

Grade 10 - Exponents:

Interactive 6: Fractions – Addition & subtraction, multiplication & division

(More advanced. Apply all exponent laws)

Screen	Question	Solution	3 wrong answer options
1	Simplify: $\frac{2^{n+2} - 2^{n+1}}{2^n}$	$\frac{2^{n+2} - 2^{n+1}}{2^n}$ $= \frac{2^n(2^2 - 2^1)}{2^n}$ $= 4 - 2$ $= 2$	2^n
			4
			1
	Simplify: $\frac{3^x - 3^{x-1}}{3^{x+2}}$	$\frac{3^x - 3^{x-1}}{3^{x+2}}$ $= \frac{3^x(1 - 3^{-1})}{3^x 3^2}$ $= \frac{2}{9}$ $= \frac{2}{27}$	$\frac{8}{9}$
			$\frac{1}{9}$
			$\frac{8}{27}$
	Simplify: $\frac{3^x - 3^{x-2}}{3^{x-2}}$	$\frac{3^x - 3^{x-2}}{3^{x-2}}$ $= \frac{3^x(1 - 3^{-2})}{3^x 3^{-2}}$ $= \frac{8}{9}$ $= \frac{1}{9}$ $= 8$	$\frac{8}{9}$
			$\frac{1}{9}$
			9

2	Simplify: $\frac{3 \cdot 2^n - 2^{n-2}}{2^{n+1}}$	$\frac{3 \cdot 2^n - 2^{n-2}}{2^{n+1}}$ $= \frac{2^n(3 - 2^{-2})}{2^n 2^1}$ $= \frac{2 \frac{3}{4}}{2}$ $= \frac{11}{8}$	$\frac{14}{8}$
			$\frac{11}{4}$
			$\frac{11}{2}$
	Simplify: $\frac{3^n - 3^{n+2}}{3^n}$	$\frac{3^n - 3^{n+2}}{3^n}$ $= \frac{3^n - 3^n 3^2}{3^n}$ $= 1 - 9$ $= -8$	8
			$\frac{1}{8}$
			10
	Simplify: $\frac{x^{n+1} - x^n}{x - 1}$	$\frac{x^{n+1} - x^n}{x - 1}$ $= \frac{x^n x^1 - x^n}{x - 1}$ $= x^n$	x^{2n}
			x^{n-1}
			x

3	Simplify: $\frac{3^{n+4} - 6 \cdot 3^{n+1}}{3^{n+3} + 2 \cdot 9^{\frac{1}{2}n+1}}$	$\frac{3^{n+4} - 6 \cdot 3^{n+1}}{3^{n+3} + 2 \cdot 9^{\frac{1}{2}n+1}}$ $= \frac{3^{n+1}(3^3 - 6)}{3^{n+1}(3^2 + 2 \cdot 3^1)}$ $= \frac{21}{15}$ $= \frac{7}{5}$	7
			5
			$\frac{4}{3}$
	Simplify: $\frac{2^{2n+1} - 2^{2n}}{4^n + 2^{2n-1}}$	$\frac{2^{2n+1} - 2^{2n}}{4^n + 2^{2n-1}}$ $= \frac{2^{2n}2^1 - 2^{2n}}{2^{2n} + 2^{2n}2^{-1}}$ $= \frac{1}{\frac{3}{2}}$ $= \frac{2}{3}$	$\frac{3}{2}$
			$\frac{1}{2}$
			$\frac{1}{3}$
	Simplify: $\frac{5 \cdot 2^x - 4 \cdot 2^{x-2}}{2^x - 2^{x-1}}$	$\frac{5 \cdot 2^x - 4 \cdot 2^{x-2}}{2^x - 2^{x-1}}$ $= \frac{5 \cdot 2^x - 2^2 \cdot 2^x 2^{-2}}{2^x - 2^x 2^{-1}}$ $= \frac{5 - 1}{1 - \frac{1}{2}}$ $= \frac{4}{\frac{1}{2}}$ $= 8$	4
			2
			$\frac{1}{8}$

4	Simplify: $\frac{5^{2x-1} \cdot 9^{x-2}}{15^{2x-3}}$	$\frac{5^{2x-1} \cdot 9^{x-2}}{15^{2x-3}}$ $= \frac{5^{2x-1} \cdot (3^2)^{x-2}}{(5 \cdot 3)^{2x-3}}$ $= \frac{5^{2x-1} 3^{2x-4}}{5^{2x-3} 3^{2x-3}}$ $= 5^{2x-1-2x+3} 3^{2x-4-2x+3}$ $= 5^2 \cdot 3^{-1}$ $= \frac{25}{3}$	15
			75
			125
	Simplify: $\frac{2^{n+1} \cdot 3^{n-1}}{6^n}$	$\frac{2^{n+1} \cdot 3^{n-1}}{6^n}$ $= \frac{2^{n+1} 3^{n-1}}{2^{n+1} 3^n}$ $= \frac{2^n 3^n}{2^{n+1} 3^n}$ $= 2^{n+1-n} 3^{n-1-n}$ $= 2 \cdot 3^{-1}$ $= \frac{2}{3}$	6
			$\frac{3}{2}$
			$\frac{1}{6}$
	Simplify: $\frac{125^x \cdot 25^{x+1}}{5^{5x+3}}$	$\frac{125^x \cdot 25^{x+1}}{5^{5x+3}}$ $= \frac{5^{3x} \cdot 5^{2x+2}}{5^{5x+3}}$ $= 5^{3x+2x+2-5x-3}$ $= 5^{-1}$ $= \frac{1}{5}$	5
			-5
			25

5	<p>Simplify:</p> $\frac{45^{x-3} \cdot 3 \cdot 75^{4-x}}{25^{-x} \cdot 15^{x+2}}$	$\frac{45^{x-3} \cdot 3 \cdot 75^{4-x}}{25^{-x} \cdot 15^{x+2}}$ $= \frac{(5 \cdot 3^2)^{x-3} \cdot 3 \cdot (3 \cdot 5^2)^{4-x}}{(5^2)^{-x} \cdot (3 \cdot 5)^{x+2}}$ $= \frac{5^{x-3} \cdot 3^{2x-6} \cdot 3 \cdot 3^{4-x} \cdot 5^{8-2x}}{5^{x-3+8-2x+2x-x-2} \cdot 3^{2x-6+1+4-x-x-2}}$ $= \frac{5^{-2x} \cdot 3^{x+2} \cdot 5^{x+2}}{5^{x-3+8-2x+2x-x-2} \cdot 3^{2x-6+1+4-x-x-2}}$ $= 5^3 \cdot 3^{-3}$ $= \frac{125}{27}$	$\frac{25}{9}$ $\frac{125}{27}$ $\frac{25}{3}$
	<p>Simplify:</p> $\frac{\sqrt[3]{a} \times \sqrt{m^3}}{a^{-\frac{2}{3}} m^{\frac{1}{2}}}$	$\frac{\sqrt[3]{a} \times \sqrt{m^3}}{a^{-\frac{2}{3}} m^{\frac{1}{2}}}$ $= \frac{a^{\frac{1}{3}} m^{\frac{3}{2}}}{a^{-\frac{2}{3}} m^{\frac{1}{2}}}$ $= a^{\frac{1}{3} + \frac{2}{3}} m^{\frac{3}{2} - \frac{1}{2}}$ $= am$	$\frac{2am}{am^2}$ a^2m
	<p>Simplify:</p> $\frac{6^{x+1} \times 9^{x-1}}{2^x \times 27^x}$	$\frac{6^{x+1} \times 9^{x-1}}{2^x \times 27^x}$ $= \frac{2^x \times 27^x}{2^{x+1} 3^{x+1} 3^{2x-2}}$ $= \frac{2^x 3^{3x}}{2^{x+1-x} 3^{x+1+2x-2-3x}}$ $= 2 \cdot 3^{-1}$ $= \frac{2}{3}$	$\frac{3}{2}$ $\frac{6}{2}$ $\frac{2}{9}$