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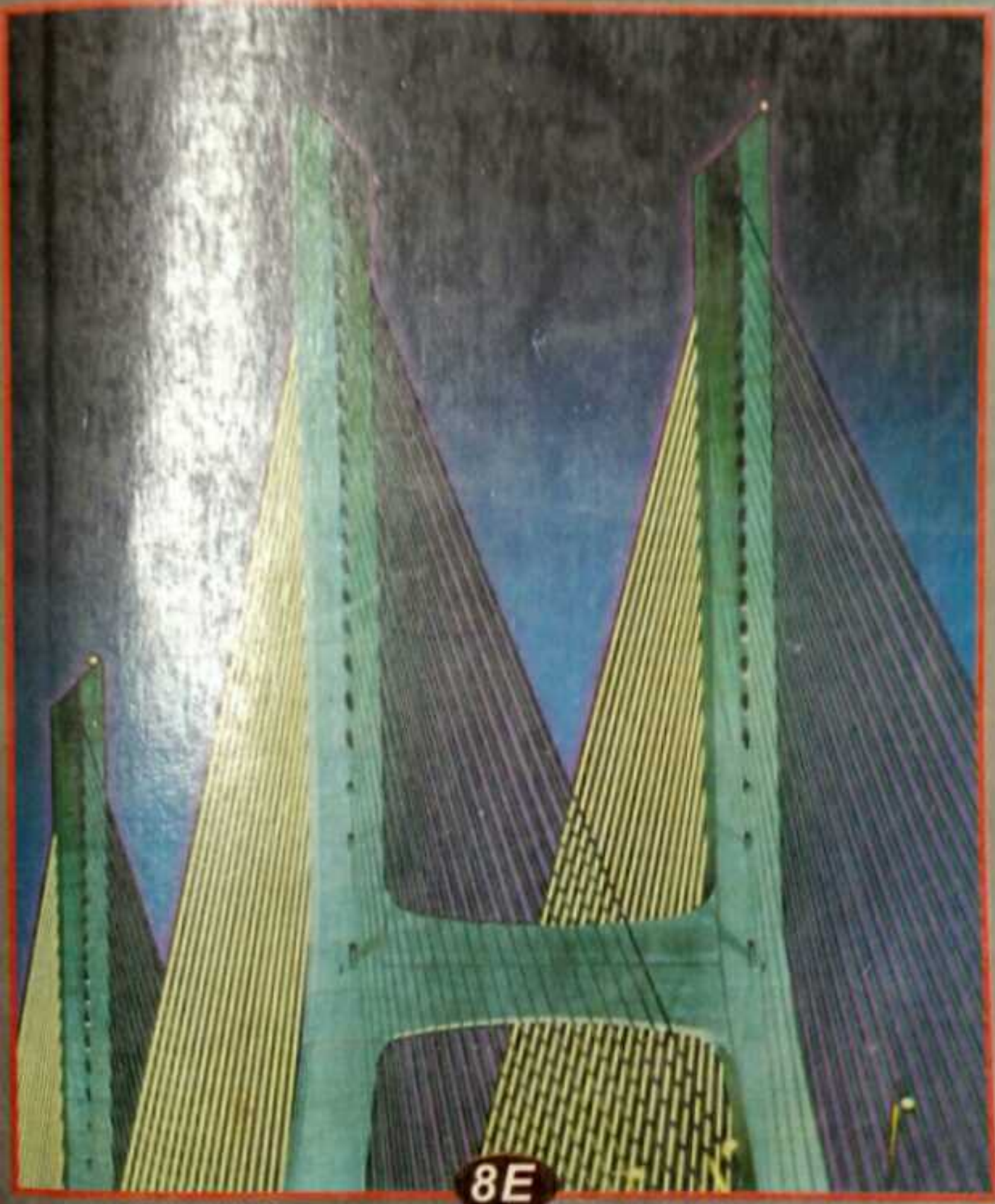

8E

Elementary Linear Algebra

APPLICATIONS VERSION

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