

Third Edition

DISCRETE MATHEMATICAL STRUCTURES



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Don't learn by heart Theorems
They are included but may be
proved by any e.g.:-

CONTENTS

Preface xiii

1 Fundamentals 1

- 1.1 Sets and Subsets 1
- 1.2 Operations on Sets 5
- 1.3 Sequences 14
- 1.4 Division in the Integers 22
- 1.5 Matrices 30
- 1.6 Mathematical Structures 39

2 Logic 46

- 2.1 Propositions and Logical Operations 46
- 2.2 Conditional Statements 52
- 2.3 Methods of Proof 58
- 2.4 Mathematical Induction 64

3 Counting 72

- 3.1 Permutations 72
- 3.2 Combinations 78
- 3.3 The Pigeonhole Principle 82
- 3.4 Elements of Probability 85
- 3.5 Recurrence Relations 95

4 Relations and Digraphs 101

- 4.1 Product Sets and Partitions 101
- 4.2 Relations and Digraphs 106
- 4.3 Paths in Relations and Digraphs 116
- 4.4 Properties of Relations 124
- 4.5 Equivalence Relations 131
- 4.6 Computer Representation of Relations and Digraphs 136
- 4.7 Manipulation of Relations 146
- 4.8 Transitive Closure and Warshall's Algorithm 157

5 Functions 167

- 5.1 Functions 167
- 5.2 Functions for Computer Science 177
- 5.3 Permutation Functions 181
- 5.4 Growth of Functions 190

6 Topics in Graph Theory 197

- 6.1 Graphs 197
- 6.2 Euler Paths and Circuits 204
- 6.3 Hamiltonian Paths and Circuits 213
- 6.4 Coloring Graphs 218

7 Order Relations and Structures 225

- 7.1 Partially Ordered Sets 225
- 7.2 Extremal Elements of Partially Ordered Sets 239
- 7.3 Lattices 246
- 7.4 Finite Boolean Algebras 259
- 7.5 Functions on Boolean Algebras 266
- 7.6 Boolean Functions as Boolean Polynomials 271

8 Trees 286

- ✓ 8.1 Trees 286 + spanning trees
- ✓ 8.2 Labeled Trees 292
- ✓ 8.3 Tree Searching 299
- ✗ 8.4 Undirected Trees 310
- ✗ 8.5 Minimal Spanning Trees 321

9 Semigroups and Groups 329

- ✓ 9.1 Binary Operations Revisited 329
- ✓ 9.2 Semigroups 334
- ✗ 9.3 Products and Quotients of Semigroups 342
- ✗ 9.4 Groups 349
- ✗ 9.5 Products and Quotients of Groups 361

10 Languages and Finite-State Machines 368

- ✗ 10.1 Languages 368
- ✗ 10.2 Representations of Special Languages and Grammars 378
- ✗ 10.3 Finite-State Machines 391
- ✗ 10.4 Semigroups, Machines, and Languages 398
- ✗ 10.5 Machines and Regular Languages 404
- ✗ 10.6 Simplification of Machines 412

11 Groups and Coding 420

- ✗ 11.1 Coding of Binary Information and Error Detection 420
- ✗ 11.2 Decoding and Error Correction 432

Appendix A Algorithms and Pseudocode 444

Appendix B Experiments in Discrete Mathematics 458

Answers to Odd-Numbered Exercises 477

Index 513