

MinCostMatching

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// Min cost bipartite matching via
// shortest augmenting paths. This is
// an  $O(n^3)$  implementation of a
// shortest augmenting path algorithm
// for finding min cost perfect
// matchings in dense graphs.
// cost[i][j] = cost for pairing
// left node i with right node j
// Lmate[i] = index of right node
// that left node i pairs with
// Rmate[j] = index of left node
// that right node j pairs with
// The values in cost[i][j] may be
// positive or negative. To perform
// maximization, simply negate the
// cost[][] matrix.
#include <algorithm>
#include <cstdio>
#include <cmath>
#include <vector>
using namespace std;
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
double MinCostMatching(const VVD
&cost, VI &Lmate, VI &Rmate) {
    int n = int(cost.size());
    VD u(n); VD v(n);
    for (int i = 0; i < n; i++) {
        u[i] = cost[i][0];
        for (int j = 1; j < n; j++)
            u[i] = min(u[i], cost[i][j]);
    }
    for (int j = 0; j < n; j++) {
        v[j] = cost[0][j] - u[0];
        for (int i = 1; i < n; i++)
            v[j] = min(v[j], cost[i][j] - u[i]);
    }
    Lmate = VI(n, -1); Rmate = VI(n, -1);
    int mated = 0;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if (Rmate[j] != -1) continue;
            if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
                Lmate[i] = j; Rmate[j] = i; mated++;
                break;
            }
        }
    }
    VD dist(n); VI dad(n); VI seen(n);
    while (mated < n) {
        int s = 0;
        while (Lmate[s] != -1) s++;
        fill(dad.begin(), dad.end(), -1);
        fill(seen.begin(), seen.end(), 0);
        for (int k = 0; k < n; k++)
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dist[k] = cost[s][k] - u[s] - v[k];

        int j = 0;
        while (true) {

            // find closest
            j = -1;
            for (int k = 0; k < n; k++) {
                if (seen[k]) continue;
                if (j == -1 || dist[k] < dist[j]) j = k;
            }
            seen[j] = 1;

            // termination condition
            if (Rmate[j] == -1) break;

            const int i = Rmate[j];
            for (int k = 0; k < n; k++) {
                if (seen[k]) continue;
                const double new_dist =
                    dist[j] + cost[i][k] - u[i] - v[k];
                if (dist[k] > new_dist) {
                    dist[k] = new_dist;
                    dad[k] = j;
                }
            }

            for (int k = 0; k < n; k++) {
                if (k == j || !seen[k]) continue;
                const int i = Rmate[k];
                v[k] += dist[k] - dist[j];
                u[i] -= dist[k] - dist[j];
            }
            u[s] += dist[j];

            while (dad[j] >= 0) {
                const int d = dad[j];
                Rmate[j] = Rmate[d];
                Lmate[Rmate[j]] = j;
                j = d;
            }
            Rmate[j] = s; Lmate[s] = j; mated++;
            double value = 0;
            for (int i = 0; i < n; i++)
                value += cost[i][Lmate[i]];

            return value;
        }
    }
}
```