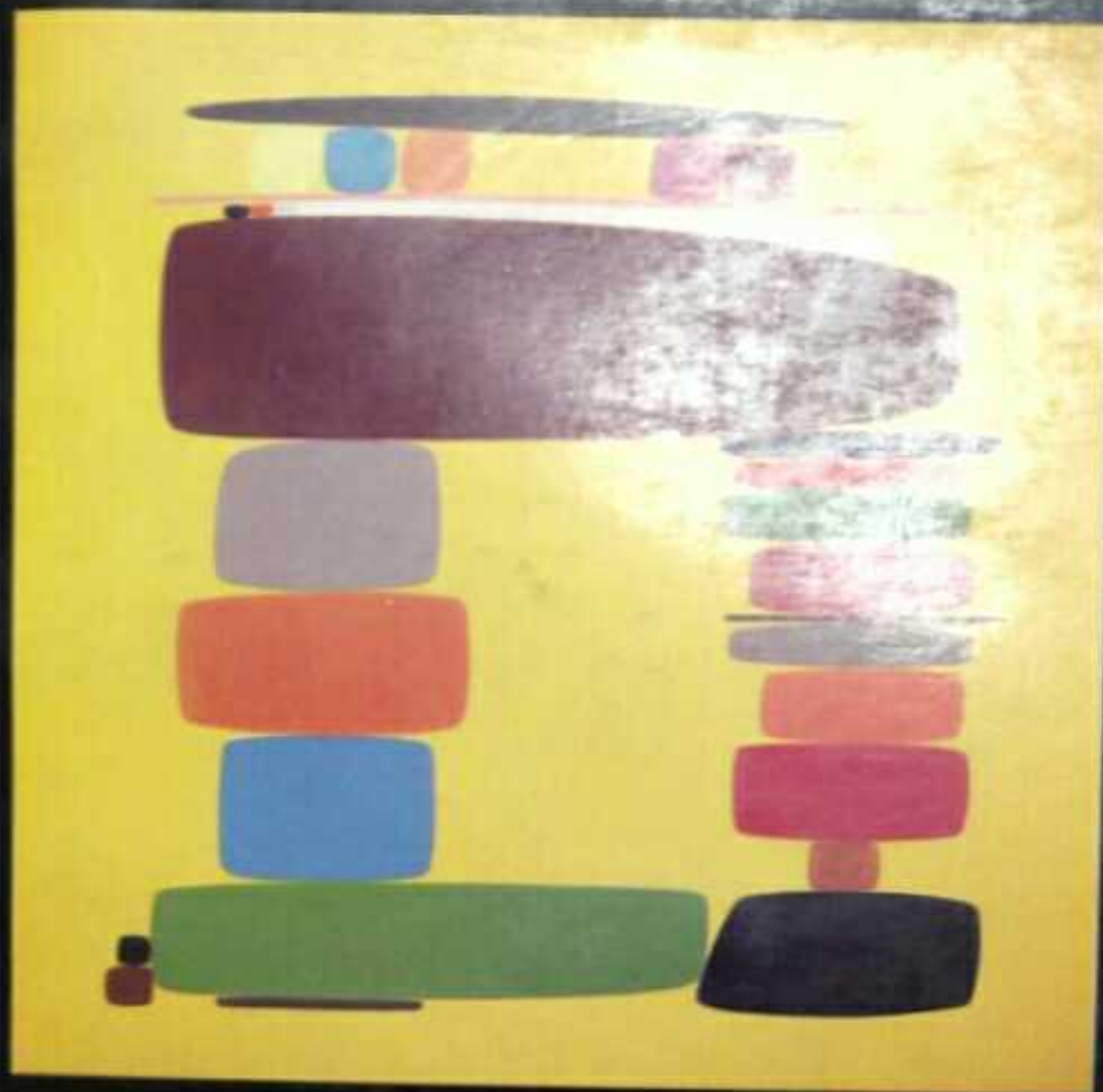


Eastern
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DISCRETE MATHEMATICAL STRUCTURES

5TH EDITION



KOLMAN
BUSBY
ROSS



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