vOptSolver – Version 0.2

Software developed with the support of the ANR/DFG-14-CE35-0034-01

Université de Nantes

https://github.com/vOptSolver https://voptsolver.github.io/vOptSpecific/ https://voptsolver.github.io/vOptGeneric/

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Convention: text in grey ⇒ functionality integrated in future releases

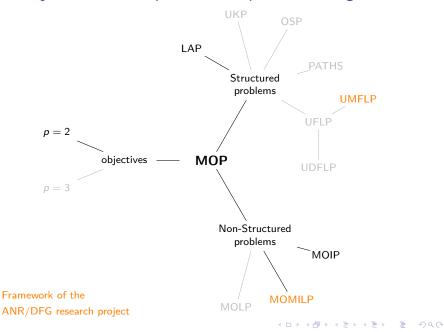


Introduction to vOptSolver

Multi-objective linear optimization problems targeted

- ▶ LP: Linear Program
- ► MILP: Mixed Integer Linear Program
- ► IP: Integer Linear program
- ► CO: Combinatorial Optimization
- ► LAP: Linear Assignment Problem
- ► OSP: One machine Scheduling Problem
- ► UKP: Unidimensional 01 Knapsack Problem
- ► MKP: Multidimensional 01 Knapsack Problem
- ► UFLP: Uncapacitated Facility Location Problem
- ► UDFLP: Discrete Uncapacitated Facility Location Problem
- ► UMFLP: Mixed Uncapacitated Facility Location Problem
- ► SSCFLP: Single Source Capacitated Facility Location Problem
- ► CFLP: Capacitated Facility Location Problem
- ► PATHS: shortest paths problem

Multi-objective linear optimization problems targeted



Solutions reached

For a given problem, the aim is to compute

Y_N, the set of nondominated "points"

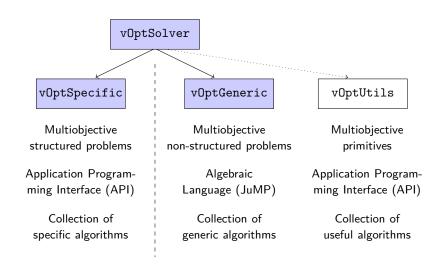
corresponding to

X_E, a complete set of efficient solutions

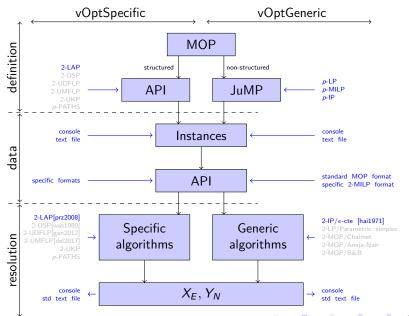
More on definitions and notations, refer to this book:

Matthias Ehrgott. *Multicriteria Optimization.*Springer-Verlag New York, 2005.

Design of vOptSolver



Design of vOptSolver in details



Design of vOptSolver in details

vOptUtils:

a collection of algorithms for managing and analyzing outcome set

- \triangleright multidimensional datastructure for filtering and storing Y_N
- ightharpoonup primitives for ploting Y_N
- ightharpoonup primitives for analyzing Y_N

Integrated specific algorithms (1/2)

► 2-LAP [prz2008]; in C:

A. Przybylski, X. Gandibleux, and M. Ehrgott. Two phase algorithms for the bi-objective assignment problem. European Journal of Operational Research, 185(2):509–533, 2008.

output: $X_E \subseteq \mathbb{N}^n$, $Y_N \subseteq \mathbb{Z}^p$

▶ 2-OSP with here $1 \mid . \mid (\Sigma C_i, T_{max})$ [was1980]; in Julia:

L.N. Van Wassenhove and L.F. Gelders. Solving a bicriterion scheduling problem. European Journal of Operational Research 4(1):42–48, 1980.

output: $X_E \subseteq \mathbb{N}^n$, $Y_N \subseteq \mathbb{Z}^p$

► 2-UKP [jor2010]; in Julia:

J. Jorge. Nouvelles propositions pour la résolution exacte du sac à dos multi-objectif unidimensionnel en variables binaires. Thèse de doctorat, Université de Nantes - France. 2010.

output: $X_E \subseteq \{0,1\}^n$, $Y_N \subseteq \mathbb{Z}^p$

Integrated specific algorithms (2/2)

▶ 2-UDFLP [gan2012]; in C++:

X. Gandibleux, A. Przybylski, S. Bourougaa, A. Derrien, A. Grimault. Computing the efficient frontier for the 0/1 biobjective uncapacitated facility location problem. 10th International Conference on Multiple Objective Programming and Goal Programming. June 11-13 2012, Niagara Falls, Canada.

output: $X_E \subseteq \{0,1\}^n$, $Y_N \subseteq \mathbb{Z}^p$

► 2-UMFLP [del2017]; in C++:

Q. Delmée, X. Gandibleux, A. Przybylski. Résolution exacte du problème de localisation de services bi-objectif sans contrainte de capacité en variables mixtes. ROADEF2017: 18ême congrés annuel de la Société Française de Recherche Opérationnelle et d'Aidie à la Décision, Feb 2017, Metz, Trance. 2017

output: $X_E \subseteq \{0,1\}^{n_1} \times \mathbb{R}^{n_2}, Y_N$

► PATHS [gan2004]; in C:

X. Gandibleux, Fr. Beugnies and S. Randriamasy: Martins' algorithm revisited for multi-objective shortest path problems with a MaxMin cost function. 40R: A Quarterly Journal of Operations Research. Volume 4, Number 1, pp. 47-59, 2006.

output: X_E , Y_N

Integrated generic algorithms (1/2)

▶ 2-IP/ ϵ -constraint method [hai1971]; in Julia:

Y.V. Haimes, L.S. Lasdon, D.A. Wismer: On a bicriterion formation of the problems of integrated system identification and system optimization. *IEEE Transactions on Systems, Man and Cybernetics*. Volume SMC-1, Issue 3, Pages 296-297, July 1971.

output: $X_E \subseteq \mathbb{Z}^n$, $Y_N \subseteq \mathbb{Z}^p$

► 2-IP/dichotomic method:

Aneja, Y. and K. Nair: Bicriteria transportation problem. Management Science 25 (1), 73?78. 1979.

output: $X_{SE} \subseteq \mathbb{Z}^n$, $Y_{SN} \subseteq \mathbb{Z}^p$

▶ 2-IP/Chalmet & al., 1986:

L.G. Chalmet, L. Lemonidis, and D.J. Elzinga. An algorithm for the bi-criterion integer programming problem. European Journal of Operational Research, 25:302-300, 1086

output: $X_E \subseteq \mathbb{Z}^n$, $Y_N \subseteq \mathbb{Z}^p$

Integrated generic algorithms (2/2)

► 2-MILP/Vincent & al., 2014:

Th. Vincent, F. Seipp, S. Ruzika, A. Przybylski, X. Gandibleux. Multiple objective branch and bound for mixed 0-1 linear programming: Corrections and improvements for the biobjective case. Computers & Operations Research, Volume 40, Issue 1, pp. 498–509, 2013.

Fl. Lucas. Multiobjective branch & cut. Master Thesis, University of Nantes, France. June 2017.

output: $X_E \subseteq \mathbb{R}^{n_1} \times \mathbb{Z}^{n_2}$, Y_N

► 2-LP/parametric simplex:

Description available in: Matthias Ehrgott. Multicriteria Optimization. Springer-Verlag New York, 2005.

output: $X_{SE} \subseteq \mathbb{R}^n$, $Y_{SN} \subseteq \mathbb{R}^p$

Selectable (MI)LP Engines

- open source:
 - GLPK (GNU Linear Programming Kit)
- commercial:
 - CPLEX
 - GUROBI

NB: CPLEX and GUROBI are currently not available on JuliaBox

Instructions for installing and running vOptSolver

Instructions for installing vOptSolver

vOptSolver has been tested with:

- ▶ Julia v0.6
- ► GLPK v4.60

Choose between:

- 1. a local use
 - on macOS (tested on v10.12.5)
 - on linux (tested on ubuntu 14.04 LTS)
 - on windows (perhaps later...)
- 2. a distant use
 - in the cloud with JuliaBox.

Instructions for a distant use in the cloud

- ► Local installation
 - 1. nothing to do
- ► Run Julia
 - 1. go to https://juliabox.com and sign in to open a session
 - 2. click on the icon "console"
 - when the prompt is ready, type in the console julia
- ▶ Before the first use of vOptSolver, add the following packages:
 - 1. when the prompt julia is ready, type in the terminal
 Pkg.add("GLPK")
 Pkg.clone("http://github.com/vOptSolver/vOptGeneric.jl")
 Pkg.clone("http://github.com/vOptSolver/vOptSpecific.jl")
 Pkg.build("vOptSpecific")

At this point, vOptSolver is properly installed

Instructions for a local use on your own computer

- ▶ Local installation
 - install Julia on your computer, instructions here: http://julialang.org/downloads/
 - 2. install (e.g.) GLPK on your computer, instructions here: http://jump.readthedocs.io/en/latest/installation.html NB: a standard C/C++ compiler must be installed (GCC is suggested)

At this point, Julia and GLPK are properly installed

- ► Run Julia
 - on linux: open a console on your computer; when the prompt is ready, type in the console julia
 - on macOS: locate the application julia and click on the icon; julia console comes on the screen
- ▶ Before the first use of vOptSolver, add both following packages:
 - 1. when the prompt julia is ready, type in the console
 Pkg.add("GLPK")
 Pkg.clone("http://github.com/vOptSolver/vOptGeneric.jl")
 Pkg.clone("http://github.com/vOptSolver/vOptSpecific.jl")
 Pkg.build("vOptSpecific")

At this point, vOptSolver is properly installed

Instructions for running vOptSolver

When vOptSolver is properly installed, vOptSpecific and vOptGeneric are ready locally or in the cloud.

- ► Run Julia
 - 1. open a console on your computer or in the cloud
 - when the prompt is ready, type in the console julia
- ▶ when the prompt *julia* is ready, type in the terminal
 - using vOptSpecific
 - 2. using vOptGeneric
 - 3. using GLPK

Remark 1: you may invoke only using vOptSpecific if you are only working with vOptSpecific. Same remark for vOptGeneric. Remark 2: you may invoke CPLEX or GUROBI in the place of GLPK (ps: in local mode, the MILP solver selected must be properly installed)

 vOptSpecific and vOptGeneric are ready. See examples for further informations

vOptSpecific problem by problem

definition (problem, inputs)
data (console, text file)
resolution (API, outputs, text file)

LAP | Definition | The linear assignment problem

$$\begin{bmatrix} & \min z^k & = & \sum_{i=1}^n \sum_{j=1}^n c_{ij}^k x_{ij} & k = 1, \dots, p \\ & s/c & & \sum_{i=1}^n x_{ij} = 1 & j = 1, \dots, n \\ & & & \sum_{j=1}^n x_{ij} = 1 & i = 1, \dots, n \\ & & & x_{ij} = (0, 1) & i = 1, \dots, n \\ & & & & j = 1, \dots, n \end{bmatrix}$$
 (p-LAP)

LAP | Definition | Inputs

Valid for 2-LAP.

- n (integer): number n of assignments task-resource
- ▶ C1 (matrix of $n \times n$ of integers): coefficients c_{ij}^1 of the objective 1
- C2 (matrix of n × n of integers): coefficients c²_{ii} of the objective 2

LAP | Data | Example (console)

```
n
C1 = [ 3
     16
        0 6 12 19;
        7
           11
              15
        11
           7
              16 3;
         5
C2 = [16]
        5
               19
                 12;
            6
     15
           13
        2
           13 2 3;
     14
           8 1 7;
           1
     10
        10
```

LAP | Data | Example (text file)

```
n
5
16
             12
                                    C1
         11
             15
          7
             16
    11
 2
     5
16
             19
15
         13
                                    C2
        13
14
         8
10
    10
         1
```

► load2LAP

Load an instance of a 2-LAP from the file fname id = load2LAP(fname)

LAP | Resolution | API

▶ set2LAP

Create a new instance of a 2-LAP and set up all required values id = set2LAP(n, C1, C2)

► LAP_Przybylski2008

Set up the solver to use for the 2-LAP solver = LAP_Przybylski2008()

▶ solveMOP

Solve the instance provided with the mentioned solver and return the results

```
z1, z2, \sigma = solveMOP( id , solver )
```

LAP | Resolution | Outputs (specification)

Valid for 2-LAP.

solveMOP returns:

- ▶ z1: vector of $1 \cdots | Y_N |$ of integers
- ▶ z2: vector of $1 \cdots | Y_N |$ of integers
- ▶ σ : vector of $1, ..., |Y_N|$ of $(\sigma_1, ..., \sigma_n)$ where
 - σ_i (i = 1, ..., n): integer; a permutation coding ($x_{ij} = 1 \Leftrightarrow \sigma_i = j$)

vOptGeneric problem by problem

definition (problem, inputs, JuMP) data (console, text file) resolution (solve, outputs, text file)

MOMILP-MOLP-MOIP | Definition

Three Multi Objective Linear Optimization Problems:

$$\begin{array}{llll} \min z(x) & = & Cx & \min z(x) & = & Cx & \min z(x) & = & Cx \\ s/t & Tx & \leqq & d & s/t & Tx & \leqq & d \\ x & \in & \mathbb{R}^{n_1} \times \mathbb{Z}^{n_2} & x & \in & \mathbb{R}^{n_1} & x & \in & \mathbb{Z}^{n_2} \end{array}$$

Multi Objective Mixed-Integer Linear Problem (MOMILP) Multi Objective Linear Problem (MOLP) Multi Objective Integer Problem (MOIP)

where:

$$\begin{array}{cccc} T\in\mathbb{Z}^{m\times n} &\longrightarrow & m \text{ constraints, } i=1,\ldots,m\\ C\in\mathbb{Z}^{n\times p} &\longrightarrow & \text{the objective matrix} \\ X=\{x\in\mathbb{R}^{n_1}\times\mathbb{Z}^{n_2}|Tx\leq d\}\subseteq\mathbb{R}^n &\longrightarrow & \text{the set of feasible solutions}\\ Y=z(X)\subseteq\mathbb{R}^p &\longrightarrow & \text{the set of images} \end{array}$$

MOMILP-MOLP-MOIP | Formulation

Following spectifications of JuMP for formulating a model, see:

http://jump.readthedocs.io/en/latest/quickstart.html# creating-a-model

Plus:

@addObjective(<model>, <opt>, <function>)

where

- model: id of the model concerned
- opt: function to Min imize or Max imize
- function: definition of the function

MOMILP-MOLP-MOIP | Example of formulation

$$\begin{array}{ll} \min & c_1^1 x_1 + c_2^1 x_2 \\ \min & c_1^2 x_1 + c_2^2 x_2 \\ \mathsf{s/t} & t_{11} x_1 + t_{12} x_2 \leq d_1 \\ & t_{21} x_1 + t_{22} x_2 \leq d_2 \\ & x_1 \in \mathbb{R}, x_2 \in \mathbb{Z} \end{array}$$

$$\begin{array}{ll} \min & c_1^1 x_1 + c_2^1 x_2 \\ \min & c_1^2 x_1 + c_2^2 x_2 \\ \mathsf{s/t} & t_{11} x_1 + t_{12} x_2 \leq d_1 \\ & t_{21} x_1 + t_{22} x_2 \leq d_2 \\ & x_1, x_2 \in \mathbb{R} \end{array}$$

$$\begin{array}{ll} \min & c_1^1 x_1 + c_2^1 x_2 \\ \min & c_1^2 x_1 + c_2^2 x_2 \\ \mathsf{s/t} & t_{11} x_1 + t_{12} x_2 \leq d_1 \\ & t_{21} x_1 + t_{22} x_2 \leq d_2 \\ & x_1, x_2 \in \mathbb{Z} \end{array}$$

```
# --- create a MOMILP and set the model ---
MOMILP = Model(solver=<working on it>)
@variable(MOMILP, x1 >= 0)
@variable(MOMILP, x2 >= 0, Int)
@objective(MOMILP, Min, c11*x1 + c12*x1)
@addObjective(MOMILP, Min, c21*x1 + c22*x1)
@addConstraint(MOMILP, t11*x1 + t12*x2 <= d1)
@addConstraint(MOMILP, t21*x1 + t22*x2 <= d2)</pre>
```

- # --- create a MOLP and set the model --MOLP = Model(solver=<working on it>)
 @variable(MOMILP, x1 >= 0)
 @variable(MOMILP, x2 >= 0)
 @objective(MOLP, Min, c11*x1 + c12*x1)
 @addObjective(MOLP, Min, c21*x1 + c22*x1)
 @addConstraint(MOLP, t11*x1 + t12*x2 <= d1)
 @addConstraint(MOLP, t21*x1 + t22*x2 <= d2)</pre>
- # --- create a MOIP and set the model --MOIP = Model(solver=GLPKSolverMIP())
 @variable(MOIP, x1 >= 0, Int)
 @variable(MOIP, x2 >= 0, Int)
 @objective(MOIP, Min, c11*x1 + c12*x1)
 @addObjective(MOIP, Min, c21*x1 + c22*x1)
 @addConstraint(MOIP, t11*x1 + t12*x2 <= d1)
 @addConstraint(MOIP, t21*x1 + t22*x2 <= d2)</pre>

MOMILP-MOLP-MOIP | Data | Example (console)

```
c11 = 3 ; c12 = 1
c21 = -1 ; c22 = -2
t11 = 0 ; t12 = 1 ; d1 = 3
t21 = 3 ; t22 = -1 ; d2 = 6
```

MOMILP-MOLP-MOIP | Data | Example (format MOP)

```
parseMOP
Load an instance (MOP format) from the file fname
jumpModel = parseMOP( fname , solver=<solver to invoke> )

NB: the MOP format is an extension of
  the MPS format
     (https://en.wikipedia.org/wiki/MPS_(format))
  to multiple objectives
     (http://moplib.zib.de/format_desc/mop_format.pdf)
```

MOMILP-MOLP-MOIP | Example of resolution

MOMIL P

Algorithm: branch&bound Solver: working on it

MOLP

Algorithm: parametric simplex

Solver: working on it

MOIP

Algorithm: ϵ -constraint Solver: GLPK or CPLEX

```
# --- solve the model ---
  status = solve(MOMILP)
# --- Get the results ---
  writeMOP( MOMILP , " mixed " )
# --- solve the model ---
  status = solve(MOLP)
# --- Get the results ---
  writeMOP( MOLP , " continuous " )
# --- solve the model ---
  status = solve(MOIP)
# --- Get the results ---
```

writeMOP(MOIP . " integer ")

MOMILP-MOLP-MOIP | Resolution | Outputs (specification)

Y_N of the 2-MOP is defined by

- ▶ 2-MILP: a mixed nondominated set (composed of edges that are either closed, half-open, open or reduced to a point)
- ▶ 2-LP: a continuous nondominated set (composed of edges)
- 2-IP: a discrete nondominated set (composed of points)

Technical overview

Technical overview

User application written in Julia		
DeclareNo-structured MOPIP/MIP/LPStructured MOPLAP $1 \mid r_i \mid (f_1, f_2)$	Solve $Specific$ $2 ext{-LAP} o Y_N \ 1 \mid . \mid (\Sigma C_i, T_{max}) o Y_N \ Generic \ 2 ext{-ILP} o Y_{SN} \ dicho$	Utils Input/Output read format MOP plot Y _N Misc maintain Y _N analyze Y _N
	2-ILP $ ightarrow$ Y_N	
Interface: Library solvers C/C++ specifics	2-MILP $\rightarrow Y_N$ B&C 2-ILP $\rightarrow Y_N$ ϵ -cte	Interface: Library solvers MIP generics
Modules C	$2\text{-LP} o Y_N$ simplex	Solvers MIP open source GLPK commercial CPLEX, GUROBI

History

History

- ▶ v1.0: July 2016; first prototype; not opened to the public
- ▶ v2.0: June 23, 2017; first stable version; released to the public with
 - ▶ a depot on github, webpages, and an user documentation
 - JuMP extended to multiple objectives (vOptGeneric)
 - primitive for loading a non-structured problem in std MOP format
 - ightharpoonup ϵ -constraint algorithm for bi-objective integer programming
 - backbone in Julia (vOptSpecific)
 - ► API and solver for bi-objective linear assignment problem

Taskforce

Taskforce

Involved in the development of vOptSolver:

Currently:

- GANDIBLEUX Xavier (coordinator)
- ▶ LUCAS Flavien
- SOLEILHAC Gauthier
- PRZYBYLSKI Anthony

Previously:

- CHATELLIER Pauline
- DUMEZ Dorian

Links and contact

Follow/joint us here

```
Homepage of vOptSolver:
http://voptsolver.github.io/vOptSolver/
  Repository of vOptSolver:
  http://github.com/vOptSolver
  Repository of vOptSpecific:
  http://github.com/vOptSolver/vOptSpecific.jl
  Repository of vOptGeneric:
  http://github.com/vOptSolver/vOptGeneric.jl
Contact concerning vOptSolver:
vopt@univ-nantes.fr
Homepage of the ANR/DFG research project "vOpt":
http://vopt-anr-dfg.univ-nantes.fr
```