

- ① Runtime of the algorithm:  
Both the inner and the outer for loops run from  $1 \rightarrow n$

$$\therefore \text{no. of iterations} = \sum_{i=1}^n \sum_{j=1}^n C = C \times \frac{n(n+1)}{2}$$

$\therefore$  the runtime is  $C \times \frac{n(n+1)}{2}$  where  $C$  is the constant runtime ~~for~~  $x = x+1$

- ② Plotted on ipynb notebooks.

- ③ The runtime is  $C \times \frac{n^2 + n}{2}$

The upper bound is  $O(n^2)$

The lower bound is  $\Omega(n^2)$

Big  $\Theta$  is also  $n^2$  because both upper and lower bound is  $n^2$

- ④ For  $n=0$  the runtime is <sup>3-10</sup> ~~so~~ about ~~6-10~~ microseconds

- ④ The ~~runtime~~ runtime for algorithm 2 is greater as there are 2 declarative statements instead of 1

- ⑤ Due to additional computation the modified function will have a greater runtime on average

- ⑥ implemented.