111528
## iter 8 value 2.111528
## iter 9 value 2.111528
## iter 9 value 2.111528
## iter 9 value 2.111528
## final value 2.111528
## converged
```

Model: (0,1,1) (1,0,1) [4] Standardized Residuals



p values for Ljung-Box statistic



```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##     reltol = tol))
##
## Coefficients:
##          ma1          sar1          sma1    constant
##        -0.6863    -0.7178     0.8165     0.1595
## s.e.    0.0346     0.0962    0.0774     0.1212
##
## sigma^2 estimated as 68.13:  log likelihood = -1818.19,  aic = 3646.38
##
## $degrees_of_freedom
```

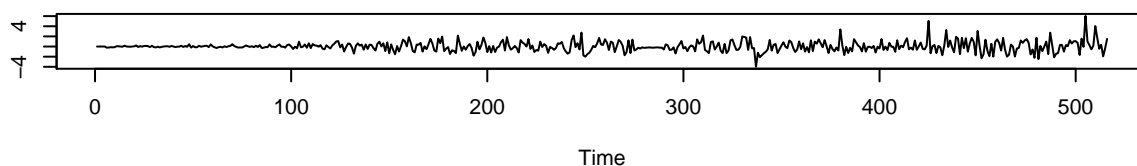
```
## [1] 511
##
## $ttable
##      Estimate      SE  t.value p.value
## ma1      -0.6863 0.0346 -19.8500 0.0000
## sar1      -0.7178 0.0962  -7.4641 0.0000
## sma1       0.8165 0.0774  10.5431 0.0000
## constant   0.1595 0.1212   1.3163 0.1887
##
## $AIC
## [1] 5.236941
##
## $AICc
## [1] 5.241045
##
## $BIC
## [1] 4.269857
```

```
sarima(terror4, 0, 1, 1, 1, 1, 1, 4)
```

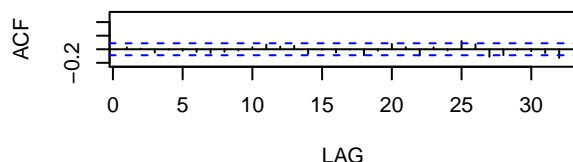
```
## initial  value 2.585951
## iter    2 value 2.295422
## iter    3 value 2.231925
## iter    4 value 2.195223
## iter    5 value 2.174548
## iter    6 value 2.150154
## iter    7 value 2.141586
## iter    8 value 2.141306
## iter    9 value 2.141144
## iter   10 value 2.141058
## iter   11 value 2.141057
## iter   11 value 2.141057
## iter   11 value 2.141057
## final   value 2.141057
## converged
## initial  value 2.141567
## iter    2 value 2.139146
## iter    3 value 2.138306
## iter    4 value 2.138235
## iter    5 value 2.138226
## iter    5 value 2.138226
## iter    5 value 2.138226
## final   value 2.138226
## converged
```

Model: (0,1,1) (1,1,1) [4]

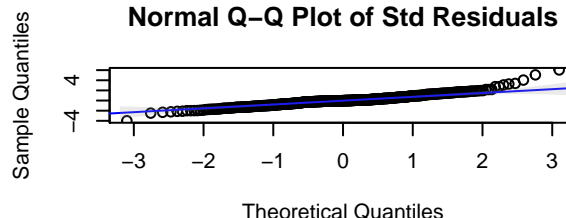
Standardized Residuals



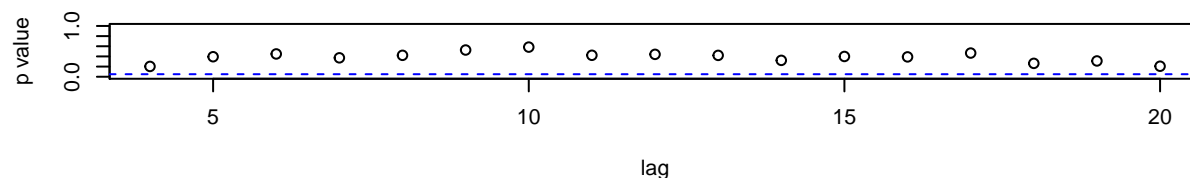
ACF of Residuals



Normal Q-Q Plot of Std Residuals



p values for Ljung-Box statistic



```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##     REPORT = 1, reltol = tol))
##
## Coefficients:
##          ma1      sar1      sma1
##      -0.6846  0.0988  -1.0000
## s.e.   0.0362  0.0450  0.0171
##
## sigma^2 estimated as 69.26:  log likelihood = -1817.71,  aic = 3643.42
##
## $degrees_of_freedom
## [1] 508
##
## $ttable
##      Estimate      SE  t.value p.value
## ma1   -0.6846 0.0362 -18.8959  0.0000
## sar1    0.0988 0.0450   2.1935  0.0287
## sma1   -1.0000 0.0171 -58.6006  0.0000
##
## $AIC
## [1] 5.249478
##
## $AICc
## [1] 5.253506
```

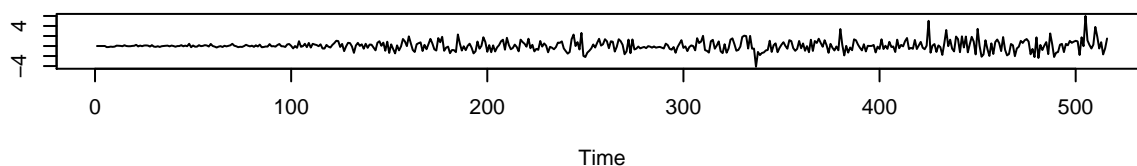


```
##  
## $BIC  
## [1] 4.274165  
sarima(terror4, 0, 1, 1, 1, 1, 2, 4)
```

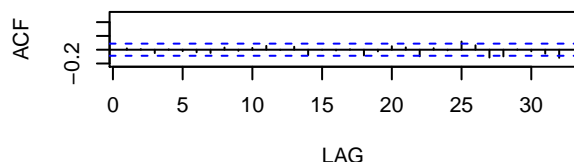
```
## initial value 2.585951  
## iter 2 value 2.271150  
## iter 3 value 2.221817  
## iter 4 value 2.190039  
## iter 5 value 2.158348  
## iter 6 value 2.137558  
## iter 7 value 2.136854  
## iter 8 value 2.134312  
## iter 9 value 2.132861  
## iter 10 value 2.132729  
## iter 11 value 2.132550  
## iter 12 value 2.130744  
## iter 13 value 2.127256  
## iter 14 value 2.126990  
## iter 15 value 2.126819  
## iter 16 value 2.126642  
## iter 17 value 2.125945  
## iter 18 value 2.125863  
## iter 19 value 2.125557  
## iter 20 value 2.125495  
## iter 21 value 2.125487  
## iter 22 value 2.125487  
## iter 22 value 2.125487  
## final value 2.125487  
## converged  
## initial value 2.133766  
## iter 2 value 2.133364  
## iter 3 value 2.133341  
## iter 4 value 2.133331  
## iter 5 value 2.133324  
## iter 6 value 2.133285  
## iter 7 value 2.133273  
## iter 8 value 2.133272  
## iter 8 value 2.133272  
## iter 8 value 2.133272  
## final value 2.133272  
## converged
```

Model: (0,1,1) (1,1,2) [4]

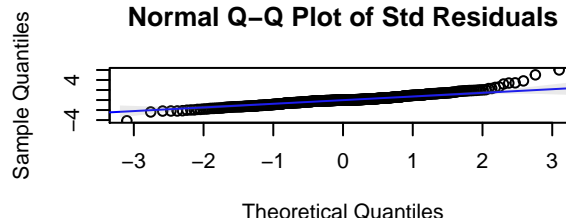
Standardized Residuals



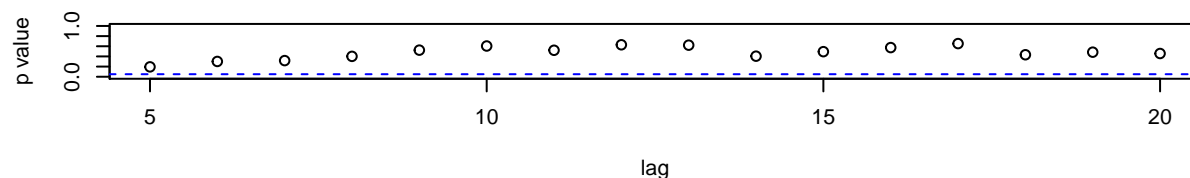
ACF of Residuals



Normal Q-Q Plot of Std Residuals



p values for Ljung-Box statistic

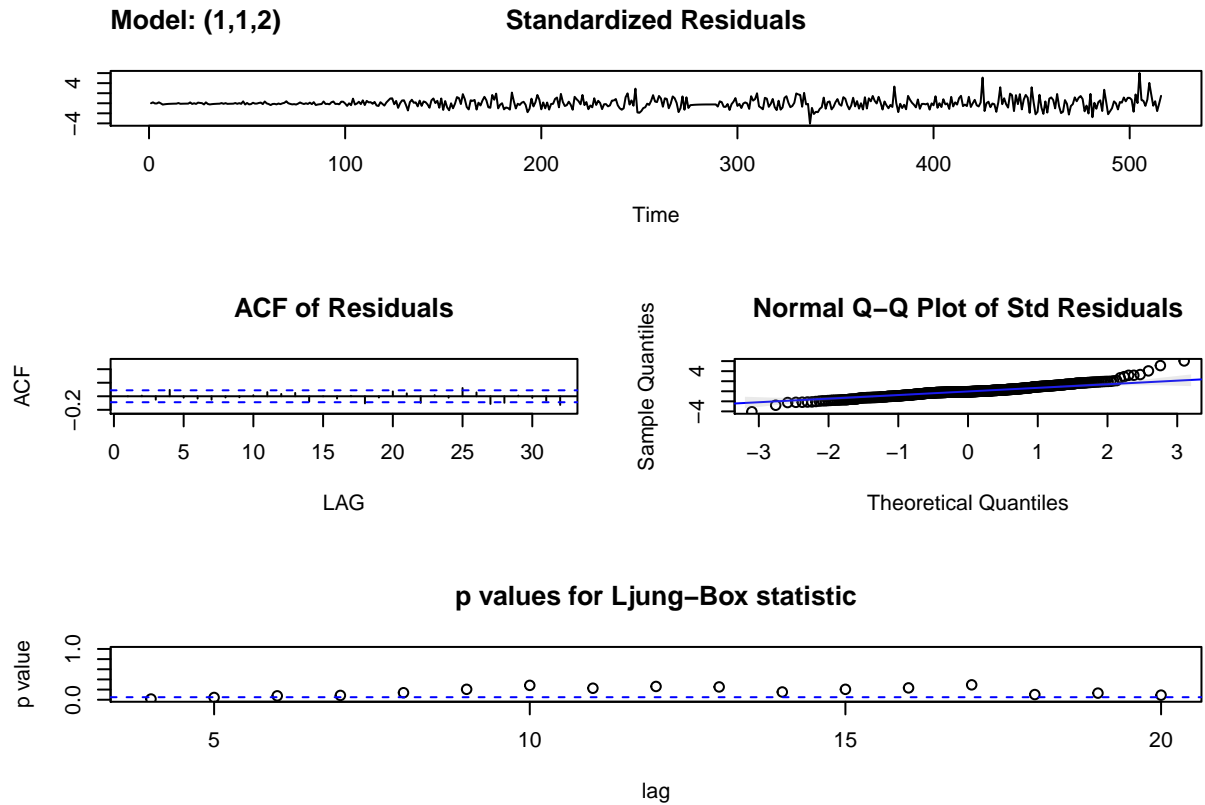


```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##     REPORT = 1, reltol = tol))
##
## Coefficients:
##      ma1      sar1      sma1      sma2
##    -0.6840 -0.7141 -0.1856 -0.8144
## s.e.   0.0348   0.0974   0.0807   0.0800
##
## sigma^2 estimated as 68.5:  log likelihood = -1815.18,  aic = 3640.36
##
## $degrees_of_freedom
## [1] 507
##
## $ttable
##      Estimate      SE  t.value p.value
## ma1   -0.6840 0.0348 -19.6474 0.0000
## sar1  -0.7141 0.0974  -7.3348 0.0000
## sma1  -0.1856 0.0807  -2.2985 0.0219
## sma2  -0.8144 0.0800 -10.1848 0.0000
##
## $AIC
## [1] 5.242331
##
## $AICc
```

```
## [1] 5.246435
##
## $BIC
## [1] 4.275247
```

```
sarima(terror4, 1, 1, 2)
```

```
## initial value 2.303604
## iter 2 value 2.181765
## iter 3 value 2.126083
## iter 4 value 2.122470
## iter 5 value 2.121316
## iter 6 value 2.121288
## iter 7 value 2.121288
## iter 8 value 2.121288
## iter 9 value 2.121288
## iter 10 value 2.121287
## iter 11 value 2.121287
## iter 12 value 2.121287
## iter 13 value 2.121287
## iter 14 value 2.121286
## iter 15 value 2.121285
## iter 16 value 2.121281
## iter 17 value 2.121269
## iter 18 value 2.121254
## iter 19 value 2.121225
## iter 20 value 2.121201
## iter 21 value 2.121196
## iter 22 value 2.121196
## iter 23 value 2.121196
## iter 23 value 2.121196
## iter 23 value 2.121196
## final value 2.121196
## converged
## initial value 2.120809
## iter 2 value 2.120807
## iter 3 value 2.120807
## iter 3 value 2.120807
## iter 3 value 2.120807
## final value 2.120807
## converged
```



```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##     reltol = tol))
##
## Coefficients:
##          ar1      ma1      ma2  constant
##          0.0064 -0.6701 -0.0121   0.1591
## s.e.  1.0042   0.9926   0.6599   0.1179
##
## sigma^2 estimated as 69.44:  log likelihood = -1822.97,  aic = 3655.94
##
## $degrees_of_freedom
## [1] 511
##
## $ttable
##      Estimate      SE t.value p.value
## ar1      0.0064 1.0042  0.0064  0.9949
## ma1     -0.6701 0.9926 -0.6751  0.4999
## ma2     -0.0121 0.6599 -0.0184  0.9854
## constant  0.1591 0.1179  1.3492  0.1779
##
## $AIC
## [1] 5.255937
##
## $AICc
```

```
## [1] 5.260041
##
## $BIC
## [1] 4.288853
```

```
sarima(terror4, 1, 1, 2, 1, 0, 1, 4)
```

```
## initial  value 2.307451
## iter    2 value 2.204058
## iter    3 value 2.126118
## iter    4 value 2.123944
## iter    5 value 2.120684
## iter    6 value 2.120475
## iter    7 value 2.120374
## iter    8 value 2.120367
## iter    9 value 2.120339
## iter   10 value 2.120273
## iter   11 value 2.120113
## iter   12 value 2.119505
## iter   13 value 2.118322
## iter   14 value 2.118280
## iter   15 value 2.115656
## iter   16 value 2.115558
## iter   17 value 2.115420
## iter   18 value 2.115254
## iter   19 value 2.114946
## iter   20 value 2.114892
## iter   21 value 2.114761
## iter   22 value 2.114757
## iter   23 value 2.114756
## iter   24 value 2.114754
## iter   25 value 2.114741
## iter   26 value 2.114716
## iter   27 value 2.114657
## iter   28 value 2.114614
## iter   29 value 2.114611
## iter   30 value 2.114610
## iter   31 value 2.114600
## iter   32 value 2.114598
## iter   33 value 2.114597
## iter   34 value 2.114595
## iter   35 value 2.114592
## iter   36 value 2.114591
## iter   37 value 2.114590
## iter   38 value 2.114587
## iter   39 value 2.114580
## iter   40 value 2.114564
## iter   41 value 2.114560
## iter   42 value 2.114558
## iter   43 value 2.114552
## iter   44 value 2.114547
## iter   45 value 2.114540
## iter   46 value 2.114539
## iter   47 value 2.114538
## iter   48 value 2.114537
```

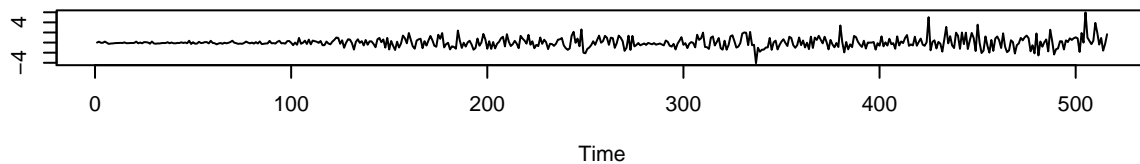
```

## iter 49 value 2.114534
## iter 50 value 2.114527
## iter 51 value 2.114514
## iter 52 value 2.114499
## iter 53 value 2.114490
## iter 54 value 2.114490
## iter 55 value 2.114490
## iter 56 value 2.114490
## iter 57 value 2.114489
## iter 58 value 2.114489
## iter 59 value 2.114489
## iter 59 value 2.114489
## iter 59 value 2.114489
## final value 2.114489
## converged
## initial value 2.110481
## iter 2 value 2.110475
## iter 3 value 2.110474
## iter 4 value 2.110473
## iter 4 value 2.110473
## iter 4 value 2.110473
## final value 2.110473
## converged

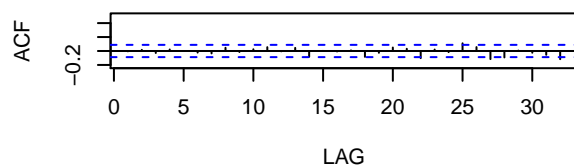
```

Model: (1,1,2) (1,0,1) [4]

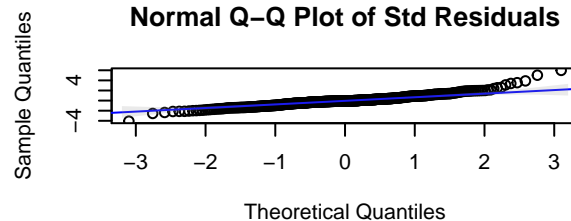
Standardized Residuals



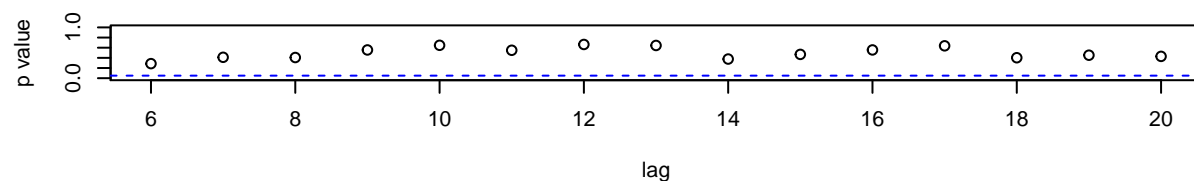
ACF of Residuals



Normal Q-Q Plot of Std Residuals



p values for Ljung-Box statistic



```

## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##      Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,

```

```

##      reltol = tol))
##
## Coefficients:
##          ar1          ma1          ma2          sar1          sma1      constant
##          0.5048      -1.1655      0.3073      -0.7013      0.8088          0.1580
## s.e.    0.5414      0.5504      0.3871      0.1014      0.0808          0.1112
##
## sigma^2 estimated as 67.99:  log likelihood = -1817.65,  aic = 3649.29
##
## $degrees_of_freedom
## [1] 509
##
## $ttable
##      Estimate      SE t.value p.value
## ar1          0.5048 0.5414  0.9324 0.3516
## ma1         -1.1655 0.5504 -2.1175 0.0347
## ma2          0.3073 0.3871  0.7938 0.4277
## sar1         -0.7013 0.1014 -6.9171 0.0000
## sma1          0.8088 0.0808 10.0109 0.0000
## constant     0.1580 0.1112  1.4203 0.1561
##
## $AIC
## [1] 5.242543
##
## $AICc
## [1] 5.246847
##
## $BIC
## [1] 4.291917
sarima(terror4, 1, 1, 2, 1, 1, 1, 4)

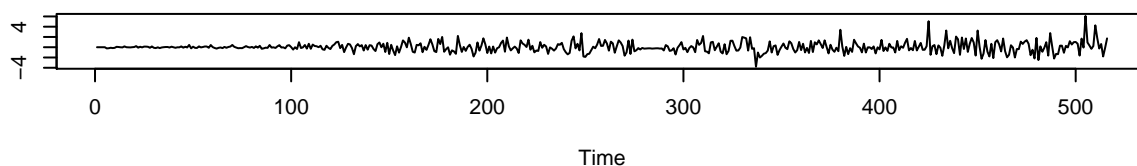
## initial  value 2.586933
## iter    2 value 2.313608
## iter    3 value 2.236307
## iter    4 value 2.190222
## iter    5 value 2.170202
## iter    6 value 2.160653
## iter    7 value 2.153824
## iter    8 value 2.143005
## iter    9 value 2.140794
## iter   10 value 2.139309
## iter   11 value 2.138297
## iter   12 value 2.138283
## iter   13 value 2.138256
## iter   14 value 2.138239
## iter   15 value 2.138099
## iter   16 value 2.137745
## iter   17 value 2.136357
## iter   18 value 2.135551
## iter   19 value 2.132692
## iter   20 value 2.131687
## iter   21 value 2.130851
## iter   22 value 2.130426
## iter   23 value 2.129721

```

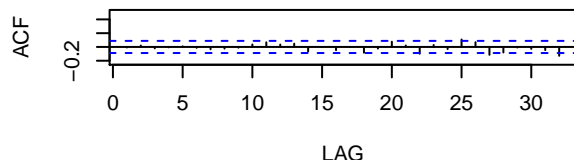
```
## iter 24 value 2.129017
## iter 25 value 2.128149
## iter 26 value 2.128113
## iter 27 value 2.127993
## iter 28 value 2.126274
## iter 29 value 2.125847
## iter 30 value 2.125462
## iter 31 value 2.125163
## iter 32 value 2.125044
## iter 33 value 2.125028
## iter 34 value 2.125024
## iter 35 value 2.125024
## iter 35 value 2.125024
## iter 35 value 2.125024
## final value 2.125024
## converged
## initial value 2.136116
## iter 2 value 2.136070
## iter 3 value 2.135997
## iter 4 value 2.135991
## iter 5 value 2.135989
## iter 6 value 2.135989
## iter 7 value 2.135988
## iter 8 value 2.135987
## iter 9 value 2.135985
## iter 10 value 2.135983
## iter 11 value 2.135980
## iter 12 value 2.135978
## iter 13 value 2.135978
## iter 14 value 2.135978
## iter 14 value 2.135978
## iter 14 value 2.135978
## final value 2.135978
## converged
```


Model: (1,1,2) (1,1,1) [4]

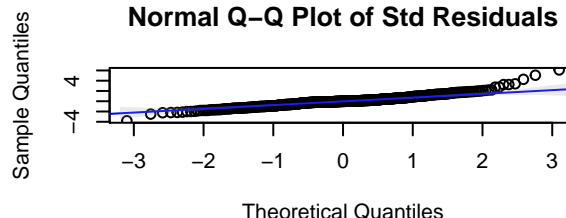
Standardized Residuals



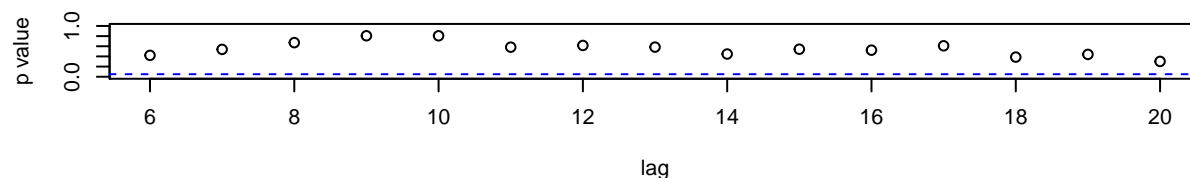
ACF of Residuals



Normal Q-Q Plot of Std Residuals



p values for Ljung-Box statistic



```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##     REPORT = 1, reltol = tol))
##
## Coefficients:
##          ar1      ma1      ma2      sar1      sma1
##          0.6052 -1.2584  0.3610  0.1332 -1.0000
## s.e.    0.3307   0.3418  0.2472  0.0504   0.0176
##
## sigma^2 estimated as 68.92:  log likelihood = -1816.56,  aic = 3645.12
##
## $degrees_of_freedom
## [1] 506
##
## $ttable
##      Estimate      SE  t.value p.value
## ar1    0.6052 0.3307   1.8302  0.0678
## ma1   -1.2584 0.3418  -3.6817  0.0003
## ma2    0.3610 0.2472   1.4603  0.1448
## sar1    0.1332 0.0504   2.6446  0.0084
## sma1   -1.0000 0.0176 -56.8115  0.0000
##
## $AIC
## [1] 5.252384
##
```

```
## $AICc
## [1] 5.25658
##
## $BIC
## [1] 4.293529
```

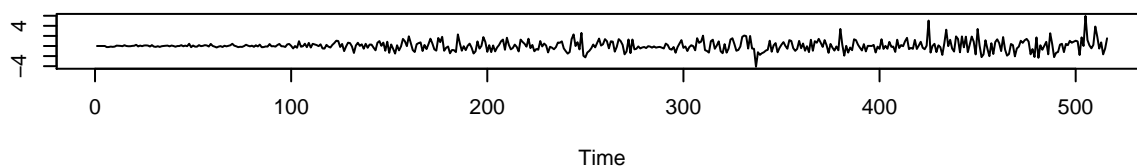
```
sarima(terror4, 1, 1, 2, 1, 1, 2, 4)
```

```
## initial value 2.586933
## iter 2 value 2.289532
## iter 3 value 2.271176
## iter 4 value 2.230852
## iter 5 value 2.225996
## iter 6 value 2.209651
## iter 7 value 2.204810
## iter 8 value 2.190472
## iter 9 value 2.184118
## iter 10 value 2.178785
## iter 11 value 2.176119
## iter 12 value 2.172137
## iter 13 value 2.166308
## iter 14 value 2.164234
## iter 15 value 2.141397
## iter 16 value 2.133893
## iter 17 value 2.129958
## iter 18 value 2.129081
## iter 19 value 2.128562
## iter 20 value 2.128395
## iter 21 value 2.128087
## iter 22 value 2.127913
## iter 23 value 2.127812
## iter 24 value 2.127776
## iter 25 value 2.127771
## iter 26 value 2.127770
## iter 27 value 2.127768
## iter 28 value 2.127764
## iter 29 value 2.127755
## iter 30 value 2.127752
## iter 31 value 2.127750
## iter 32 value 2.127748
## iter 33 value 2.127746
## iter 34 value 2.127741
## iter 35 value 2.127737
## iter 36 value 2.127735
## iter 37 value 2.127733
## iter 38 value 2.127726
## iter 39 value 2.127708
## iter 40 value 2.127662
## iter 41 value 2.127488
## iter 42 value 2.127435
## iter 43 value 2.127375
## iter 44 value 2.127362
## iter 45 value 2.127347
## iter 46 value 2.127333
## iter 47 value 2.127317
```

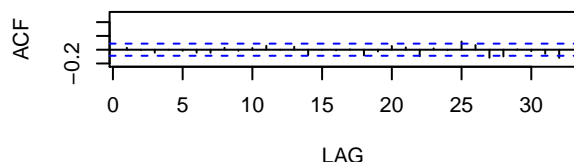
```
## iter 48 value 2.127314
## iter 49 value 2.127312
## iter 50 value 2.127307
## iter 51 value 2.127296
## iter 52 value 2.127264
## iter 53 value 2.127228
## iter 54 value 2.127190
## iter 55 value 2.127175
## iter 56 value 2.127173
## iter 57 value 2.127169
## iter 58 value 2.127152
## iter 59 value 2.127148
## iter 60 value 2.127139
## iter 61 value 2.127132
## iter 62 value 2.127131
## iter 63 value 2.127131
## iter 64 value 2.127129
## iter 65 value 2.127127
## iter 66 value 2.127123
## iter 67 value 2.127121
## iter 68 value 2.127121
## iter 69 value 2.127121
## iter 70 value 2.127121
## iter 71 value 2.127121
## iter 72 value 2.127121
## iter 73 value 2.127120
## iter 74 value 2.127120
## iter 74 value 2.127120
## iter 74 value 2.127120
## final value 2.127120
## converged
## initial value 2.133693
## iter 2 value 2.133179
## iter 3 value 2.133153
## iter 4 value 2.133143
## iter 5 value 2.133139
## iter 6 value 2.133127
## iter 7 value 2.133103
## iter 8 value 2.133100
## iter 9 value 2.133100
## iter 10 value 2.133100
## iter 11 value 2.133099
## iter 12 value 2.133097
## iter 13 value 2.133092
## iter 14 value 2.133082
## iter 15 value 2.133082
## iter 16 value 2.133080
## iter 17 value 2.133080
## iter 18 value 2.133080
## iter 18 value 2.133080
## iter 18 value 2.133080
## final value 2.133080
## converged
```

Model: (1,1,2) (1,1,2) [4]

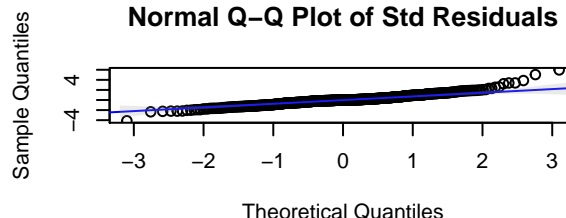
Standardized Residuals



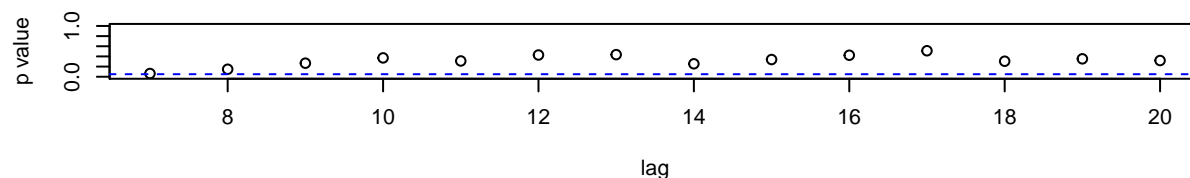
ACF of Residuals



Normal Q-Q Plot of Std Residuals

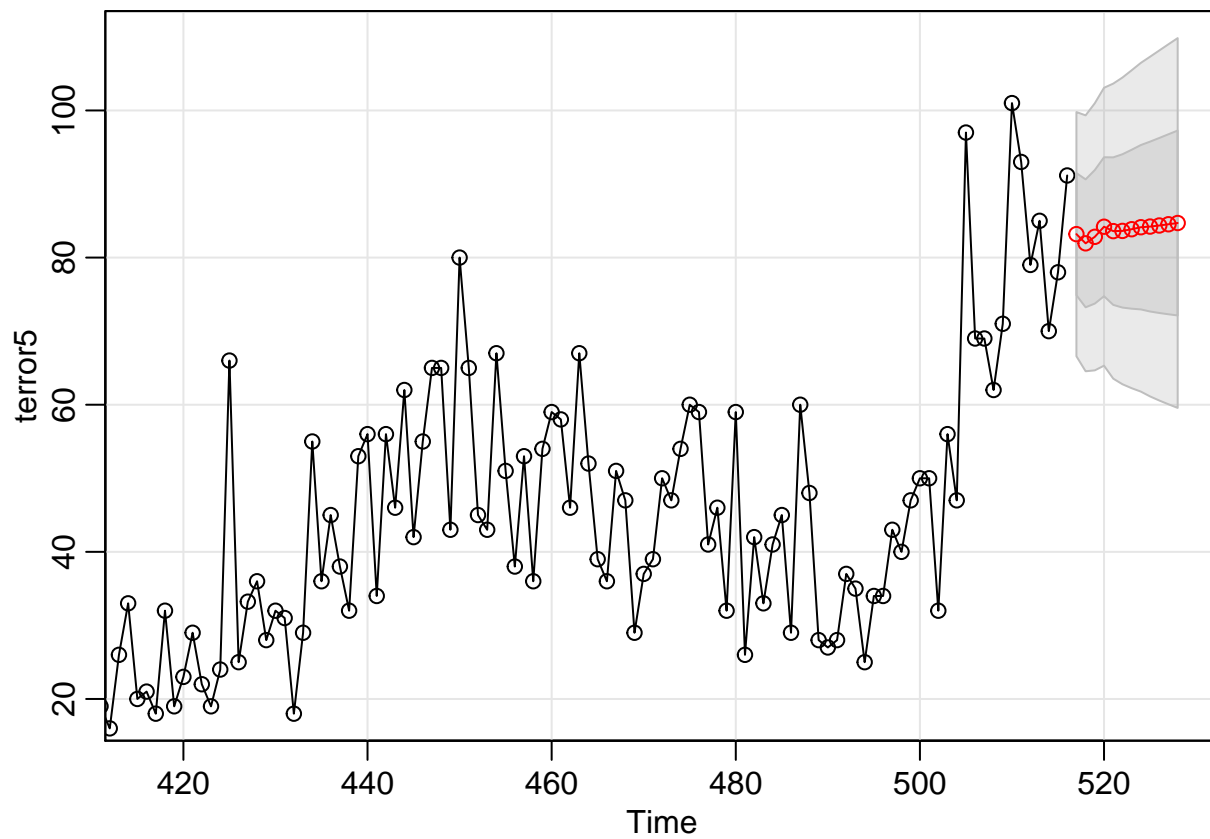


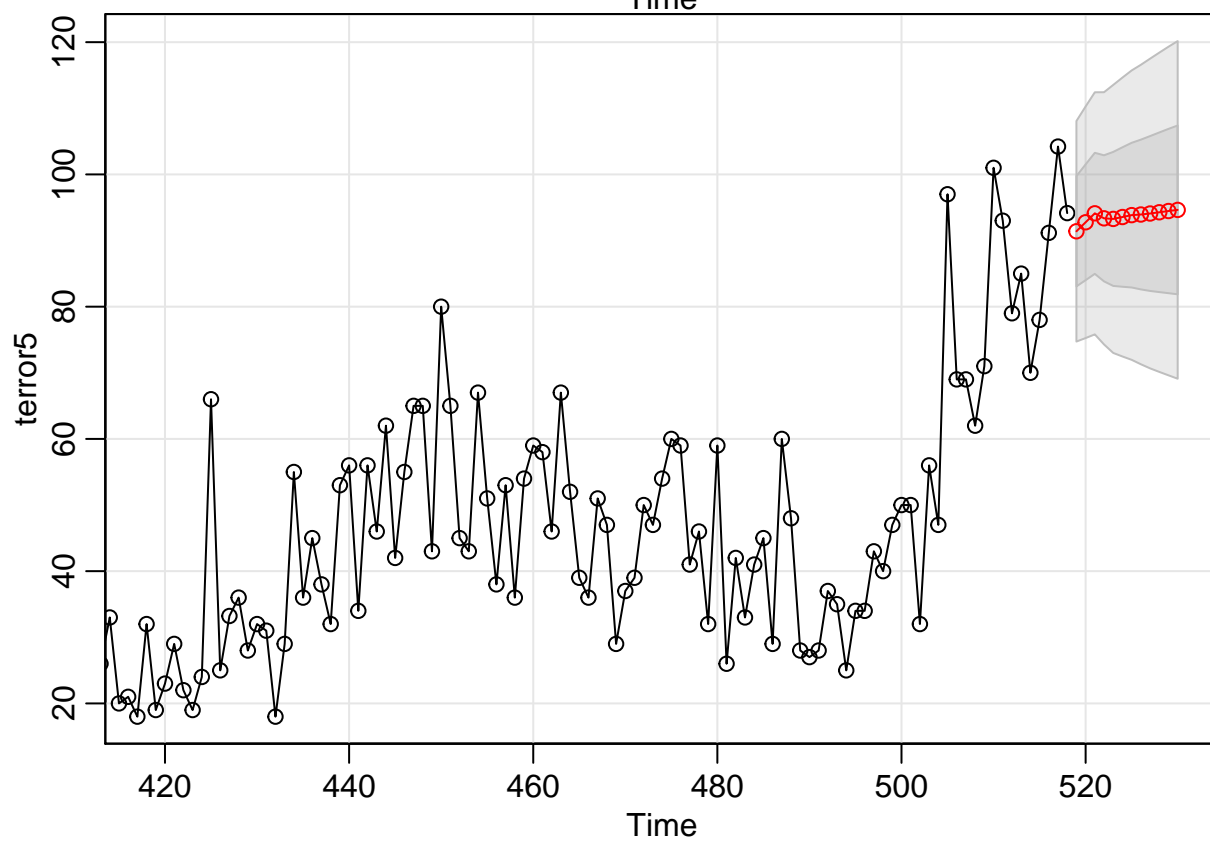
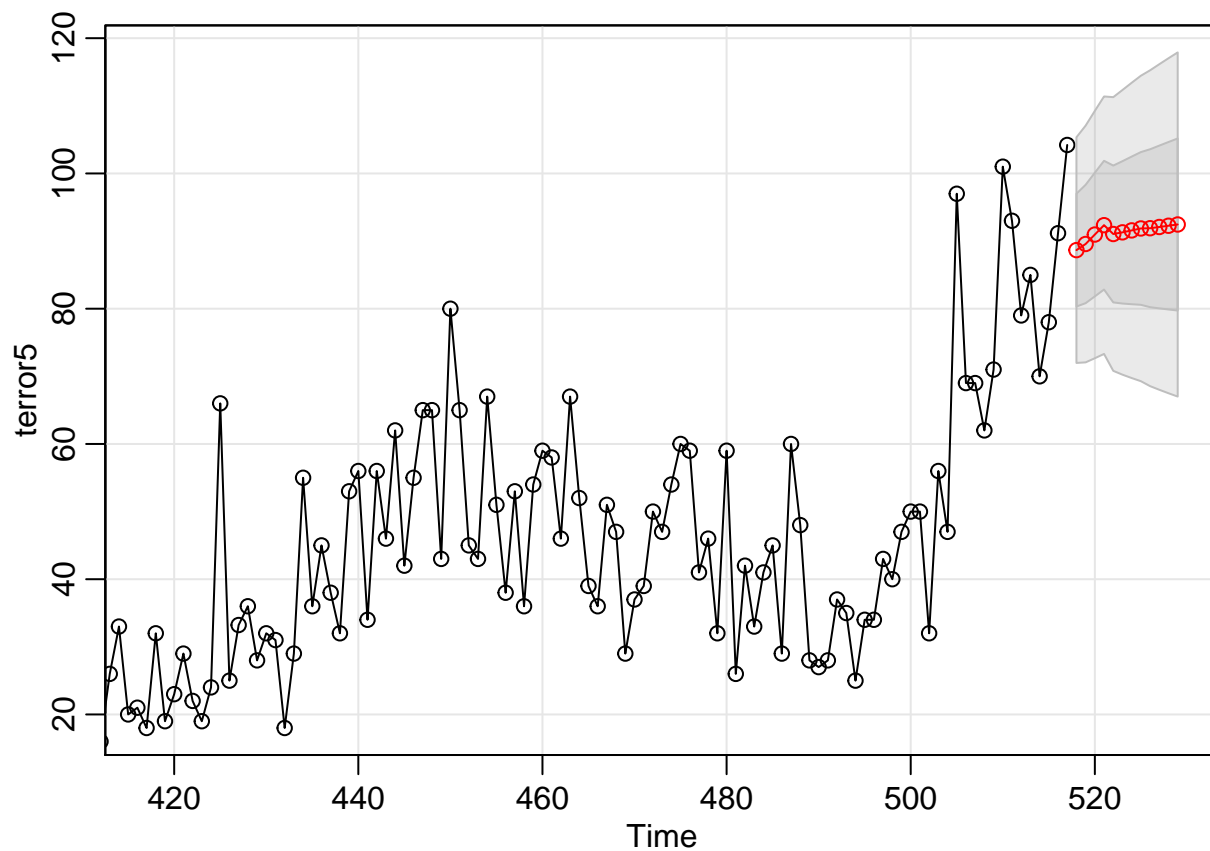
p values for Ljung-Box statistic

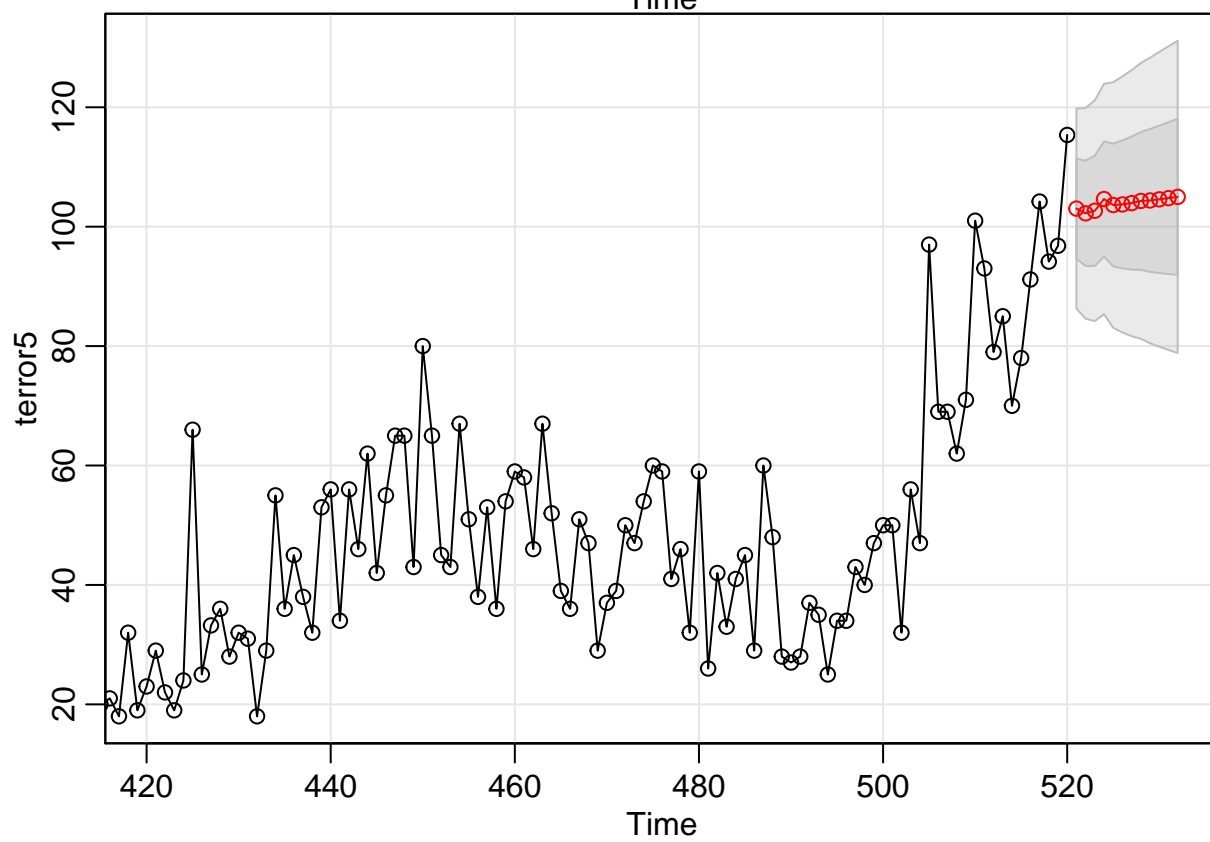
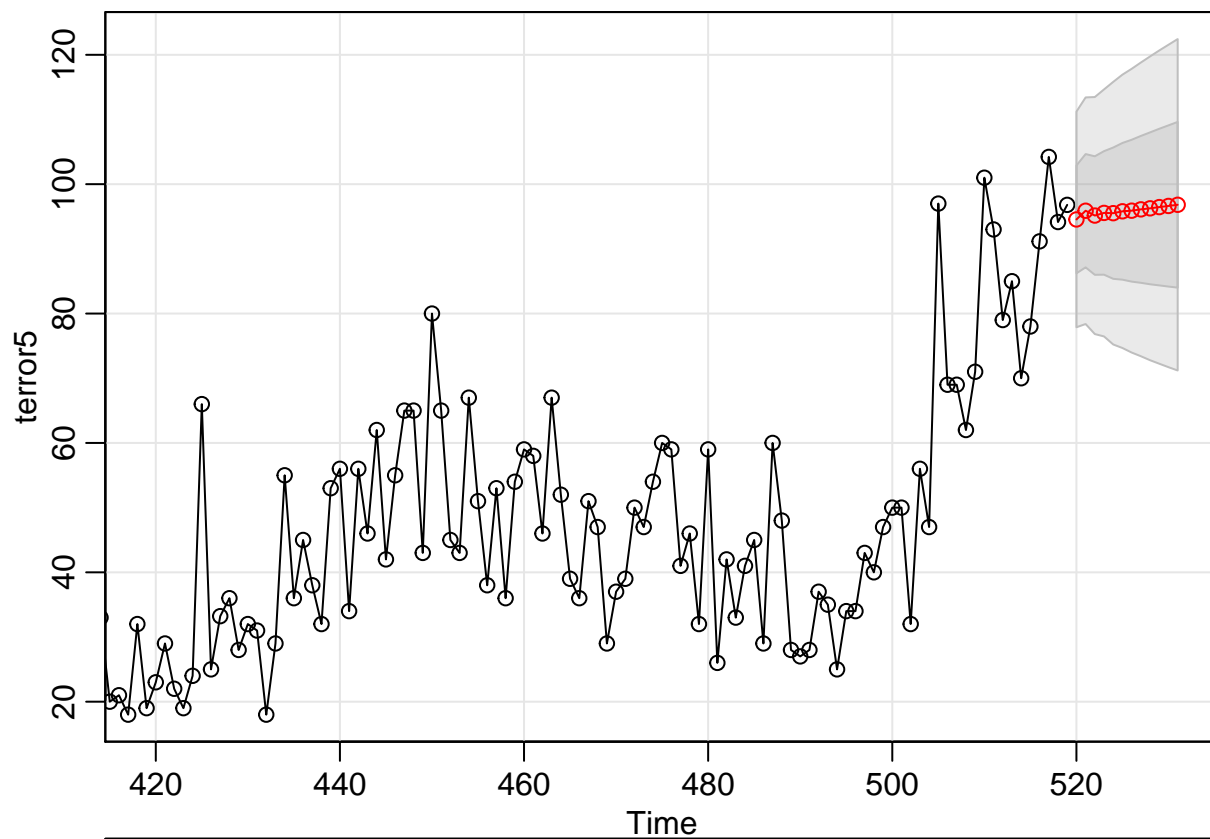


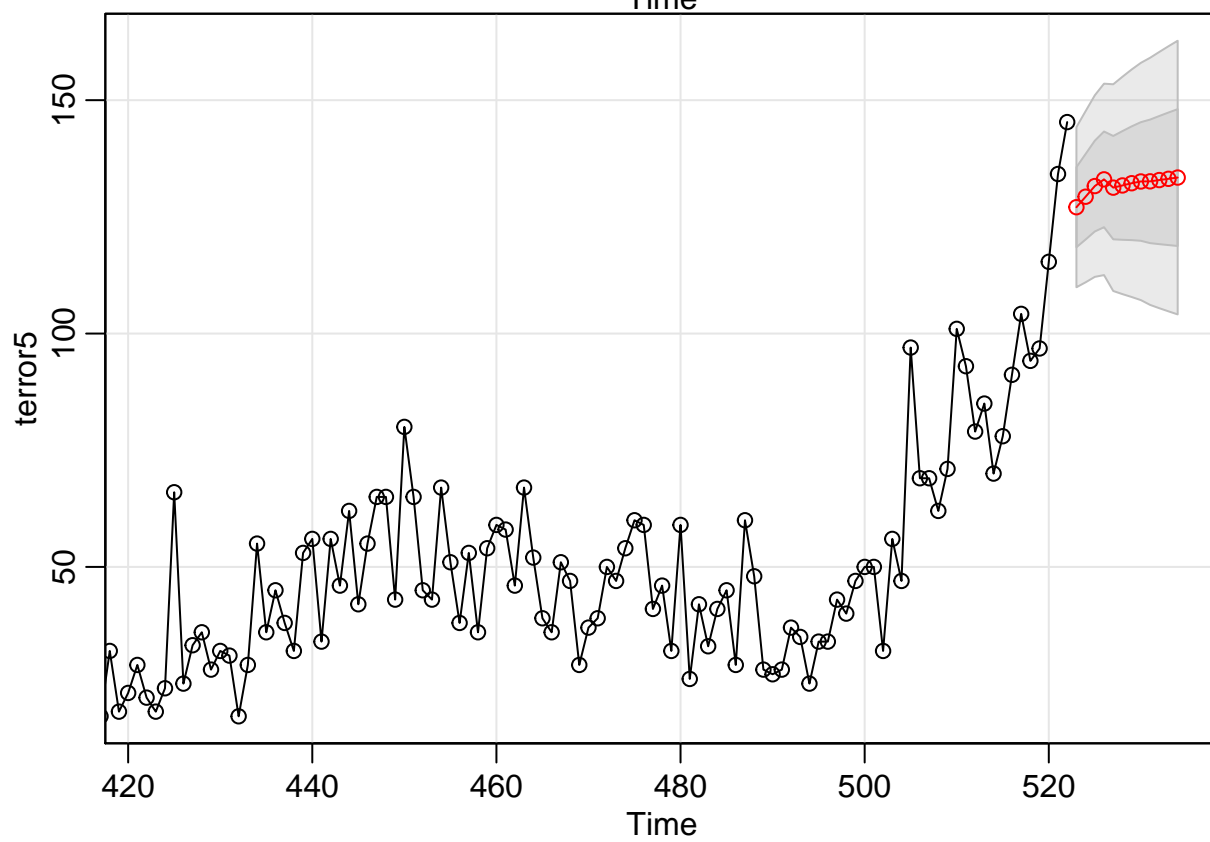
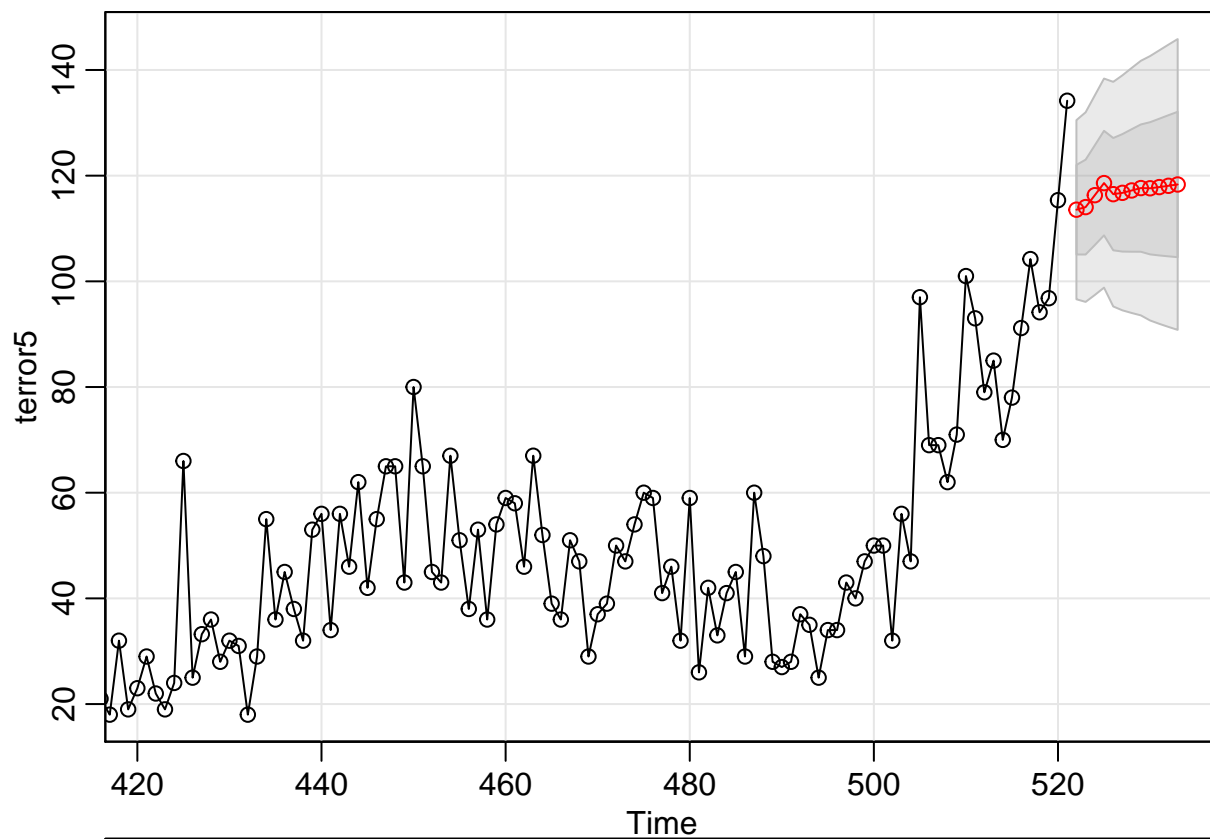
```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##     REPORT = 1, reltol = tol))
##
## Coefficients:
##          ar1      ma1      ma2      sar1      sma1      sma2
##      -0.8094  0.1185 -0.5406 -0.7206 -0.1827 -0.8172
## s.e.   0.2450  0.2505  0.1769  0.0978  0.0806  0.0798
##
## sigma^2 estimated as 68.49:  log likelihood = -1815.08,  aic = 3644.16
##
## $degrees_of_freedom
## [1] 505
##
## $ttable
##      Estimate      SE  t.value p.value
## ar1   -0.8094  0.2450  -3.3039  0.0010
## ma1    0.1185  0.2505   0.4730  0.6364
## ma2   -0.5406  0.1769  -3.0563  0.0024
## sar1   -0.7206  0.0978  -7.3717  0.0000
## sma1   -0.1827  0.0806  -2.2673  0.0238
## sma2   -0.8172  0.0798 -10.2401  0.0000
##
## $AIC
## [1] 5.24995
```

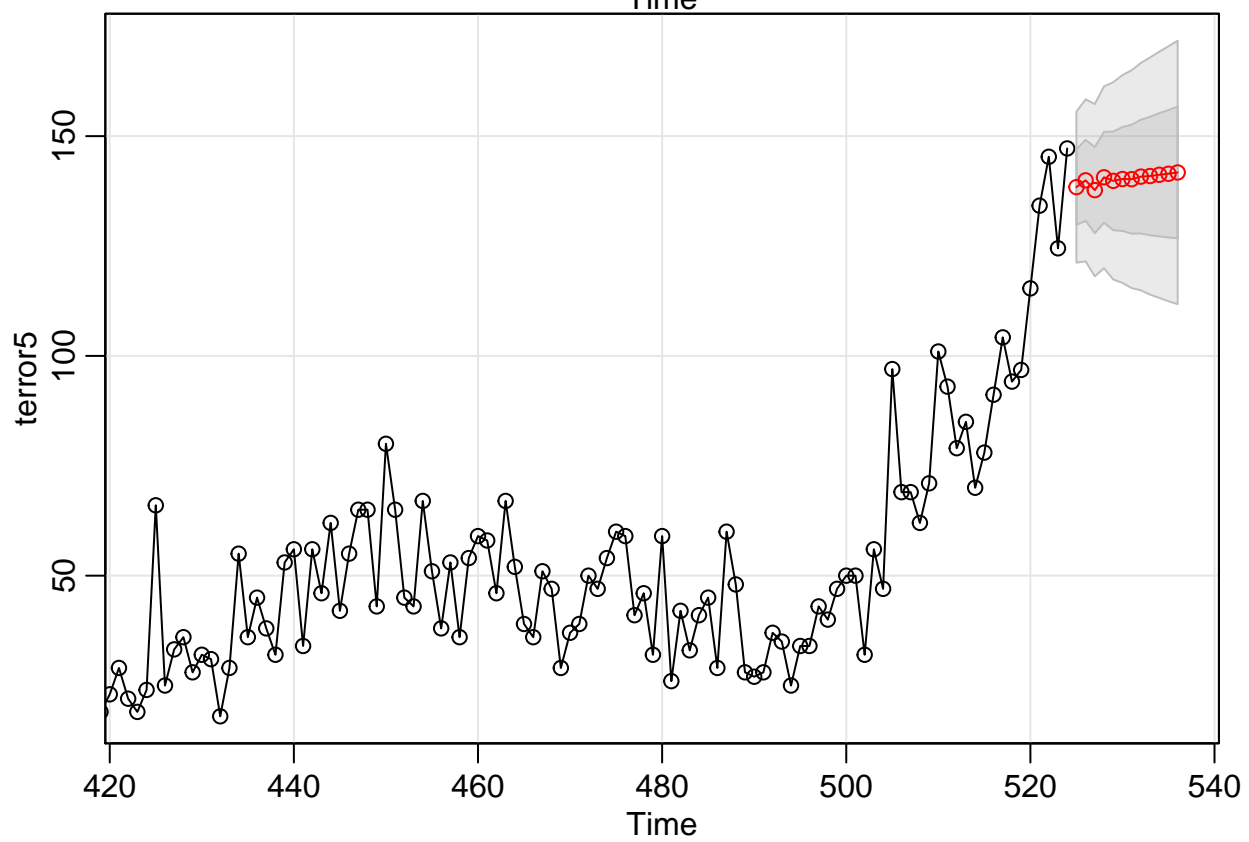
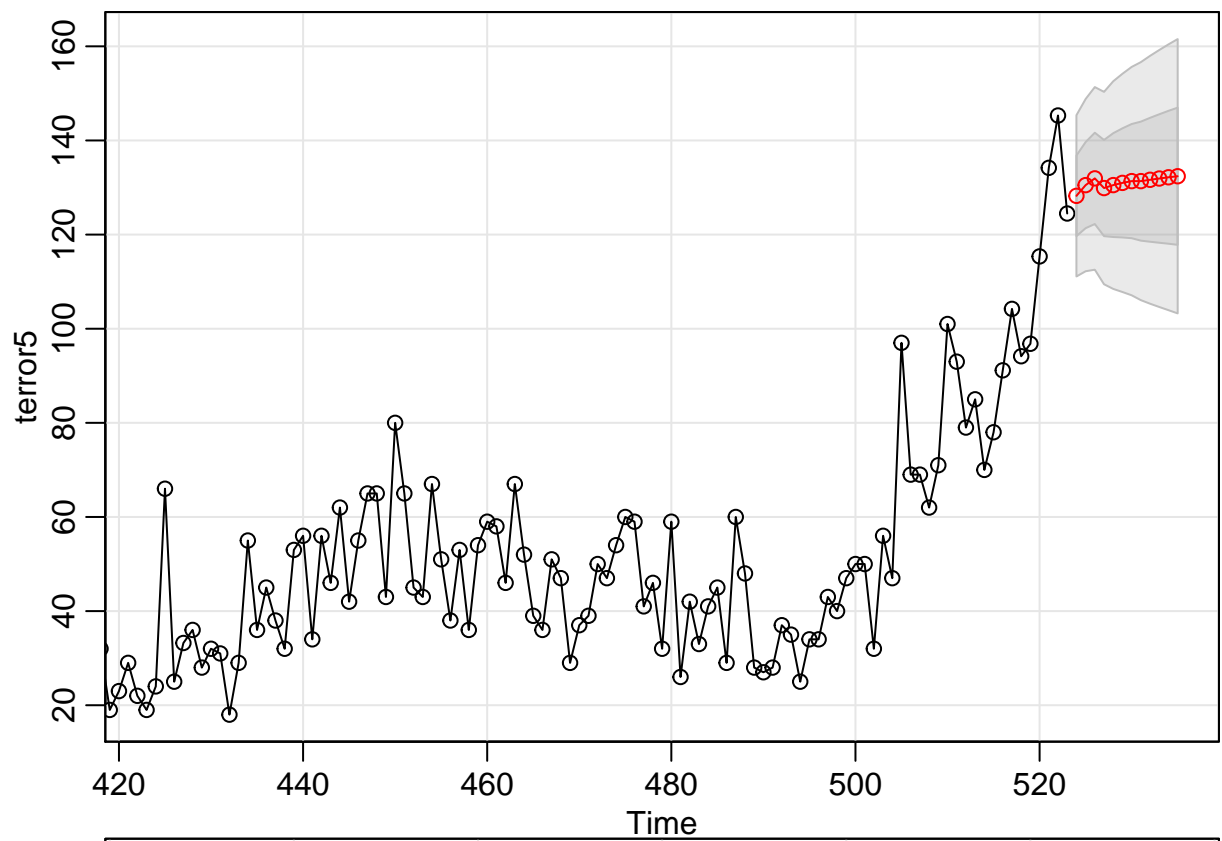
```
##
## $AICc
## [1] 5.254253
##
## $BIC
## [1] 4.299323
#eacf(diff(diff(log_terror4)))
terror5 <- terror4
total_error <- 0
for (i in 1:(length(terror4.valid) - 11))
{
  actual <- terror4.valid[i : i + 11]
  predicted <- sarima.for(terror5, 12, 0, 1, 1, 1, 0, 0, 4)$pred
  total_error <- total_error + sum((actual - predicted)^2)
  terror5 <- c(terror5, terror4.valid[i])
}
```

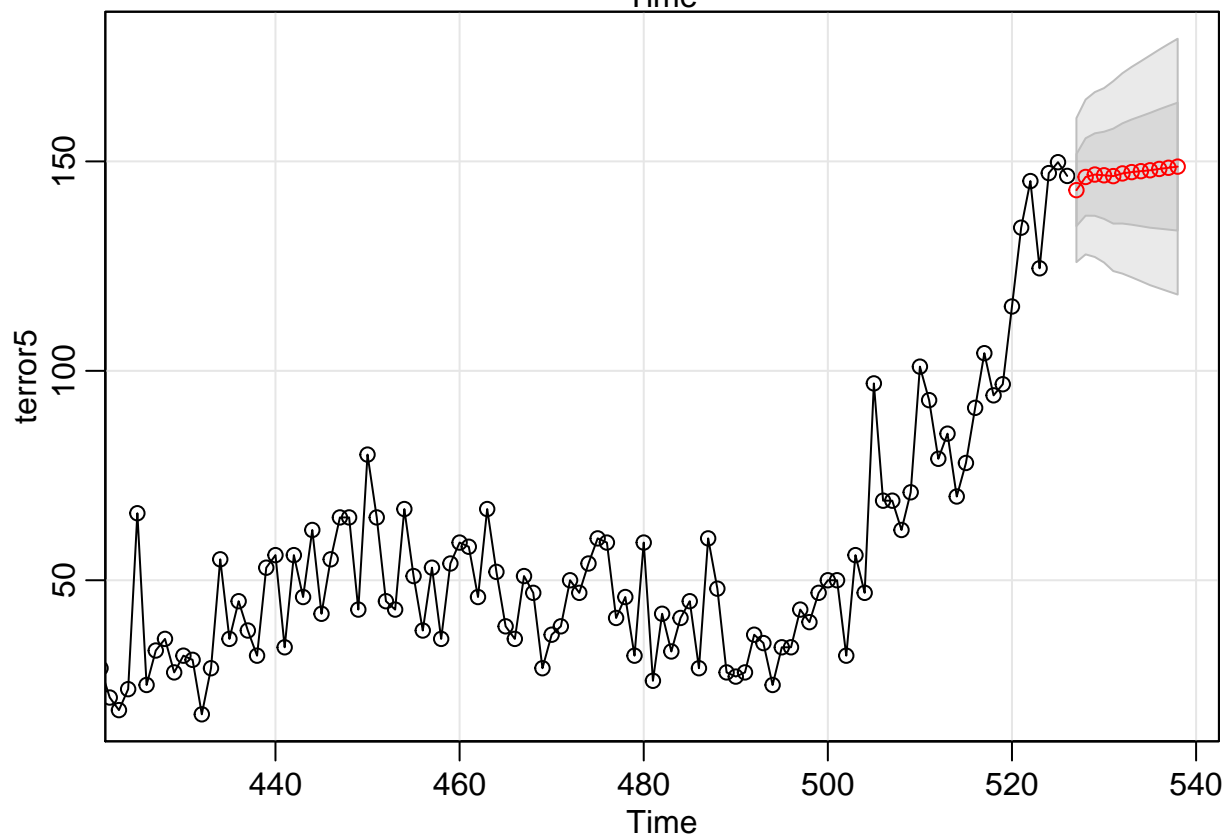
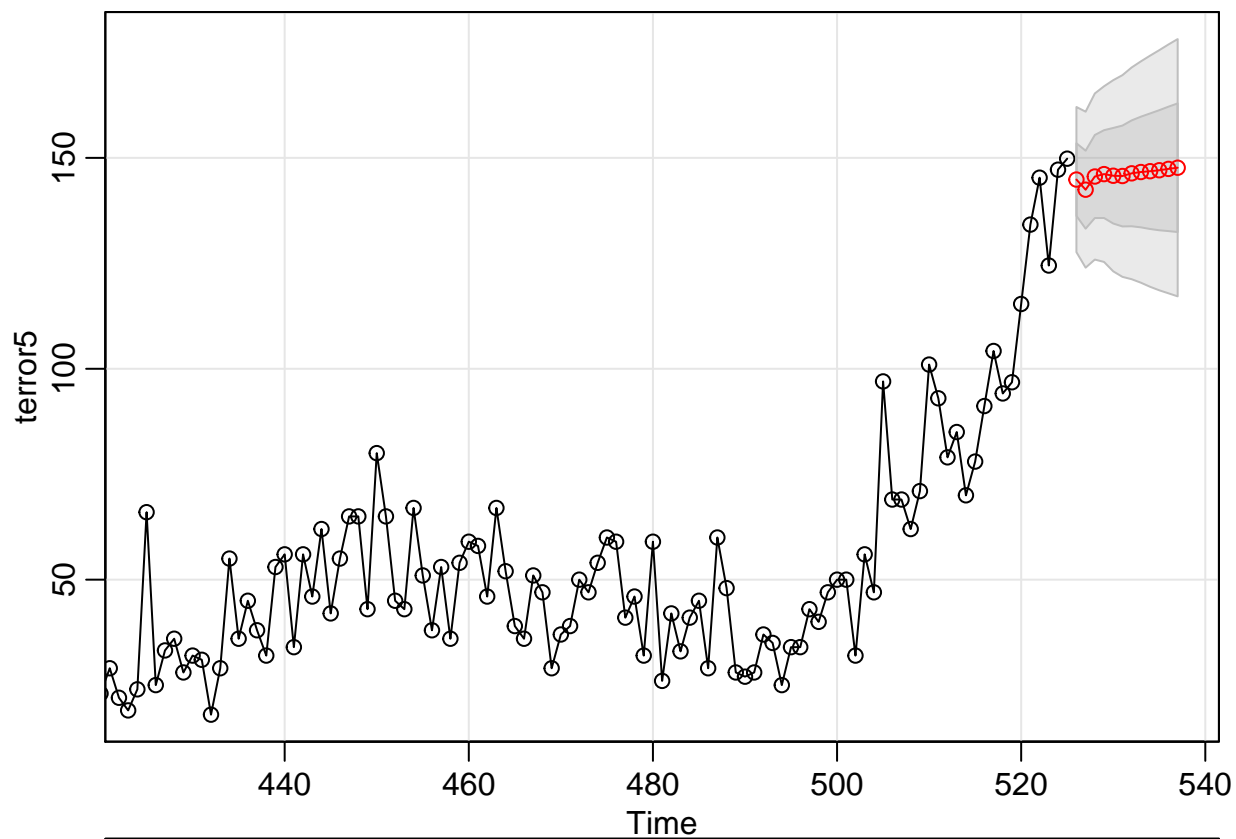


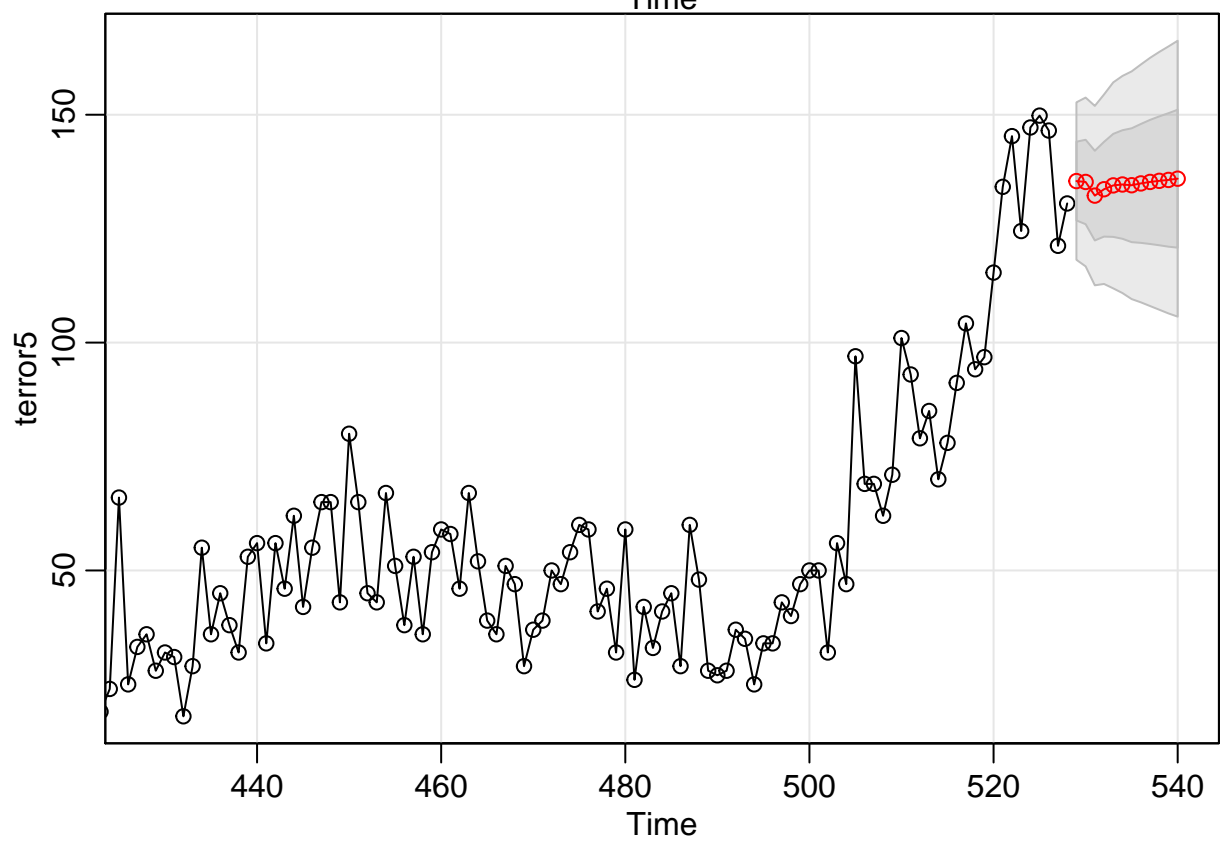
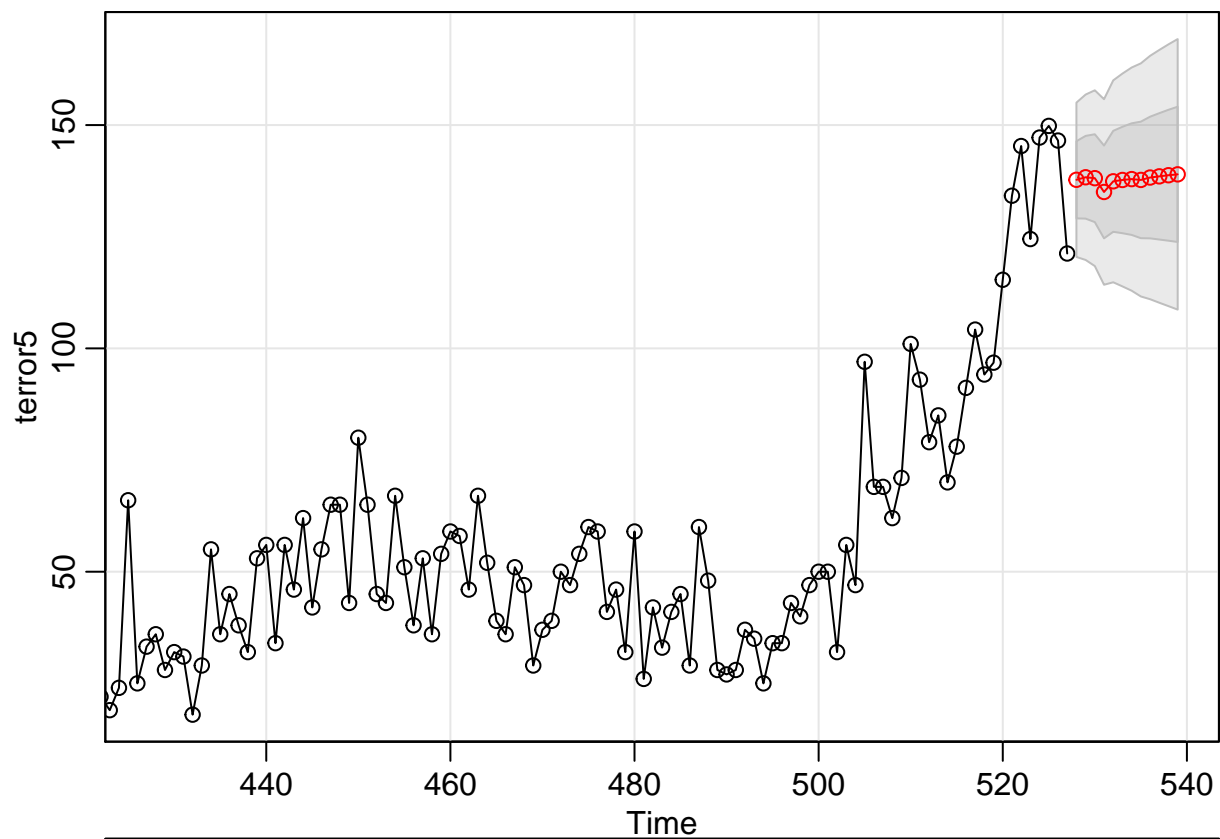


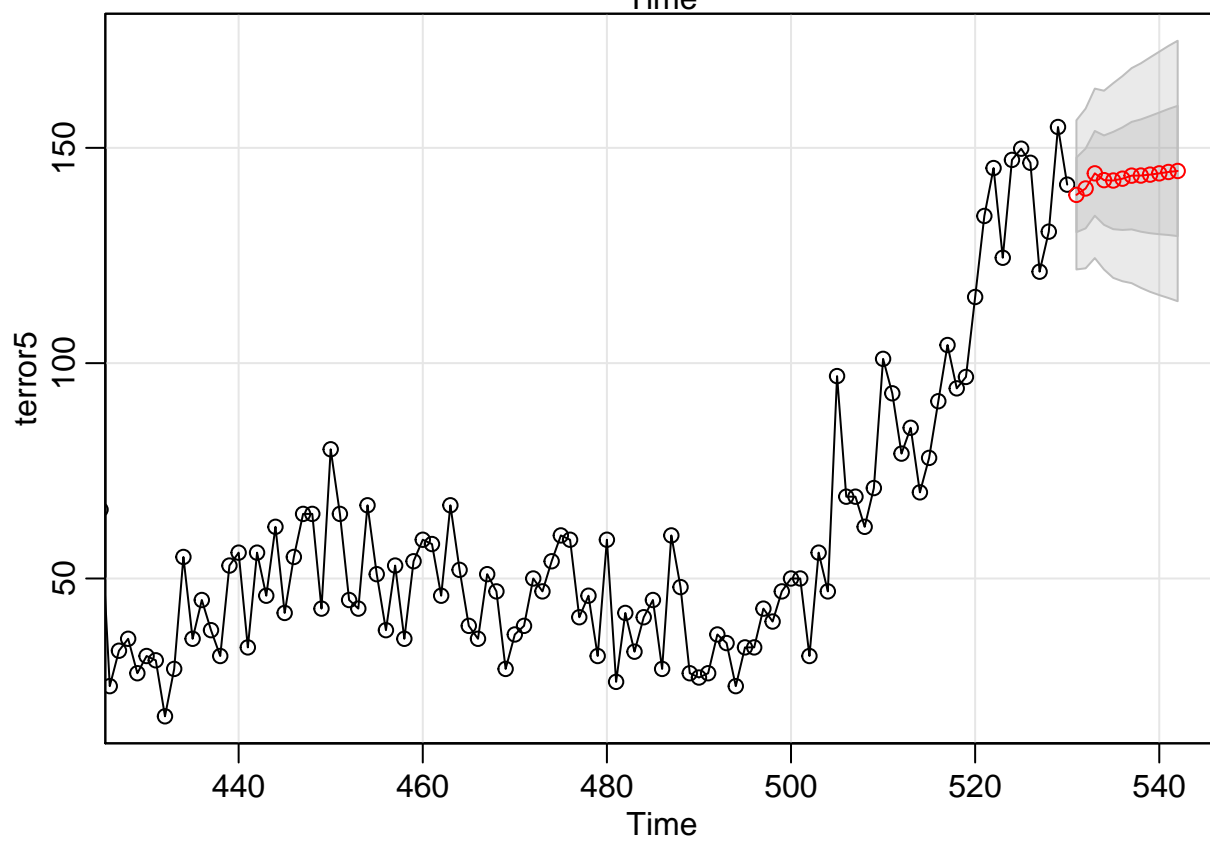
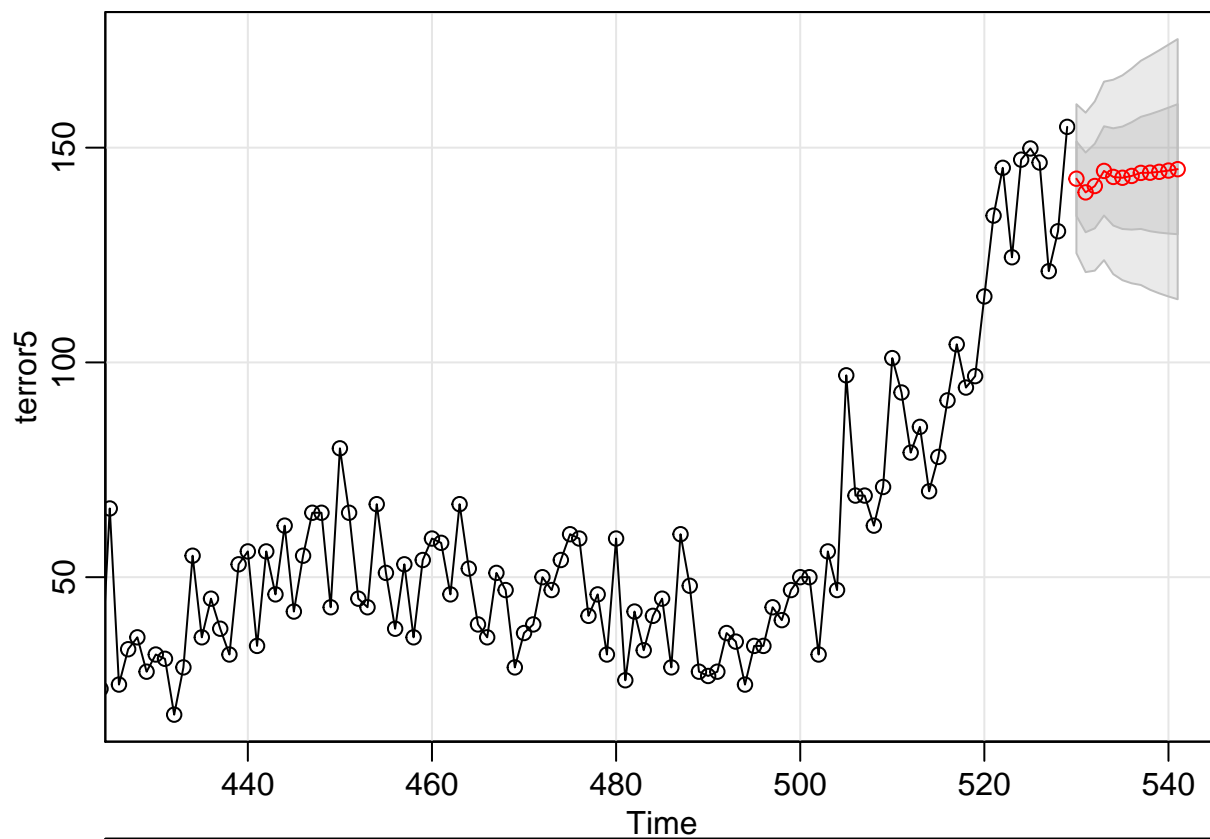


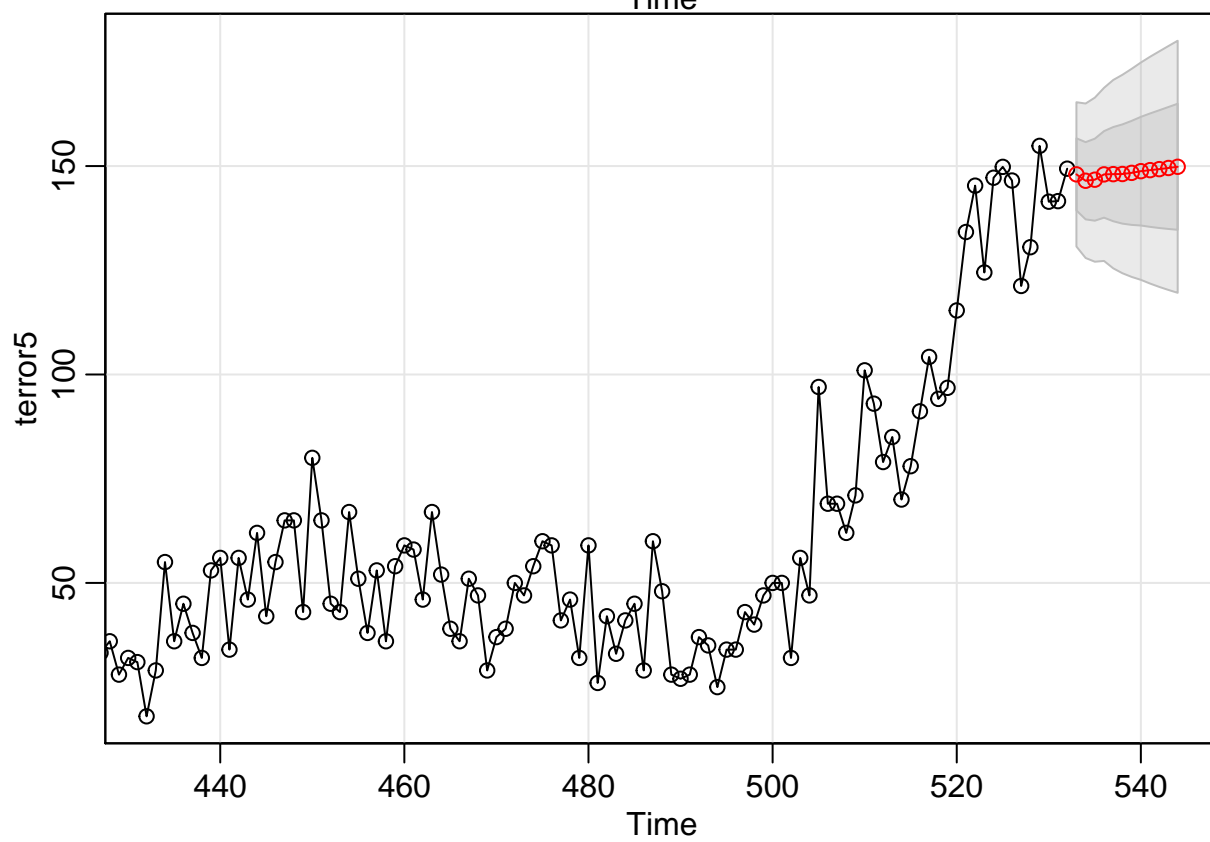
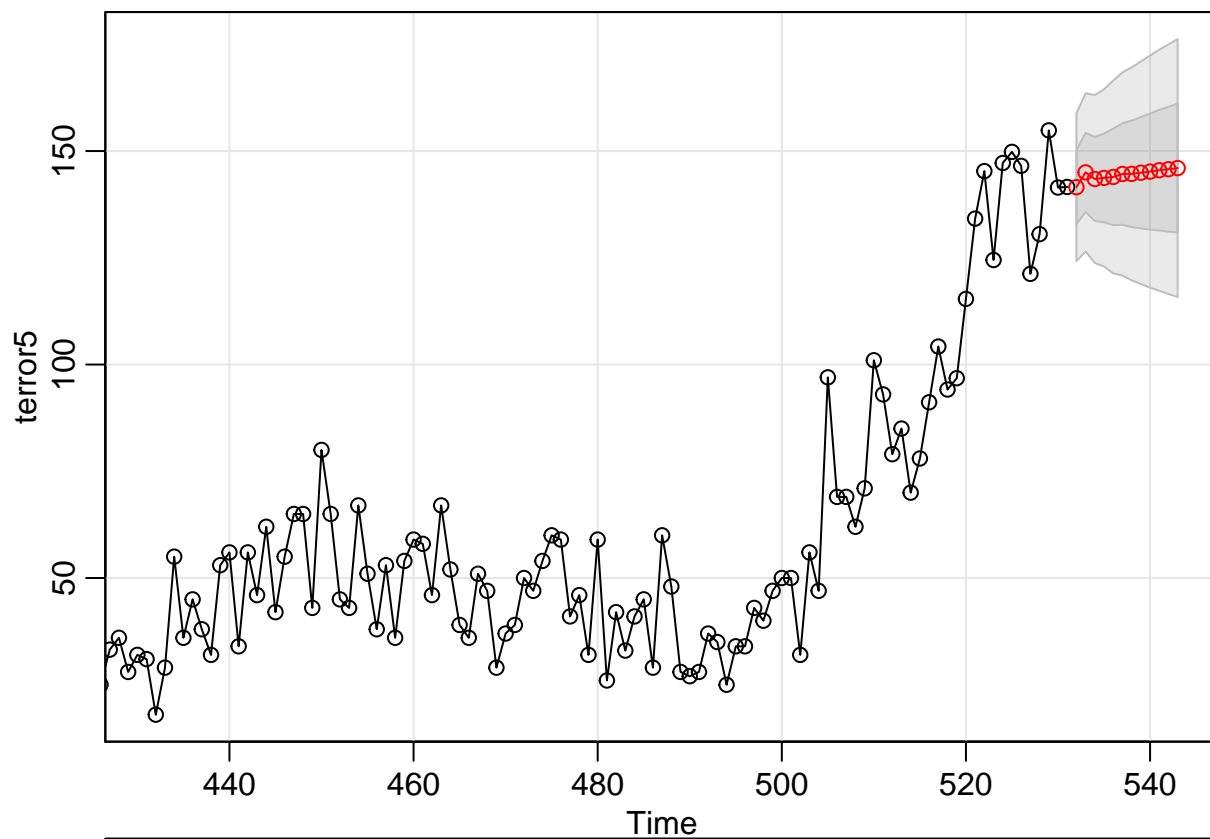


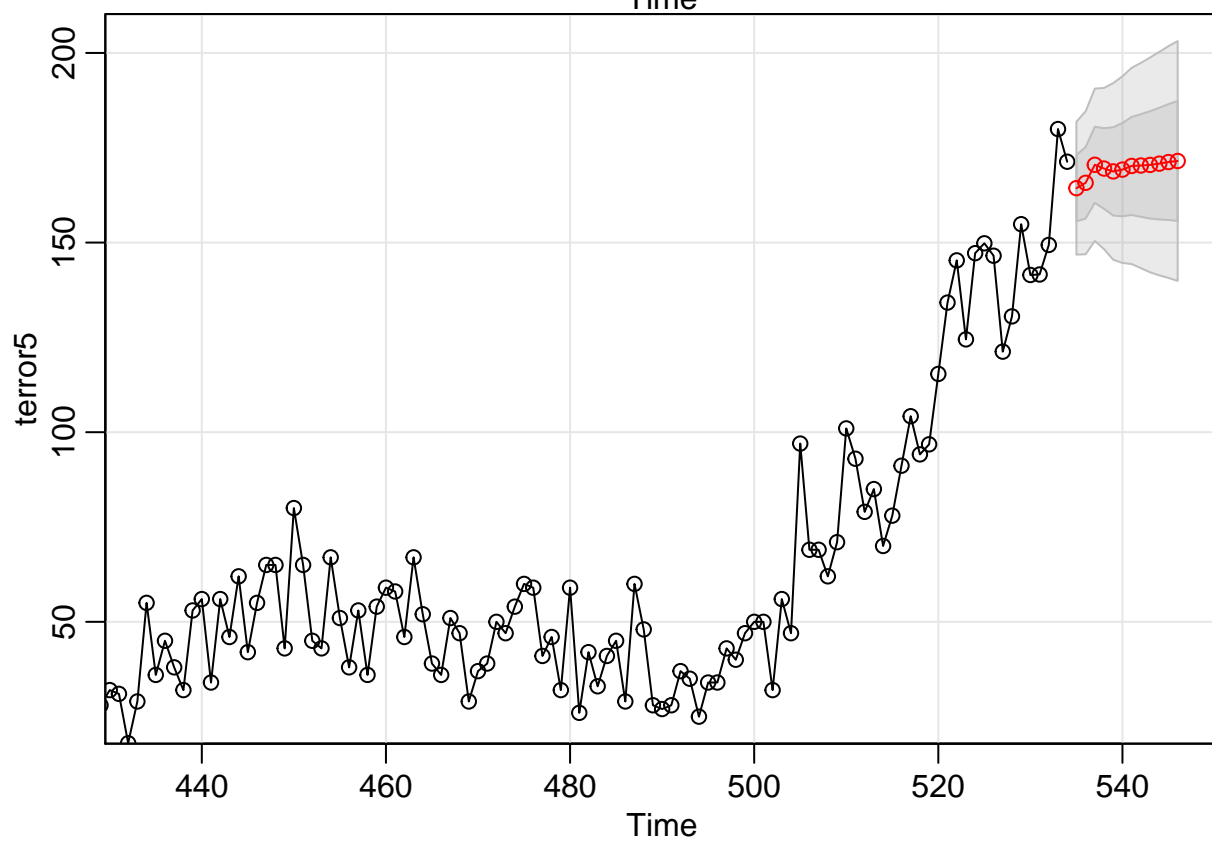
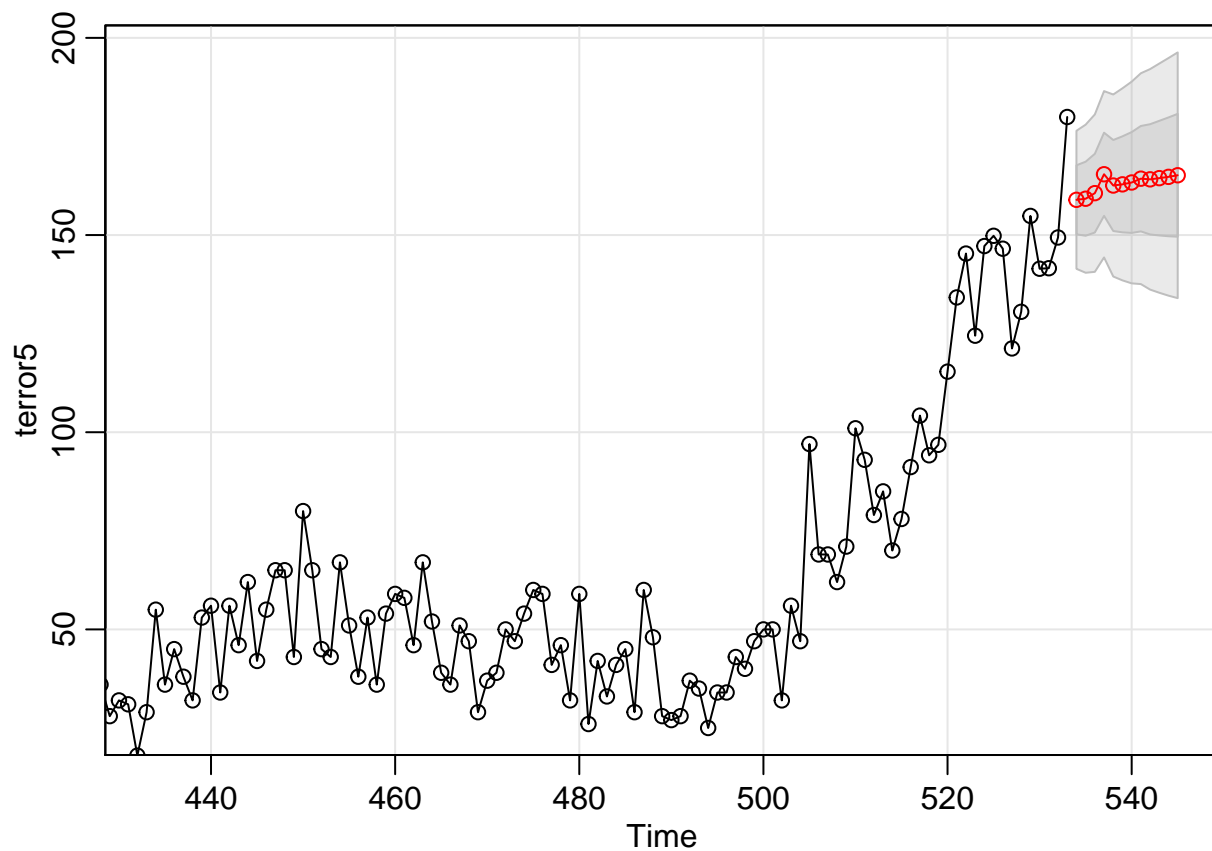


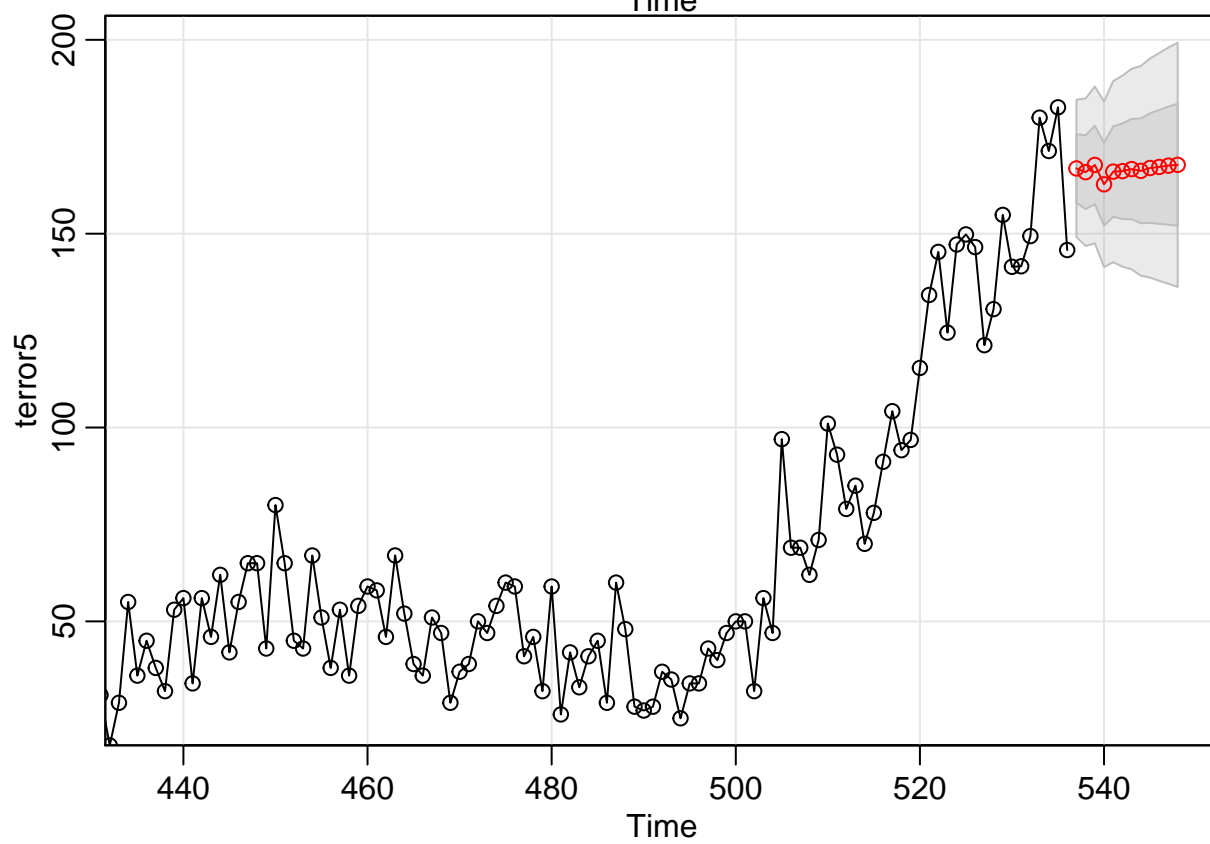
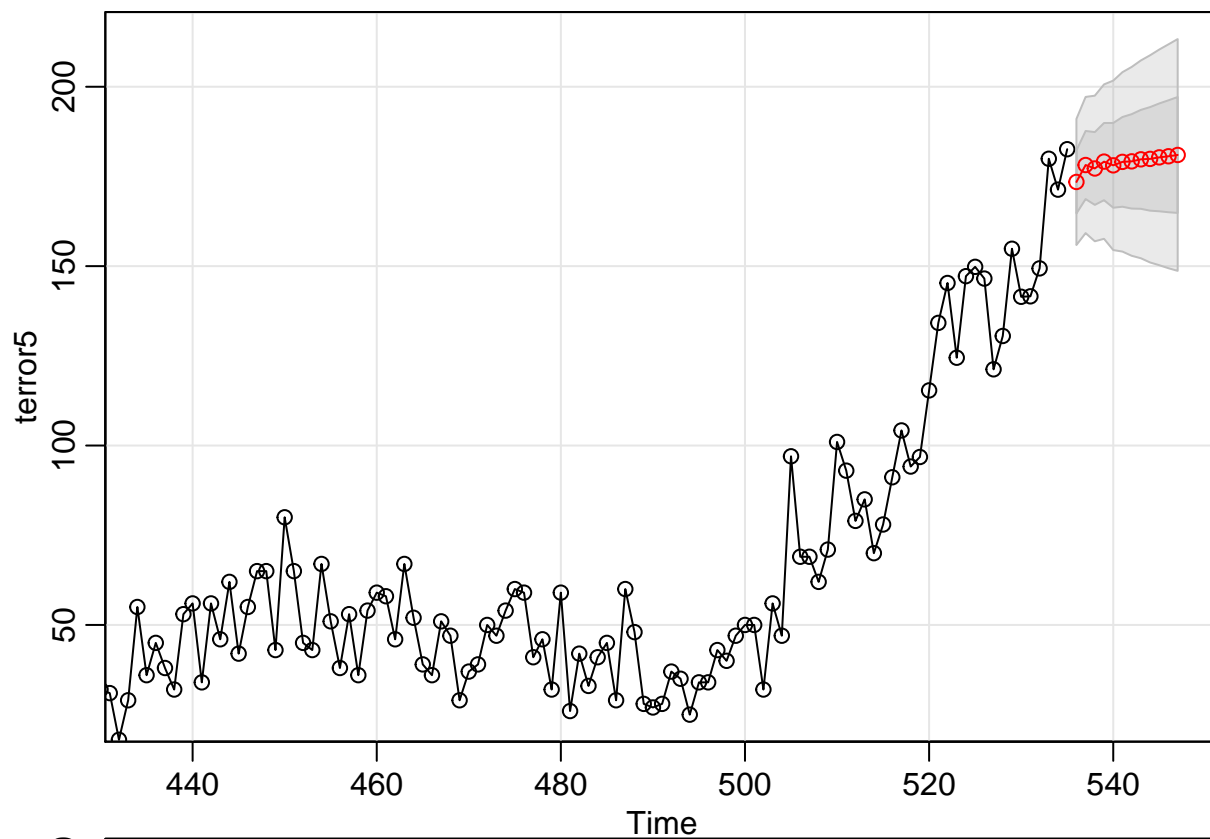


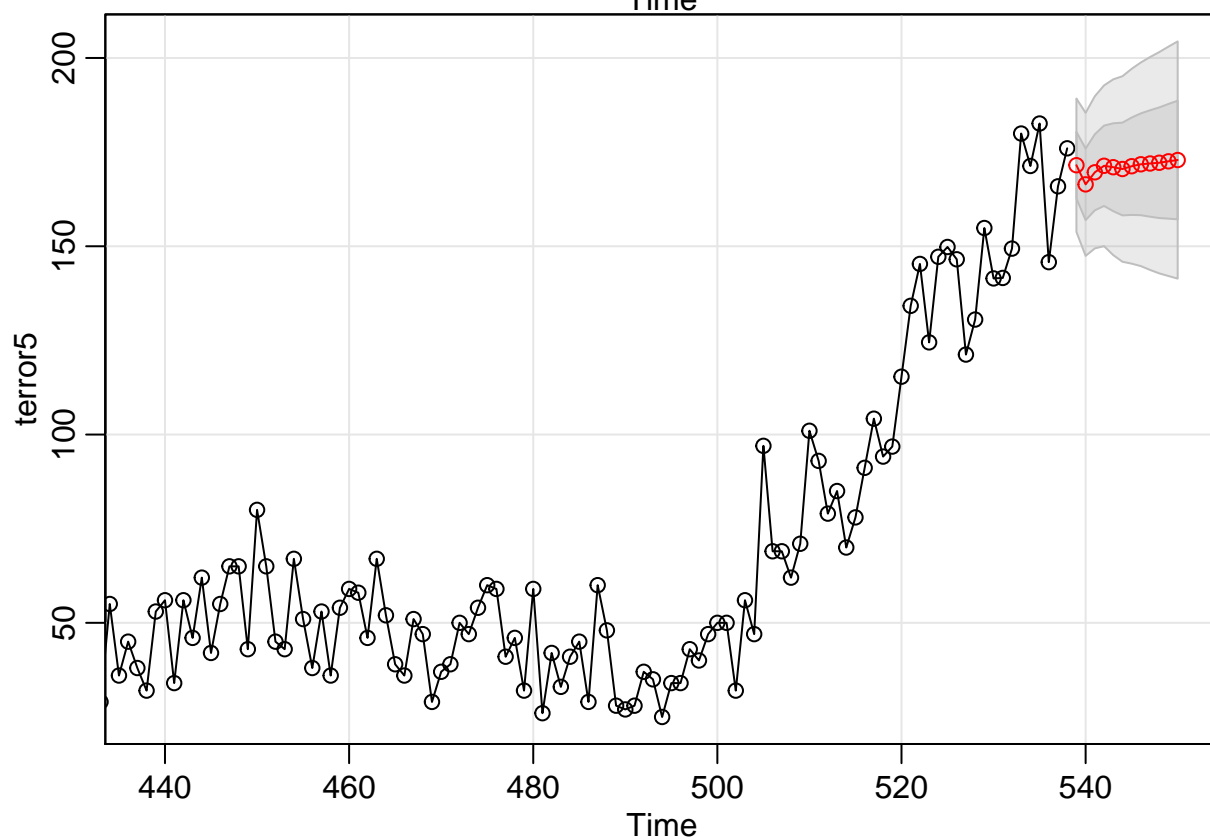
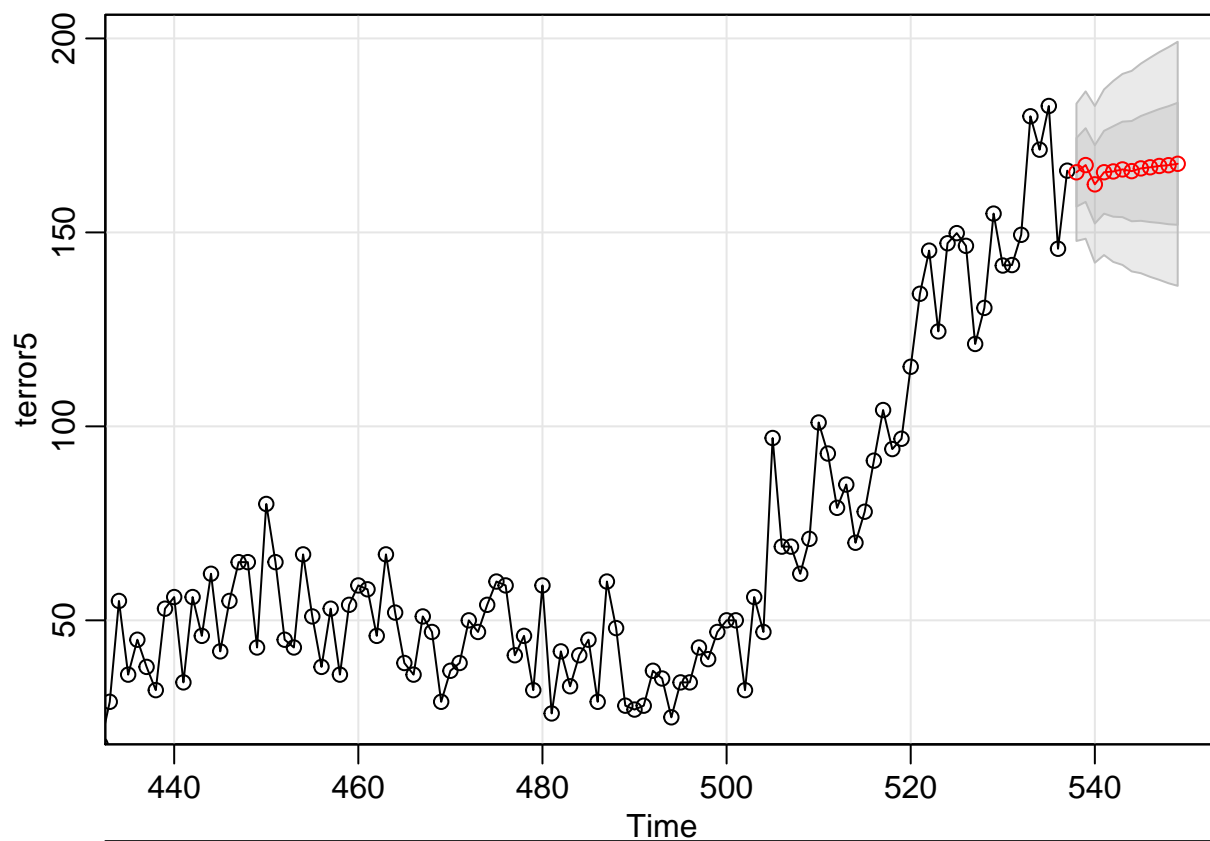


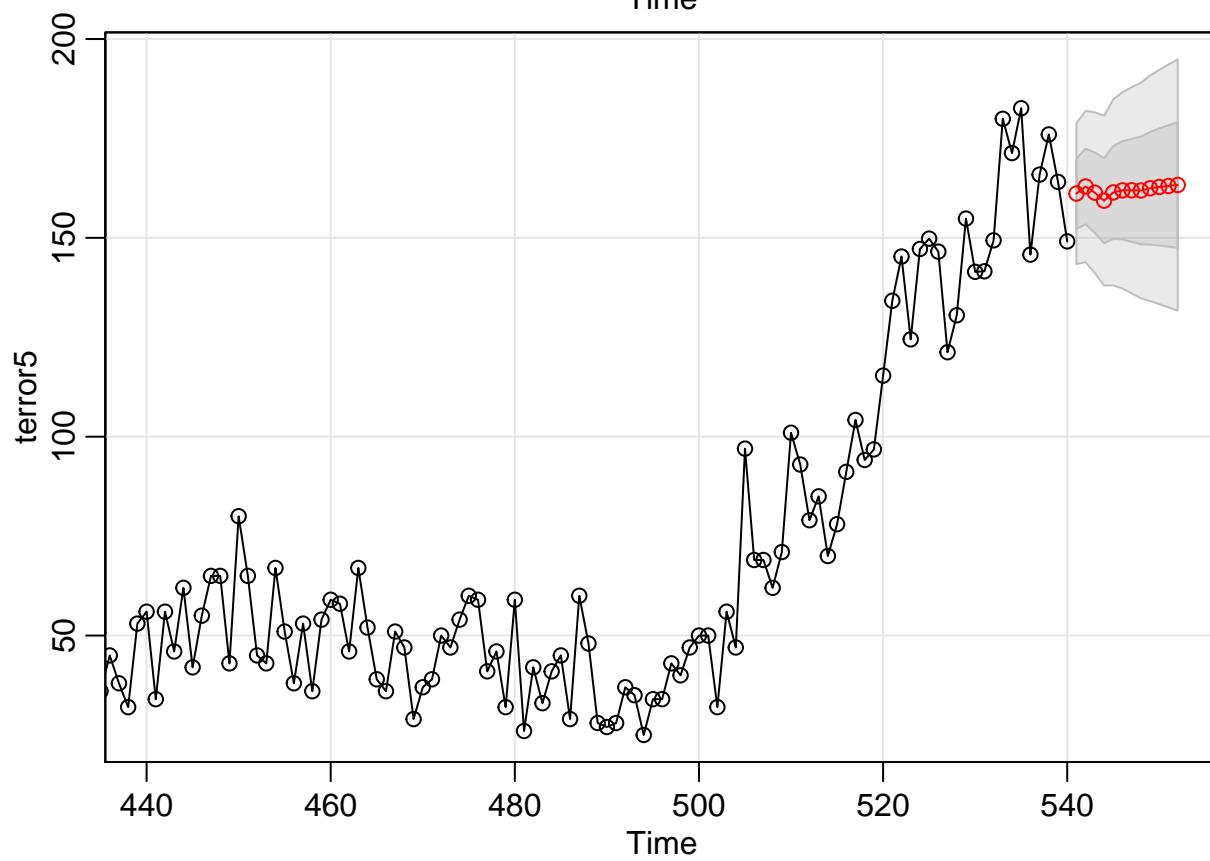
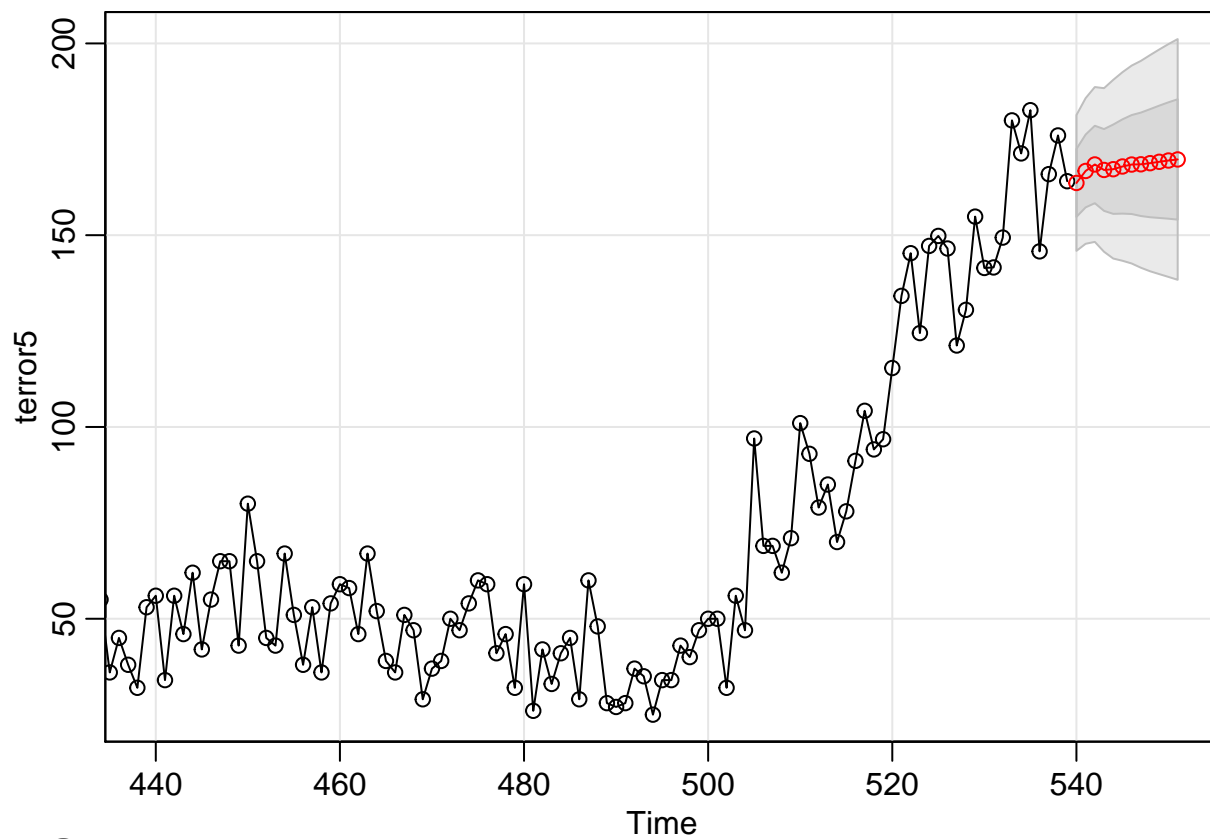






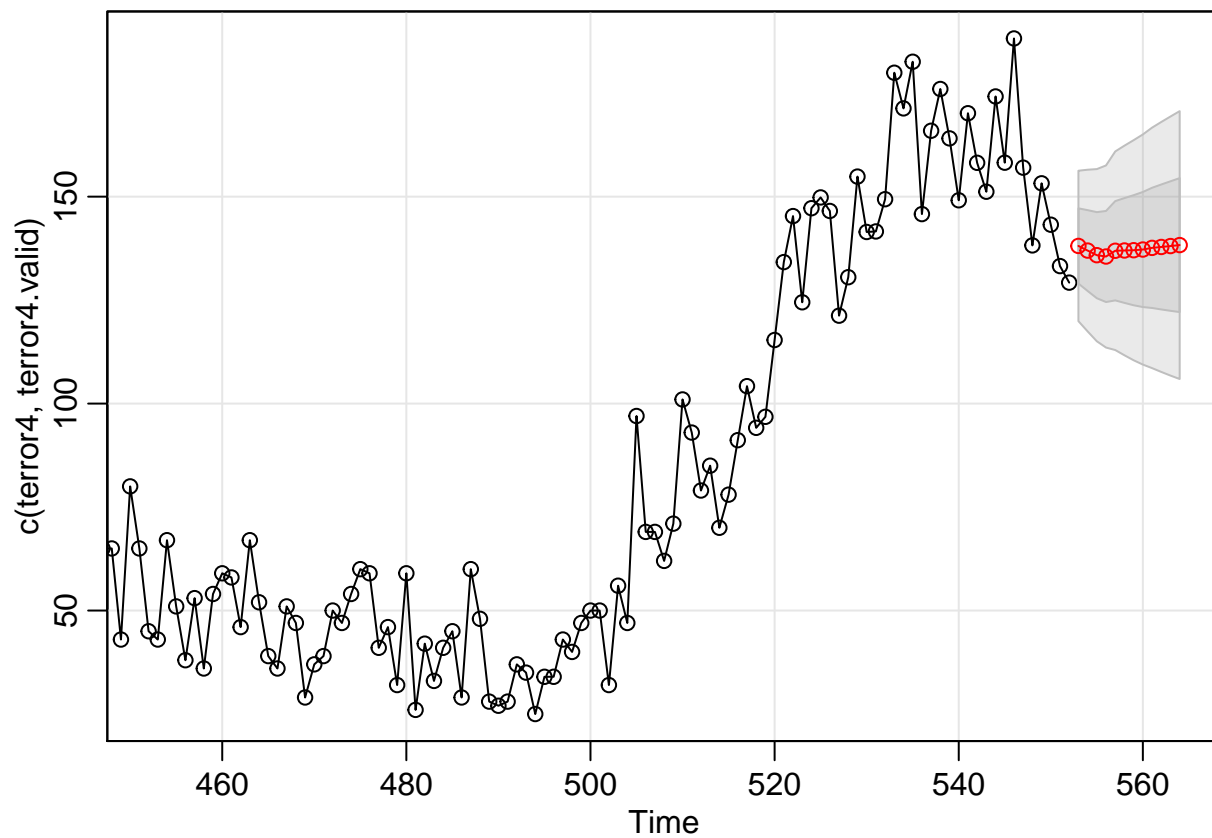






```
mse <- total_error / (length(terror4.valid) - 11)
```

```
val <- sarima.for(c(terror4, terror4.valid), 12, 0, 1, 1, 1, 0, 0, 4)
```



```
pred <- val$pred
```

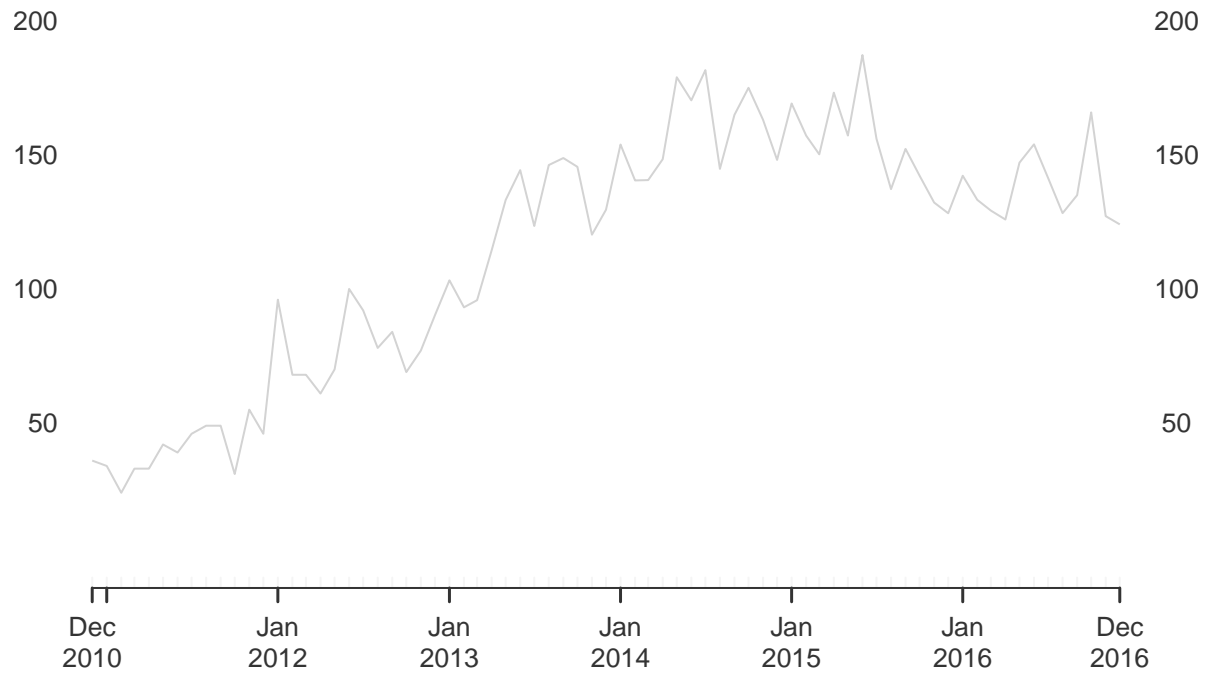
```
err <- val$se
```

```
total <- c(terror4, terror4.valid, terror4.testing)
```

```
plot(as.xts(ts(total, frequency = 12, start=1970))[492:length(total)], main = "Number of Terrorist Attacks")
```

Number of Terrorist Attacks (Training Set)

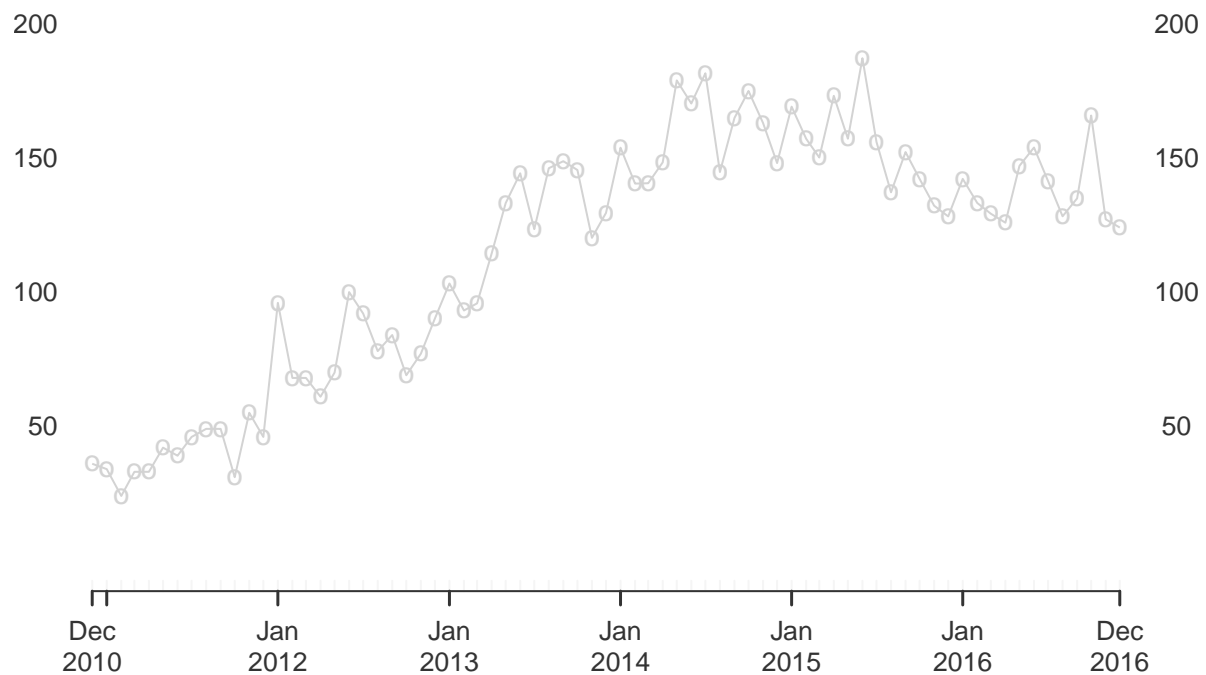
Dec 2010 / Dec 2016



```
points(as.xts(ts(total, frequency = 12, start=1970)),col="lightgray",pch="o")
```

Number of Terrorist Attacks (Training Set)

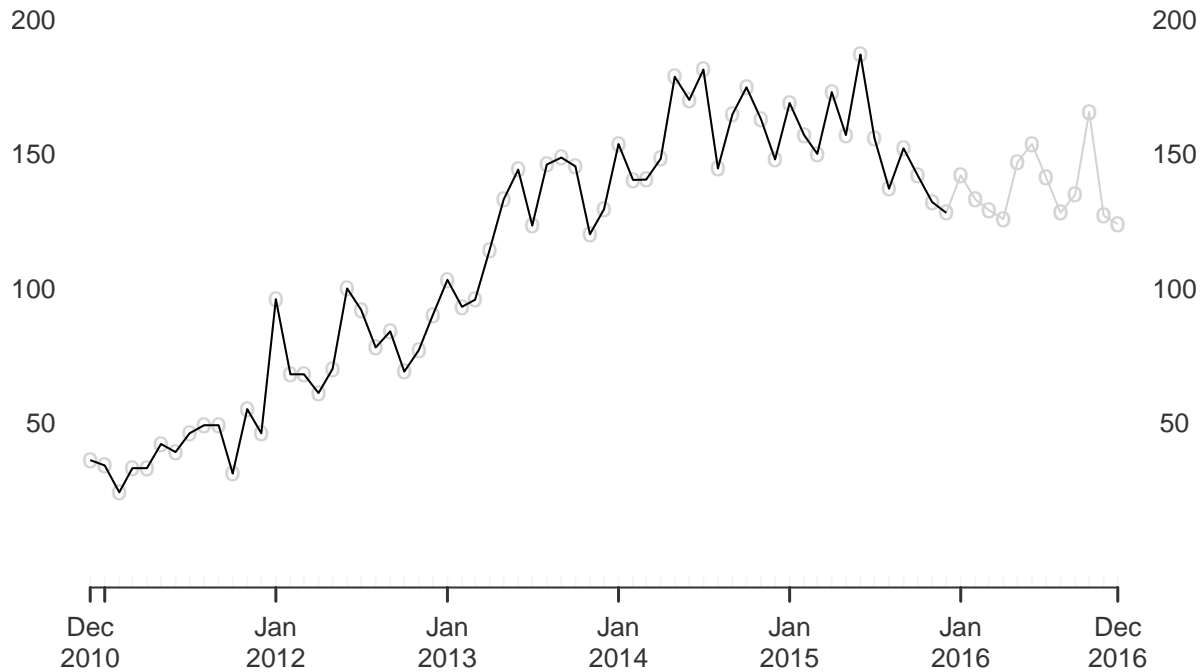
Dec 2010 / Dec 2016



```
lines(as.xts(ts(c(terror4, terror4.valid), frequency = 12, start=1970)),col="black")
```

Number of Terrorist Attacks (Training Set)

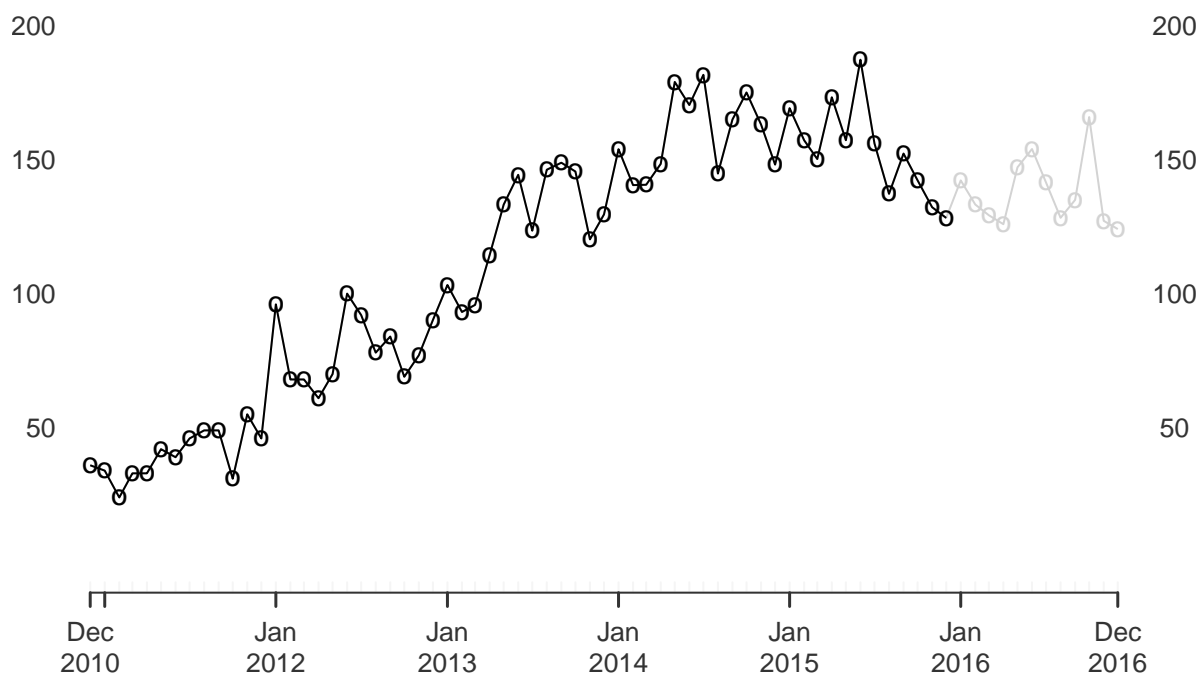
Dec 2010 / Dec 2016



```
points(as.xts(ts(c(terror4, terror4.valid), frequency = 12, start=1970)),col="black",pch="o")
```

Number of Terrorist Attacks (Training Set)

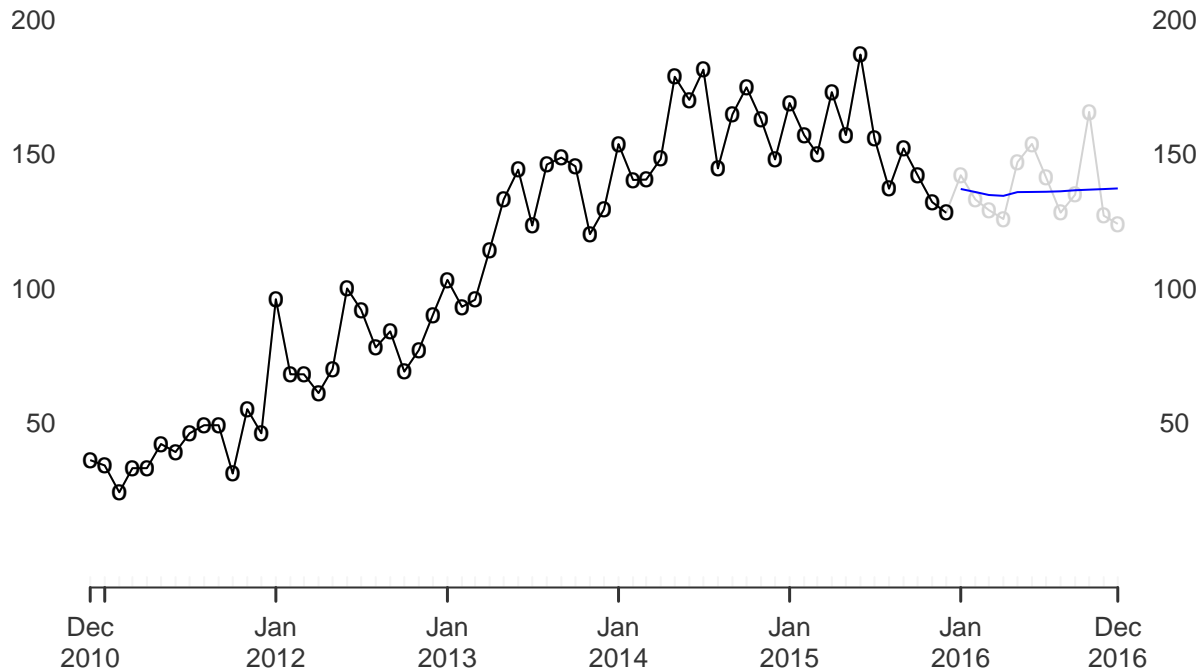
Dec 2010 / Dec 2016



```
lines(as.xts(ts(pred, frequency = 12, start=2016)),col="blue")
```

Number of Terrorist Attacks (Training Set)

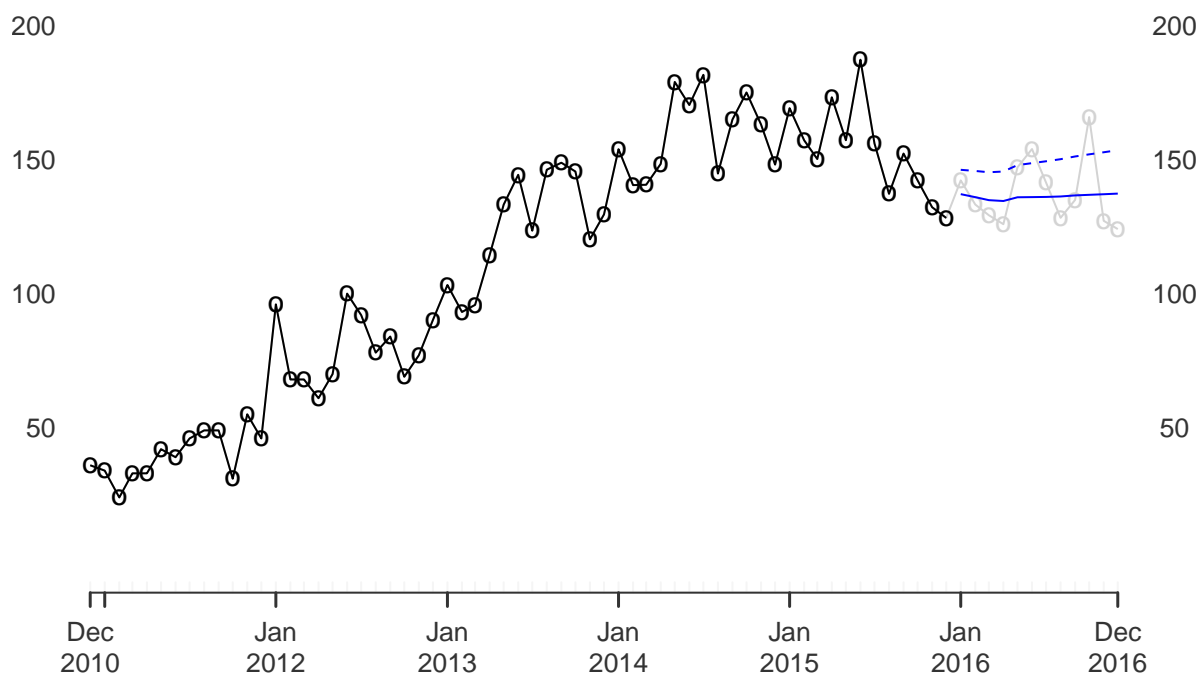
Dec 2010 / Dec 2016



```
lines(as.xts(ts(pred + err, frequency = 12, start=2016)),col="blue", lty="dashed")
```

Number of Terrorist Attacks (Training Set)

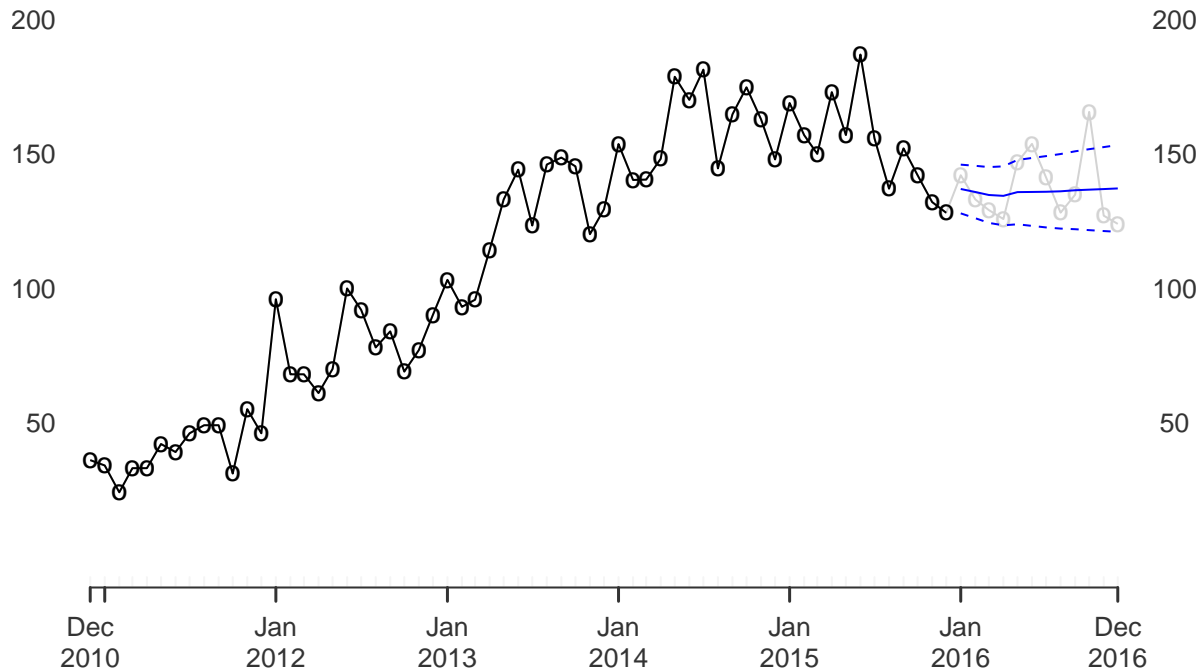
Dec 2010 / Dec 2016



```
lines(as.xts(ts(pred - err, frequency = 12, start=2016)),col="blue", lty="dashed")
```

Number of Terrorist Attacks (Training Set)

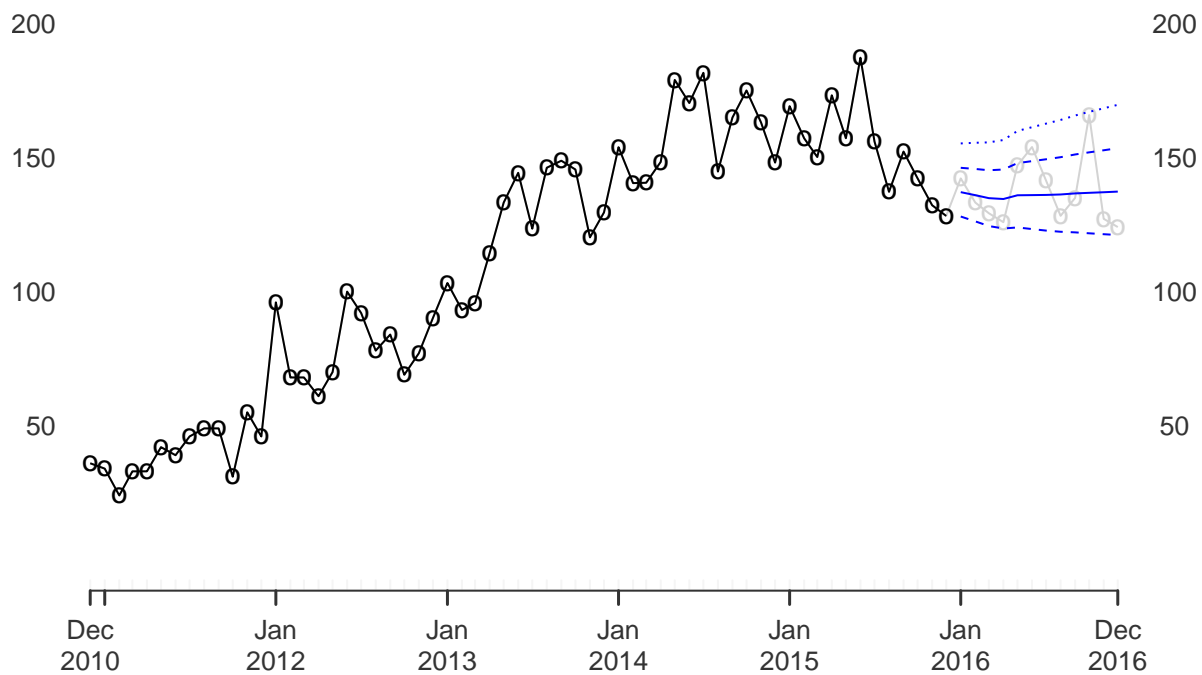
Dec 2010 / Dec 2016



```
lines(as.xts(ts(pred + 2*err, frequency = 12, start=2016)),col="blue", lty="dotted")
```

Number of Terrorist Attacks (Training Set)

Dec 2010 / Dec 2016



```
lines(as.xts(ts(pred - 2*err, frequency = 12, start=2016)),col="blue", lty="dotted")
```

Number of Terrorist Attacks (Training Set)

Dec 2010 / Dec 2016

