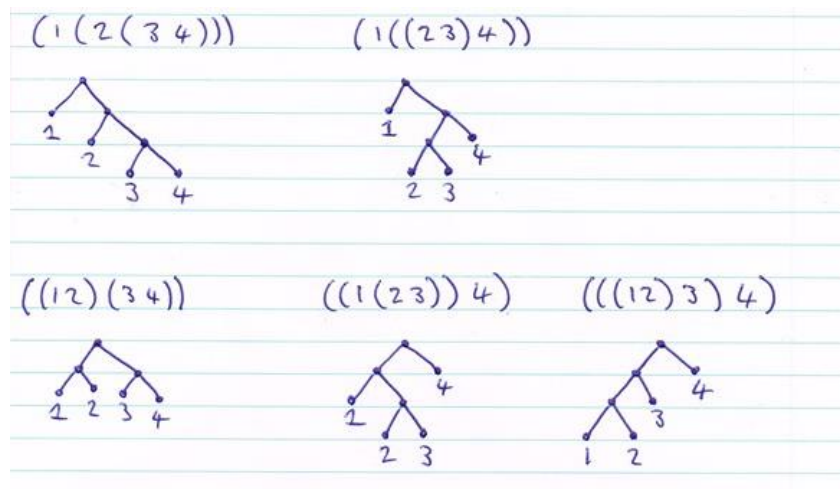


Catalan Questions

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Task 1: By hand draw the binary tree equivalences for line 3 of our example, that is to say, for $C(3)$.



Task 2: By hand, work out $C(4)$, i.e. given the five numbers 1 2 3 4 and 5, how many different ways can we place brackets to pair off the numbers.

All Possibilities:

$(1(2(3(45))))$, $(1(2((34)5)))$, $(1((2(34))5))$, $(1(((23)4)5))$,
 $(1((23)(45)))$, $((1(2(34)))5)$, $((1((23)4))5)$, $((((1(23))4)5))$,
 $(((((12)3)4)5))$, $((((12)(34))5))$, $((1(23))(45))$, $((((12)3)(45))$,
 $((12)(3(45)))$, $((12)((34)5))$

$C(4) = 14$ (14 Possibilities)

Task 3: Write a program that uses 64-bit integers to calculate $C(n)$ for $n = 1 \dots 35$.
(Question corrected to what was said in the email)

Program:

```
public class Catalan {
    public static void main(String[] args) {
        int n = 35;
        long[] answers = new long[n + 1];
        answers[0] = 1;
        for(int i = 1; i <= n; i++){
            for(int j = 0; j < i; j++){
                answers[i] += answers[j] * answers[i - 1 - j];
            }
        }
        for(int i = 1; i < n + 1; i++){
            System.out.println("C(" + i + "): " + answers[i]);
        }
    }
}
```

Catalan Questions

Output of the program:

C(1): 1
C(2): 2
C(3): 5
C(4): 14
C(5): 42
C(6): 132
C(7): 429
C(8): 1430
C(9): 4862
C(10): 16796
C(11): 58786
C(12): 208012
C(13): 742900
C(14): 2674440
C(15): 9694845
C(16): 35357670
C(17): 129644790
C(18): 477638700
C(19): 1767263190
C(20): 6564120420
C(21): 24466267020
C(22): 91482563640
C(23): 343059613650
C(24): 1289904147324
C(25): 4861946401452
C(26): 18367353072152
C(27): 69533550916004
C(28): 263747951750360
C(29): 1002242216651368
C(30): 3814986502092304
C(31): 14544636039226909
C(32): 55534064877048198
C(33): 212336130412243110
C(34): 812944042149730764
C(35): 3116285494907301262