

- Keldysh basis relations:

$$\begin{aligned}
c^{(1)} &= \frac{1}{\sqrt{2}} (c^+ + c^-), \quad c^{(2)} = \frac{1}{\sqrt{2}} (c^+ - c^-), \\
c^\pm &= \frac{1}{\sqrt{2}} (c^{(1)} \pm c^{(2)}); \\
G^R &\equiv G^{12} = \frac{1}{2} (G^{++} - G^{--} - G^{+-} + G^{-+}), \\
G^A &\equiv G^{21} = \frac{1}{2} (G^{++} - G^{--} + G^{+-} - G^{-+}), \\
G^K &\equiv G^{11} = \frac{1}{2} (G^{++} + G^{--} + G^{+-} + G^{-+}), \\
G^{\pm\pm} &= \frac{1}{2} [G^K \pm (G^R + G^A)], \quad G^{\pm\mp} = \frac{1}{2} [G^K \mp (G^R - G^A)];
\end{aligned} \tag{46}$$

- Self-energy (and inverse Green's functions):

$$\begin{aligned}
\Sigma^R &\equiv \Sigma^{21} = \frac{1}{2} (\Sigma^{++} - \Sigma^{--} + \Sigma^{+-} - \Sigma^{-+}), \\
\Sigma^A &\equiv \Sigma^{12} = \frac{1}{2} (\Sigma^{++} - \Sigma^{--} - \Sigma^{+-} + \Sigma^{-+}), \\
\Sigma^K &\equiv \Sigma^{22} = \frac{1}{2} (\Sigma^{++} + \Sigma^{--} - \Sigma^{+-} - \Sigma^{-+}); \\
\Sigma^{\pm\pm} &= \frac{1}{2} [\Sigma^K \pm (\Sigma^R + \Sigma^A)], \quad \Sigma^{\pm\mp} = -\frac{1}{2} [\Sigma^K \mp (\Sigma^R - \Sigma^A)];
\end{aligned} \tag{47}$$

- Fluctuation-dissipation theorem (FDT)

$$G^K = 2i \tanh\left(\frac{\beta(\omega - \mu)}{2}\right) \text{Im } G^R \tag{48}$$

- Orbital and bonding-antibonding basis:

$$c_\pm = (c_1 \pm c_2) / \sqrt{2} \tag{49}$$

- Symmetries of the Green's functions

$$\begin{aligned}
G^A(\tau) &= G^R(-\tau)^* \implies G^A(\omega) = G^R(\omega)^*, \\
G^K(\tau) &= -G^K(-\tau)^* \implies G^K(\omega) = -G^K(\omega)^* \implies \text{Re}(G^K) = 0
\end{aligned} \tag{50}$$