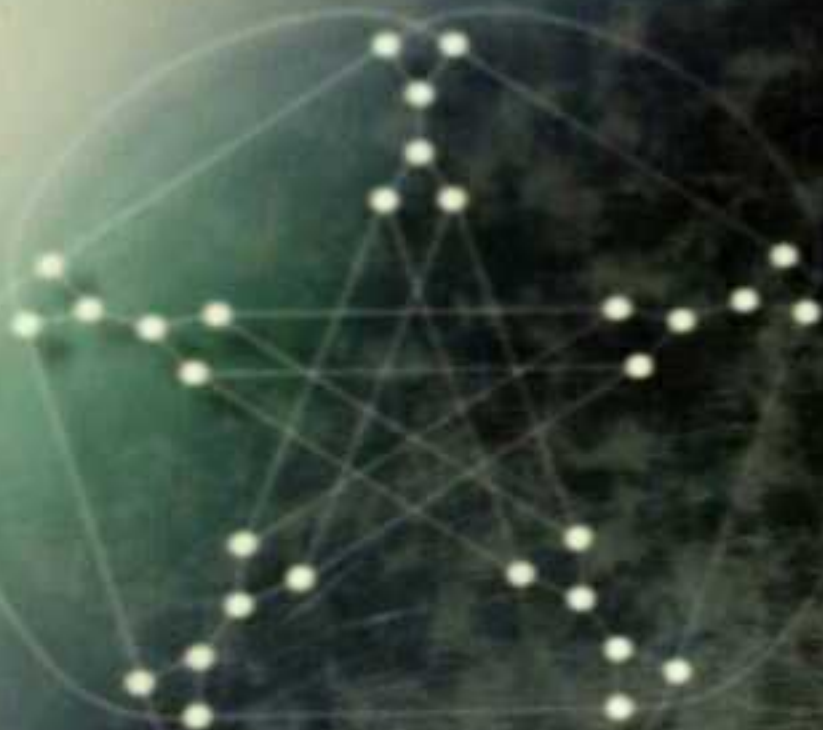


GRAPHS & DIGRAPHS

FIFTH EDITION



GARY CHARTRAND
LINDA LESNIAK
PING ZHANG



CRC Press
Taylor & Francis Group

A CHAPMAN & HALL BOOK

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Table of Contents

Preface to the Fifth Edition	xi
1. Introduction to Graphs	1
1.1 Graphs and Subgraphs	1
1.2 Degree Sequences	22
1.3 Connected Graphs and Distance	30
1.4 Multigraphs and Digraphs	45
2. Trees and Connectivity	55
2.1 Nonseparable Graphs	55
2.2 Trees	61
2.3 Spanning Trees	69
2.4 Connectivity and Edge-Connectivity	89
2.5 Menger's Theorem	97
3. Eulerian and Hamiltonian Graphs	107
3.1 Eulerian Graphs	107
3.2 Hamiltonian Graphs	115
3.3 Powers of Graphs and Line Graphs	137
4. Digraphs	149
4.1 Strong Digraphs	149
4.2 Tournaments	156
4.3 Flows in Networks	171
5. Graphs: History and Symmetry	195
5.1 Some Historical Figures of Graph Theory	195
5.2 The Automorphism Group of a Graph	201
5.3 Cayley Color Graphs	206
5.4 The Reconstruction Problem	212
6. Planar Graphs	221
6.1 The Euler Identity	221
6.2 Planarity versus Nonplanarity	235
6.3 The Crossing Number of a Graph	250
6.4 Hamiltonian Planar Graphs	263

7. Graph Embeddings	285
7.1 The Genus of a Graph	285
7.2 2-Cell Embeddings of Graphs	285
7.3 The Maximum Genus of a Graph	285
7.4 The Graph Minor Theorem	285
8. Vertex Colorings	311
8.1 The Chromatic Number of a Graph	311
8.2 Color-Critical Graphs	311
8.3 Bounds for the Chromatic Number	323
8.4 Perfect Graphs	327
8.5 List Colorings	340
9. Map Colorings	353
9.1 The Four Color Problem	353
9.2 Colorings of Planar Graphs	375
9.3 The Conjectures of Hajós and Hadwiger	384
9.4 Chromatic Polynomials	388
9.5 The Heawood Map-Coloring Problem	395
10. Matchings, Factorization and Domination	401
10.1 Matchings and Independence in Graphs	401
10.2 Factorization	419
10.3 Decomposition and Graceful Graphs	427
10.4 Domination	438
11. Edge Colorings	447
11.1 Chromatic Index and Vizing's Theorem	447
11.2 Class One and Class Two Graphs	456
11.3 Tait Colorings	464
11.4 Nowhere-Zero Flows	473
11.5 List Edge Colorings and Total Colorings	484
12. Extremal Graph Theory	493
12.1 Turán's Theorem	493
12.2 Cages	499
12.3 Ramsey Theory	508

Hints and Solutions to Odd-Numbered Exercises	523
Bibliography	547
Index of Names	565
Index of Mathematical Terms	571
List of Symbols	583