

International Student Edition

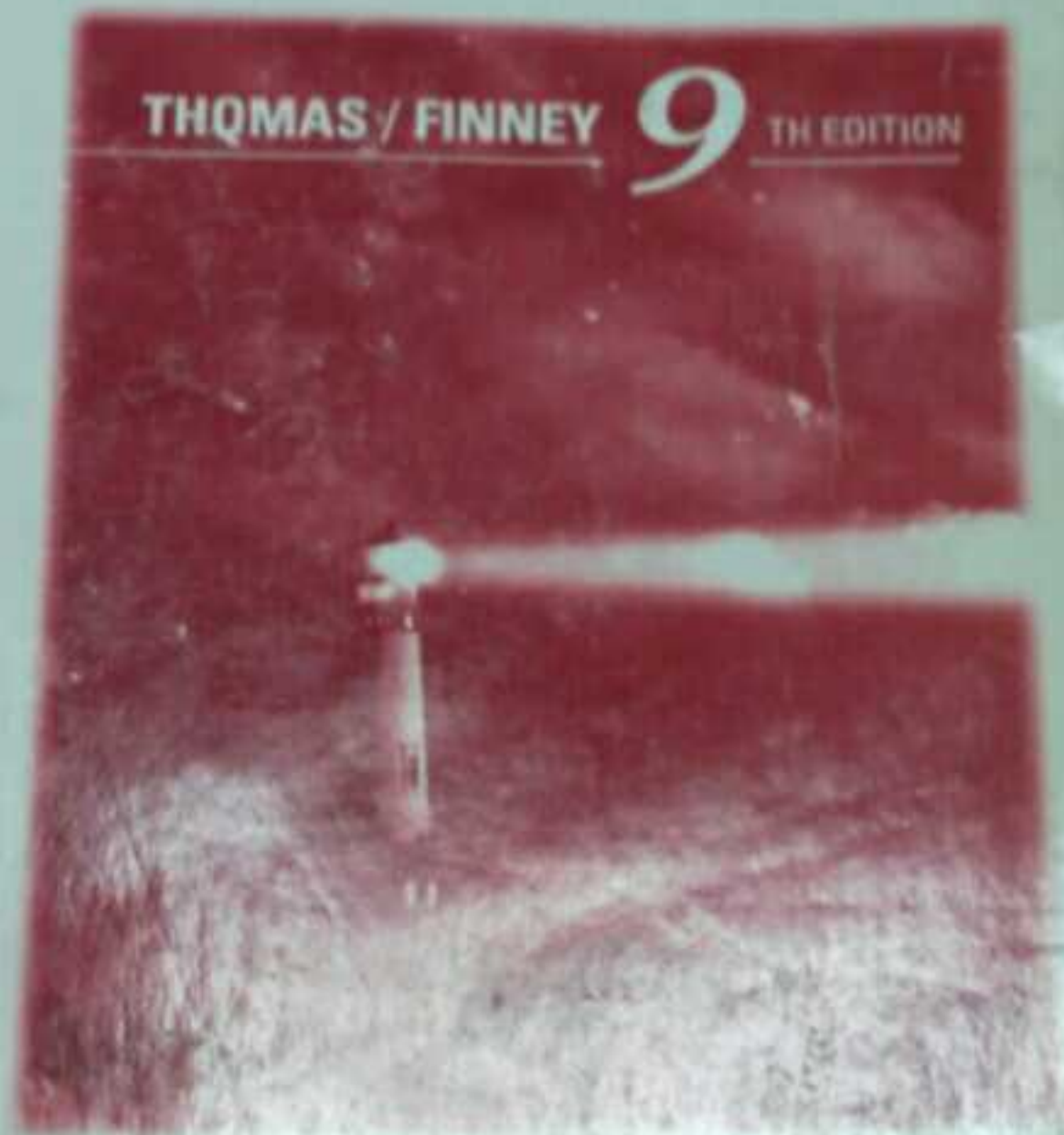
CALCULUS AND ANALYTIC GEOMETRY

NINTH EDITION

THOMAS / FINNEY

9

TH EDITION



THOMAS / FINNEY

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