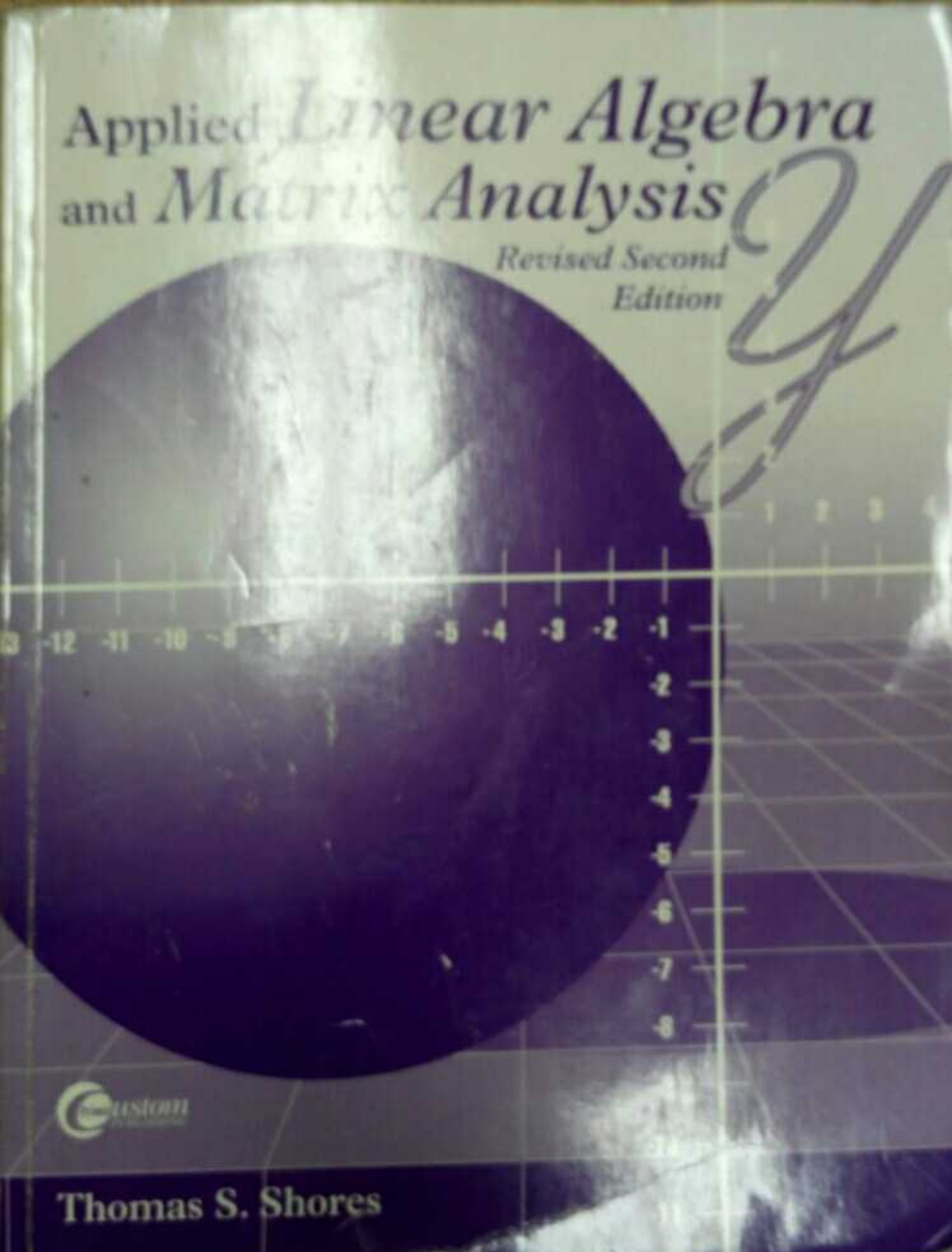
# Applied Linear Algebra and Matrix Analysis

*Revised Second Edition*



**Thomas S. Shores**

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