



## INTRODUCTION TO LINEAR MODELING IN PYTHON

# Modeling Real Data

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# Scikit-Learn

```
from sklearn.linear_model import LinearRegression
```

```
# Initialize a general model  
model = LinearRegression(fit_intercept=True)
```

```
# Load and shape the data  
x_raw, y_raw = load_data()  
x_data = x_raw.reshape(len(y_raw), 1)  
y_data = y_raw.reshape(len(y_raw), 1)
```

```
# Fit the model to the data  
model_fit = model.fit(x_data, y_data)
```



# Predictions and Parameters

```
# Extract the linear model parameters
intercept = model.intercept_[0]
slope = model.coef_[0,0]
```

```
# Use the model to make predictions
future_x = 2100
future_y = model.predict(future_x)
```



# statsmodels

```
x, y = load_data()  
df = pd.DataFrame(dict(times=x_data, distances=y_data))
```

```
fig = df.plot('times', 'distances')
```

```
model_fit = ols(formula="distances ~ times", data=df).fit()
```



# Uncertainty

```
a0 = model_fit.params['Intercept']  
a1 = model_fit.params['times']
```

```
e0 = model_fit.bse['Intercept']  
e1 = model_fit.bse['times']
```

```
intercept = a0  
slope = a1  
uncertainty_in_intercept = e0  
uncertainty_in_slope = e1
```



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**Let's practice!**



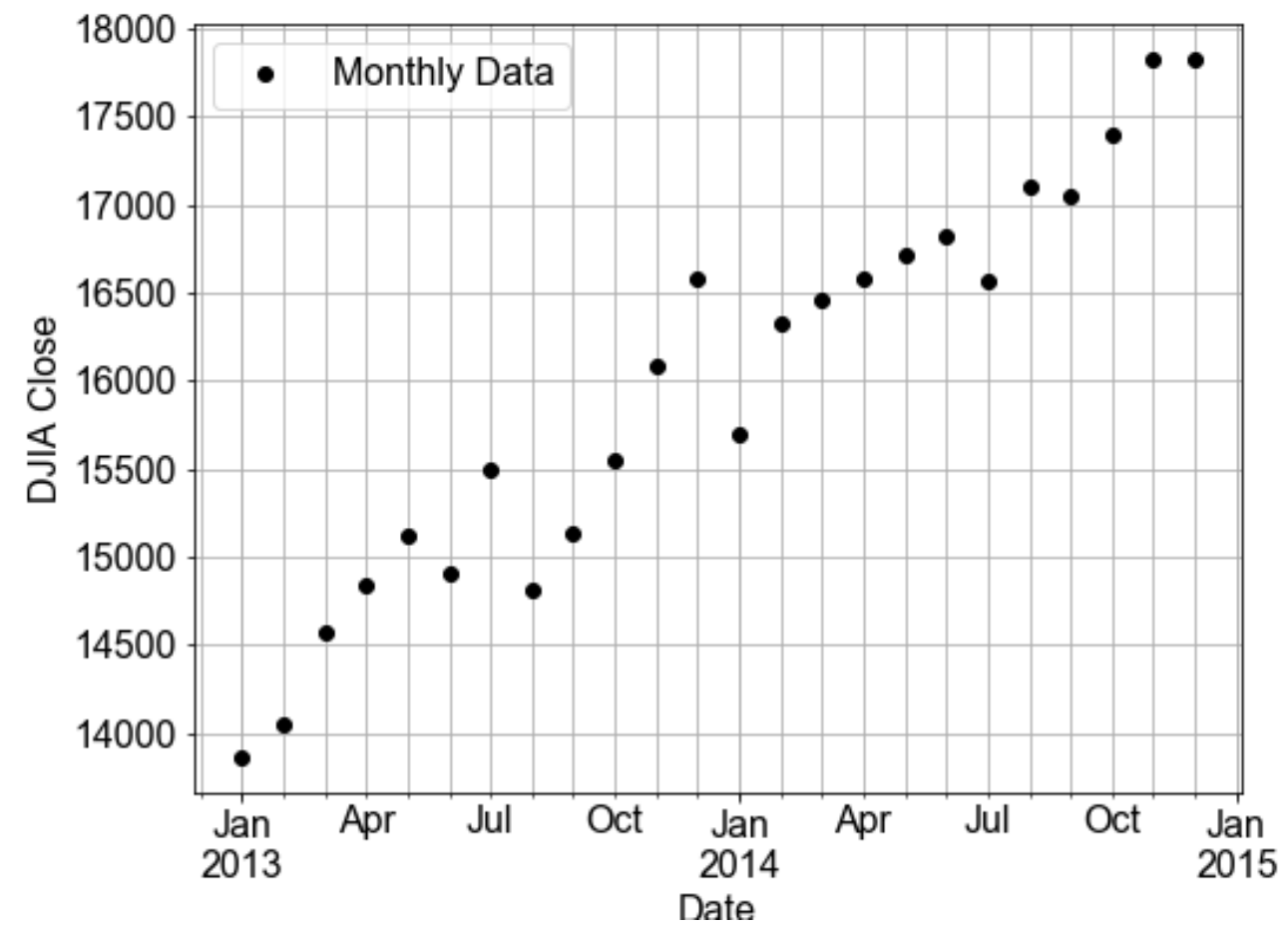
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# The Limits of Prediction

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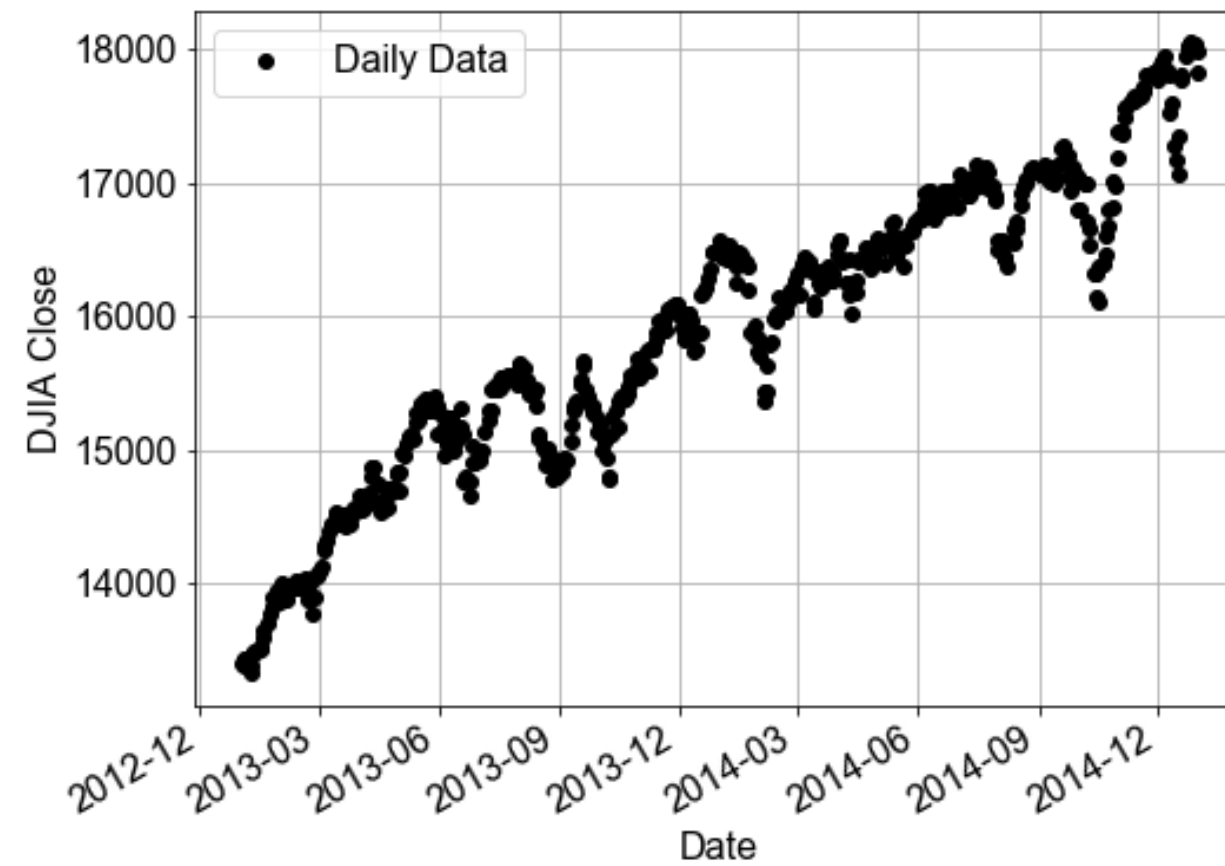
# Interpolation





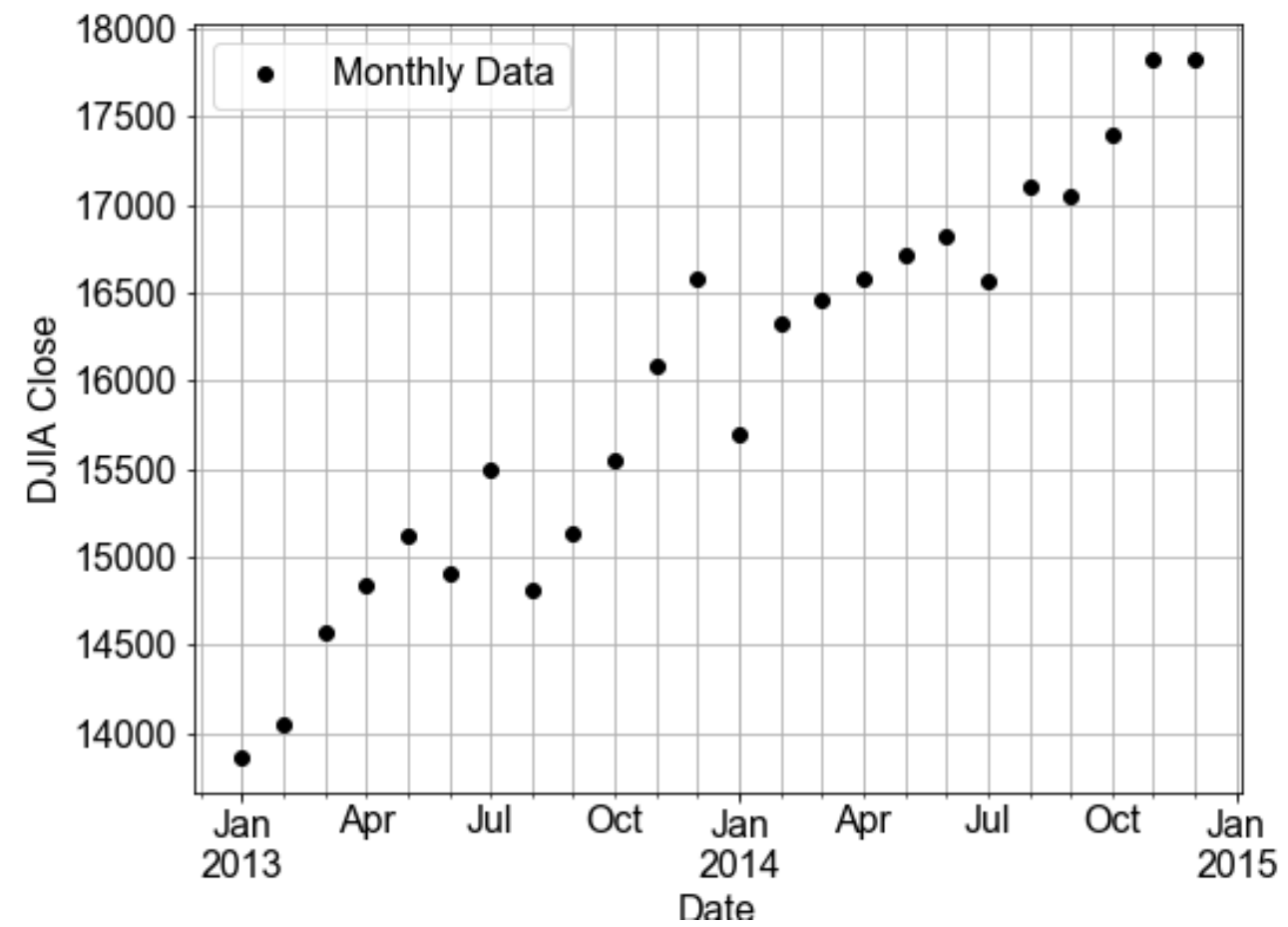


# Interpolation



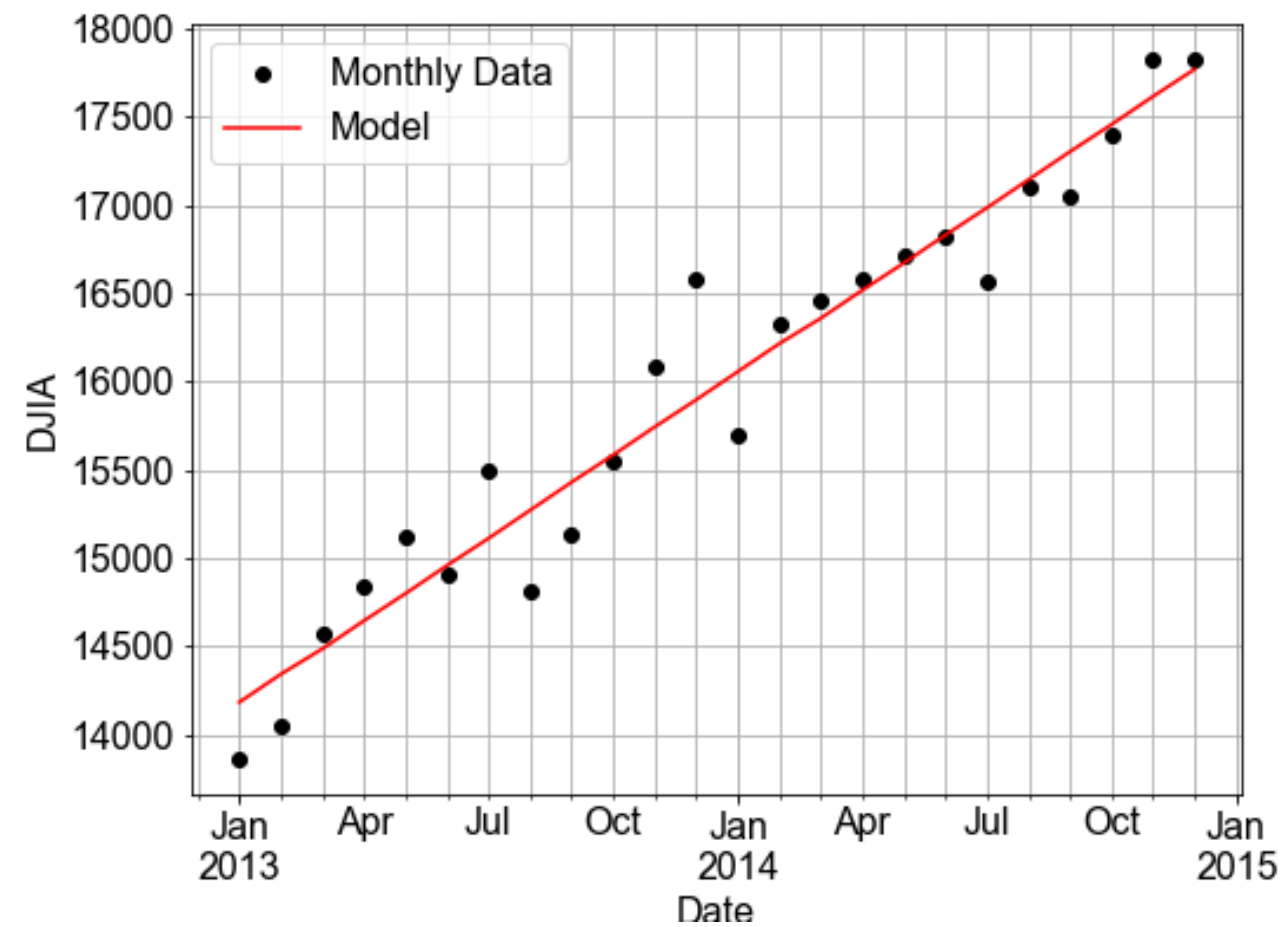


# Interpolation



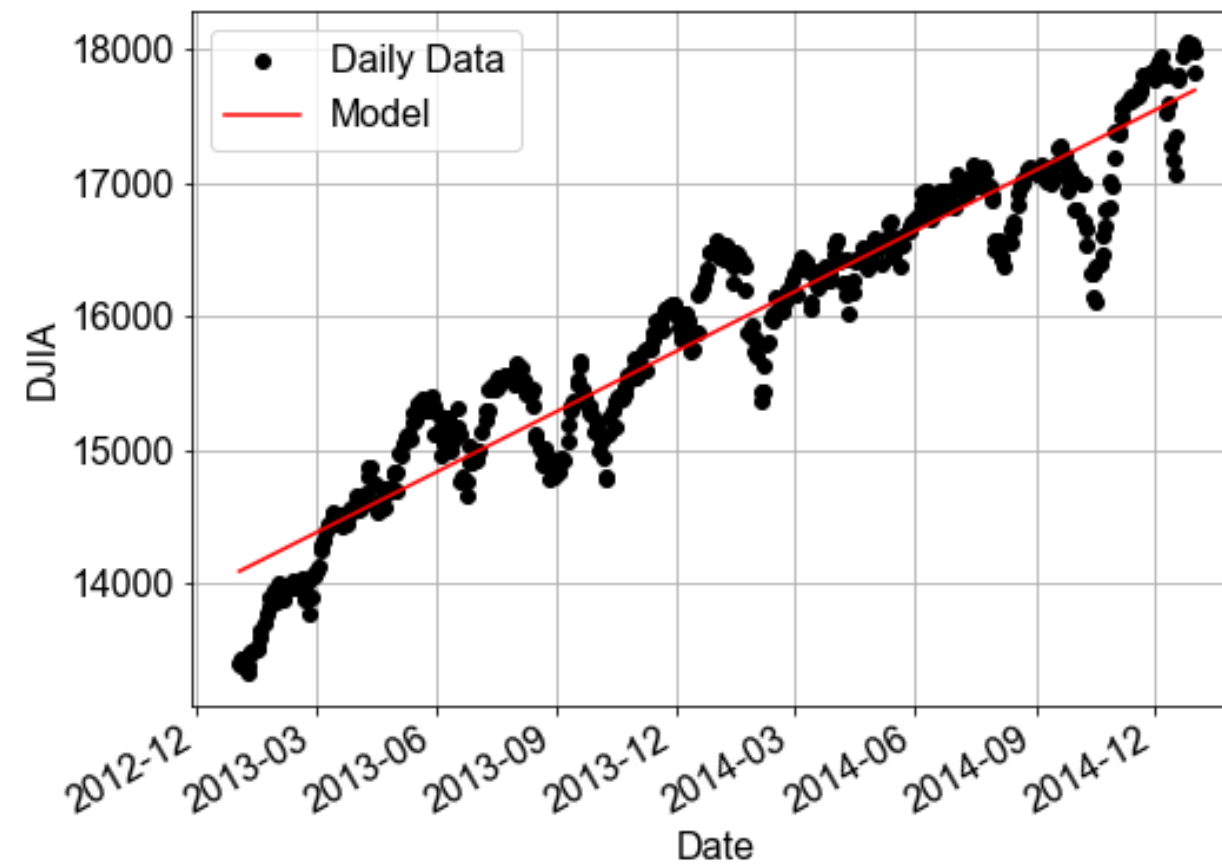


# Interpolation





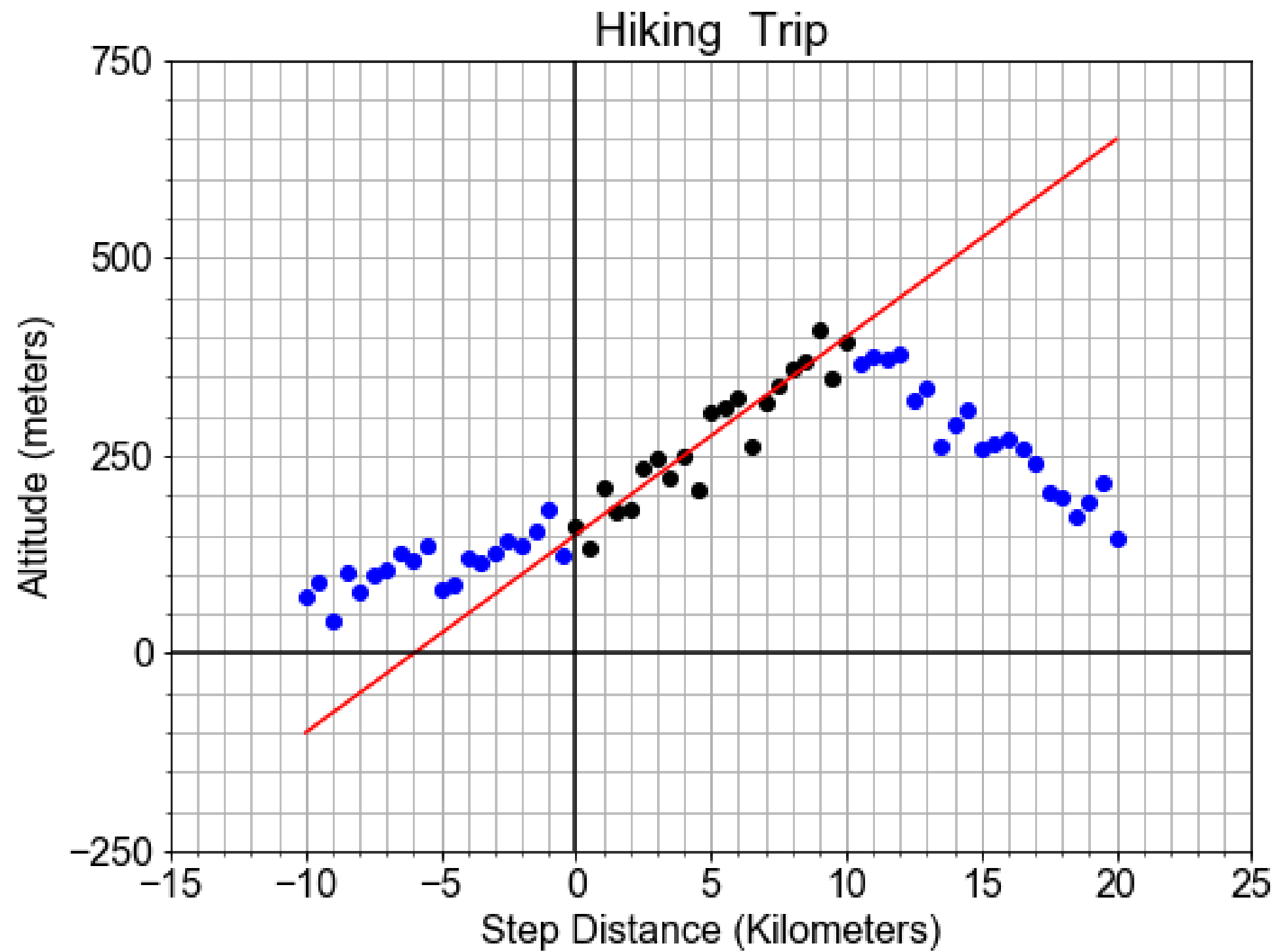
# Interpolation





# Domain of Validity

- zoom in: data looks linear
- model assumption:  $a_2 * x^{**2} + a_3 * x^{**3} + \dots = \text{zero}$ .
- build a linear model:  $a_0 + a_1 * x$
- zoom out: your model breaks





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# Goodness-of-Fit

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# 3 Different R's

Building Models:

- RSS

Evaluating Models:

- RMSE
- R-squared



# RMSE

```
residuals = y_model - y_data  
RSS = np.sum( np.square(residuals) )
```

```
mean_squared_residuals = np.sum( np.square(residuals) ) / len(residuals)
```

```
MSE = np.mean( np.square(residuals) )
```

```
RMSE = np.sqrt(np.mean( np.square(residuals)))
```

```
RMSE = np.std(residuals)
```



# R-Squared in Code

## Deviations:

```
deviations = np.mean(y_data) - y_data  
VAR = np.sum(np.square(deviations))
```

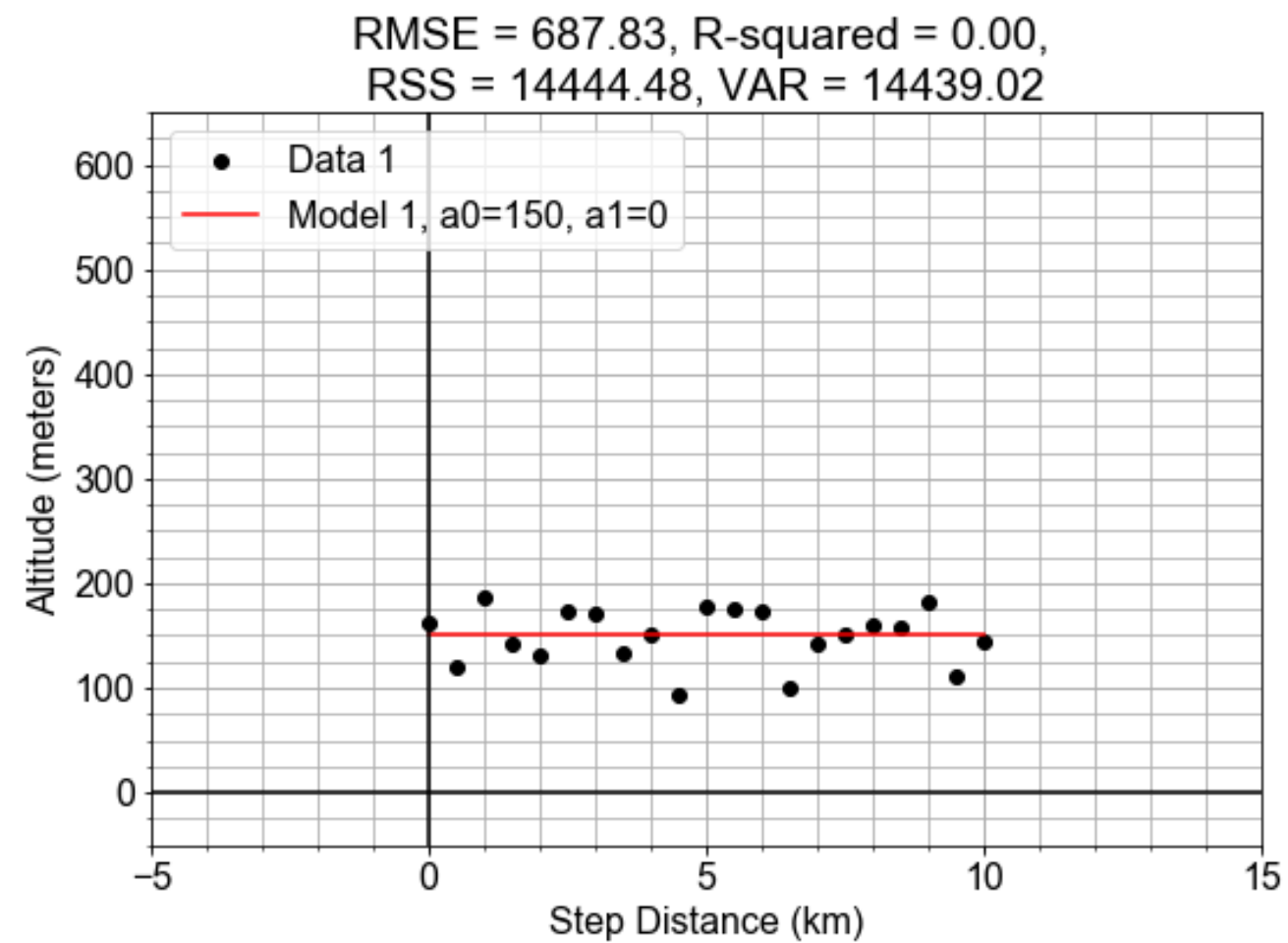
## Residuals:

```
residuals = y_model - y_data  
RSS = np.sum(np.square(residuals))
```

## R-squared:

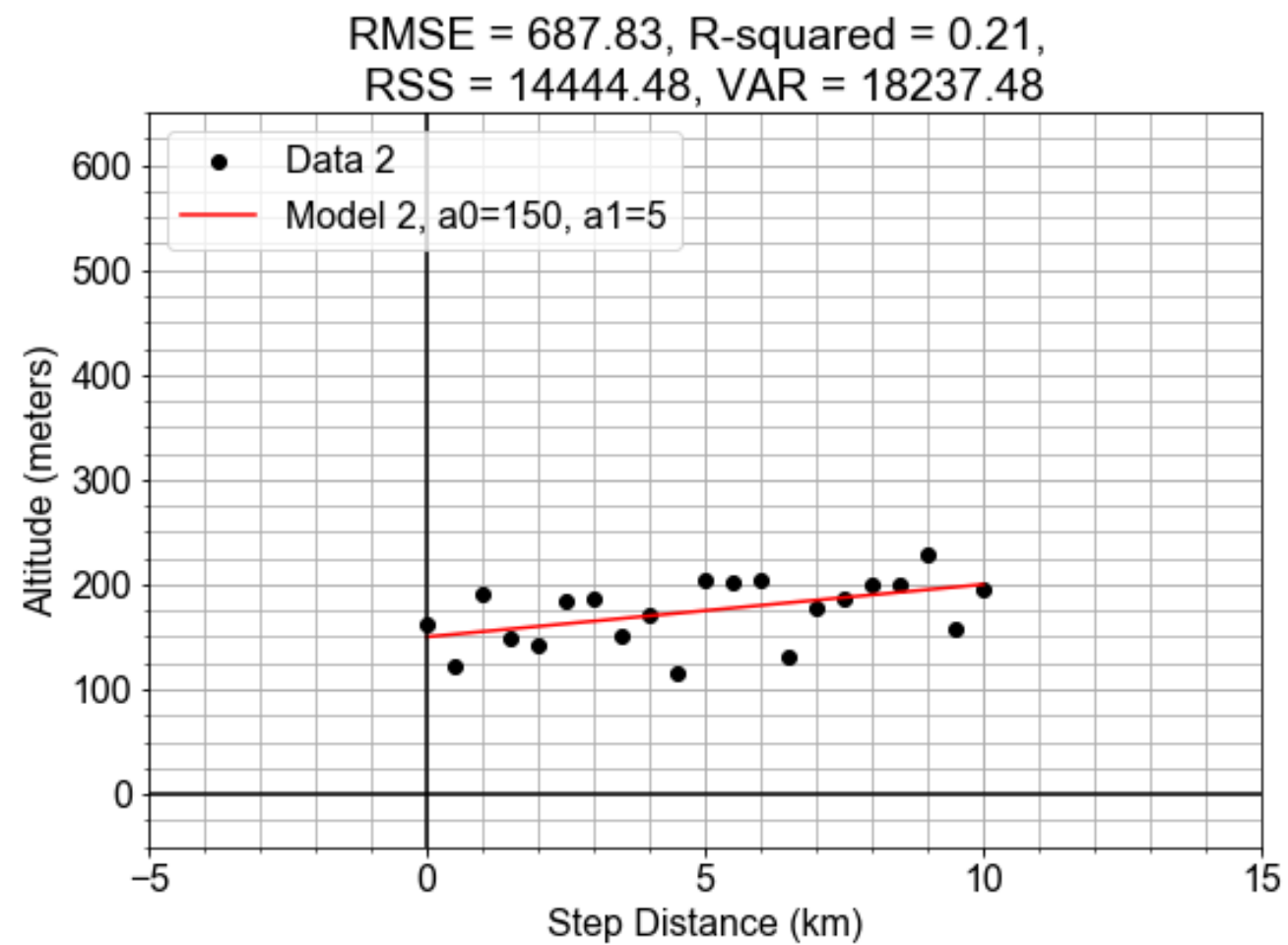
```
r_squared = 1 - (RSS / VAR)  
r = correlation(y_data, y_model)
```

# R-Squared in Data



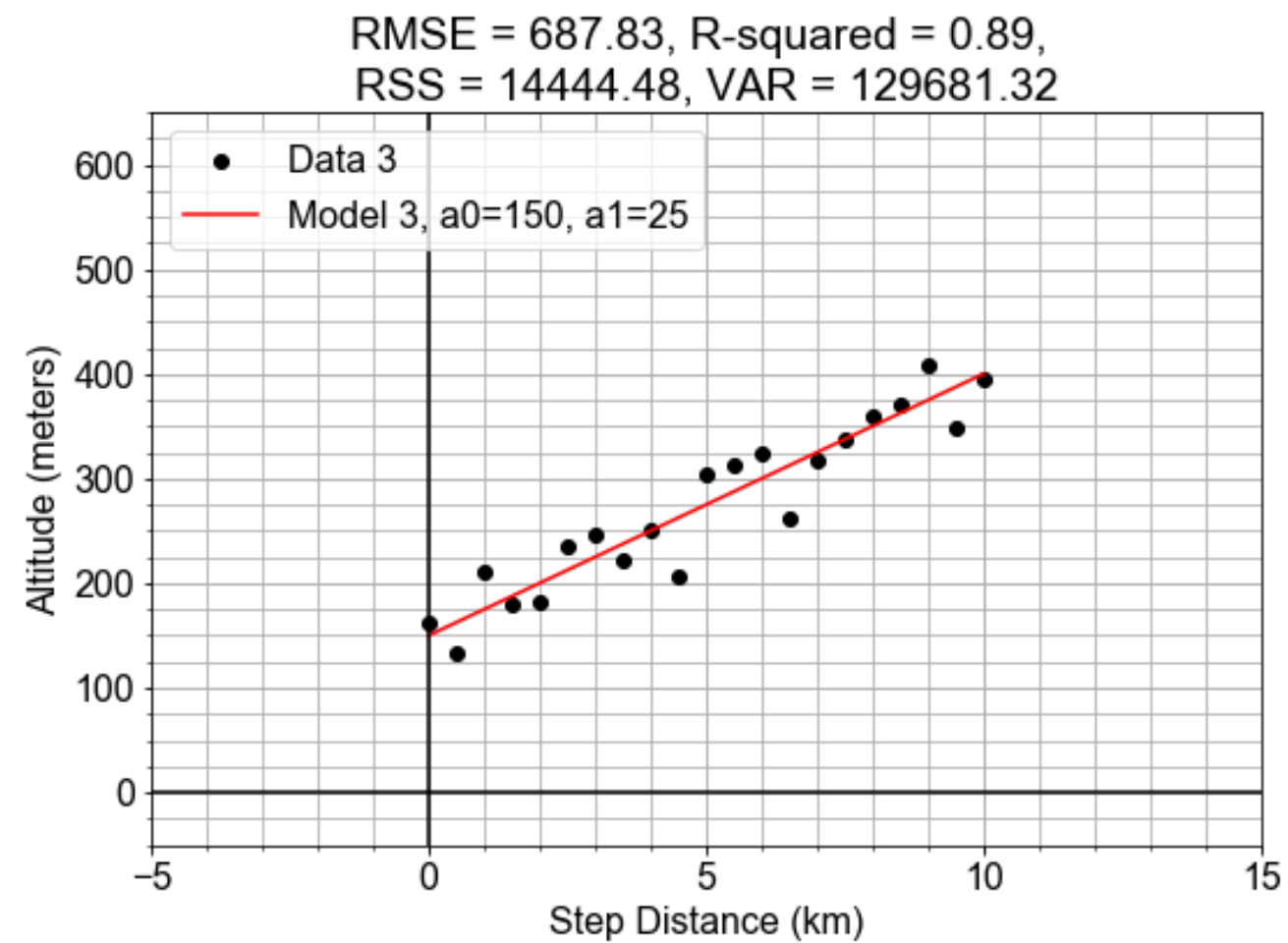


# R-Squared in Data



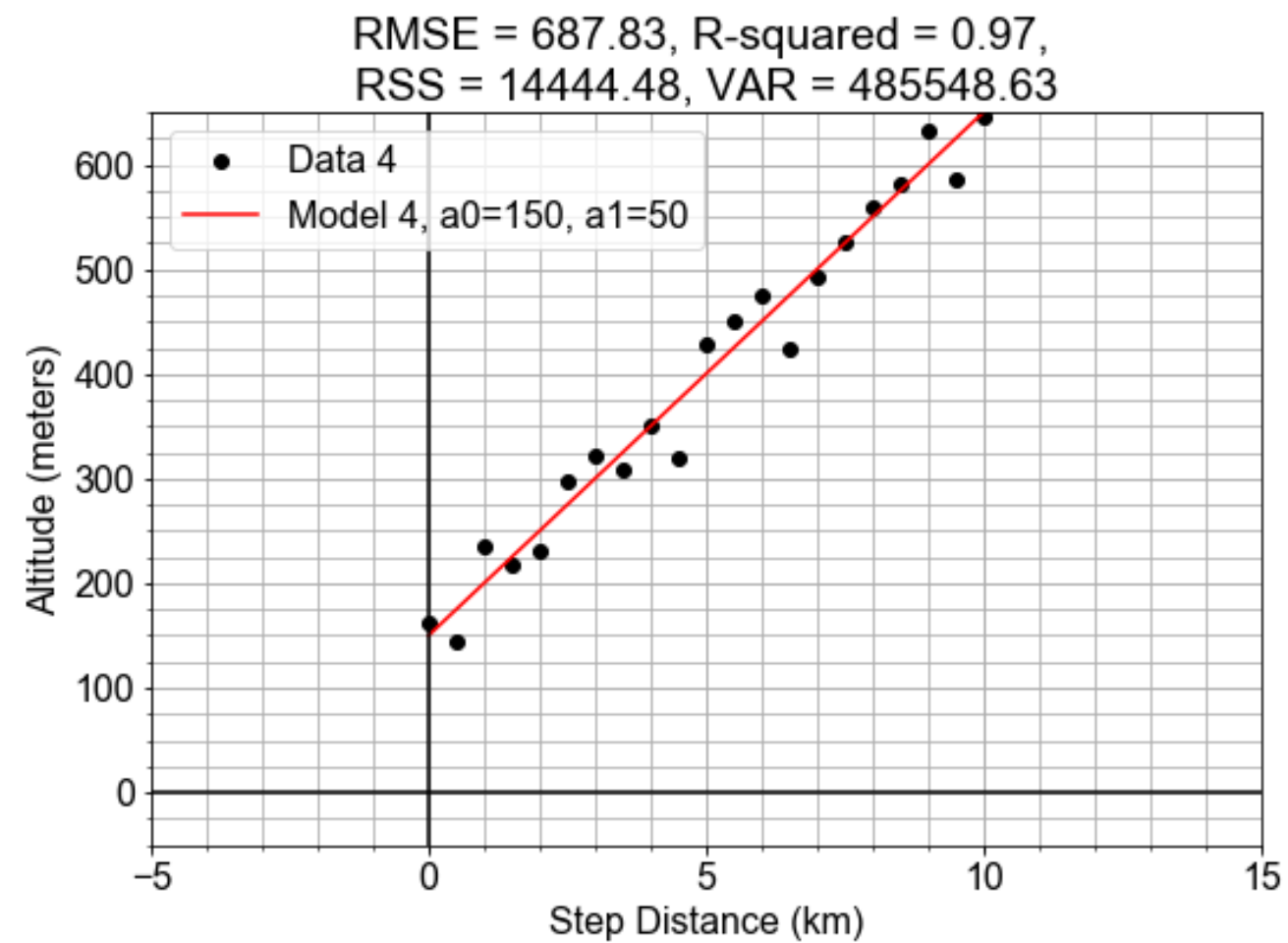


# R-Squared in Data





# R-Squared in Data





# RMSE vs R-Squared

- RMSE: how much variation is residual
- R-squared: what fraction of variation is linear





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# Standard Error

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# Uncertainty in Predictions

Model Predictions and RMSE:

- predictions compared to data gives residuals
- residuals have spread
- RMSE, measures residual spread
- RMSE, quantifies prediction goodness



# Uncertainty in Parameters

Model Parameters and Standard Error:

- Parameter value as center
- Parameter standard error as spread
- Standard Error, measures parameter uncertainty

# Computing Standard Errors

```
df = pd.DataFrame(dict(times=x_data, distances=y_data))
```

```
model_fit = ols(formula="distances ~ times", data=df).fit()
```

```
a1 = model_fit.params['times']  
a0 = model_fit.params['Intercept']
```

```
slope = a1  
intercept = a0
```

```
e0 = model_fit.bse['Intercept']  
e1 = model_fit.bse['times']
```

```
standard_error_of_intercept = e0  
standard_error_of_slope = e1
```



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