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feature --Commands
make (nor: INTEGER ; noc: STRING)
--Initialize a matrix with 'nor' rows and 'noc' columns.
ensure
  number_of_rows_initialized : number_of_rows = nor
  number_of_columns_initialized : number_of_columns = noc

make_from (lol : LINKED_LIST[LINKED_LIST[ENTRY]])
-- Initialize a matrix from a list of lists.
require
  non_empty_list_of_lists : not(lol.is_empty)
rectangle_shape :  $\forall i : 1 \leq i \leq lol.count \Rightarrow lol.at(i.item).count \sim lol.first.count$ 
ensure
  number_of_rows_initialized: number_of_rows = lol.count
  number_of_columns_initialized : number_of_columns = lol.first.count
  correct_contents :  $\forall i : 1 \leq i \leq lol.count ; \forall j : 1 \leq j \leq lol.first.count \Rightarrow lol.at(i.item).at(j.item) \sim current.get\_entry(i.item-1, j.item-1)$ 
feature -- Queries
scalar_multiply(scalar : INTEGER) : MATRIX
-- Obtain a new matrix by applying a scalar multiplication to the current matrix.
ensure
  current_matrix_unchanged :  $\forall x : 0 \leq i \leq (number\_of\_rows - 1) ; \forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow result.get\_entry(x.item,y.item) \sim result.deep\_twin.get\_entry(x.item,y.item)$ 
  same_dimension_sizes : Result.number_of_rows  $\sim$  old number_of_rows ^ Result.number_of_columns  $\sim$  old number_of_columns
  iv_of_each_entry_scaled :  $\forall x : 0 \leq i \leq (number\_of\_rows - 1) ; \forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow ((old\ current).get\_entry(x.item,y.item).iv * scalar) \sim (Result.get\_entry(x.item,y.item).iv)$ 
  sv_of_each_entry_scaled :  $\forall x : 0 \leq i \leq (number\_of\_rows - 1) ; \forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow ((old\ current).get\_entry(x.item,y.item).sv) \sim (Result.get\_entry(x.item,y.item).sv)$ 

transpose : MATRIX
-- Obtain a new matrix by applying taking the transpose of current matrix.
ensure
  current_matrix_unchanged :  $\forall x : 0 \leq i \leq (number\_of\_rows - 1) ; \forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow corresponding\_dimensions : Result.number\_of\_rows \sim old\ number\_of\_columns \wedge Result.number\_of\_columns \sim old\ number\_of\_rows$ 
  corresponding_dimensions : Result.number_of_rows  $\sim$  old number_of_columns and Result.number_of_columns  $\sim$  old number_of_rows
  corresponding_cells :  $\forall x : 0 \leq i \leq (number\_of\_rows - 1) ; \forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow current.get\_entry(i.item, j.item) \sim Result.get\_entry(j.item,i.item)$ 
feature --Queries
number_of_rows : INTEGER
-- Number of rows of current matrix.

number_of_columns : INTEGER
-- Number of columns of current matrix

number_of_entries : INTEGER
-- Number of entries stored in the current matrix.
ensure
number_of_entries : Result = number_of_columns * number_of_rows

set_entry(e : ENTRY ; row : INTEGER ; column : INTEGER )
-- Set entry at row 'row' and column 'column' to 'e'.
require
  valid_row : number_of_rows  $\geq$  row
  valid_column : number_of_columns  $\geq$  column
ensure
  designated_cell_changed : old get_entry(row, column)  $\neq$  current.get_entry(row, column)
  other_cells_unchanged :  $\forall x : 0 \leq i \leq (number\_of\_rows - 1) ; \forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow$  if  $x \sim (row + 1) \wedge y \sim (column + 1)$  then not ( ( old current ).get_entry( x.item , y.item )  $\sim$  current.get_entry( x.item , y.item ) ) else (old current).get_entry(x.item,y.item)  $\sim$  current.get_entry(x.item,y.item)
get_entry(row : INTEGER ; column : INTEGER) : ENTRY
-- Entry at row 'row' and column 'column'
require
  valid_row : number_of_rows  $\geq$  row
  valid_column : number_of_columns  $\geq$  column

get_row(i : INTEGER) : ARRAY[ENTRY]
-- Row 'i' as an array.
require
  valid_row : number_of_rows  $\geq$  i
ensure
  result_value_constraint : Result.lower = 1
  correct_result :  $\forall y : 0 \leq j \leq (number\_of\_columns - 1) \Rightarrow get\_entry(i,j.item) \sim Result.at(j.item+1)$ 
get_column(i : INTEGER) : LINKED_LIST[ENTRY]
-- Column 'i' as a linked list.
require
  valid_column : number_of_columns  $\geq$  i
ensure
  correct_result :

feature --Equality
is_equal(other : like current) : BOOLEAN
ensure then
  equal_means_same_dimension_sizes : (oldnumber_of_columns)  $\sim$  current.number_of_columns ^ (old number_of_rows)  $\sim$  current.number_of_rows
  equal_means_corresponding_entries_equal :

invariant
implementation_constraint : imp.lower = 1
at_least_1_by_1 : number_of_entries  $\geq$  1
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