

# Lab 1: Brute-force algorithms

## Q1. Find the contiguous subarray of largest sum.

*Problem statement:* Given an array of  $n$  integers,  $\{a_1, a_2, \dots, a_n\}$ . Apply the Brute-force approach to find the subsequence  $\{a_i, a_{i+1}, \dots, a_{j-1}, a_j\}$  such that  $\sum_{k=i}^j a_k$  is largest, where  $1 \leq i \leq k \leq j \leq n$ . If all integers in the sequence are negative, the subsequence is empty and the result is 0.

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $n$  to indicate the size of the input array
- 2<sup>nd</sup> line:  $n$  integers, two consecutive numbers are separated by a single space “ ”

*Output:* Print the output data to the console as follows

- The subsequence with the largest sum of elements
- The sum of the above subsequence

*Example of input and output:*

| Input text file           | Output to console |
|---------------------------|-------------------|
| 8<br>-2 -3 4 -1 -2 1 5 -3 | 4 -1 -2 1 5<br>7  |

*Other requirements:* **You must implement all the three algorithms shown in the lecture** and present all the results to the console once.

## Q2. The change-making problem.

*Problem statement:* Given  $k$  denominations:  $d_1 < d_2 < \dots < d_k$  where  $d_1 = 1$ . Apply the Brute-force approach to find the minimum number of coins (of certain denominations) that add up to a given amount of money  $n$ .

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $k$  to indicate the number of denominations
- 2<sup>nd</sup> line:  $k$  positive integers describing  $k$  denominations, sorted descending, two consecutive numbers are separated by a single space “ ”. The last value must be one.
- 3<sup>rd</sup> line: a positive integer  $n$  to indicate the amount of money required exchange

*Output:* If there exists a solution, print the amount of each denomination to the console. Otherwise, output the string “No solution”.

*Example of input and output:*

| Input text file      | Output to console              |
|----------------------|--------------------------------|
| 4<br>25 10 5 1<br>72 | 25: 2<br>10: 2<br>5: 0<br>1: 2 |

### Q3. The convex-hull problem.

*Problem statement:* Given a set of  $n$  two-dimensional points. Apply the Brute-force approach to find the convex-hull of these points, i.e., the smallest convex polygon that contains all the points either inside or on its boundary.

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $n$  to indicate the number points
- $n$  next lines: Each line represents the two-dimensional coordinate of a point, in which the two coordinate values are separated by single space " ".

*Output:* Print to the console the set of points belonging to the convex-hull, each point is on a line.

*Example of input and output:*

| Input text file | Output to console |
|-----------------|-------------------|
| 7               | 0 0               |
| 0 0             | 4 0               |
| 1 1             | 4 4               |
| 3 3             | 0 4               |
| 1 3             |                   |
| 0 4             |                   |
| 4 0             |                   |
| 4 4             |                   |

*Other requirements:* You must use the algorithm given in the lecture.

### Q4. The traveling salesman problem.

*Problem statement:* Given a set of  $n$  cities, some pairs of adjacent cities are connected with given distances. Apply the Brute-force approach to find the shortest tour through  $n$  cities such that we visit each city exactly once before returning to the city where we started.

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $n$  to indicate the number of cities. The cities are indexed from 1 to  $n$ .
- Each of the next lines shows a pair of cities and their distance,  $\langle \text{point1 point 2 distance} \rangle$ , two consecutive numbers are separated by single space " ".
- The last line shows the number -1, indicating the end of the file

*Output:* If there exists a solution, print the below output data to the console. Otherwise, print the string "No solution".

- A sequence of cities forming the tour (in their exact order)
- The length of the tour

*Example of input and output:*

| Input text file | Output to console |
|-----------------|-------------------|
| 5               | 1 2 5 3 4         |
| 1 2 4           | 16                |
| 1 4 8           |                   |
| 3 4 2           |                   |
| 2 5 1           |                   |
| 3 5 1           |                   |
| -1              |                   |

### Q5. The sum of subsets problem.

*Problem statement:* Given a set of  $n$  distinct positive integers,  $A = \{a_1, a_2, \dots, a_n\}$ . Apply the Brute-force approach to find all subsets of  $A$  that sum to a positive integer  $k$ .

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $n$  to indicate the size of the input array
- 2<sup>nd</sup> line:  $n$  integers, two consecutive numbers are separated by a single space “ ”
- 3<sup>rd</sup> line: a positive integer  $k$

*Output:* If there exists a solution, print all the subsets to the console, one per line, and two consecutive numbers in a subset are separated by a single space “ ”. Otherwise, print the string “No solution”.

*Example of input and output:*

| Input text file   | Output to console |
|-------------------|-------------------|
| 4<br>1 2 3 4<br>7 | 3 4<br>1 2 4      |

### Q6. The Knapsack problem.

*Problem statement:* Given  $n$  items of known weights,  $\{w_1, w_2, \dots, w_n\}$ , and their corresponding values,  $\{v_1, v_2, \dots, v_n\}$ , and a knapsack of capacity  $C$ . Apply the Brute-force approach to find the most valuable subset of the items that fit into the knapsack.

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $C$  to indicate the capacity of the knapsack
- 2<sup>nd</sup> line: a positive integer  $n$  to depict the number of items
- Each of  $n$  following lines represent the weight  $w_i$  and value  $v_i$  of the item  $i$ , where  $i = 1, \dots, n$ . The two values are separated by a single line “ ”.

*Output:* If there exists a solution, print the output data to the console as follows. Otherwise, print the string “No solution”.

- The list of chosen items, whose sum of weights equals  $C$
- The total value of the chosen items

*Example of input and output:*

| Input text file                             | Output to console |
|---|-------------------|
| 20<br>5<br>10 5<br>4 2<br>9 4<br>6 6<br>7 1 | 1 2 4<br>13       |

### Q7. The assignment problem.

*Problem statement:* There are  $n$  people who need to be assigned to execute  $n$  jobs, one person per job. The cost if the  $i^{th}$  person is assigned to the  $j^{th}$  job is a known quantity  $C_{i,j}$  (which is a positive

integer) for each pair  $i, j = 1, 2, \dots, n$ . Apply the Brute-force approach to find an assignment with the minimum total cost.

*Input:* Read the input data from a text file whose format is as follows

- 1<sup>st</sup> line: a positive integer  $n$  to indicate the number of people, as well as the number of jobs.
- The matrix of people vs. jobs is represented in the next  $n$  lines, one row per line. Each line contains  $n$  positive integers, two consecutive numbers are separated by a single space “ ”.

*Output:* Print the output data to the console as follows

- The job assignment to the first person, second person, and so on.
- The corresponding minimum total cost.

*Example of input and output:*

| Input text file                               | Output to console |
|---|-------------------|
| 4<br>9 2 7 8<br>6 4 3 7<br>5 8 1 8<br>7 6 9 4 | 2 1 3 4<br>13     |

### Regulations for completing the lab work

- Each question must be implemented as an independent program in a single C++ file (of format .cpp).
- The program must receive input and return output as specified Submissions with wrong regulation will result in a "0" (zero).
- Plagiarism and Cheating will result in a "0" (zero) for the entire course.
- Contact: [Here](#).