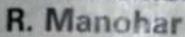
## Discrete Mathematical Structures with Applications to Computer Science

J. P. Tremblay







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