

1.1 Experimental Units Identify the experimental units on which the following variables are measured:

- a. Gender of a student **Student**
- b. Number of errors on a midterm exam..... **Midterm Exam**
- c. Age of a cancer patient **Cancer patient**
- d. Number of flowers on an azalea plant..... **azalea plant**
- e. Color of a car entering a parking lot **Car.**

1.2 Qualitative or Quantitative? Identify each variable as quantitative or qualitative:

- a. Amount of time it takes to assemble a simple puzzle quantitative
- b. Number of students in a first-grade classroom..... quantitative
- c. Rating of a newly elected politician (excellent, good, fair, poor)..... qualitative
- d. State in which a person lives..... Qualitative

1.3 Discrete or Continuous? Identify the following quantitative variables as discrete or continuous:

- a. Population in a particular area of the United States..... discrete
- b. Weight of newspapers recovered for recycling on a single day..... continuous
- c. Time to complete a sociology exam..... continuous
- d. Number of consumers in a poll of 1000 who consider nutritional labeling on food products to be important..... discrete

1.20 Consider this set of data:

4.5, 3.2, 3.5, 3.9, 3.5, 3.9, 4.3, 4.8, 3.6, 3.3, 4.3, 4.2, 3.9, 3.7, 4.3, 4.4, 3.4, 4.2, 4.4, 4.0, 3.6, 3.5, 3.9, 4.0.

- a. Construct a stem and leaf plot by using the leading digit as the stem.

$$\left(\begin{array}{c|l} 1 & \\ 2 & \\ 3 & 2 \ 3 \ 4 \ 5 \ 5 \ 5 \ 6 \ 6 \ 7 \ 9 \ 9 \ 9 \ 9 \\ 4 & 0 \ 0 \ 2 \ 2 \ 3 \ 3 \ 3 \ 4 \ 4 \ 5 \ 8 \end{array} \right) \dots \text{leaf unit=Key =0.1}$$

2.3 You are given $n = 10$ measurements: 3, 5, 4, 6, 10, 5, 6, 9, 2, 8.

a. Calculate $mean = \bar{X} = 58/10 = 5.8$

b. Find $median = m = 5$

c. Find the mode = None

2.15 You are given $n = 8$ measurements: 4, 1, 3, 1, 3, 1, 2, 2.

a. Find the range = $R = 4 - 1 = 3$

b. Calculate $mean = \bar{X} = \frac{17}{8} = 2.13$.

c. Calculate **variance** = $s^2 = 8.875/7 = 1.27$

d. Calculate $s^2 = (45 - (17^2)/8)/7 = 1.27$

e. $S = \sqrt{1.27} = 1.13$

f. Approximating standard deviation (S) = $Range/4 = 3/4 = 0.75$

X_i	X_i^2	$(X_i - \bar{X})^2$
4	16	3.4969
1	1	1.2769
3	9	0.7569
1	1	1.2769
3	9	0.7569
1	1	1.2769
2	4	0.0169
2	4	0.0169
17	45	8.8752

2.37 Suppose that some measurements occur more than once and that the data x_1, x_2, \dots, x_k are arranged in a frequency table as shown here:

X_i	f_i	$X_i \cdot f_i$	$X_i^2 \cdot f_i$
0	4	0	0
1	5	5	5
2	2	4	8
3	4	12	36
sum	15	21	49

a. Mean = $\bar{X} = \sum \frac{X_i \cdot f_i}{n} = \frac{21}{15} = 1.40$, $n = \sum f_i$

b. Variance = $S^2 = \frac{\sum X_i^2 \cdot f_i - \frac{(\sum X_i \cdot f_i)^2}{n}}{n-1} = \frac{49 - \frac{(21)^2}{15}}{14} = 1.4$

2.42 Given the following data set: 8, 7, 1, 4, 6, 6, 4, 5, 7, 6, 3, 0

1. Sort data : 0, 1, 3, 4, 4, 5, 6, 6, 6, 7, 7, 8
2. Find $Q1 = 3 + 0.25 \cdot (4 - 3) = 3.25$Position $Q1 = 0.25 \cdot (13) = 3.25$
3. Find $Q2 = 5 + 0.5 \cdot (6 - 5) = 5.5$Position $Q2 = 0.5 \cdot (13) = 6.5$.
4. Find $Q3 = 6 + 0.75 \cdot (7 - 6) = 6.75$Position $Q3 = 0.75 \cdot (13) = 9.75$
5. $IQR = Q3 - Q1 = 6.75 - 3.25 = 3.50$.
6. **Lower fence** = $Q1 - 1.5(IQR) = 3.25 - 1.5 \cdot 3.5 = -2$
7. **Upper fence** = $Q3 + 1.5(IQR) = 6.75 + 1.5 \cdot 3.5 = 12$
8. Find $P90 = 7 + 0.70 \cdot (8 - 7) = 7.70$Position $P90 = 0.90 \cdot (13) = 11.70$
9. Find the range = $R = 8 - 0 = 8$.
10. Calculate $mean = \bar{X} = \frac{56}{12} = 4.67$.
11. Calculate **variance** = $s^2 = 70.67 / 11 = 6.42$
12. $S = 2.53$
13. Calculate the z-score for the smallest observations, $x=0$?
14. $Z = (0 - 4.67) / 2.53 = -1.85$
15. 11. Calculate the z-score for the largest observations, $x=8$?
16. $Z = (8 - 4.67) / 2.53 = 1.32$

3.11 A set of bivariate data consists of these measurements on two variables, x and y : (3, 6) (5, 8) (2, 6) (1, 4) (4, 7) (4, 6)

- Draw a scatterplot to describe the data.
- Does there appear to be a relationship between x and y ?
- Calculate the correlation coefficient, r .
- Find the best-fitting line using the computing formulas.

x	y	xy	X ²	Y ²
3	6	18	9	36
5	8	40	25	64
2	6	12	4	36
1	4	4	1	16
4	7	28	16	49
4	6	24	16	36
19	37	126	71	237

- $\bar{X} = \frac{\sum x}{n} = \frac{19}{6} = 3.17.$
- $\bar{y} = \frac{\sum y}{n} = \frac{37}{6} = 6.17.$
- $s_x^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n-1} = \frac{71 - \frac{(19)^2}{6}}{5} = 2.17, \dots \dots \dots Sx = 1.47$
- $s_y^2 = \frac{\sum y^2 - \frac{(\sum y)^2}{n}}{n-1} = \frac{237 - \frac{(37)^2}{6}}{5} = 1.77, \dots \dots \dots Sy = 1.33$
- $s_{xy} = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{n-1} = \frac{126 - \frac{(19)(37)}{6}}{5} = 1.77$
- $r = \frac{s_{xy}}{s_x s_y} = \frac{1.77}{(1.47)(1.33)} = 0.903$
- Find the slope, $b = \frac{r \cdot s_y}{s_x} = \frac{(0.903)(1.33)}{1.47} = 0.82,$
- The y-intercept, $a = \bar{y} - b\bar{x} = 6.17 - (0.82 \cdot 3.17) = 3.57.$
- Write the regression line $y = a + bx = 3.57 + 0.82x$.
- If $x = 10$ then $y = 3.57 + 0.82(10) = 11.77.$