

Practical no-2

39

```

> c(2, 3, 5, 7)^2
[1] 4 9 25 49
> c(2, 3, 5, 7) * c(2, 3, 6, 2)
[1] 4 9 30 14
> c(2, 3, 5, 7) / 12
[1] 4 9 25 49
> c(6, 2, 7, 5) / c(4, 5)
[1] 1.50 0.40 1.75 1.00
> c(2, 3, 5, 7) + c(2, 3)
[1] 4 9 10 2
> c(1, 6, 2, 3) * c(-2, -3, -4, -1)
[1] -2 -18 -8 -3
> c(4, 6, 8, 9, 4, 5) %c(1, 2, 3)
[1] 4 36 512 916 2125
> x=20 > y=30 > z=2
> x^2 + y^3 + z
[1] 27402
> sqrt(x^2+y)
[1] 20.73644
> x^2 + y^2
[1] 1300

```

- Aim:- Basic of R Software
- R is a software for statistical analysis cmd data computing.
 - It is an effective data handling software and outcome storage is possible.
 - It is capable of graphical display.
 - It is a free software.

To solve the followings.

(i) $4+6+8 \div 2 - 5$
 $\rightarrow 4+6+8/2 - 5$
[1] 9

(ii) $2^2 + (-3) + \sqrt{45}$
 $\rightarrow \sqrt{2} \rightarrow \text{abs}(-3) + \sqrt{45}$
[1] 13.7082

(iii) $5^3 + 7 \times 5 \times 0 + 46/5$
 $\rightarrow 5^3 + 7 \times 5 + 0 + 46/5$
[1] 414.2

(iv) $\sqrt{4^2 + 5^2} + 1/6$
 $\rightarrow \sqrt{4^2 + 5^2} + 1/6$
[1] 5.671567

(v) round off
 $46 \div 7 + 9 \times 0$
 $\rightarrow \text{round}(46/7 + 9 * 0)$
[1] 17.14

Q4

> x<-matrix(x (nrow=4, ncol=2, data=c(1,2,3,

4,5,6,7,8))

>x
>
[1] [1,] E1 5
[2,] 2 6
[3,] 3 7
[4,] 4 8
[5,]

Q5 And $x+y$ and $2x+3y$ where: $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$

$$y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

> x<-matrix (nrow=3, ncol=3, data=c(4,7,9,6,

>
x
[1,] 4 10 12
[2,] 7 12 15
[3,]

> y<-matrix (nrow=3, ncol=3, data=c(4,7,9,6,

>
y
[1,] 4 10 12
[2,] 7 12 15
[3,]>
y
[1,] 4 10 12
[2,] 7 12 15
[3,]

Q)

x	p(x)
1	0.2
2	0.2
3	0.3
4	0.2
5	0.2

The condition for p.m.f is $\sum p(x) = 1$

$$\text{So, } \sum p(x) = p(1) + p(2) + p(3) + p(4) + p(5)$$

$$= 0.2 + 0.2 + 0.3 + 0.2 + 0.2$$

\therefore the given data is not a p.m.f because
the $p(x) \neq 1$

③

x	p(x)
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for p.m.f is $\sum p(x) = 1$

1) $p(x) > 0$ we satisfy

$$2) \sum p(x) = 1$$

$$\begin{aligned} \sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \end{aligned}$$

\therefore The given data is p.m.f.

$$\begin{aligned} \text{Code:} & \quad (0.2, 0.2, 0.35, 0.15, 0.1) \\ \text{Prob:} & \quad \frac{\text{Code}}{\text{Sum (prob)}} \\ & \quad [1] \perp \end{aligned}$$

Q2 find the c.d.f. for the following p.m.f
and sketch the graph.

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.96 & 40 \leq x < 50 \\ 1 & x \geq 50 \end{cases}$$

Q2

x	1	2	3	4	5	6
$p(x)$	0.05	0.25	0.1	0.2	0.2	0.1

$$F(x) = \begin{cases} 0 & x < 1 \\ 0.15 & 1 \leq x < 2 \\ 0.40 & 2 \leq x < 3 \\ 0.50 & 3 \leq x < 4 \\ 0.70 & 4 \leq x < 5 \\ 0.90 & 5 \leq x < 6 \\ 1.00 & x \geq 6 \end{cases}$$

```

> prob = C(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)
> sum(prob)
[1] 1
> csum(prob)
[1] 0.15, 0.40, 0.50, 0.10, 0.90, 1.00
> x = c(1, 2, 3, 4, 5, 6)

```

p=0.3

1 > $\text{dbinom}(10, 100, 0.1)$

> $x = 5.1310653$

2 > i) $\text{dbinom}(4, 12, 0.2)$

[1] 0.1320756

ii) $\text{pbinom}(4, 12, 0.2)$

[1] 0.9274445

iii) $\text{l-phi}(4, 12, 0.2)$

[1] 0.01940528

3 > $\text{dbinom}(0, 5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.00810

4 - 0.00045

5 - 0.00001

4

i) $\text{dbinom}(5, 12, 0.25)$

[1] 0.1032414

2 > $\text{pbinom}(5, 12, 0.25)$

[1] 0.9455978

3 > $\text{l-phi}(5, 12, 0.25)$

[1] 0.0027815

4 > $\text{dbinom}(6, 12, 0.25)$

[1] 0.04014945

Practical no 3

Topic :- Binomial distribution.

$$\# P(X=x) = {}^n \text{C}_x \text{ binom}(x, n, p)$$

$$\# P(X \leq x) = P_{\text{binom}}(x, n, p)$$

$$\# \text{ If } x \text{ is unknown} \\ P_1 = P(X \leq x) = q \text{ binom}(p, n)$$

1) find the probability of exactly 10 success in hundred trials when $p=0.1$.

2) suppose there are 12 mcq each question has 5 option out of having which 1 is correct. find the probability of having exactly

4 correct answer.
 i) Atmost 4 correct answers.
 ii) More than 5 correct answers.

3) find the complete distribution when $n=5$ and $p=0.1$

a) $n=12$, $p=0.25$ find following probability

$$\begin{aligned} i) & P(X=5) & ii) & P(X>7) \\ iii) & P(X \leq 5) & iv) & P(X \geq 7) \end{aligned}$$

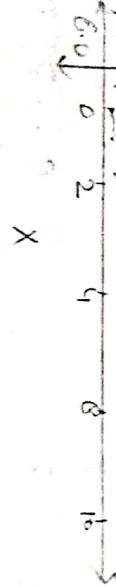
4) the probability of a salesman making a sale to customer 0.15 find the probability of

i) No sales out of 10 customers.
 ii) More than 3 sales out of 20 customers.

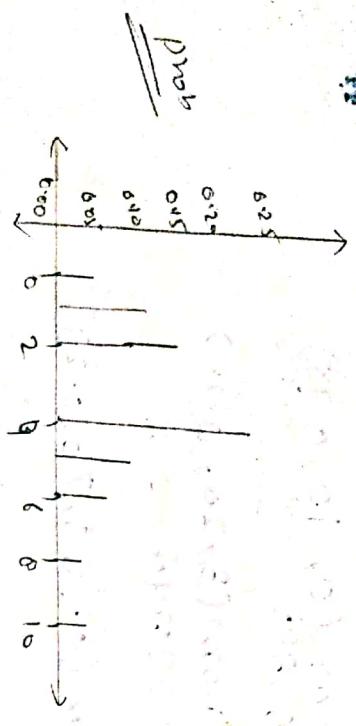
5) A sales man has 20% probability of making a sale to customer. Out of 30 customer

what minimum number of sales he can make with 88% of probability.

6) follows binomial distribution with $n=10$, $p=0.3$ plot the graph p.m.f and c.d.f



) plot (x , $\text{cumprob}["S"]$)



(x , $\text{cumprob}["S"]$) + hold <

$p_4 = \text{norm}(5, 12, 3)$

> p_4
 [1] 15.254928 11.6540505 11.2000555 6.4514994 12.232

c χ^2 follows normal distribution with $\mu = 10, \sigma = 2$
 Find (i) $P(X \leq 7)$ (ii) $P(5 < X \leq 12)$ (iii) $P(X \geq 12)$

(iv) Generate 10 observations
 (v) find K such that $P(X \geq K) = 0.4$

> $a_1 = \text{pnorm}(7, 10, 2)$

> a_1

[1] 0.668872

> $a_2 = \text{pnorm}(5, 10, 2) - \text{pnorm}(12, 10, 2)$

> a_2

[1] -0.0351351

> $a_3 = 1 - \text{pnorm}(12, 10, 2)$

> a_3

[1] 0.1586558

> $a_4 = \text{norm}(10, 10, 2)$

> a_4

[1] 11.608931 9.920417 12.637741 8.093359

8.721380 9.193226 9.366824 11.702106

9.537584 10.715006

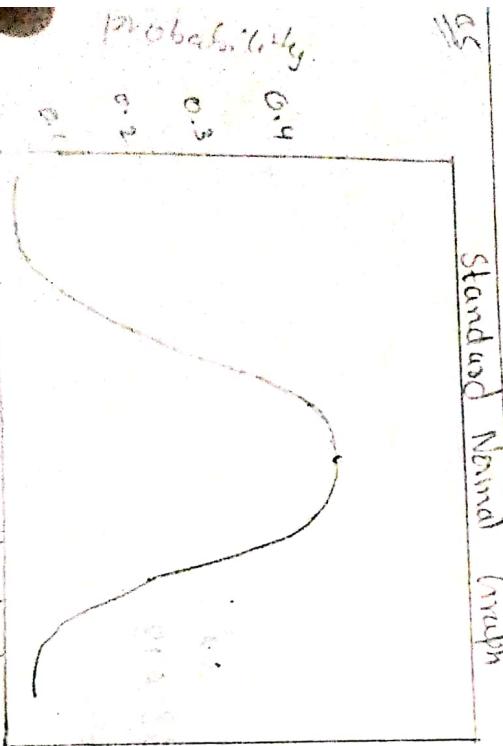
> $a_5 = \text{norm}(0.4, 10, 2)$

> a_5

[1] 9.493306

Q4 $X \sim N(30, 100) . \sigma = 10$

- $P(X < 40)$
- $P(25 < X < 35)$
- Find K such that $P(X < K) = 0.6$
- $f_1 = \text{pnorm}(40, 30, 10)$
- $f_2 = 0.8413447$



Q5 Plot the standard normal graph.

> $x = \text{seq}(-3, 3, \text{by} = 0.1)$
> $y = \text{dnorm}(x)$
> plot(x, y, xlab = "x values", ylab = "probability")

Q6

- ```

> f1 = 1 - pnorm(35, 30, 10)
> f2 = 0.3085395
> p3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)
> p4 = qnorm(0.6, 30, 10)
> f4 = 0.3029249
> f4 = qnorm(0.6, 30, 10)
> f4 = 32.53347

```

(1) Set the hypothesis  $H_0: \mu = 15, H_1: \mu \neq 15$   
 Random sample of size 400 drawn and it  
 is collected the sample mean is 14  
 and the standard deviation is 3. Test the  
 hypothesis at 5% level of significance.

```

> mo = 15
> me = 14; sd = 3
> n = 400
> scale = (me - mo) / (sd + sqrt(n))
> scale
[1] -6.66667
> pvalue = 2 * (1 - pnorm (abs (scale)))
> pvalue
[1] 2.618796e-11

```

i. The p-value is less than 0.5 we  
 reject the value  $H_0 \text{ i.e. } 15$ .

(2) Test the hypothesis  $H_0: \mu = 10, H_1: \mu \neq 10$ .  
 Random Sample mean 10.2 and  
 Standard deviation 2.25 test the  
 hypothesis at 5% level of significance.

$\therefore$  P value is less than 0.05 we reject null value.

- (g) last year the farmers bought 20% of their crop and remaining sample of 60 fields were collected and it was found that a field crop are insect polluted and the hypothesis at 5% level of significance.

```

> p=0.2
> p=9/60
> m=60
> q=1-p
> zcal=(p-q)/sqrt(p*(1-p)/n)
> zcal
[1] -0.9602450
> pvalue = 2*pnorm(zcal)
> pvalue
[1] 0.3329216

```

- $\therefore$  The pvalue is greater than 0.01 we accept the value of  $H_0$ .  $H_0: \mu = 12.5$  from the following sample at 5% level of significance.

The pvalue is less than 0.05 we reject the value.

(h)

$$\begin{aligned} \text{Mean} &= \text{mean}(x) \\ \text{Variance} &= ((n-1) * \text{var}(x)) / n \\ s.d &= \text{sqrt}(\text{variance}) \\ m_0 &= 12.5 \\ t &= (m_a - m_0) / (s.d / \text{sqrt}(n)) \\ \text{pvalue} &= 2 * \text{pnorm}(\text{abs}(t)) \end{aligned}$$

[1] 8.84409

$\therefore$  The pvalue is less than 0.05 we

reject the value.

Practical no.: 6

Topic :- New sample test -

Q. In the population mean (the average spent per customer in a restaurant) is 250. A sample of 100 customers selected. The standard deviation 30. Test the hypothesis that the population is not 250 or not at 5% level of significance.

A. On a random sample of 100 students it is found that is 275. Test the hypothesis that the population proportion is at 1% level of significance.

~~H<sub>0</sub>~~

$$H_0 = \mu = 250$$

$$\text{against } H_1 = \mu \neq 275$$

- >  $m \bar{x} = 275$
- >  $n = 100$
- >  $m_0 = 250$
- >  $s_d = 30$
- >  $Z_{\text{cal}} = (\bar{x} - m_0) / (s_d / \sqrt{n})$
- >  $Z_{\text{cal}} = 2.67$
- [9] Q. 333333

Ques Find a sample of 600 students in a college who use blue ink in another college from a sample of 600 student who use blue ink test the hypothesis that the proportion of student using blue ink in 2 colleges is one equal or not at 1% level of significance.

2)

$H_0: \mu = 0.8$  opoint  $H_1: \mu \neq 0.8$  ;  
 $\alpha = 1 - \rho$

$$> zcal = (\bar{p} - p) / \sqrt{\frac{pq}{n}}$$

> zcal

[z] = 3.452047

> pvalue = 2 \* (1 - norm(abs(zcal)))

> pvalue  
~~[1] 7.72268e-05~~

Since the value is less than 1%. level of significance we reject the hypothesis.

5

$$> n_1 = 600$$

$$> n_2 = 900$$

$$> p_1 = 400/600$$

$$> p_2 = 450/900$$

$$> p = (n_1 * p_1) + (n_2 * p_2) / (n_1 + n_2)$$

$$> q = 1 - p$$

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{(p * q) / (n_1 + n_2)}$$

$$[5] 0.01972648$$

$$> p\text{value} = 2 * \text{pnorm}(\text{abs}(z_{\text{cal}}))$$

$$> p\text{value}$$

$$[5] 1.253222e-10$$

The p-value is less than 1% level of significance we reject the hypothesis.

⑥

$$\begin{aligned} H_0: H_1 &= -p_1 = p_2 \text{ against } H_1: p_1 \neq p_2 \\ &> n_1 = 200: n_2 = 200: p_1 = 44/200; p_2 = 30/200 \\ &> p_1 = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2) \\ &> p \\ &> p = 0.185 \end{aligned}$$

$$q = 1 - p$$

$$[5] = 0.815$$

$$\text{zcal} = (p_1 - p_2) / \sqrt{p_1 * q / (n_1 + n_2)}$$

$$z_{\text{cal}}$$

$$[5] 1.802441$$

52

$$> p\text{value} = 2 * \text{pnorm}(\text{abs}(z_{\text{cal}}))$$

$$> p\text{value}$$

$$[5] 0.02$$

If p-value is greater than 0.05 we accept the hypothesis.

C. ✓

Topic : Small sample test.

i) The marks of 10 students are given by  
63, 63, 66, 67, 68, 70, 71, 72. Test the hypothesis  
that the sample from the population with  
mean  $\mu = 68$ .

$$H_0: \mu = 66$$

$$H_a: \mu > 66 \quad (\text{one tail test})$$

One sample + - test

Data:  $x$

$$t = 6.8319 \quad df = 9, \text{ p-value} = 1.58e-13$$

True mean is not equal to 0  
95 percent confidence interval  
65.6519 - 76.44829

Sample estimate  
mean of  $x$

$$67.9$$

: The p-value is less than 0.05 we reject  
the hypothesis at 5% level of  
significance.

Ex

Q.

Two group of student the following marks test the hypothesis that there is no significant diff between the 2 groups.

GK1 - 18, 22, 21, 17, 20, 27, 23, 20, 22, 21  
GK2 - 18, 20, 14, 21, 20, 18, 13, 15, 17, 21

H0 : there is not diff b/w the 2 groups.

>  $x = \{18, 22, 21, 17, 20, 19, 23, 20, 22, 21\}$

>  $y = \{18, 20, 14, 21, 20, 18, 13, 15, 17, 21\}$

>  $t = t_{stat}(x, y)$

which two sample t-test is

data :  $X$  and  $Y$

$t = 2.2523$  df = 16.375 p value = 0.0398

alternative hypothesis.

True diff is mean w/ not equal. To 0.95 percent confidence interval.

0:  $\mu_1 = \mu_2$  S. 0371795

Sample estimates:

mean of  $X$  mean of  $Y$

20.1

> p-value = 0.3798

> if (pvalue > 0.05) cat("accept h0")  
else cat("reject h0")  
reject h0.

④ following are the weight before and after the diet program is the diet program effective.

Before : 120, 125, 115, 130, 123, 119

After = 100, 114, 95, 90, 115, 99

Soln : H<sub>0</sub>: There is no significant diff?  
H<sub>a</sub>:  $\mu_{\text{before}} > \mu_{\text{After}}$   
 $t$ . test (if  $H_0$  paired = T, alternative = "less")

Data:  $x$  and  $y$

$t = 4.3458$ ,  $df = 5$  p-value = 0.9483  
alternative hypothesis: true difference  
in mean is not less than 0.  
95 percent confidence interval:

- inf 20.0295  
sample estimates:  
mean of the diff n.

p-value is greater than 0.05 we  
accept the hypothesis at 5%, with  
o significance.

19. Q3 333

practical no. 8

Topic large and small test.

①

$$H_0: \mu = 55, H_1: \mu \neq 55$$

$$> n = 100$$

$$> m_x = 52$$

$$> m_o = 55$$

$$> s_d = 7$$

$$> z_{cal} = (m_x - m_o) / (s_d / \sqrt(n))$$

$$> z_{act}$$

$$0.3 - 4.205 > 1.4$$

$$\rightarrow p\text{value} = 2 * (1 - \text{norm.pdf}(z_{act}))$$

$$\rightarrow p\text{value}$$

$$[1] 1.82153e-05$$

As p-value is less than 0.05 we reject  $H_0$  at 5% level of significance.

$H_0: \rho = 0.5$  against  $H_1: \rho \neq 0.5$

$$\rightarrow \rho = 0.5$$

$$> n = 100$$

$$> z_{act} = (\rho - \rho_0) / (\sigma_{\rho} \sqrt{n})$$

$$> z_{act} = [1] 0$$

$$> p\text{ value} = 2 * (1 - \text{pnorm}(z_{act}))$$

$$\rightarrow p\text{ value}$$

If p-value is greater than 0.05 we accept  $H_0$  at 5% level of the significance.

Q

$H_0: \mu = 100$  against  $H_1: \mu \neq 100$

> var = 64

> n = 100

> m0 = 100

> m\* = 100

> sd = sqrt(var)

> sd

m &

> zcal = (m-m0) / (sd / sqrt(n))

> zcal

0.25

> pvalue = 2 \* (1 - pnorm(zabs(zcal)))

> pvalue

0.1241933

Some pvalue is less than 0.05 we  
reject  $H_0$  at 5% level of significance.

Q5  $H_0: \mu = 66$  against  $H_1: \mu \neq 66$

> x = c(63, 63, 60, 69, 71, 71, 72)

> t.test(x)

One sample t-test

data: x

t = 4.94 df = 6 p-value = 5.522e-09

alternative hypothesis true mean is not equal  
to 66 95 percent confidence interval:

64.66729

sample estimates:

mean of x

since p value is less than 0.05 we reject  $H_0$  at 1% level of significance.

since p value is less than 0.05 we reject  $H_0$  at 1% level of significance.

specie  
of 633 were  $p = 0.5$   
process is less than 0.05 we reject  
 $H_0$

$$\textcircled{8} \quad H_0: p_1 = p_2 \quad \text{against} \quad H_1: p_1 \neq p_2$$

$$> n_1 = 200$$

$$> n_2 = 300$$

$$> p_1 = 44/200$$

$$> p_2 = 56/300$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p = 0.2$$

$$> q = 1 - p$$

$$> q = 0.8$$

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z_{\text{cal}} = 0.912009$$

$$> \text{rule} = 2 * (1 - \text{norm}(z_{\text{cal}}))$$

process

156.3613104

So, process is greater than 0.05 we  
reject the null at 1% level of  
significance.

Q1 use the following data to whether the condition of home and the condition of child are independent or not.

→ condition of home

| clean        | clean | dirty |
|--------------|-------|-------|
| fairly clean | 70    | 50    |
| dirty        | 80    | 20    |

→

$H_0$ : condition of home and child are independent  
 $\chi^2 = c(70, 80, 35, 20, 45)$

$$m = 2$$

$y = \text{matrix}(x, nrow = m, ncol = n)$

|      |      |      |
|------|------|------|
| [1,] | [1,] | [2,] |
| 70   | 50   |      |
| 80   | 20   |      |
| 35   | 45   |      |

•  $PV = \text{chisq.test}(y)$

PV person's chi-squared test.

data: y

$$\chi^2 = 25.646 \quad df = 2 \quad pvalue = 7.88e-06$$

∴  $H_0$  is rejected since  $pvalue < 0.05$

$$0.05$$

| Type | Observations   |
|------|----------------|
| A    | 50, 52         |
| B    | 53, 55, 53     |
| C    | 60, 58, 57, 55 |
| D    | 52, 54, 54, 55 |

→

H<sub>0</sub>: The means are equal for A, B, C, D.

$$x_1 = c(50, 52)$$

$$x_2 = c(53, 53, 55, 53)$$

$$x_3 = c(60, 58, 57, 56)$$

$$x_4 = c(52, 54, 54, 55)$$

$$d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 =$$

named(d))

[1] "values" "ind"

→ One-way-test (values ~ ind, kstep = d, var = equal = T.)

One-way anaylsis of means

data: values, kstep = ind, num df = 3, denom df = 9, F = 11.935, pvalue = 0.000285

> anova = aov(values ~ ind, data = d)  
summary(anova).

0.03

0.15  
0.3  
0.44  
0.453

mean 3.0479  
f value 8.045  
P value 0.0021

nd 2.0  
sd 0.9000

5. How to import a csv file in  
→ X = read.csv("C:/Users/admin/Desktop/stat.  
csv")

point (x)

| #  | stats | maths |
|----|-------|-------|
| 2  | 40    | 60    |
| 3  | 43    | 40    |
| 4  | 42    | 42    |
| 5  | 45    | 20    |
| 6  | 37    | 25    |
| 7  | 36    | 27    |
| 8  | 49    | 57    |
| 9  | 89    | 50    |
| 10 | 20    | 25    |
| 11 | 27    | 27    |

cm = mean(x + stats)

cm

[2] 37

= length(x + stats)

n = var.stats / n

sd = sqrt((n-1) \* var.stats) / n

sd = 12.649

dm = mean(x + maths)

[3] 39.4