

INTERNATIONAL Edition

DISCRETE
**MATHEMATICAL
STRUCTURES**

4th
EDITION



KOLMAN

| BUSBY

| ROSS

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